SOUTHERN UNIVERSITY OF SCIENCE AND TECHNOLOGY
SCHOOL OF MICROELECTRONIC

Lab 6 Frquency Domain Filtering

Student name & ID: *YUAN Tong 11810818*

Course: *LAB Session I* – Professor: *YU Yajun*
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Introduction

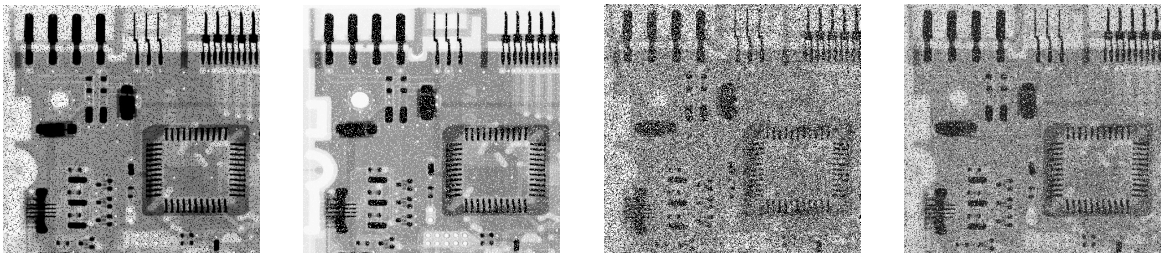
The objective of restoration is to improve a given image in some predefined sense. Compare with image enhancement which is largely a subjective process, image restoration is for the most part an objective process. When we apply image restoring to a degraded image, we will first construct a model about how the image was degraded and then we apply the degrade filter to the restoring filter. After that we could get the reconstructed image, however, we can't build the degrade model precisely and there may be some overlap in frequency domain after the image was degrade, so we can not always restore that image like what it used to be.

In this lab, there are three tasks will be performed.

1. Apply adeptive filter to the image with high noise intensity
2. Apply full inverse filtering, radially limited inverse filtering and Wiener filtering to a image degraded by atomsphere turbulence. Discuss how the parameters, if any, are determined, and the different effects by using the different algorithms.
3. Restore a image degraded by motion blur and noise.

Task I: Adaptive Filter for Image Denoising

Remove the noise from the input images Q6_1_1.tif, Q6_1_2.tif, Q6_1_3.tif and Q6_1_4.tif. Explain your observation and the method used to each of the images, and why such methods are used.



(a) Q6_1_1 (b) Q6_1_2 (c) Q6_1_3 (d) Q6_1_4

Figure 1: Task I, Figures with noise

Analysis. For traditional noise filter in spstial domain, the size of the filter is limited, here comes the problem: if the size of the filter is too small, for areas with hihg noise intensity, the filetr can't reduce all the noise, for example, when a apply a midtern filter to a 3X3 sqare with more than 5 pixels are noise with 255, the midterm will always be the 255, for average filter, the number of the result will be greatly affected by the noise.

To solve this problem, two differnet methods are designed.

Smart filter. The first method is called "smart filter". The filter will analysis the noise situation of the square being filtered, if the noise intensity in the square is high, some pixels in extremely high or low intensity will be removed in future operation. The procedure of the algorithms is shown below.

Algorithm 1: Smart denoise filter

input : The image with noise
output: The denoised image

forall *Pixels in the given image* **do**
  if *Pixels with intensity between (5, 250) is contianed in the image* **then**
    Find the normal pixel most close to the middle
  else
    Calculate the average value
  Assign the value to the related pixels in the output image

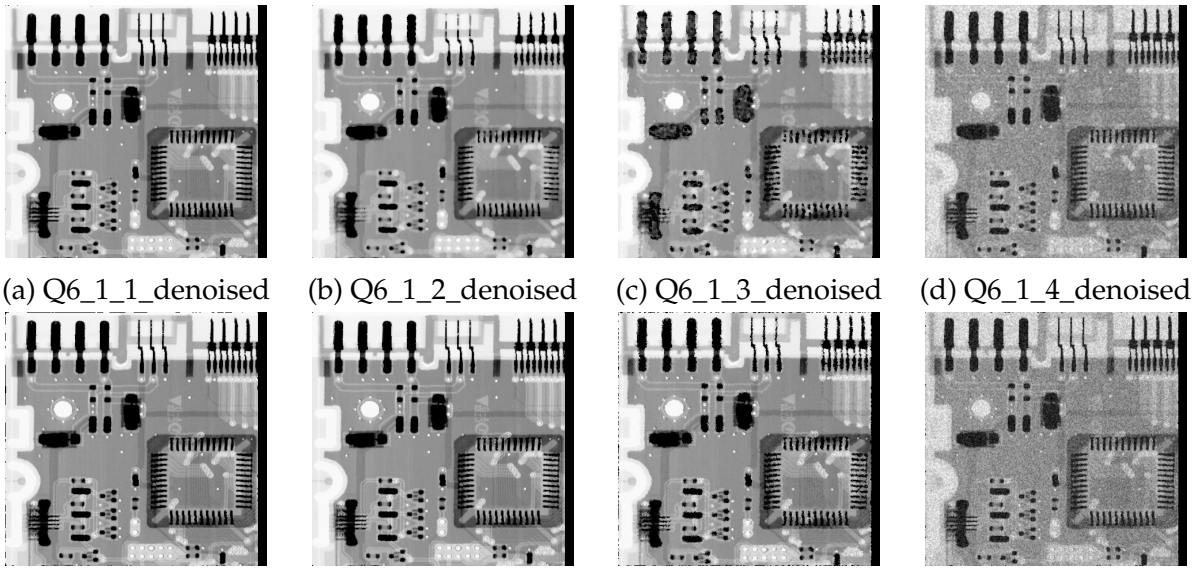
Adaptive filter. In this method, if the given square has high noise intensity, we will expand the size of the filter until the noise intensity in the domain fit our requirement. The procedure is shown below.

