

```
import time
```

```
#Variable Initalization
```

```
def attack1(e, n, C):                                     # This attack 1
function will begin by taking three parameters e n and C it will then progress to
compute i such that  $i^e \bmod n = C$ '
    time_start = time.time()                             # Imported from the
time libairy this will keep track of how long the attack has taken to create these
lists
```

```
    found = False                                         #Initalizes found
to false and i to 0 to begin from couting i from 0
    i = 0
```

```
    while not found:                                     #This while loop
will remain true until found is equal to true, found will equal true once the value
of i is computed with  $M = i^e \bmod n$  to be queal to C ( $M == C$ ) this will ensure you
have found the correct i within the equation
```

```
        i += 1
        M = pow(i, e, n)                                #pow function will
return the value of i to the power of e and since there is a third value present it
will return i to the power e with modulus n
        if M == C:
            found = True
```

```
    time_end = time.time()
```

```
    return i, time_end - time_start
```

```
def attack2(e, n, C):                                     # Attack2 too
will take in same parameters as 1 but it will utalize the facrotize funtion to find
factors p and q of n it will then compute  $\phi = (p-1) * (q-1)$ 
```

```
    time_start = time.time()                             # Next this
function will call find_d in order to find the value d which satisfies  $d * e \bmod \phi = 1$ . After success it will compute  $M = C^d \bmod n$ 
```

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and inefficient modular exponentiation algorithm it i will brute force through and
return p q d and M
```

```
    p, q = factorize(n)
    phi = (p-1) * (q -1)
    d = find_d(e, phi)
```

```
    M = pow(C , d, n)                                     # Naive and
inefficient modular exponentiation
```

```
    time_end = time.time()
    return f"{p, q, d, M}, {time_end - time_start}"
```

```
def factorize(n):                                         # Takes in integer
parameter n and will return the two factors of i and  $n//i$  where i is the smallest
factor of  $n > 1$ 
```

```
    for i in range(2, n):
        if n % i == 0:
```

```

        return i, n//i                                # Returns the
current value of i and then the integral result with the discarded remainder

def find_d(e, phi):                                    # Takes in two
parameters e and phi returns an integer value d such that  $d * e \bmod \phi = 1$ , by
iterating over values of d from 2 to phi and checking if  $(d * e) \bmod \phi = 1$  and if
so return d
    for d in range(2, phi):
        if (d*e) % phi == 1:
            return d

# #a and b with attack1
a1_1 = attack1(e = 3, n = 15, C = 8)
a2_1 = attack1(e = 13, n = 527, C = 152)

# #a and b with attack2
a_1_2 = attack2(e = 3, n = 15, C = 8)
a_2_2 = attack2(e = 13, n = 527, C = 152)

#Guess and check c for attack1 and attack2
#Attack 1
a3_1 = attack1(e = 445, n = 51500, C = 43)

#Attack 2
a3_2 = attack2(e = 445, n = 51500, C = 300)

print(" Attack 1: ", "e = 3, n = 15, C = 8 :", a1_1, "\n ",          "e = 13, n
= 527 , C = 152 : ", a2_1, "\n\n", " Attack 2: ", "e = 3, n = 15, C = 8 : ", a_1_2,
"\n" ,
        "e = 13, n = 527 , C = 152 : ", a_2_2)
print("-----")
print(" Part C Guess Attack 1: ", "e = 445, n = 51500, C = 43 : ", a3_1, "\n", "
Part C Guess Attack 2: ", "e = 445, n = 51500, C = 300 : ", a3_2  )

#===== Guess and Check Part C Work
=====#
#Values with resonable results
# e = 12 , n = 534, C = 4 // Results: (4,0.0)
# e = 445, n = 51500, C = 43 // Attack 1: (4823, 0.0039899349212646484)
# Attack 1: (123, 0.0)
# Attack 1: (43, 0.0)
# Attack 1: (123, 0.0)
#

```

```

#Values that did not work

```

#Attack 1

```
# e = 18, n = 661, C = 252
# e = 12, n = 528, C = 100
# e = 12, n = 20, C = 100
# e = 12, n = 54, C = 56
# e = 12, n = 534, C = 4
# e = 12, n = 528, C = 173
# e = 12, n = 3, C = 321
# e = 12, n = 534, C = 4
# e = 12, n = 528, C = 173
# e = 12, n = 54, C = 56
# e = 12, n = 534, C = 4
# e = 12, n = 528, C = 173
# e = 445, n = 51500, C = 42
# e = 445, n = 323, C = 43
#e =
```

#Attack 2

```
# e = 24, n = 771, C = 420
# e = 16, n = 771, C = 300
# e = 12, n = 54, C = 56
# e = 12, n = 334, C = 4
# e = 12, n = 451, C = 173
# e = 12, n = 543, C = 321
# e = 12, n = 5321, C = 4
# e = 12, n = 528, C = 173
# e = 12, n = 54, C = 56
# e = 12, n = 534, C = 4
# e = 12, n = 528, C = 173
# e = 445, n = 51500, C = 42
# e = 445, n = 323, C = 43
```