

# Coalgebraic effects and their cohandlers in programming languages

(Efekty koalgebraiczne oraz ich kohandlery  
w językach programowania)

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## Abstract

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# Chapter 1

## Introduction

*My algebraic methods are really methods of working and thinking; this is why they have crept in everywhere anonymously. ~ Emmy Noether*

In this thesis we present experimental programming language Freak, which is an implementation of Continuation Passing Style for Effect Handlers paper [10], with the addition of a few basic constructs. We start by presenting the related work, then discuss syntax and operational semantics. Basic usage guide for playing with the language is provided, as well as implementation details and examples. We conclude by stating what are the possible augmentations, that are intended to be made in the future.

### 1.1 Problem Analysis

What are the issues with normal algebraic effects?

### 1.2 Problem Statement

Brief and concise description of the problem

### 1.3 Thesis Outline



## Chapter 2

# Background

### 2.1 Computational Effects

Since the rapid development of computational theory in 1930s by A. Turing, K. Godel and A. Church, we have a well-established notion of what can and what cannot be done through algorithmic means, which we can almost directly translate to being computable by our machines. Through next years we have developed mainstream languages that are used almost everywhere, with a great success.

Under these circumstances one may pose a question, why do we still bother with development of languages theory, since so much has been done already. Is there anything that drives us towards further research? Indeed, one active branch revolves around equational theory to assess equality of two programs, which we know that in general setting is undecidable. Proof methods may include extensional, contextual or logical equality. However, there is no doubt that these formal ways of reasoning about programs, while being crucial for assessing correctness, do not bring direct benefits for practical, everyday use cases.

Other branch of languages theory, that we shall investigate more in this thesis, is about handling complexity of programs. Various methods of static analysis has been developed, most notably, type systems.

What is the source of complexity? Thanks to strong and static type systems along with their implementations, we have solid tools to work efficiently on functions that are pure. That being said, we claim that the sole complexity of programs comes from side effects, which we cannot avoid in writing anything useful.

We need to have a good way for handling computational effects, which so far has been modeled through monads [14].

However, they were found to be, to say the least, cumbersome to work with when complexity and number of different effects increases. It is perhaps not a coincidence that many functional programming languages do not have them, because of the

non-composable nature of them.

Having functions  $f : a \rightarrow mb$  and  $g : b \rightarrow m'c$ , it should not be an issue to compose them together.

Recall that the main idea of monads lies on the fact that we provide a function to lift value into a functor and associative kleisli composition operator to combine computations together. It turns out, that it becomes complex and unpleasant to combine two functors together to form a new monad. For this purpose, monad transformers arose in Haskell.

Most of the common languages avoid this by not expressing computational effects in the type system, and instead one may think about functions as being implicitly embed in a Kleisli Category over a functor  $T$ , where  $T$  is a hidden signature over all possible side effects that occur in our program.

Not only we would like to bring back effects to our type system, but also do it in a way that is composable. This is where algebraic effects comes to the rescue.

From theoretical point of view, we need to develop equa about our effects to assert correctness of our language as well as to have the right hammer to reason about our programs.

That is the point where we would like to introduce to unfamiliar read a notion of algebraic effects.

## 2.2 Algebraic Effects

What are algebraic effects?

Algebraic effects can be thought as an public interface for computational effects. Declarative approach allow us to write programs in which the actual semantic of source code is dependent on handler that defines the meaning of a subset of effects.

This is really a breakthrough from practical point of view, as we may substitute logic depending on execution environment. As an example, fetching for resources can behave differently as we run tests, debug our code, or run it on production. In the same manner, they neatly allow us to abstract over implementation details.

## 2.3 Categorical Setting of Universal Algebra

For the purpose of describing the duality between algebra and coalgebra, we allow ourselves to wander a bit deeper into category theory.

### 2.3.1 Algebraic Theories

Sigma-Signatures, Sigma-Terms, Sigma-Equations, Interpretations, Models, Free models

### 2.3.2 Free models form monads

Maybe not a subsection but just a lemma

### 2.3.3 Models homomorphisms

T-homomorphisms with respect to theory T

### 2.3.4 Parametrized operations

## 2.4 Duality

### 2.4.1 Comodels

Comodel in  $\mathcal{C}$  is just a Model in  $\mathcal{C}^{op}$ .