Algorithm 2: Smart denoise filter

input : The image with noise, the initial size, the max size
output: The denoised image
S_{xy}: The domain we apply the filter
z_{min}: The minimum intensity value in S_{xy}
z_{max}: The maximum intensity value in S_{xy}
z_{med}: median intensity value in S_{xy}
z_{xy}: intensity value at coordinates (x, y)
S_{max}: maximum allowed size of S_{xy}

forall *Pixels in the given image* **do**
  repeat
    $A_1 = z_{med} - z_{min}$
    $A_2 = z_{med} - z_{max}$
    if $A_1 > 0$ *and* $A_2 < 0$ **then**
      $B_1 = z_{xy} - z_{min}$
      $B_2 = z_{xy} - z_{max}$
      if $B_1 > 0$ *and* $B_2 < 0$ **then**
        output z_{xy}
      else
        output z_{med}
    else
      Increase the size of S_{xy} **if** *size* < S_max **then**
        repeat the loop
      else
        output z_{med}
  until *output is generated*

Result. After applying both filter to the given given image, we obtain the following results



(a) Q6_1_1_denoised (b) Q6_1_2_denoised (c) Q6_1_3_denoised (d) Q6_1_4_denoised

(e) Q6_1_1_adaptive (f) Q6_1_2_adaptive (g) Q6_1_3_adaptive (h) Q6_1_4_adaptive

Figure 2: The first line is denoised by smart denosie filter, the second line is denoised by adaptive filter.

Discussion. From the result we found that, as the intencity of the noise increase, some noise in relatively low frequency domain will remain in the image, that is because the noise have cover most of the information in the image, so some information cannot be restored.

Compare two differnet method, we found that the adaptive filter cause less damage to the details. Previous study had proved that filter with larger size have better ability to reduce the noise but may cause change of some features, the adaptive filter has overcome this problem, provides a method with better noise reducing ability and less image damage.

Task II: Image Restoration

Image Q6_2.tif was degraded from an original image due to the atmosphere turbulence given on slide 65 with k = 0.0025. Restore the original image from the input Q6_2.tif by using full inverse filtering, radially limited inverse filtering and Wiener filtering. Discuss how the parameters, if any, are determined, and the different effects by using the different algorithms.

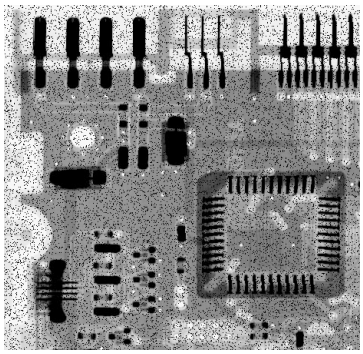


Figure 3: Q6_1_1

Analysis. In this task we will apply three different kinds of inverse filters including full inverse filtering, radially limited inverse filtering and Wiener filtering. Then we will compare the performance of each filter.

full inverse filtering. The image degrade process can be modeled as image filtering process with degrade filter

$$H(u,v)$$

and get result $G(u,v)$, so most directly, the process can be inversed by constructing the inverse filter

$$\frac{1}{H(u,v)}$$

Then the inverse filter will be applied to the degraeded image. Here we have

$$\widehat{F}(u,v) = \frac{G(u,v)}{H(u,v)}$$

In this task we will apply the filters to a image degraded by atmosphere turbulence blur

$$H(u,v) = e^{-k(u-M/2)^2+(v-N/2)^2}$$

with k = 0.0025.

Radially limited inverse filtering. The edge of most of the lowpass is close to 0 so when we apply the inverse filter, due to the error in digital computing and image storing, the noise in high frequency will be greatly enhanced, so to avoid the situation, we will add a cutoff filter, here a Butterworth lowpass function of order 10. This provided a sharp (but smooth) transition at the desired radius.

Wiener filtering. Here we discuss an approach that incorporates both the degradation function and statistical characteristics of noise into the restoration process. So that the image degrading during image storing and computing process can be take into consideration.

The filter can be obtained by the expression

$$\widehat{F}(u,v) = [\frac{1}{H(u,v)} \frac{|H(u,v)|^2}{|H(u,v)|^2 + S_\eta(u,v)/S_f(u,v)}]G(u,v)$$

However for most of the case we can not get the exact value of $S_\eta(u,v)/S_f(u,v)$ which represent the signal noise ratio (SNR) of the image, so we will represent it by K so the expression become

$$\widehat{F}(u,v) = [\frac{1}{H(u,v)} \frac{|H(u,v)|^2}{|H(u,v)|^2 + K}]G(u,v)$$

