

Master Computer Science

Applying Counterfactual Explanations and Multivariate Forecasting to Medical Prediction Tasks

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Abstract

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1 Introduction

Time series forecasting plays a crucial role in a number of different applications, such as stock market predictions, weather forecasting, healthcare monitoring, and personalized treatment planning. The main goal of time series forecasting is to use historical observations to predict future values. For this task there are various models, including statistical approaches such as ARIMA, regression-based methods like Linear Regression, as well as deep learning models like N-Beats and transformer-based models such as DLinear. Especially the latter models have shown promising results in recent years, achieving very accurate predictions. Despite these recent developments, many deep-learning based forecasting systems are considered "black-box"-models, as it is challenging to interpret and understand both the modelling process and the forecasting outcome. This is particularly problematic in healthcare applications, where especially interpretability is very important, as clinicians need to understand the reasoning behind the predictions to make informed decisions. One approach to tackle this problem is working with counterfactual explanations, which aim to identify small changes in the input variables needed to change a model's forecast to a more desirable outcome.

In healthcare, time series forecasting has been applied to a number of different tasks, especially the analysis of electronic health records (EHRs). These contain information about a patient's health over time, allowing predictions about the disease progression, treatment efficacy or patient mortality. For example, forecasting glucose levels in diabetic patients or predicting heart failure with preserved ejection fraction (HFpEF) can aid early interventions and optimize treatment plans.

1.1 Diabetes

For patients with conditions such as type 1 diabetes mellitus (T1DM), closely tracking their glucose levels is a necessity. To reduce the risk of complications such as hyperglycaemia or hypoglycaemia, these patients rely on continuous glucose monitoring (CGM) devices and automated insulin delivery. Using machine learning (ML) to model CGM, can help to gain a better understanding of predicting abnormal glucose events and help with insulin dosage planning. By also incorporating variables such as insulin intake, carbohydrate consumption, and physical activity, a predictive model can allow timely interventions through the generation of actionable recommendations for patients or healthcare providers. This allows for more dynamic treatment based on these forecasted expected glucose trends, which can reduce the long-term risk of diabetes-related complications[Com25].

1.2 HFpEF

Another possible application is identifying early warning signs of heart failure or more specific HFpEF and suggest either lifestyle or treatment changes. Using the vital signs, as for example the heart rate and blood pressure, of a patient as well as other factors like gender and possible comorbidities, allows specific and personal monitoring of disease progression. This way, early warning signs of worsening heart condition can be identified and personalized modifications to lifestyle or medication can be suggested. Such proactive monitoring can help reduce hospital readmissions and improve patient outcomes.

1.3 Counterfactual Explanations

Traditional time series forecasting focuses mainly on predicting future values given historical observations, but modifying past values is not feasible in real-world settings, especially in healthcare applications. Instead, a more practical approach is to explore how changing exogenous variables during the forecast horizon could lead to a desired outcome. This approach allows continuous monitoring of patients, making it possible to dynamically adjust treatment plans to lead towards more optimal results.

1.4 Related Work

Recent research has explored various deep learning (DL) models for time series forecasting, including recurrent neural network (RNN)-based models such as gated recurrent units (GRU) and long short-term memory (LSTM), as well as attention-based architectures like transformers. Transformer-based models, including Autoformer and Informer, have demonstrated strong performance in both univariate and multivariate forecasting tasks by capturing long-range dependencies more effectively than traditional RNN approaches.

In the clinical domain, deep learning models have been applied extensively to glucose forecasting. For instance, Deep Multi-Output Forecasting [FAJ+18] introduced a multi-step forecasting framework that explicitly models the distribution of future glucose values over a prediction horizon using a multi-output deep architecture. Similarly, WaveNet has been adapted for glucose forecasting by leveraging dilated convolutional neural networks (CNNs) to model long-term dependencies [ZLH+18]. In addition, transfer learning techniques have been employed to enhance predictive performance by fine-tuning pre-trained models on patient-specific data while incorporating exogenous covariates such as insulin dosage and carbohydrate intake [MB20]. Beyond predictive performance, explainability remains a critical challenge in deep learningbased forecasting models. Traditional statistical models, such as ARIMAX and VARIMAX, are able to quantify relationships between exogenous factors and the target variable, but their forecasting accuracy is often outperformed by DL approaches. Recent research has focused on integrating explainability into forecasting models to combine the strengths of both interpretability and predictive performance. For example, NBEATSx extends the NBEATS framework by incorporating exogenous variables into its deep architecture, enabling a more structured decomposition of trend and seasonality. However, its interpretability remains static and does not fully capture the dynamic nature of forecasting outcomes.

To address the need for explainability, counterfactual explanations have gained traction in time series analysis. Initial efforts focused on time series classification, where counterfactuals were generated through instance-based modifications and gradient-based perturbations [AALC21]. This was done by introducing a framework for generating counterfactual explanations for multivariate time series classification, identifying minimal input modifications needed to alter the model's decision, providing interpretability for high-dimensional time series models.

