

Evaluation rule for call expressions:

1. Evaluate the operator and operand subexpressions.
2. Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

Applying user-defined functions:

1. Create a new local frame with the same parent as the function that was applied.
2. Bind the arguments to the function's formal parameter names in that frame.
3. Execute the body of the function in the environment beginning at that frame.

Execution rule for def statements:

1. Create a new function value with the specified name, formal parameters, and function body.
2. Its parent is the first frame of the current environment.
3. Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

1. Evaluate the expression(s) on the right of the equal sign.
2. Simultaneously bind the names on the left to those values, in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order.

1. Evaluate the header's expression.
2. If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

1. Evaluate the subexpression <left>.
2. If the result is a true value v, then the expression evaluates to v.
3. Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

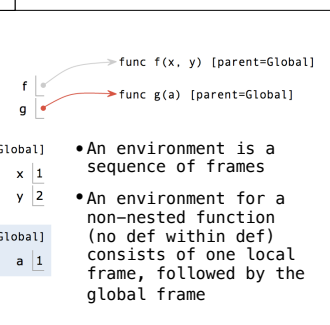
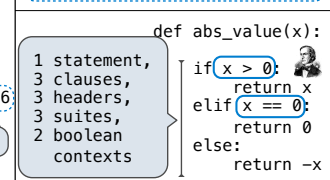
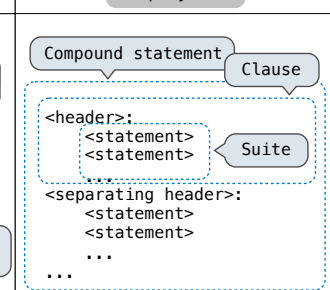
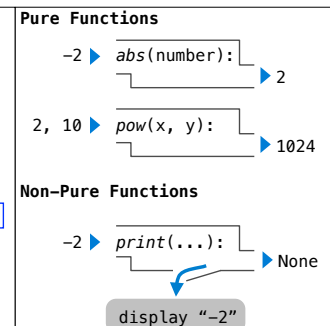
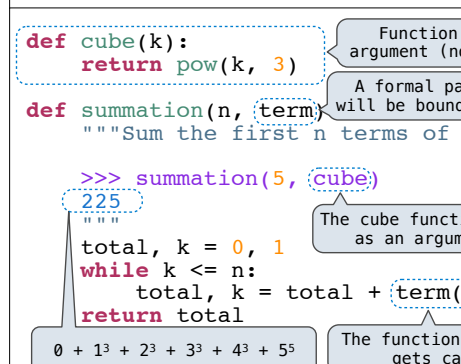
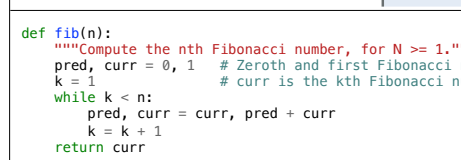
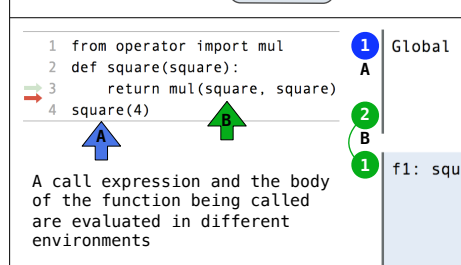
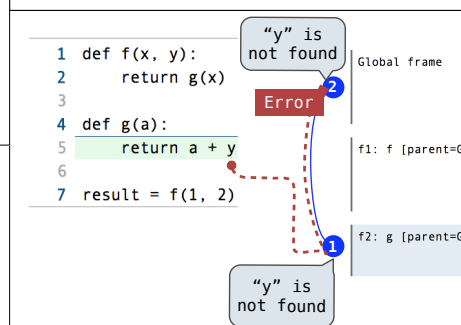
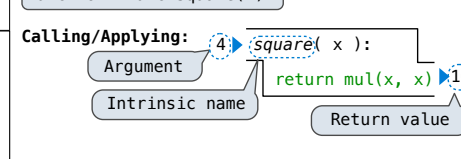
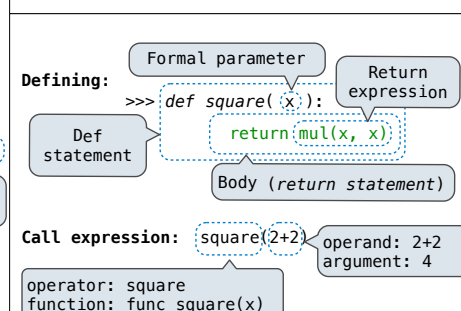
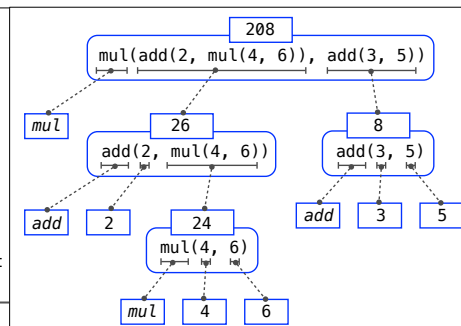
1. Evaluate the subexpression <left>.
2. If the result is a false value v, then the expression evaluates to v.
3. Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

1. Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

1. Evaluate the header's expression.
2. If it is a true value, execute the (whole) suite, then return to step 1.



square = `lambda x,y: x * y`

Evaluates to a function.
No "return" keyword!

A function
with formal parameters `x` and `y`
that returns the value of `"x * y"`

Must be a single expression

`def make_adder(n):`

A function that returns a function

Return a function that takes one argument `k` and returns `k + n`.

`>>> add_three = make_adder(3)`

The name `add_three` is bound to a function

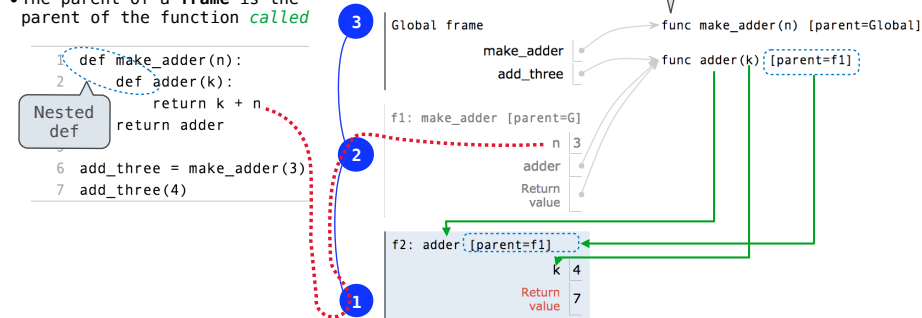
`>>> add_three(4)`

A local def statement

`def adder(k):`
`return k + n`
`return adder`

Can refer to names in the enclosing function

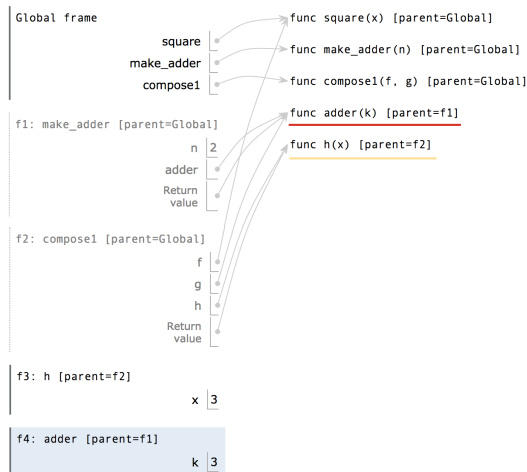
- Every user-defined function has a **parent frame** (often global)
- The parent of a **function** is the frame in which it was **defined**
- Every local **frame** has a **parent frame** (often global)
- The parent of a **frame** is the parent of the function **called**



`1 def square(x):`
`2 return x * x`
`3`
`4 def make_adder(n):`
`5 def adder(k):`
`6 return k + n`
`7 return adder`
`8`
`9 def compose1(f, g):`
`10 def h(x):`
`11 return f(g(x))`
`12 return h`
`13`
`14 compose1(square, make_adder(2))(3)`