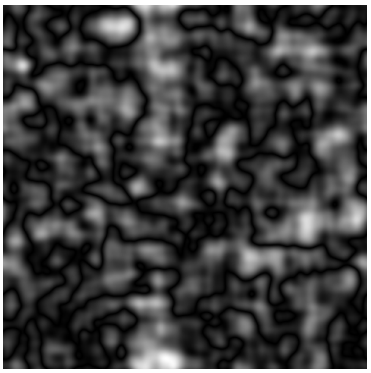
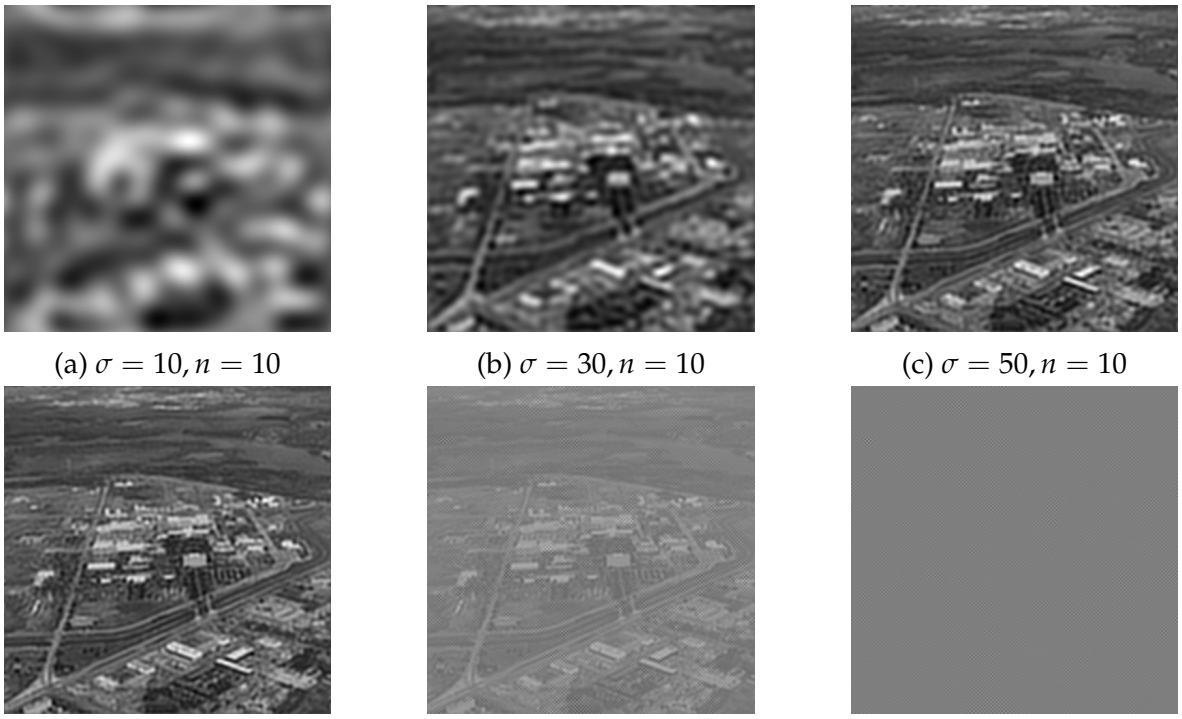