More recently, counterfactual explanations have been extended to time series forecasting. ForecastCF [WMSP23] proposed a deep learning-based method for generating counterfactuals in time series forecasting by identifying minimal input changes required to achieve desired prediction outcomes. Building on this, COMET [WSMP24] extended counterfactual explanations to multivariate time series forecasting, focusing on modifying exogenous variables (e.g., insulin, carbohydrates, and exercise) to generate actionable recommendations for glucose management. In addition to counterfactual forecasting, diagnostic tools like TimeTuner [HSYZ23] have been developed to analyse how time representations influence forecasting models. By employ-

ing counterfactual explanations, TimeTuner enables the evaluation of multivariate time series representations and their impact on model predictions.

Despite these advances, counterfactual explanations for multivariate time series analysis remain an emerging research area. While existing methods demonstrate the feasibility of generating counterfactuals for univariate forecasts, their generalization to multivariate forecasting and real-world clinical applications remains limited. Our work aims to extend on these existing methods by integrating counterfactual reasoning with multivariate forecasting models, focusing on modifying exogenous variables within the prediction horizon to provide actionable and interpretable interventions.

1.5 Main Contributions

Time series forecasting can be quite useful in healthcare by predicting how well a treatment works or predicting the risk of complications, relapse or mortality. Recent studies, such as COMET [WSMP24], have been focusing on counterfactuals in time series forecasting, but these methods work by altering historical observations. Our work aims to bridge this gap by developing a counterfactual forecasting mechanism that identifies optimal changes in exogenous variables during the forecast horizon to achieve desirable outcomes. More specifically, we propose a method that learns the relationship between the forecasted targets and exogenous variables, which leads to a more effective and interpretable decision-making in healthcare. The main contributions of this paper can be summarized as follows:

- We propose a new model for counterfactual time series forecasting to achieve a desired constrained forecast by modifying exogenous variables within the forecast horizon.
- We incorporate existing forecasting models, such as SARIMAX, OLS, GRU and NBEATSx, for learning the relationship between exogenous variables and a target variable to ensure actionable and interpretable predictions.
- We evaluate the models on two applications in healthcare, specifically for glucose level prediction and HFpEF management, demonstrating the practical utility of our approach.

2 Methodology

2.1 Problem Formulation

1) Let $\mathbf{X} := (\mathbf{x}_i)_{i \in \{1, \dots, n\}}$ be a time series of length n (back horizon), with each $x_i \in \mathbb{R}^{m+1}$ composed of the target variable $y_i \in \mathbb{R}$ and the exogenous variables

$$z_i = \begin{pmatrix} z_{1,i} \\ \vdots \\ z_{m,i} \end{pmatrix} \in \mathbb{R}^m.$$

Then **X** can be denoted as the combined matrix of the target vector $\mathbf{y} \in \mathbb{R}^{1 \times n}$ and the exogenous matrix $\mathbf{Z} \in \mathbb{R}^{m \times n}$:

$$\mathbf{X} = egin{pmatrix} \mathbf{y} \\ \mathbf{Z} \end{pmatrix} := egin{pmatrix} y_1 & \dots & y_n \\ z_{1,1} & \dots & z_{1,n} \\ \vdots & \ddots & \vdots \\ z_{m,1} & \dots & z_{m,n} \end{pmatrix}.$$

The relationship between \mathbf{y} and \mathbf{Z} can be described by the function:

$$r: \mathbb{R}^{m \times n} \to \mathbb{R}^{1 \times n}$$

which calculates the target vector from the exogenous matrix:

$$r(\mathbf{Z}) = \mathbf{y}.$$

2) Given a time series forecasting model f that predicts the next t values (forecasting horizon) of X, we define the forecast as:

$$f(\mathbf{X}) = \mathbf{X}' := (x_{n+i})_{i \in \{1,\dots,t\}}.$$

Additionally, consider a lower and upper bound set of constraints for each time step in the forecasting horizon, denoted as:

$$\alpha = (\alpha_{n+i})_{i \in \{1,...,t\}}, \beta = (\beta_{n+i})_{i \in \{1,...,t\}}.$$

The objective is to generate a counterfactual time series sample \mathbf{Z}^* , such that $\mathbf{y}^* = r(\mathbf{Z}^*)$ satisfies the given bounds:

$$\alpha_i \leq y_i^* \leq \beta_i, \forall y_i^* \in \mathbf{y}^*, i \in \{n+1, \dots, n+t\}.$$

Summarized research objective: Given a target vector \mathbf{y} affected by the exogenous matrix \mathbf{Z} , a forecast horizon t, the original forecasted vector \mathbf{y}' and the original forecasted exogenous matrix \mathbf{Z}' , the goal is to modify \mathbf{Z}' to \mathbf{Z}^* such that the corresponding target vector \mathbf{y}^* is within constraints α and β .