Models — Worlds

### 2.4.2 Cooperations

Derive from Models duality

### 2.4.3 Coalgebraic Effects

### 2.4.4 Coinductive Reasoning

Coinduction, and coinductive structures, provide us a way of observation of the behaviour, as a contracty to construction in inductive reasoning. Simple example of the duality can be expressed through induction over finite list and coinductive observation of infinite streams.

Doing the latter may involve modification of the internal state of the machine that is generating the infinite streams, or in more concrete scenario, alternation of the external resource that is providing us the data.

This is one of the cases where interaction with external resource multiple times, or more specifically in case of algebraic effects, invoking resumption more than once, may lead to unexpected behaviour that would not be expected in standard control

flow. This captures the excessive generality of effects, and is the issue that we would like to address with coalgebraic effects.

## 2.5 Related Work

### 2.5.1 Algebraic Effects

Except from Links language [10], on which the implementation is based, there are currently many other alternatives available. One may take a look at Frank [13], which provides a support for multihandlers, Koka [12], Helium [6] or Eff [3]. Except from separate languages, many libraries arose for existing ones like Haskell, Idris, Scala or Multicore OCaml.

As can be seen in the J. Yallop repository [7], algebraic effects and handlers are now trending branch in the programming languages theory.

### 2.5.2 Coalgebraic Effects

Ahman and Bauer [1]

## Chapter 3

# Potential Solutions

One-shot continuations

Detecting whether resumption is called only once is undecidable.

### 3.1 Dynamic Constraints Checking

### 3.2 Linear Types

Solve the issue through introduction of linear type system.

### 3.3 Data-Flow Analysis

Another static analysis of the program.

### 3.4 Cohandlers as Separate Constructs

Simplify semantics by separating coalgebraic effects into a new, restricted construct in programming language





## Chapter 4

# Effectful and Coeffectful Programming

### 4.1 Examples

In this section we present a few examples to show the capabilities of the language. The ideas have been based on [4], and thus will not be described in great details. More exemplary programs in Freak language can be found under <https://github.com/Tomatosoup97/freak/tree/master/src/programs>.

#### 4.1.1 Choice

The first example will be based on modelling (nondeterministic) choice in the program. We will make two decisions, which will affect the computation result:

```
let c1 <- do Choice () in
let c2 <- do Choice () in
let x <- if c1 then return 10 else return 20 in
let y <- if c2 then return 0 else return 5 in
  return x - y
```

With that in hand, we may want to define effect handlers:

```
handle ... with {
  Choice p r ->
    let t <- r 1 in
    let f <- r 0 in
    <PLACEHOLDER> |
```

```

    return x -> return x
}

```

where in the `<PLACEHOLDER>` we can define on what to do with the computation. For example, min-max strategy for picking the minimum value:

```

if t < f then return t else return f

```

where the code evaluates to 5. Another example is a handler that collects all possible results, which can be achieved by putting `return (t, f)` in the `<PLACEHOLDER>`, which evaluates to `((10, 5), (20, 15))`.

### 4.1.2 Exceptions

Exceptions are simply algebraic effect handlers which drop the resumption.

```

handle
  if x == 0 then do ZeroDivisionError ()
    else return 1/x
with {
  ZeroDivisionError p r -> return 42 |
  return x -> return x
}

```

Where we imagine that `x` variable has been bound previously.

### 4.1.3 Taming Side effects

The complexity of the programs and their performance usually comes from side effects. Algebraic effects allow us to define code in a declarative manner, and hence neatly tame the side effects that they produce. This gives us a lot of flexibility in the actual meaning without duplicating the code. Let's consider the following very basic code snippet:

```

let x <- do Fetch () in
-- operate on x

```

The code is dependent on a context in which it is executed, which here is the handler that defines the behaviour of the algebraic `Fetch` effect. In the imperative, or even functional approach, we would need to provide the interface for fetching the data by doing dependency injection or even embedding the operation directly. Here we are just stating what operation we are performing, leaving the interpretation up to the execution context, which could do the fetching or mock the external resource.

These implications are straightforward when looking from a categorical standpoint, where effects are viewed as free models of algebraic theories [16], and handlers are homomorphisms preserving the model structure [15]. Nevertheless, the results are very exciting for programming use cases. The current Freak implementation does not support I/O.