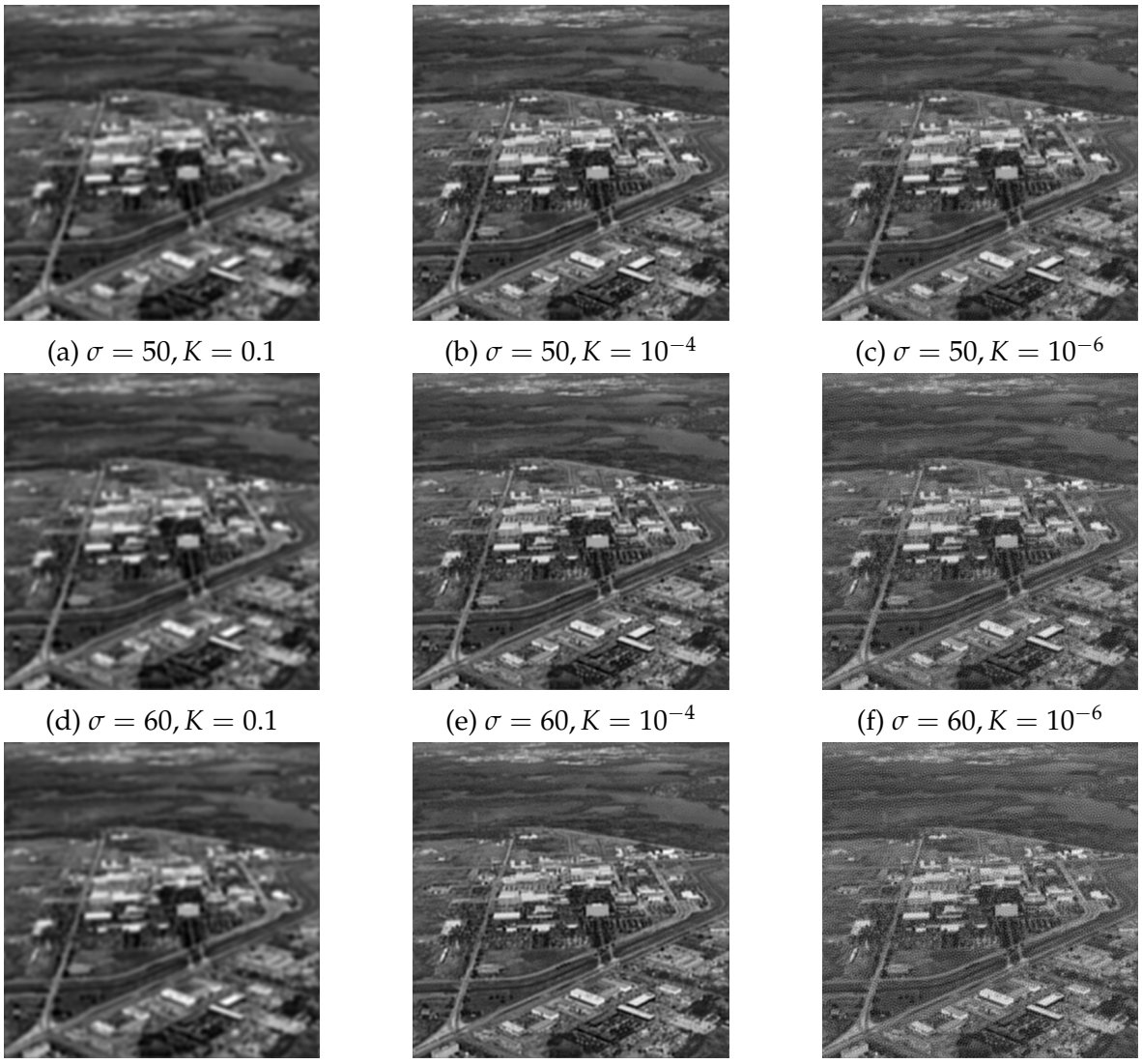
Figure 4: Full inverse filtering



(a) $\sigma = 10, n = 10$ (b) $\sigma = 30, n = 10$ (c) $\sigma = 50, n = 10$

(d) $\sigma = 60, n = 10$ (e) $\sigma = 70, n = 10$ (f) $\sigma = 85, n = 10$

Figure 5: Fitered by redially limited inverse filter



(a) $\sigma = 50, K = 0.1$ (b) $\sigma = 50, K = 10^{-4}$ (c) $\sigma = 50, K = 10^{-6}$

(d) $\sigma = 60, K = 0.1$ (e) $\sigma = 60, K = 10^{-4}$ (f) $\sigma = 60, K = 10^{-6}$

(g) $\sigma = 70, K = 0.1$ (h) $\sigma = 70, K = 10^{-3}$ (i) $\sigma = 70, K = 10^{-6}$

Figure 6: Fitered by wiener filter

Result.

Discussion. The result shows that full inverse filter is mot capable for most of the case due to the error that may occur that we discussed in the Analysis section.

Fig 5 shows that $\sigma = 60$ can be a proper cut off frquency for the filter, when σ keeps increase, the high frequency noise will appear again, when σ keeps decrease, the details in the image will also be filtered.

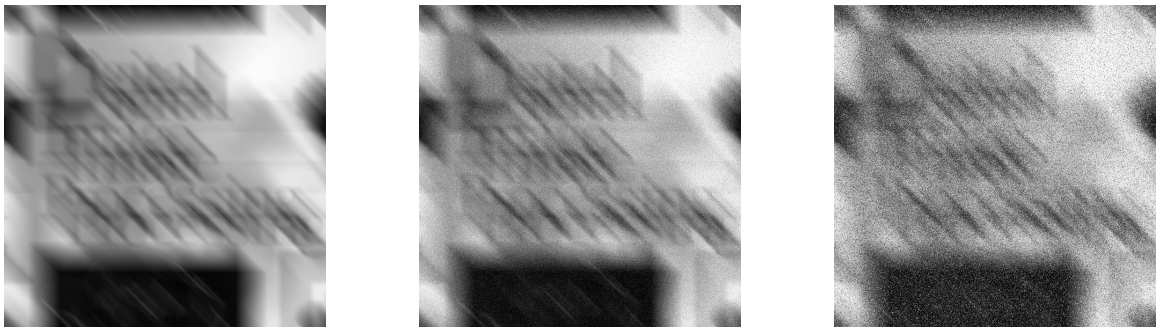
Fig 6 shows that $\sigma = 60, K = 10^{-4}$can be a proper pair to restore the image by wiener filter, comparing between each image in the image set, when K is decreasing, more details in the image will be restored while the noise increase, that because the detail of the image and noise are similar somehow, so when less detail is filtered, less nise will be filtered. The adjustment of σ has been discussed in last paragraph.

Compare between two filters, we found that obviously wiener filter shown better performance, one possiable reason can be that during the store of the image, some information, such as phase, lost, so the inverse filter can't restore the information perfectly. But for wiener filter, such kind of information loss can be treated as noise and

can be reduced.

Task III: Motion Debluring

Restore the original images from the inputs Q6_3_1.tif, Q6_3_2.tif and Q6_3_3. Explain your observation and the method used.



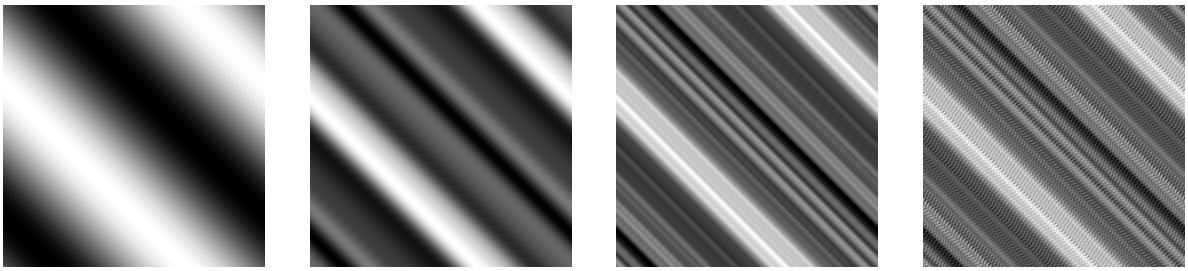
(a) Q6_3_1 (b) Q6_3_2 (c) Q6_3_3

Figure 7: Task III, Figures with motion blur

Analysis. In this task we will reconstruct the image degraded by motion blur and noise. The motion blur can be expressed as filter

