

### Problem 3:

Calculate all verification conditions generated by the following annotated specification

```
{x = n}
y:=1;
  while x!= 0 do
    invariant x! * y = n!
    y:=y*x;
    x:=x-1
{x = 0 ∧ y = n!}
```

Precondition {x=n}

- This specifies the initial condition where 'x' is equal to 'n'

Postcondition {x = 0 ∧ y = n!}

- This specifies the final state of the program where 'x=0' and 'y=n'

The Loop variant hold true at the beginning of the Programm and after each while-loop

1. After the first while loop
  - verification condition: because 'x = n' ->  $x! * y = n! * 1 = n!$
2. Inside the while loop
  - verification condition:  $x! * y = n! \wedge x \neq 0 \rightarrow (x-1)! * (y * x) = (x-1)! * n = (n-1)! * n = n!$
3. After the while loop
  - Verification condition:  $x! * y = n! \wedge x = 0 \rightarrow y = n!$
  - This condition is valid because it ensures that the loop terminates ('x' become 0) and 'y' is equal to 'n!'

➔ All the conditions generate by the annotated specification are valid