2.2 Algorithm

Counterfactual hybrid forecasting first forecast, then make counterfactuals gradient perturbation

Algorithm 1 Counterfactual Hybrid Forecasting

```
1: Input: Time series data: target t, exogonous variables E, learning rate \eta, desired
     bounds (\alpha, \beta), clipping range (\rho, \phi), max iterations max_iter, differentiable forecaster
      f(\cdot) differentiable regressor r(\cdot), w, \mathcal{G}
 2: Output: Counterfactual E' with desired outcome t'
 3: (t^*, E^*) \leftarrow (t, E)
 4: (\hat{t}^*, \hat{E}^*) \leftarrow f(t^*, E^*)
 5: S \leftarrow \text{SelectTestSamples}
 6: (\alpha, \beta) \leftarrow \text{GenerateBounds}(S)
 7: C \leftarrow \text{ActivityTemporalConstraint?}??
 8: loss \leftarrow L((t^*, E^*), \alpha, \beta, (t, E), C)???
 9: t \leftarrow 0
10: while (\hat{t}^* > \beta \text{ or } \hat{t}^* < \alpha) \land (t < \text{max\_iter}) \text{ do}
           \hat{E}^* \leftarrow \text{AdamOptimize}(\hat{E}^*, loss, \eta)
           \hat{E}^* \leftarrow \text{Clip}(\hat{E}^*, \rho, \phi)???
12:
          \hat{t}^* \leftarrow r(\hat{E}^*)
13:
          C \leftarrow \text{HistValueConstraint}(\hat{E}^*, \mathcal{G})
14:
          loss \leftarrow L(\hat{E}^*, w, \alpha, \beta, X^*, C)???
15:
          t \leftarrow t + 1
16:
17: end while
18: (t', E') \leftarrow (t, E)
19: return (t', E')
```

2.3 Experiments

2.3.1 Data preparation

There are many possible applications for the proposed model, including domains outside of health care. However, this research will focus only on medical applications, specifically on trying to identify optimal treatment plans for two different use cases: type 1 diabetes management and heart failure with preserved ejection fraction (HFpEF). The datasets used in this study contain physiological and treatment-related variables, allowing personalized forecasts and counterfactual interventions. To prepare the data for the proposed model, different preprocessing steps have been taken. The data is split into training, validation and test sets and normalized using min-max scaling to ensure stable model training, as well as split into the target and exogenous data. Then a sequence generator is used to slice the data into sequences of back horizon input and horizon targets for the prediction task and into sequences of back horizon input and horizon of both the exogenous and target features. This creates overlapping time series segments, of which any sequences with missing values are discarded.

SimGlucose: The SimGlucose dataset is generated using the FDA-approved UVA/PADOVA type 1 diabetes simulator [Xie18]. This Python-based simulator models the physiological responses of patients with type 1 diabetes and contains 30 virtual patients (10 adults, 10 adolescents, 10 children). It provides CGM measurements along with insulin dosage and carbohydrate intake. The dataset is generated with a predefined CGM sampling frequency and insulin pump settings according to the developed model [MML+14]. For this study, the measurements of ten adults over the course of one week were simulated. The blood glucose levels are used as the target variable, while the insulin dosages and carbohydrate intakes are used as exogenous

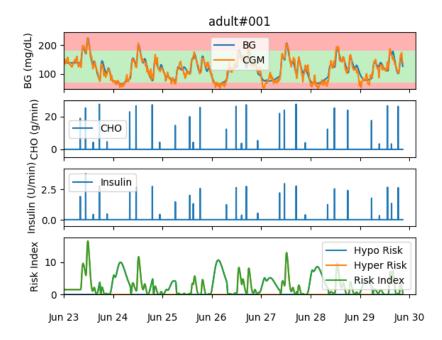


Figure 1: Simulation of an adult patient over the span of one week.

variables. After generating the simulated data, the data is preprocessed to be useable for the predictive model. One example can be seen in figure 1, where BG is the blood glucose level, CHO the carbohydrate intake and Insulin the insulin dosage. The risk index shows the hyperglycaemic or hypoglycaemic risk for the patient. For the blood glucose the level the green range shows normal glucose levels between 70 and 180, and the red ranges are hyper- or hypoglycaemic glucose levels.

OhioT1DM: The OhioT1DM dataset [MB20] contains real-world glucose monitoring data from 12 individuals with type-1 diabetes, collected by Ohio University over 8 weeks. According to earlier studies [CHN+21], [WSMP24], we extracted the most clinically relevant features, which includes the CGM measurements, basal insulin, bolus insulin, carbohydrate intake and physical activity. Compared to the SimGlucose dataset, this dataset includes more exogenous variables such as bolus and basal insulin, carbohydrate intake and physical activity, as. Since this dataset is collected from real patients, it includes missing data and irregular sampling intervals, which are handled using interpolation techniques and resampling. The availability of more exogenous variables allows for more complex counterfactual interventions, improving the performance of the forecasting model. Figure 2 shows example measurement in a 24-hour window of one of the patients.