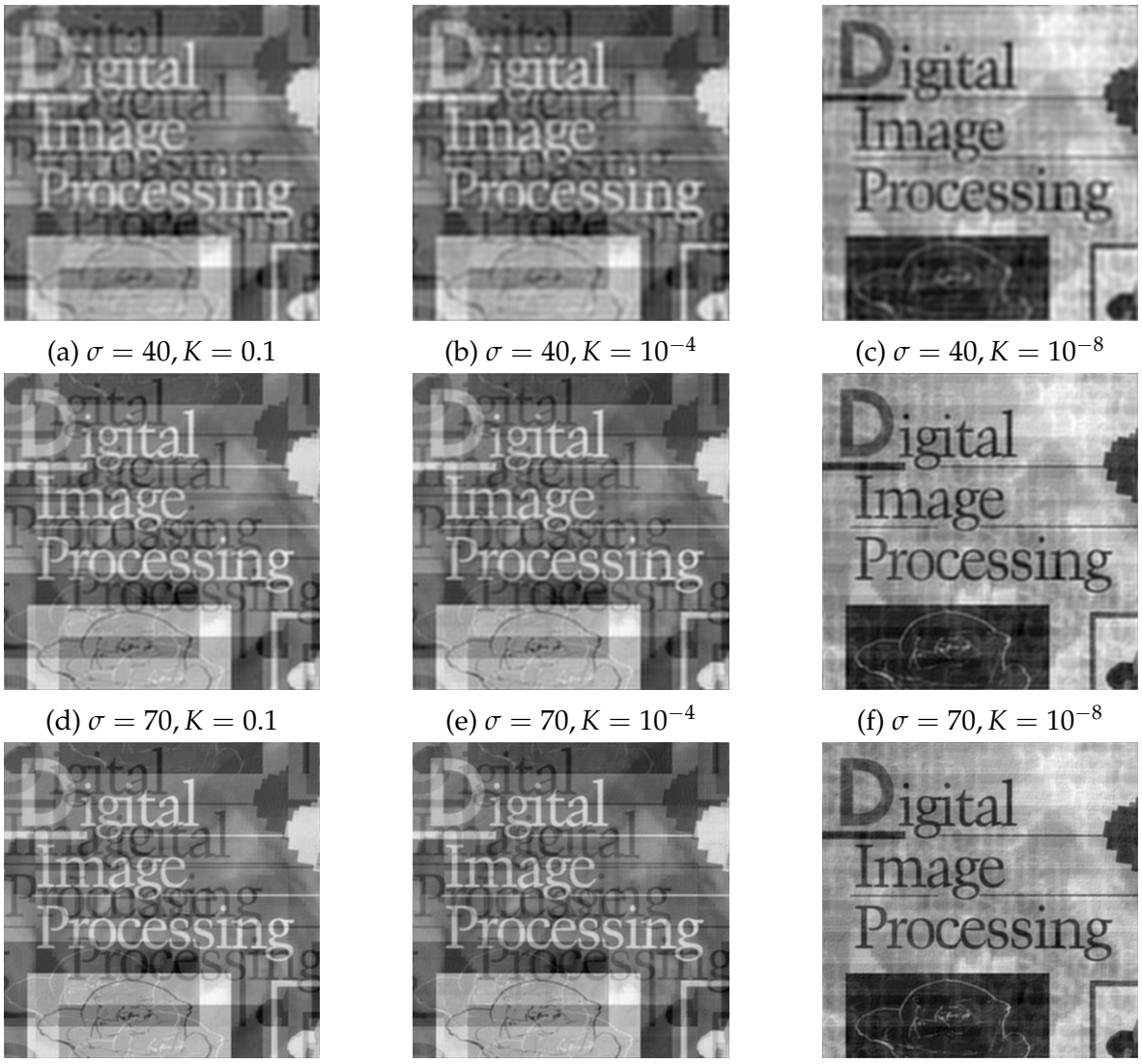
$$\begin{aligned} H(u,v) &= \int_0^T e^{-j2\pi[ux_0(t)+vy_0(t)]}dt \\ * \qquad &= \int_0^T e^{-j2\pi[ua+vb]t/T}dt \\ &= \frac{T}{\pi(ua+vb)}\sin[\pi(ua+vb)]e^{-j\pi(ua+vb)} \end{aligned} \tag{1}$$

And we will apply radially limited inverse filter and wieber filter to the degreaded image.



(a) $\sigma = 1$ (b) $\sigma = 10$ (c) $\sigma = 50$ (d) $\sigma = 100$

Figure 8: Filtered by radially limited inverse filter

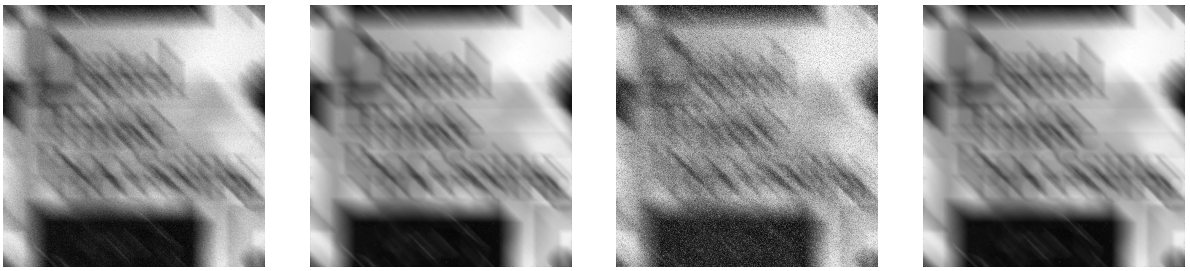


(a) $\sigma = 40, K = 0.1$ (b) $\sigma = 40, K = 10^{-4}$ (c) $\sigma = 40, K = 10^{-8}$