## 4.2 Coexamples

Examples for cohandlers

## 4.3 Usage guide

As of this day, two implementations are available, one based on the curried translation and Appel [2], and the second one based directly on the uncurried translation with continuations as explicit stacks from paper. More details can be found in Section 6. All commands are available within `src` directory.

### 4.3.1 Build and install

- Install dependencies: `make install`
- Select implementation: `make link-lists` (default) vs `make link-appel`
- Compile: `make build`
- Link to PATH: `sudo make link`
- Remove artifacts: `make clean`

After compiling and linking program to PATH, one may evaluate program as follows: `freak programs/choicesList.fk`. The actual code is described in Section 4.1.1

### 4.3.2 Running tests

Test cases are available [here](#), they include both inline and file-based tests. For more details about writing tests, one may refer to *HUnit documentation* [11].

- Run tests: `make tests`
- Run code linter: `make lint`
- Compile, run linter and tests: `make check`

## Chapter 5

# Calculus of Freak language

### 5.1 Syntax

The syntax for the calculus is shown below.  $\text{nat } n$  represents an integer  $n$ ,  $V \oplus W$  and  $V \approx W$  are respectively binary and relational operators, where we support basic arithmetic and comparison operations. **if**  $V$  **then**  $M$  **else**  $N$  is a standard branching statement. The other constructs are just as in Links, with slight syntax modifications. Actual programs in Freak can be found in Section 4.1.

$$\begin{aligned} \langle \text{Values } V, W \rangle ::= & x \mid \text{nat } n \\ & \mid \lambda x : A \rightarrow M \mid \mathbf{rec } g \ x \rightarrow M \\ & \mid V \oplus W \mid V \approx W \\ & \mid \langle \rangle \mid \{\ell = V; W\} \mid [\ell V]^R \end{aligned}$$
$$\begin{aligned} \langle \text{Computations } M, N \rangle ::= & V \ W \\ & \mid \mathbf{if } V \ \mathbf{then } M \ \mathbf{else } N \\ & \mid \mathbf{let } \{\ell = x; y\} = V \ \mathbf{in } N \\ & \mid \mathbf{case } V \{\ell \ x \rightarrow M; y \rightarrow N\} \mid \mathbf{absurd } V \\ & \mid \mathbf{return } V \mid \mathbf{let } x \leftarrow M \ \mathbf{in } N \\ & \mid \mathbf{do } \ell \ V \mid \mathbf{handle } M \ \mathbf{with } \{H\} \end{aligned}$$
$$\langle \text{Handlers } H \rangle ::= \mathbf{return } x \rightarrow M \mid \ell \ p \ r \rightarrow M, H$$
$$\langle \text{Binary operators } \oplus \rangle ::= + \mid - \mid * \mid /$$
$$\langle \text{Relational operators } \approx \rangle ::= < \mid \leq \mid > \mid \geq \mid == \mid !=$$

## 5.2 Typing Rules

## 5.3 Operational Semantics

The source language's dynamics have been described extensively by providing small-step operational semantics, continuation passing style transformation [10] as well as abstract machine [8], which was proved to coincide with CPS translation. That being said, Freak introduces new basic constructs to the language, for which we shall define the semantics.

Extension of the evaluation contexts:

$$\mathcal{E} ::= \mathcal{E} \oplus W \mid \text{nat } n \oplus \mathcal{E} \mid \text{if } \mathcal{E} \text{ then } M \text{ else } N$$

Small-step operational semantics:

$$\begin{aligned} \text{if } \text{nat } n \text{ then } M \text{ else } N &\rightsquigarrow M && \text{if } n \neq 0 \\ \text{if } \text{nat } n \text{ then } M \text{ else } N &\rightsquigarrow N && \text{if } n = 0 \end{aligned}$$

$$\begin{aligned} \text{nat } n \oplus \text{nat } n' &\rightsquigarrow n'' && \text{if } n'' = n \oplus n' \\ \text{nat } n \approx \text{nat } n' &\rightsquigarrow 1 && \text{if } n \approx n' \\ \text{nat } n \approx \text{nat } n' &\rightsquigarrow 0 && \text{if } n \not\approx n' \end{aligned}$$

## 5.4 Continuation Passing Style Transformation

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## Chapter 6

# Implementation

The Freak implementation is available at <https://github.com/Tomatosoup97/freak>, written purely in Haskell. While the paper provided a good overview of the language and the translation, the lower-level details were omitted. That being said, two inherently different takes at the implementations were made. The first one is based on curried translation and A. Appel [2] book, and the second one directly on the uncurried translation to target calculus with continuations represented as explicit stacks from the paper. We start by presenting core data structures, and afterwards move to actual translation details.