<code>MIMIC-III:</code> Beyond diabetes forecasting, the proposed model aims to generalize to other medical applications, such as predicting disease progression in HFpEF patients. The MIMIC-III dataset $[JPS^+16]$ contains de-identified electronic health records (EHRs) of ICU patients, including vital signs (heart rate, blood pressure, oxygen saturation, etc.), medication records and laboratory results. For this study, a subset of MIMIC-III focusing on cardiovascular patients is used. The target variable is the mortality risk, splitting into two groups (death within 30 days, death within 1 year). The exogenous variables include vital signs and laboratory values,

add more explanation of data

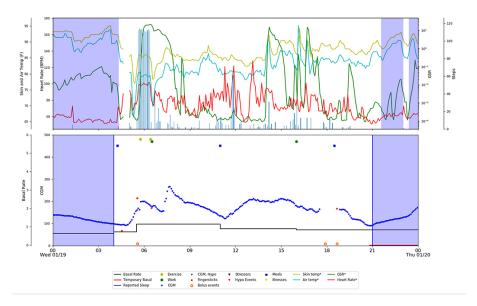


Figure 2: 24-hour measurements of one patient from the OhioT1DM Viewer [MB20].

Title	ICD Code	Frequency
Unspecified diastolic (congestive) heart failure	I5030	33
Diastolic heart failure, unspecified	42830	71
Acute diastolic (congestive) heart failure	I5031	84
Acute diastolic heart failure	42381	169
Chronic diastolic (congestive) heart failure	I5032	249
Chronic diastolic heart failure	42382	428
Acute on chronic diastolic (congestive) heart failure	I5033	411
Acute on chronic diastolic heart failure	42833	598

Table 1: ICD Codes

while gender and comorbidities are used to split the data into multiple cohorts. By analysing the data in different cohorts, it is possible to get more specific and accurate counterfactual interventions.

2.3.2 Experimental Setup

The model can be split into two main parts. Initially a multivariate forecasting model is used to make a first forecast for both the target variable and the exogenous variables. This forecast is then used for the second part, where different regression models are used to change the exogenous and target variable to get the desired outcome. For the forecasting part we used GRU and NBEATS and for the second part we used four different models. Here the focus lies on using very different kinds of models, like a statistical (SARIMAX), a regression based (OLS), and two different deep learning based (GRU and NBEATSx) models.

Multivariate Forecasting: For the multivariate forecasting, two main models have been used: (1) a 2-layer GRU model with 200 units at each layer and a linear output; and (2) a 4-layer NBEATS model with a forecast and backcast layer as well as a linear output. For both models early stopping with a patience of 10 epochs was applied to prevent over-fitting, with a fixed

add
list of
features,
list
of comorbidities

analyze clusters, split into clusters

Feature types	Specifics	Occurrences
Targets		
	Death within 30 days	133
	Death within 1 year	146
Vital signs and laboratory values		
	Heart Rate	1766
	Systolic BP	1759
	$\operatorname{SpO2}$	1766
	Temperature	1754
	BMI	1766
	Bicarbonate	1749
	Creatinine	1751
	Hemoglobin	1739
	Platelet Count	1738
	WBC Count	1739
	Sodium	1751
	NT-proBNP	74
	Troponin	928
Comorbidities		
	AMI	232
	PVD	562
	CEVD	219
	Dementia	73
	COPD	654
	Rheumatoid Disease	51
	PUD	41
	Mild LD	44
	Moderate/Severe LD	29
	Diabetes	771
	Diabetes + Complications	150
	HP/PAPL	31
	RD	737
	Cancer	64
	Metastatic Cancer	47
	Hypertension	614
	Coronary Artery Disease	736
	Pulmonary Hypertension	175
	Atrial Fibrillation	409
Other features		
	Male	732
	Female	1034