(d) $\sigma = 70, K = 0.1$ (e) $\sigma = 70, K = 10^{-4}$ (f) $\sigma = 70, K = 10^{-8}$

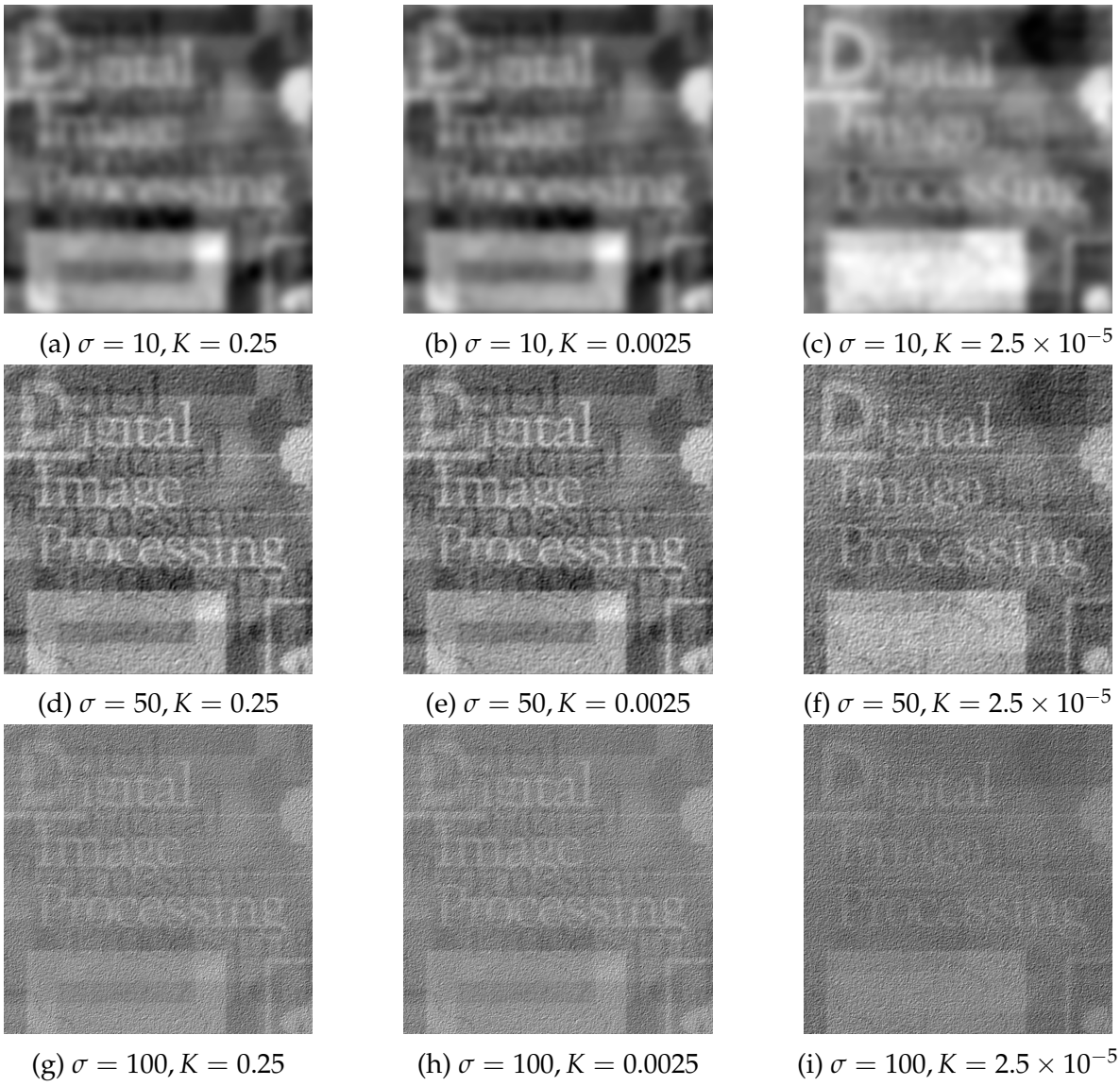
(g) $\sigma = 100, K = 0.1$ (h) $\sigma = 100, K = 10^{-4}$ (i) $\sigma = 100, K = 10^{-8}$

Figure 9: Fitered by wiener filter



(a) Q6_3_2 (b) Q6_3_2 denoised (c) Q6_3_3 (d) Q6_3_3 denoised

Figure 10: original image and denoised image



(a) $\sigma = 10, K = 0.25$ (b) $\sigma = 10, K = 0.0025$ (c) $\sigma = 10, K = 2.5 \times 10^{-5}$

(d) $\sigma = 50, K = 0.25$ (e) $\sigma = 50, K = 0.0025$ (f) $\sigma = 50, K = 2.5 \times 10^{-5}$

(g) $\sigma = 100, K = 0.25$ (h) $\sigma = 100, K = 0.0025$ (i) $\sigma = 100, K = 2.5 \times 10^{-5}$

