Project 1: Implementing Algorithms

Group members

Andrew Lau - andrewlau2019@csu.fullerton.edu Tommy Le - tommyle@csu.fullerton.edu

Pseudocode for lawnmower

```
def sort_lawnmower() {
   int swap = 0
  for i = 0 to (n+1)/2 step 1 do
      for j = 0 to 2n - 1 step 1 do
         if(get(j) == DISK_DARK && get(j+1) == DISK_LIGHT)
            then swap(j)
                 swap++
         endif
      endfor
      for j = 2n - 1 to 0 step -1 do
         if(get(j) == DISK_LIGHT && get(j - 1) == DISK_DARK)
            then swap(j-1)
                 swap++
         endif
      endfor
   endfor
   return(swap)
}
```

Pseudocode for Alternate

Step Count for lawnmower

```
def sort lawnmower() {
   int swap = 0
                                                                         // 1 tu
   for i = 0 to (n+1)/2 step 1 do
                                                   //[(n+1)/2 - 1 = (n-1)/2]
                                                   ((n-1)/2 - 0/1) + 1 = (n+1)/2 times
      for j = 0 to 2n - 1 step 1 do
                                                       //[2n-1 - 1 = 2n-2]
                                                          ((2n-2 - 0/1) + 1 = 2n - 1 \text{ times})
          if(get(j) == DISK DARK && get(j+1) == DISK LIGHT)
                                                                        // 14 tu
                                                                         // 9 tu
             then swap(j)
                   swap++
                                                                         // 1 tu
          endif
      endfor
      for j = 2n - 1 to 0 step -1 do
                                                            //[0 - 1 = -1/-1 = 1]
                                                          ((1 - (2n-1)/-1) + 1 = 2n - 1 \text{ times})
          if(get(j) == DISK_LIGHT && get(j-1) == DISK_DARK)
                                                                        // 14 tu
             then swap(j-1)
                                                                         // 10 tu
                                                                         // 1 tu
                   swap++
          endif
      endfor
   endfor
   return(swap)
}
void swap(size t left index) {
  assert(is index(left index));
                                                   // 3 tu
  auto right index = left index + 1;
                                                   // 2 tu
  assert(is index(right index));
                                                   // 3 tu
  std::swap( colors[left index], colors[right index]);
                                                                 // 1 tu
 }
                                                                  Total: 3 + 2 + 3 + 1 = 9 tu
bool is index(size t i) const {
  return (i < total count()); // 2 tu
 }
size t total count() const {
```

```
return _colors.size(); // `1 tu
 }
disk color get(size t index) const {
  assert(is_index(index));
                                          // 3 tu
  return _colors[index];
 }
SC = 1 * (n+1)/2 * [(2n-1) * (14 + 9 + 1)] * [(2n-1) * (14 + 10 + 1)]
       = 1 * (n+1)/2 * ([(2n-1) * 24] + [(2n-1) * (25)]) = 1 * (n+1)/2 * [48n-24 + 50n -25]
       = (n+1)/2 * [98n-49] = 49n^2 + 49n/2 - 49/2
Proof
49n^2 + 49n/2 - 49/2 \in O(n^2)
Lim n->infinity f(n)/g(n) = L
Lim n-> infinity (49n^2 + 49n/2 - 49/2)/(n^2)
Lim n-> infinity (49n^2/n^2) + (49n/2/n^2) + (49/2/n^2)
Lim n-> infinity 49 + Lim n-> infinity 49n^3/2 + Lim n-> infinity 49n^2/2
49 + 0 + 0 = 49
49 >= 0 therefore 49n^2 + 49n/2 + 49/2 \in O(n^2)
```

Step Count for Alternate

```
def sort alternate() {
   int swap = 0
                                                                        // 1 tu
   for i = 0 to n + 1 step 1 do
      for j = i % 2 to 2n - 1 step 2 do
         if(get(j) == DISK DARK && get(j+1) == DISK LIGHT)
                                                                        // 14 tu
                                                                        // 9 tu
             then swap(j)
                  swap++
                                                                        // 1 tu
          endif
      endfor
   endfor
   return(swap)
}
S.C = \sum_{n=0}^{\infty} \sum_{n=0}^{\infty} \{step \ 2\} \ 24 = 24 * [(2n-2-0/2) + 1] * [(n-0/1) + 1] = 24 * (n)
(n+1) = 24n (n+1) = 24n^2 + 24n
Proof
24n^2 + 24n \in O(n^2)
Lim n->infinity f(n)/g(n) = L
Lim n->infinity (24n^2 + 24n)/n^2
Lim n->infinity 24 + Lim n-> infinity 24/n
24 + 0 = 24
Since it is a constant and it's greater than 0, therefore 24n^2 + 24n \in O(n^2)
```