Table 2: Features, targets, data types

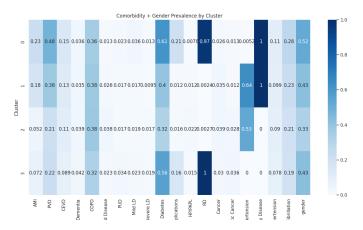


Figure 3: Caption

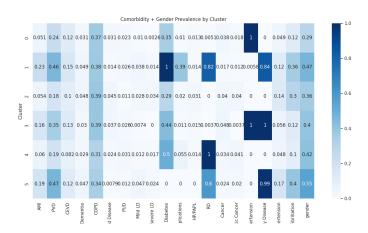


Figure 4: Caption

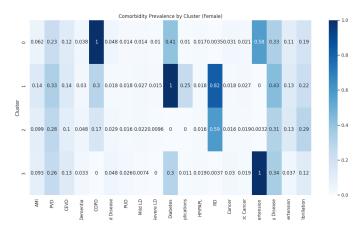


Figure 5: Caption

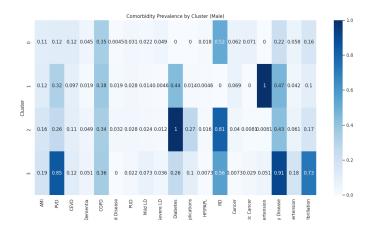


Figure 6: Caption

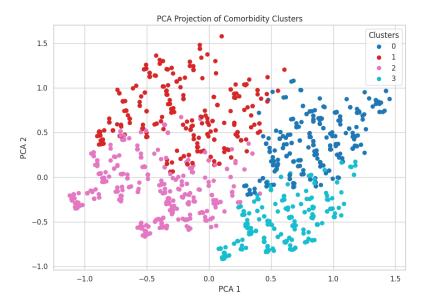


Figure 7: Caption

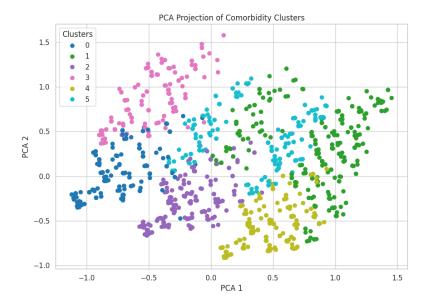


Figure 8: Caption

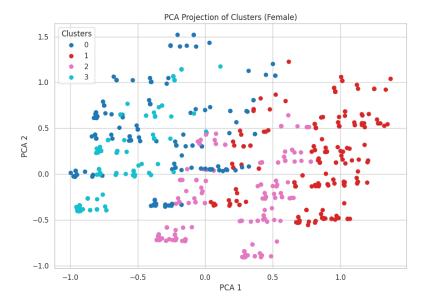


Figure 9: Caption

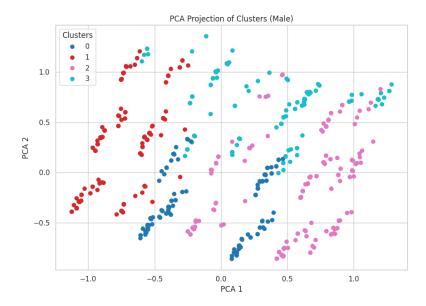


Figure 10: Caption

learning rate of 0.0001. For the forecasting tasks different back horizons and forecast windows were used and analysed. To evaluate the DL models two metrics were used: symmetric mean absolute percentage error (sMAPE) and root mean squared error (RMSE), where lower scores indicated a better predictive performance. The best performing model was then used for the counterfactual generation.

Counterfactual Generation: For the counterfactual generation four different models have been used, all following a similar implementation. First two subsets of test samples were selected using two thresholds. This way, the samples were divided into a hyperglycemia set (blood glucose levels $\geq 180~\text{mg/dL}$) and a hypoglycemia set (blood glucose levels $\leq 70~\text{mg/dL}$) and then the following procedure was used:

- Bound Generation: Polynomial-based upper and lower bounds were generated for each test sample's predicted output, targeting desired glucose thresholds within a given window.
- Gradient Perturbation: For each forecasting model, the model was inverted by optimizing
 the exogenous inputs via gradient descent to steer the predicted output within the
 generated bounds.
- Loss Function: A custom loss function was used to penalize deviation from the bounds, and gradients were approximated using automatic differentiation or finite differences depending on model compatibility.

The models used for the counterfactual generation span both traditional statistical methods and deep learning architectures.

SARIMAX: The Seasonal Autoregressive Integrated Moving Average with Exogenous Variables (SARIMAX) model was employed to account for seasonality and external factors. Model parameters, including the order of autoregression (p), differencing (d), and moving average (q), were selected based on the Akaike Information Criterion (AIC). Exogenous inputs such as

insulin dosage and carbohydrate intake were incorporated as regressors, and model parameters were optimized using maximum likelihood estimation.

OLS: Ordinary Least Squares (OLS) regression was used to examine linear relationships between exogenous variables and the target series. Feature engineering involved the creation of time-lagged variables and interaction terms between insulin and carbohydrate intake. To mitigate overfitting, regularization was applied. Additionally, linear constraints on exogenous variables were enforced post-hoc to facilitate counterfactual generation.

GRU: A Gated Recurrent Unit (GRU) network was implemented. The GRU architecture consisted of two layers, each with 128 hidden units, and dropout regularization set at 0.2 to prevent overfitting. The network was trained using the Adam optimizer with an initial learning rate of 0.001, which was reduced by a factor of 0.1 if the validation loss plateaued over five epochs. Counterfactual explanations were generated by computing gradients of the output with respect to exogenous inputs, enabling identification of minimal interventions.

