# Computation of MSA-Level Wage Premia

### Project Workflow Automation

June 3, 2025

### 1 Introduction

This document outlines the methodology used to compute MSA-level wage premia based on ACS data. The goal is to estimate the extent to which wages in different Metropolitan Statistical Areas (MSAs) differ after controlling for individual worker characteristics.

### 2 Data Source

The primary data source for this analysis is a Stata file ('extract19.dta') containing pooled cross-sections from the American Community Survey (ACS) for the years 2005-2023. Key variables utilized from this dataset include:

- incwage: Individual's annual wage and salary income.
- wkswork1: Weeks worked last year.
- uhrswork: Usual hours worked per week.
- perwt: Person weight.
- age: Age of the individual.
- sex: Sex of the individual.
- race: Race of the individual.
- educ: Educational attainment of the individual.
- met2013: Metropolitan Statistical Area identifier (CBSA 2013 definition).
- year: Survey year.

## 3 Methodology

### 3.1 Hourly Wage Calculation

First, an hourly wage is computed for each individual i as:

$$\text{wage\_hr}_i = \frac{\text{incwage}_i}{\text{wkswork1}_i \times \text{uhrswork}_i} \tag{1}$$

Individuals with non-positive or non-finite hourly wages are excluded from the analysis. The natural logarithm of the hourly wage is then taken:

$$ln(w_i) = log(wage_hr_i)$$
(2)

#### 3.2 Regression Model

For each year t from 2005 to 2023, the following regression model is estimated using Ordinary Least Squares (OLS), weighted by perwt:

$$\ln(w_{ijmt}) = \beta_0 + \beta_1 \operatorname{age}_{it} + \beta_2 \operatorname{age}_{it}^2 + \mathbf{X}'_{it}\gamma + \alpha_{mt} + \epsilon_{ijt}$$
(3)

where:

- $w_{ijmt}$  is the hourly wage of individual i in MSA m in year t.
- age<sub>it</sub> and age<sup>2</sup><sub>it</sub> control for age in a quadratic form.
- $\mathbf{X}_{it}$  is a vector of dummy variables for individual characteristics: sex, race, and educational attainment.  $\gamma$  is the corresponding vector of coefficients.
- $\alpha_{mt}$  represents the fixed effect for MSA m in year t. These are the key parameters of interest.
- $\epsilon_{ijt}$  is the error term.

The model is specified in 'fixest::feols' syntax as:

lnw ~ age + I(age extasciicircum2) + factor(sex) + factor(race) + factor(educ) | met2013 This effectively means that met2013 (representing  $\alpha_{mt}$ ) captures the average log-wage difference for MSA m in year t relative to a baseline MSA (omitted by the estimation procedure), after controlling for the specified individual characteristics.

### 3.3 Wage Premia

The estimated fixed effects,  $\hat{\alpha}_{mt}$ , are interpreted as the skill-adjusted log-wage premia for each MSA m in year t. These are denoted as fe\_adj\_lnw in the output data.

These log-wage premia ( $\mathtt{fe\_adj\_lnw}_{mt}$ ) represent the component of wages attributable to geographic location (MSA) after accounting for differences in the observable skill composition of the workforce across MSAs.

### 4 Output

The primary output containing these premia is data/output/msa\_wage\_premia\_2005\_2023\_simplified.csv. This file includes met2013, year, and fe\_adj\_lnw, among other variables.