Figure 11: motion deblur of the figure

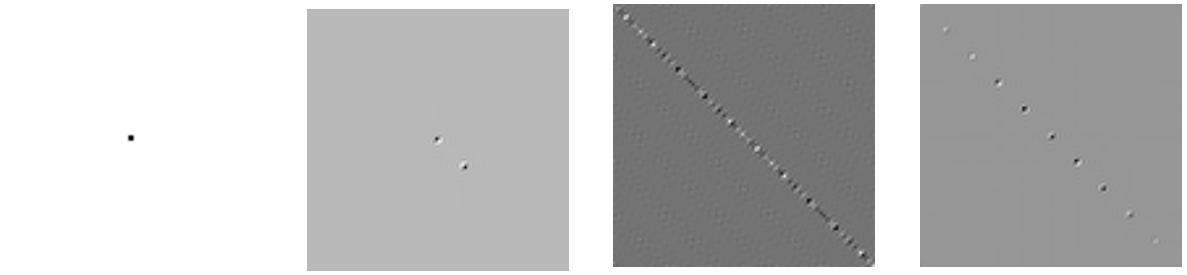
(a) $\sigma = 10, K = 0.25$ (b) $\sigma = 10, K = 0.0025$ (c) $\sigma = 10, K = 2.5 \times 10^{-5}$

(d) $\sigma = 50, K = 0.25$ (e) $\sigma = 50, K = 0.0025$ (f) $\sigma = 50, K = 2.5 \times 10^{-5}$

Figure 12: motion deblur of the figure with more noise

Result.

Discussion. Fig 8 indicate that we can't use radially limited inverse filter to restore the image. Here a unit impluse is used to estimate the behavior of the filters



(a) The unit inpluse (b) Motion blur (c) inverse filter (d) winber filter

Figure 13: The behavier of the system to unit impluse

After the system is applied to the unit impluse response, we can see a motion blur appeared, then two inverse filters are applied to the degraded image. By inverse filter, the motion blur become more severe, for winber filter, the impluse appear periodicly and their intensity decrease when their distance to the center of the image increase.

However, in previous process, we will save the image and read it again before we apply the inverse filter to it, to save the image, we need to apply `abs()` function to convert it from complex number to pure real number, so during this process some information is lost. Which create a special kind of noise, then, in further process, the noise is enhanced by the inverse filter. That's why we get useless result in Fig 8.

Fig 9 shows the result after restored by wiener filter, here $\sigma = 100, K = 10^{-4}$ is a proper pair to restore the image. Compare between image, if the details of the image is not clear enough, we just increase σ, if the shadow is to outstanding, we increase the K and if the noise appeared, we increase K.

In addition, the reason of the shadow have been analysised when we apply the system to the unit impluse.

Then we try to apply the filter to image with noise, first we denoise the image by adaptive filter we introduced in section 1, after filtering 3-5 times, we get the filtered image with most of the noise removed, then the wiener filter is applyed to the image. In the result we found that $\sigma = 50K = 0.25$, is a proper pair to restore the image, however, there is still a layer of noise in the result, that is because, the denoise process also create lot of noise with differnet motion to the image, so the noise is also enhanced during the filtering. And for image with higher noise, as shown in Fig 12, the affect of such kind of noise become more severe.

Conclusion

In this lab, we studied adaptive image denoise and image reconstruction method, we found that the adaptive filter is a better method for image denoiseing due to its auto adjusting feature.

When we use image restoring technic, we have one or multiple parameters to adjust. For example, σ in both radially limited inverse filter and wieber filter is used to reduce the high frequency noise, and K in wiener filter can adjust the reduced noise, when we adjust the parameters, one demision of image quality will increase while another decrease, so we need to find a balance between each demision of image quality.