NBEATS: The NBEATSx model was utilized, extending on the standard N-BEATS architecture by incorporating exogenous variables into its forecasting blocks. The model employed trend and seasonality decomposition through fully connected layers, and included exogenous inputs such as carbohydrate intake, insulin dosage, and physical activity. Quantile loss was used during training to capture distributional uncertainty, and feature importance analyses were performed to assess the contribution of exogenous variables to forecast accuracy.

2.3.3 Evaluation Metrics

To evaluate the quality of the counterfactual interventions, multiple evaluation metrics were implemented. First, traditional forecasting performance was measured using Root Mean Squared Error (RMSE) and Symmetric Mean Absolute Percentage Error (sMAPE), giving a quantitative assessment of prediction accuracy across the forecast horizon. For the evaluation of counterfactual forecasts, several additional metrics were introduced. The average value of change quantifies the magnitude of adjustments made to the exogenous variables in order to achieve the desired forecasted outcome. The fraction of values to change captures the proportion of exogenous variable entries that required modification, offering insight into the sparsity of the interventions. To further characterize the nature of the interventions, the Severity of change metric measures the relative intensity of the modifications compared to the original values. Additionally, the fitting of predictions within bounds was evaluated, reflecting the extent to which the counterfactual predictions adhered to the predefined upper and lower target constraints. This was done using the euclidean distance of the predicted target to the bounds. Finally, to ensure the plausibility of the counterfactual scenarios, the modified exogenous variable profiles were compared to reference profiles from healthy patients. This comparison provides a qualitative and quantitative check on the biological or clinical realism of the generated counterfactual forecasts. RMSE, sMAPE scores sum of MSE scores, normalize for horizon? Average value of change average of orig against average of new Fraction of values to change how many of the timepoints stay the same/change Severity of change outlier score, LOF-score compare original exog to changed prediction Fitting of predictions in bounds how good is the prediction, one in the band better than others? Compare exogenous variables to those of a healthy patient what are the differences in exog? changes from healthy patient

3 Results

3.1 Multivariate Forecasting

3.1.1 OhioT1DM

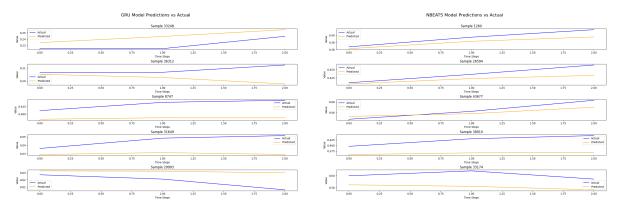
3.1.2 SimGlucose

3.1.3 MIMIC

The results of the evaluation of the multivariate forecasting can be seen in table 3. It shows the quality of the forecast using the sMAPE and RMSE score, for the two different models and the different datasets. Figure 11 and Figure 12 show some corresponding examples to show the correctness of the forecasting results for the OhioT1DM dataset, while Figure 14 and Figure 13 show the same for the SimGlucose dataset.

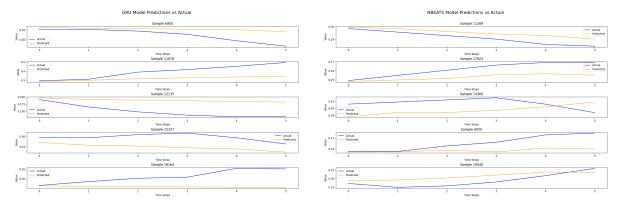
Table 3: Multivariate forecasting training metrics.

Dataset	Back Horizon	Horizon	Model	sMAPE	RMSE
OhioT1DM	6	3	GRU	3.7648	9.3329
			NBEATS	3.1741	9.1723
	12	6	GRU	6.2525	14.8269
			NBEATS	6.1397	14.3862
SimGlucose	6	3	GRU	0.4699	1.9799
			NBEATS	0.4017	1.6730
	12	6	GRU	0.9970	4.3754
			NBEATS	0.9904	3.6312
	40	10	GRU	1.5436	5.6069
			NBEATS	1.4608	3.0223



(a) Results of the multivariate forecasting using (b) Results of the multivariate forecasting using GRU. NBEATS.

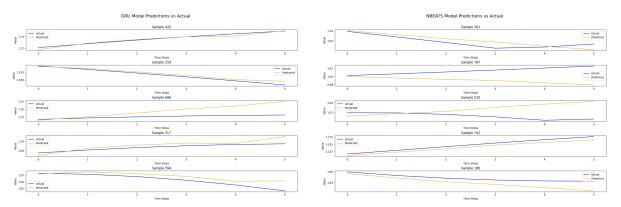
Figure 11: Results of the multivariate forecasting for the OhioT1DM dataset with back horizon = 6 and forecast horizon = 3, showing the accuracy of the forecasting.



(a) Results of the multivariate forecasting using (b) Results of the multivariate forecasting using GRU.