Nested def

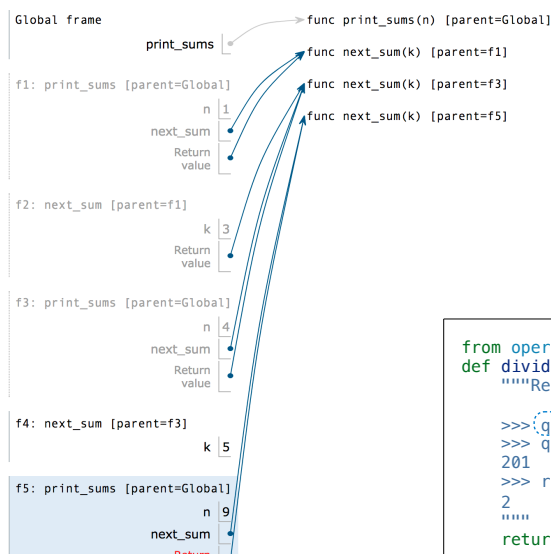
Return value of `make_adder` is an argument to `compose1`



`1 def print_sums(n):`
`2 print(n)`
`3 def next_sum(k):`
`4 return print_sums(n+k)`
`5 return next_sum`
`6`
`7 print_sums(1)(3)(5)`

Printed output:

1
4
9



square = `lambda x: x * x` VS `def square(x):`
`return x * x`

- Both create a function with the same domain, range, and behavior.
- Both functions have as their parent the environment in which they were defined.
- Both bind that function to the name `square`.
- Only the `def` statement gives the function an intrinsic name.

When a function is defined:

1. Create a **function value**: `func <name>(<formal parameters>)`
2. Its parent is the current frame.

f1: make_adder func adder(k) [parent=f1]

3. Bind `<name>` to the **function value** in the current frame (which is the first frame of the current environment).

When a function is called:

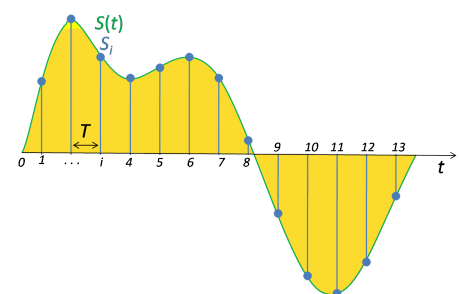
1. Add a **local frame**, titled with the `<name>` of the function being called.
2. Copy the parent of the function to the **local frame**: `[parent=<label>]`
3. Bind the `<formal parameters>` to the arguments in the **local frame**.
4. Execute the body of the function in the environment that starts with the **local frame**.

`>>> min(2, 1, 4, 3)` `>>> 2 + 3`
1 5
`>>> max(2, 1, 4, 3)` `>>> 2 * 3`
4 6
`>>> abs(-2)` `>>> 2 ** 3`
2 8
`>>> pow(2, 3)` `>>> 5 / 3`
8 1.6666666666666667
`>>> len('word')` `>>> 5 // 3`
4 1
`>>> round(1.75)` `>>> 5 % 3`
2 2
`>>> print(1, 2)`
1 2

`def search(f):`
"""Return the smallest non-negative integer `x` for which `f(x)` is a true value.
"""
`x = 0`
`while True:`
 if `f(x)`:
 return `x`
 `x += 1`

`def is_three(x):`
"""Return whether `x` is three.
"""
`>>> search(is_three)`
3
"""
return `x == 3`

`def inverse(f):`
"""Return a function `g(y)` that returns `x` such that `f(x) == y`.
"""
`>>> sqrt = inverse(lambda x: x * x)`
`>>> sqrt(16)`
4
"""
return `lambda y: search(lambda x: f(x)==y)`



`from operator import floordiv, mod`
`def divide_exact(n, d):`
"""Return the quotient and remainder of dividing `N` by `D`.
"""
`>>> q, r = divide_exact(2012, 10)` Multiple assignment to two names
`>>> q`
201
`>>> r`
2
"""
return `floordiv(n, d), mod(n, d)` Two return values, separated by commas