### 6.1 Abstract Syntax Tree

The language's AST is defined without surprises, just as syntax is:

```
data Value
  = VVar Var
  | VNum Integer
  | VLambda Var ValueType Comp
  | VFix Var Var Comp
  | VUnit
  | VPair Value Value
  | VRecordRow (RecordRow Value)
  | VExtendRow Label Value Value
  | VVariantRow (VariantRow Value)
  | VBinOp BinaryOp Value Value

data Comp
  = Eval Value
  | ELet Var Comp Comp
  | EApp Value Value
```

```

| ESplit Label Var Var Value Comp
| ECase Value Label Var Comp Var Comp
| EReturn Value
| EAbsurd Value
| EIf Value Comp Comp
| EDo Label Value
| EHandle Comp Handler

```

Similarly for the target calculus data structure. However, as one may notice, for convenience the **let** translation is homomorphic, as opposed to be to lambda abstracted with immediate application:

```

data UValue
  = UVar Var
  | UNum Integer
  | UBool Bool
  | ULambda Var UComp
  | UUnit
  | UPair UValue UValue
  | ULabel Label
  | URec Var Var UComp
  | UBinOp BinaryOp UValue UValue

data UComp
  = UVal UValue
  | UApp UComp UComp
  | USplit Label Var Var UValue UComp
  | UCase UValue Label UComp Var UComp
  | UIf UValue UComp UComp
  | ULet Var UComp UComp
  | UAbsurd UValue

```

The final answer, common to both evaluations, is represented as a **DValue**, where the meaning of the coproduct is as one would expect:

```

type Label = String
type FuncRecord = [DValue] -> Either Error DValue
data DValue
  = DNum Integer
  | DLambda FuncRecord

```



```

| DUnit
| DPair DValue DValue
| DLabel Label

```

## 6.2 Target calculus

## 6.3 Curried translation

The first take was heavily inspired by A. Appel's Compiling with Continuations [2], which provides a translation for a simplified ML calculus. The calculus was extended and translation adapted to handle algebraic effects and their handlers. The translation is based on the curried first-order translation. That being said, the source code diverged a lot from the paper on which it was based, leading to a different transformation for which the correctness and cohesion with operational semantics should be proved separately. Indeed, while the interpreter worked well on the use cases defined in tests, the evaluation had a part which was not tail-recursive. What's more, nested handlers were not supported, and the implementation was found to be trickier than it should, as it was not obvious on how to adopt the technique proposed in the paper.

In terms of improving the performance of the evaluation, uncurried higher-order translation should be adapted, so that administrative redexes are contracted and proper tail-recursion is obtained. The core data structure, into which the source program is transformed, is defined as follows:

```

data ContComp
  = CPSApp CValue [CValue]
  | CPSResume CValue ContComp
  | CPSFix Var [Var] ContComp ContComp
  | CPSBinOp BinaryOp CValue CValue Var ContComp
  | CPSValue CValue
  | CPSLet Var CValue ContComp
  | CPSSplit Label Var Var CValue ContComp
  | CPSCase CValue Label Var ContComp Var ContComp
  | CPSIf CValue ContComp ContComp
  | CPSAbsurd CValue

```

Most of the terms at the end have a coinductive reference to itself, which represents the rest of the computation that needs to be done. For more clarification, one may

take a look into the book mentioned above [2]. The source code for curried translation and evaluation can be found respectively in `CPSAppel.hs` and `EvalCPS.hs`.