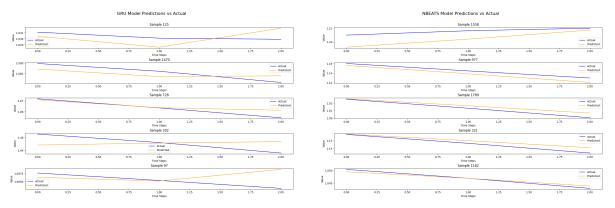
NBEATS.

Figure 12: Results of the multivariate forecasting for the OhioT1DM dataset with back horizon = 12 and forecast horizon = 6, showing the accuracy of the forecasting.



(a) Results of the multivariate forecasting using (b) Results of the multivariate forecasting using GRU. NBEATS.

Figure 13: Results of the multivariate forecasting for the SimGlucose dataset with back horizon = 12 and forecast horizon = 6, showing the accuracy of the forecasting.



(a) Results of the multivariate forecasting using (b) Results of the multivariate forecasting using GRU. NBEATS.

Figure 14: Results of the multivariate forecasting for the SimGlucose dataset with back horizon = 6 and forecast horizon = 3, showing the accuracy of the forecasting.

- 3.2 Counterfactuals
- 3.2.1 OhioT1DM
- 3.2.2 SimGlucose
- 3.2.3 MIMIC
- 3.3 Measurements
- 3.3.1 Average value of change
- 3.3.2 Fraction of values to change
- 3.3.3 Severity of change
- 3.3.4 Target prediction within bounds
- 3.3.5 Comparison to healthy patient

Comorbidities Threshold 0.3: General k=4: Comorbidity prevalence per cluster: AMI PVD CEVD Dementia COPD Rheumatoid Disease cluster 0 0.093702 0.273425 0.125960 0.030722 0.376344 0.033794 1 0.075515 0.141876 0.098398 0.041190 0.386728 0.036613 2 0.113523 0.133556 0.108514 0.036728 0.307179 0.023372 3 0.218289 0.849558 0.138643 0.053097 0.401180 0.008850

PUD Mild LD Moderate/Severe LD Diabetes cluster 0 0.023041 0.009217 0.001536 0.376344 1 0.009153 0.027460 0.034325 0.302059 2 0.028381 0.018364 0.016694 0.569282 3 0.026549 0.050147 0.014749 0.560472

Metastatic Cancer Hypertension Coronary Artery Disease cluster 0 0.012289 1.000000 0.400922 1 0.036613 0.000000 0.194508 2 0.028381 0.001669 0.252087 3 0.020649 0.032448 0.920354 Pulmonary Hypertension Atrial Fibrillation cluster 0 0.046083 0.109063 1 0.144165 0.306636 2 0.055092 0.115192 3 0.179941 0.525074

Most prevalent comorbidities per cluster:

Cluster 0 (651 patients): - Hypertension: 100.0- Coronary Artery Disease: 40.1- COPD: 37.6-Diabetes: 37.6

Cluster 1 (437 patients): - COPD: 38.7- Atrial Fibrillation: 30.7- Diabetes: 30.2

Cluster 2 (599 patients): - RD: 100.0- Diabetes: 56.9- COPD: 30.7

Cluster 3 (339 patients): - Coronary Artery Disease: 92.0- PVD: 85.0- RD: 74.0- Diabetes: 56.0- Atrial Fibrillation: 52.5- COPD: 40.1

General k=6: Comorbidity prevalence per cluster: AMI PVD CEVD Dementia COPD Rheumatoid Disease cluster 0 0.063536 0.240331 0.080110 0.016575 0.124309 0.016575 1 0.163462 0.397436 0.128205 0.035256 0.362179 0.035256 2 0.139752 0.357143 0.121118 0.086957 0.288820 0.021739 3 0.220386 0.418733 0.146006 0.038567 0.603306 0.022039 4 0.051680 0.237726 0.124031 0.028424 0.377261 0.031008 5 0.060714 0.135714 0.100000 0.028571 0.421429 0.039286

PUD Mild LD Moderate/Severe LD Diabetes cluster 0 0.024862 0.016575 0.011050 0.367403 1 0.022436 0.009615 0.000000 0.439103 2 0.027950 0.049689 0.046584 0.347826 3 0.022039

0.022039 0.005510 0.887052 4 0.023256 0.010336 0.002584 0.346253 5 0.010714 0.032143 0.032143 0.250000

Metastatic Cancer Hypertension Coronary Artery Disease cluster 0 0.046961 0.000000 0.154696 1 0.009615 0.868590 1.000000 2 0.018634 0.012422 0.409938 3 0.008264 0.002755 0.760331 4 0.018088 1.000000 0.000000 5 0.042857 0.000000 0.117857

Pulmonary Hypertension Atrial Fibrillation cluster 0 0.046961 0.000000 1 0.067308 0.105769 2 0.298137 1.000000 3 0.041322 0.146006 4 0.038760 0.113695 5 0.082143 0.000000 Most prevalent comorbidities per cluster:

