```
In [1]:
         import itertools # product()
         import numpy as np
         import qutip
         import qutip.states
         import tomographer
         import tomographer.querrorbars
         import tomographer.jpyutil
         from IPython.display import display, Markdown
In [2]:
         rho target Bell = qutip.states.ket2dm(qutip.Qobj(np.array([0,1,1j,0]/np.sqr
         t(2))))
         display(Markdown('rho target Bell = '))
         display(rho target Bell)
         # The data below were simulated from the following true state:
         rho_sim = 0.95*rho_target_Bell + 0.05*qutip.qeye(4)/4;
         display(Markdown('rho_sim = '))
         display(rho_sim)
         rho target Bell =
         Quantum object: dims = [[4], [4]], shape = [4, 4], type = oper, isherm = True
           0.0
                  0.0
                           0.0
                                   0.0
           0.0
                 0.500
                         -0.500j
                                   0.0
                0.500j
                          0.500
           0.0
                                   0.0
           0.0
                  0.0
                           0.0
                                   0.0
         rho sim =
         Quantum object: dims = [[4], [4]], shape = [4, 4], type = oper, isherm = True
           0.013
                    0.0
                              0.0
                                       0.0
            0.0
                   0.487
                           -0.475j
                                       0.0
            0.0
                   0.475j
                             0.487
                                       0.0
            0.0
                                      0.013
                    0.0
                              0.0
```

```
In [3]: # All POVM effects when measuring Pauli X, Y, or Z on a single qubit
        MeasEffects1Qubit = [ [
                np.array([[.5, .5],[.5, .5]]),
                                                   # X, +1 outcome
                                                 # X, -1 outcome
                np.array([[.5, -.5],[-.5, .5]]),
                np.array([[.5, -.5j],[.5j, .5]]), # Y, +1 outcome
                np.array([[.5, .5j],[-.5j, .5]]), # Y, -1 outcome
                np.array([[1,0],[0,0]]),
                                                   # Z, +1 outcome
                np.array([[0,0],[0,1]]),
                                                   # Z, -1 outcome
            ]
        ]
        # Listing of all POVM effects of product Paulis on two qubits (with individ
        ual outcomes on each qubit)
        Emn = [ None ] * 36 # prepare 36 elements
        for i in range(3):
            for j in range(3):
                for s in range(2):
                    for t in range(2):
                        idx = j*3*2*2 + i*2*2 + t*2 + s
                        Emn[idx] = np.kron(MeasEffects1Qubit[i][s], MeasEffects1Qub
        it[j][t])
        # These are the measurement counts. Nm[k] is the number of times the POVM e
        ffect
        # Emn[k] was observed. The numbers here were obtained by simulating measure
        ments
        # from the state `rho sim` given above using the described measurement sett
        ings.
        Nm = np.array([
           122,
                         135,
                                138, # counts for XX for outcomes (+1, +1), (+1, -1)
                105,
        ), (-1, +1), (-1, -1)
           248,
                   7,
                          5,
                                240, # counts for XY for outcomes (+1, +1), (+1, -1)
        ), (-1, +1), (-1, -1)
                                148, # counts for XZ for outcomes (+1, +1), (+1, -1)
           102,
                 131,
                        119,
        ), (-1, +1), (-1, -1)
                 252, 240,
                                  1, # counts for YX for outcomes (+1, +1), (+1, -1)
             7,
        ), (-1, +1), (-1, -1)
                                113, # counts for YY for outcomes (+1, +1), (+1, -1)
           125,
                 135, 127,
        ), (-1, +1), (-1, -1)
           140,
                 124, 118,
                                118, # counts for YZ for outcomes (+1, +1), (+1, -1)
        ), (-1, +1), (-1, -1)
           122,
                 119, 135,
                                124, # counts for ZX for outcomes (+1, +1), (+1, -1)
        ), (-1, +1), (-1, -1)
           126,
                                117, # counts for ZY for outcomes (+1, +1), (+1, -1)
                 123, 134,
        ), (-1, +1), (-1, -1)
                                  5, # counts for ZZ for outcomes (+1, +1), (+1, -1)
             9, 233, 253,
        ), (-1, +1), (-1, -1)
        ]);
```

```
In [4]: # An entanglement witness which is appropriate for our target state, as a q
    utip.Qobj
    EntglWitness = (- qutip.qeye(4)
        # how do you "collapse systems together" with qutip?? we could do this
    with np.kron() also...
        - qutip.Qobj(qutip.tensor(qutip.sigmax(),qutip.sigmay()).data,dims=[[4]
        ,[4]])
        + qutip.Qobj(qutip.tensor(qutip.sigmay(),qutip.sigmax()).data,dims=[[4]
        ,[4]])
        - qutip.Qobj(qutip.tensor(qutip.sigmaz(),qutip.sigmaz()).data,dims=[[4]
        ,[4]]) )
        display(EntglWitness)
```

Quantum object: dims = [[4], [4]], shape = [4, 4], type = oper, isherm = True -2.00.00.00.00.0 -2.0i0.0 0.00.0 0.02.0i0.0-2.00.0 0.0 0.0

In [5]: # Value for rho_target_Bell maximally entangled state: +2
display(qutip.expect(EntglWitness, rho_target_Bell))

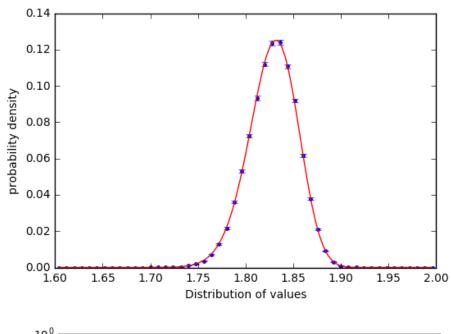
1.99999999999999

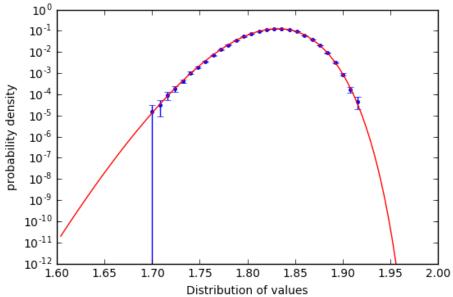
- -1.0
- -2.0
- 0.0

```
In [7]: # Now, we're ready to run our tomography procedure. We'll be estimating
        # the expectation value of the entanglement witness.
        r = None # global variable
        with tomographer.jpyutil.RandWalkProgressBar() as prg:
            r = tomographer.tomorun.tomorun(
                # the dimension of the quantum system
                # the tomography data
                Nm=Nm,
                Emn=Emn,
                # Histogram: values in [1.8, 2.0] split into 50 bins
                hist params=tomographer.UniformBinsHistogramParams(1.6,2,50),
                # Random Walk parameters: step size, sweep size, number of thermali
        zation sweeps, number of live sweeps
                mhrw params=tomographer.MHRWParams(0.009,120,500,32768),
                # figure of merit:
                fig of_merit="obs-value",
                observable=EntglWitness.data.toarray(),
                #num_repeats=12, # default value = auto-detect number of CPU's
                progress_fn=prg.progress_fn
            prg.displayFinalInfo(r['final_report_runs'])
```

```
In [8]: # Collect the histogram
final_histogram = r['final_histogram']
```

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Fit parameters: a2 = 35.6502 a1 = 235.3 m = 41.574 c = 112.619 Quantum Error Bars: f0 = 1.832 Delta = 0.03601 gamma = 0.002452
```





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In [ ]:
```