## 6.4 Uncurried translation

Having in mind the drawbacks mentioned above, alternative translation was written, that coincides with the translation from the paper. Namely, with the uncurried translation to target calculus with continuations represented as explicit stacks. The target calculus was described in Section 6.1, for which the evaluation is straightforward. The continuations are represented as `Cont`, with syntactic distinction between pure and effectful computations, which occupy alternating positions in the stack. Explicit distinction gave more control in the source code.

```
type CPSMonad a = ExceptT Error (State Int) a

type ContF = UValue -> [Cont] -> CPSMonad UComp

data Cont = Pure ContF
          | Eff ContF
```

Where `CPSMonad` is a monad transformer over `Either` and `State`. `State` was required to generate labels for fresh variables that came from the translation. The core code is split into five functions:

```
cps      :: Comp      -> [Cont] -> CPSMonad UComp
cpsVal   :: Value     -> [Cont] -> CPSMonad UValue
cpsHRet  :: Handler   -> Cont
cpsHOps  :: Handler   -> Cont
forward  :: Label     -> UValue -> UValue -> [Cont] -> CPSMonad UComp
```

Where the first two are implementing `cps` for computations and values. `cpsHRet` and `cpsHOps` are yielding pure and effectful continuations, based on a given handler. The last one is responsible for forwarding the computation to the outer handler.

This results in an implementation that finally supports nested handlers, as can be seen by evaluating `programs/complexNestedHandlers.fk` program. Unfortunately, following closely translation from the paper resulted in a behaviour, in which invoked resumption forgets its pure continuation. This means, that the following code, evaluating correctly on the Appel-based translation, returns 0 rather than 1:

```
handle do Drop () with { Drop p r -> let t <- r 0 in return 1 }
```

Nevertheless, working out this issue appears as less demanding than coping with discrepancies created in the first translation. The source code for uncurried translation and evaluation can be found respectively in `CPSLists.hs` and `EvalTarget.hs`.

## 6.5 Cohandlers

...

## 6.6 Source Code Structure

The source code is divided into a number of modules, where the most crucial parts have already been described.

<code>AST.hs</code>	- AST data structures
<code>CommonCPS.hs</code>	- Common functions for CPS translation
<code>CommonEval.hs</code>	- Common functions for evaluation
<code>CPSAppel.hs</code>	- Appel-based CPS translation
<code>CPSLists.hs</code>	- Uncurried CPS translation
<code>EvalCPS.hs</code>	- Evaluation of the Appel's CPS structure
<code>EvalTarget.hs</code>	- Evaluation of the target calculus
<code>Freak.hs</code>	- API for the language
<code>Main.hs</code>	- Main module running evaluator on given filename
<code>Parser.hs</code>	- Parser and lexer
<code>TargetAST.hs</code>	- AST for the target calculus
<code>Tests.hs</code>	- Tests module
<code>Types.hs</code>	- Common types definition
<code>programs/</code>	- Exemplary programs used in tests



## Chapter 7

# Conclusion

### 7.1 Summary

What was achieved, what was described, what needs to be done or researched.

### 7.2 Future work

#### 7.2.1 Abstract machine

The Links language also provides small-step operational semantics and an abstract machine [8]. Implementing another way of evaluation could serve as a way to empirically assert correctness, as opposed to formally.

#### 7.2.2 Type inference and row polymorphism

The type system as of this day is not implemented, as the focus has been put on CPS transformation. Further work is required here, especially considering the fact that a huge advantage of algebraic effects is that they are explicitly defined in the type of a computation.

#### 7.2.3 Multiple instances of algebraic effects

The Freak language is limited to a single instance of an effect. We would need to support cases where many instances of the algebraic effects, with the same handler code, could be instantiated. The current state of the art introduces a concept of resources and instances, as in Eff [4], or instance variables, as in Helium [5].

#### 7.2.4 Selective CPS

Other languages, like Koka [12], or even the core of the Links, are performing selective CPS translation, which reduces the overhead on code that does not perform algebraic effects. Our current translation is fully embedded in the CPS.

#### 7.2.5 Exceptions as separate constructs

Exceptions are a trivial example of algebraic effect where the resumption is discarded, and as described in §4.5 [10], they can be modeled as a separate construct to improve performance.

#### 7.2.6 Shallow handlers

Shallow and deep handlers while being able to simulate each other up to administrative reductions, have a very different meaning from a theoretical point of view. Implementing them as defined by Lindley et al. [9] could be another way of enhancing Freak.

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