Cluster 0 (362 patients): - RD: 100.0- Diabetes: 36.7

Cluster 1 (312 patients): - Coronary Artery Disease: 100.0- Hypertension: 86.9- Diabetes: 43.9-PVD: 39.7- COPD: 36.2

Cluster 2 (322 patients): - Atrial Fibrillation: 100.0- RD: 45.0- Coronary Artery Disease: 41.0-PVD: 35.7- Diabetes: 34.8

Cluster 3 (363 patients): - RD: 94.2- Diabetes: 88.7- Coronary Artery Disease: 76.0- COPD: 60.3- PVD: 41.9

Cluster 4 (387 patients): - Hypertension: 100.0- COPD: 37.7- Diabetes: 34.6

Cluster 5 (280 patients): - COPD: 42.1

Male: Comorbidity prevalence per cluster: AMI PVD CEVD Dementia COPD Rheumatoid Disease cluster 0 0.111607 0.116071 0.116071 0.044643 0.348214 0.004464 1 0.115741 0.324074 0.097222 0.018519 0.379630 0.018519 2 0.161943 0.259109 0.105263 0.048583 0.344130 0.032389 3 0.189781 0.846715 0.116788 0.051095 0.357664 0.000000

PUD Mild LD Moderate/Severe LD Diabetes cluster 0 0.031250 0.022321 0.049107 0.000000 1 0.027778 0.013889 0.004630 0.439815 2 0.028340 0.024291 0.012146 1.000000 3 0.021898 0.072993 0.036496 0.255474

Diabetes + Complications HP/PAPL RD Cancer cluster 0 0.000000 0.017857 0.517857 0.062500 1 0.013889 0.004630 0.000000 0.069444 2 0.271255 0.016194 0.809717 0.040486 3 0.102190 0.007299 0.562044 0.007299

Metastatic Cancer Hypertension Coronary Artery Disease cluster 0 0.071429 0.000000 0.218750 1 0.000000 1.000000 0.467593 2 0.008097 0.008097 0.425101 3 0.029197 0.051095 0.912409 Pulmonary Hypertension Atrial Fibrillation cluster 0 0.058036 0.160714 1 0.041667 0.101852 2 0.060729 0.170040 3 0.182482 0.729927

Most prevalent comorbidities per cluster:

Cluster 0 (224 patients): - RD: 51.8- COPD: 34.8

Cluster 1 (216 patients): - Hypertension: 100.0- Coronary Artery Disease: 46.8- Diabetes: 44.0- COPD: 38.0- PVD: 32.4

Cluster 2 (247 patients): - Diabetes: 100.0- RD: 81.0- Coronary Artery Disease: 42.5- COPD: 34.4

Cluster 3 (137 patients): - Coronary Artery Disease: 91.2- PVD: 84.7- Atrial Fibrillation: 73.0-RD: 56.2- COPD: 35.8

Female: Comorbidity prevalence per cluster: AMI PVD CEVD Dementia COPD Rheumatoid Disease cluster 0 0.062284 0.231834 0.124567 0.038062 1.000000 0.048443 1 0.138973 0.329305 0.138973 0.030211 0.299094 0.018127 2 0.099359 0.278846 0.102564 0.048077 0.166667 0.028846 3 0.092593 0.255556 0.125926 0.033333 0.000000 0.048148

PUD Mild LD Moderate/Severe LD Diabetes cluster 0 0.013841 0.013841 0.010381 0.408304 1 0.018127 0.027190 0.015106 1.0000000 2 0.016026 0.022436 0.009615 0.000000 3 0.025926 0.007407 0.000000 0.303704

Diabetes + Complications HP/PAPL RD Cancer cluster 0 0.010381 0.017301 0.003460 0.031142 1 0.247734 0.018127 0.824773 0.018127 2 0.000000 0.016026 0.589744 0.016026 3 0.011111 0.018519 0.003704 0.029630

Metastatic Cancer Hypertension Coronary Artery Disease cluster 0 0.020761 0.577855 0.328720 1 0.027190 0.000000 0.432024 2 0.019231 0.003205 0.314103 3 0.018519 1.000000 0.344444 Pulmonary Hypertension Atrial Fibrillation cluster 0 0.107266 0.186851 1 0.126888 0.223565 2 0.134615 0.294872 3 0.037037 0.118519

Most prevalent comorbidities per cluster:

Cluster 0 (289 patients): - COPD: 100.0- Hypertension: 57.8- Diabetes: 40.8- Coronary Artery Disease: 32.9

Cluster 1 (331 patients): - Diabetes: 100.0- RD: 82.5- Coronary Artery Disease: 43.2- PVD: 32.9

Cluster 2 (312 patients): - RD: 59.0- Coronary Artery Disease: 31.4

Cluster 3 (270 patients): - Hypertension: 100.0- Coronary Artery Disease: 34.4- Diabetes: 30.4

4 Discussion

- 4.1 Results
- 4.2 Limitations
- 4.3 Future Work
- 5 Conclusion

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