Appendix: Source Code

```
import numpy as np
import numpy.fft
from skimage import io, data
import math
from scipy import interpolate
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.image as mplimg
from numba import njit,prange
import EE326_SUSTech as ee
import time

@njit(parallel=True)
def adaptive_11810818(input_image, n_size, smax):
    output_image = np.zeros(input_image.shape, dtype=np.uint8)
    m, n = input_image.shape

    for i in prange(m):
        for j in prange(n):
            n_size_2 = n_size

            while True:
                step = (int)((n_size_2 - 1) / 2)
                pixels = np.zeros(n_size_2 * n_size_2)

                for i2 in range(n_size_2):
                    for j2 in range(n_size_2):
                        if i - step + i2 >= 0 \
                                and i - step + i2 < input_image.shape[0]
                                 ↪  \
                                and j - step + j2 >= 0 \
                                and j - step + j2 <
                                 ↪  input_image.shape[0]:
                            pixels[j2 * n_size_2 + i2] = input_image[i -
                             ↪  step + i2, j - step + j2]

                pixels_sorted = np.sort(pixels)
                med = (int)((n_size_2 * n_size_2-1)/2)
                a1 = pixels_sorted[med] - pixels_sorted[0]
                a2 = pixels_sorted[med] - pixels_sorted[n_size_2 *
                 ↪  n_size_2-1]
                if(a1>0 and a2<0):
                    b1 = input_image[i, j] - pixels_sorted[0]
                    b2 = input_image[i, j] - pixels_sorted[n_size_2 *
                     ↪  n_size_2-1]
```

```
                    if(b1>0 and b2<0):
                        output_image[i, j] = pixels[med]
                    else:
                        output_image[i, j] = pixels_sorted[med]
                    break
                else:
                    if(n_size_2 < smax):
                        n_size_2 += 2
                    else:
                        output_image[i, j] = pixels_sorted[med]
                        break

    return output_image

if __name__ == '__main__':
    for i in [1
        , 2
        , 3
        , 4
             ]:
        start_time = time.time()
        input_image = "Q6_1_" + str(i)
        output_name = "plots/" + str(input_image) + "_adaptive.png"
        input_image = io.imread(input_image + ".tiff")
        output_image = adaptive_11810818(input_image, 3, 20)
        print(time.time() - start_time)
        mplimg.imsave(output_name,
                      output_image,
                      cmap=cm.gray)

        print("Finish processing " + str(i))
```

```
import numpy as np
import numpy.fft
from skimage import io, data
import math
from scipy import interpolate
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.image as mplimg
import EE326_SUSTech as ee
import time


def atmosphere_turbulence(shape, k):
    col, row = shape
```

```
    u, v = np.meshgrid(np.linspace(0, col-1, col), np.linspace(0, row-1,
     ↪  row))
    u = u - col / 2
    v = v - row / 2
    d = u * u + v * v
    h = np.exp(-(k * (d ** (5/6))))

    return h


def full_inverse_filtering_11810818(input_image):
    input_image = io.imread(input_image + ".tif")
    m, n = input_image.shape
    input_image = np.pad(input_image, ((0, m), (0, n)))

    filter = atmosphere_turbulence(input_image.shape, 0.0025)
    inverse_filter = 1/filter

    input_image = np.fft.fft2(input_image)
    input_image = np.fft.fftshift(input_image)
    input_image = input_image*inverse_filter
    input_image = np.fft.fftshift(input_image)
    output_image = np.abs(np.fft.ifft2(input_image))

    return output_image

def radially_limited_inverse_filtering_11810818(input_image, sigma):
    input_name = input_image
    input_image = io.imread(input_image + ".tif")
    m, n = input_image.shape
    # input_image = np.pad(input_image, ((0, m), (0, n)))
    # m, n = input_image.shape

    filter = atmosphere_turbulence(input_image.shape, 0.0025)
    inverse_filter = np.reciprocal(filter)
    # g = ee.gaussian_filter(m,n,sigma)
    g = ee.butterworth_filter(m, n, [m/2, n/2], 10, sigma)

    input_image = np.fft.fft2(input_image)
    input_image = np.fft.fftshift(input_image)
    input_image = input_image * inverse_filter * g
    input_image = np.fft.ifftshift(input_image)
    output_image = np.real(np.fft.ifft2(input_image))

    return output_image

def wiener_filter_11810818(input_image, sigma, k):
```

```
    input_image = io.imread(input_image + ".tif")
    m, n = input_image.shape
    # input_image = np.pad(input_image, ((0, m), (0, n)))
    # m, n = input_image.shape

    g = ee.gaussian_filter(m, n, sigma)
    filter = atmosphere_turbulence(input_image.shape, 0.0025)

    f = ((1/filter)*(filter**2/(filter**2 + k*np.ones([m, n])))) * g

    input_image = np.fft.fft2(input_image)
    input_image = np.fft.fftshift(input_image)
    output_image = input_image*f
    output_image = np.fft.fftshift(output_image)
    output_image = np.fft.ifft2(output_image)
    output_image = np.abs(output_image)

    return output_image


if __name__ == '__main__':

    input_image = "Q6_2"
    # output_name = "plots/" + str(input_image) + "_full_inverse.png"
    # output_image = full_inverse_filtering_11810818(input_image)
    # mplimg.imsave(output_name,
    #               output_image,
    #               cmap=cm.gray)
    # print("Finish processing full inverse filtering")

    for i in [10, 30, 35, 40, 45, 50, 55, 60, 65, 70, 85]:
        start = time.time()
        output_name = "plots/" + str(input_image) + "_radially_limited"
        ↪  + str(i) + ".png"
        output_image =
        ↪  radially_limited_inverse_filtering_11810818(input_image, i)
        print(time.time() - start)
        mplimg.imsave(output_name,
                      output_image,
                      cmap=cm.gray)

    print("Finish processing radially limited filtering")

    for sigma in [50, 60, 70]:
        for K in [0.0000000001, 0.00000001, 0.000001, 0.0001, 0.01,
        ↪  0.1]:
            start = time.time()
```

```
105             output_name = "plots/" + str(input_image) + "_wiener_" +
                ↪  str(sigma) + "_" + str(K) + ".png"
106             output_image = wiener_filter_11810818(input_image, sigma, K)
107             print(time.time() - start)
108             mplimg.imsave(output_name,
109                           output_image,
110                           cmap=cm.gray)
111
112     print("Finish processing wiener filtering")
```

```
1  import numpy as np
2  import numpy.fft
3  from skimage import io, data
4  import math
5  from scipy import interpolate
6  import matplotlib.pyplot as plt
7  from matplotlib import cm
8  import matplotlib.image as mplimg
9  import EE326_SUSTech as ee
10 import adaptive_filter_11810818 as ada
11
12
13 def undergo(a, b, u, v, T):
14     u, v = np.meshgrid(np.linspace(1, u, u), np.linspace(1, v, v))
15     d = a * u + b * v
16     # h = (T / (np.pi * d)) * np.sin(np.pi * d) * np.exp(-1j*(np.pi *
       ↪  d))
17     h = (T / (np.pi * d)) * np.sin(d * np.pi) * np.exp(-1 * 1j * np.pi *
       ↪  d)
18
19     return h
20
21
22
23 def radially_limited_inverse_filtering_11810818(input_image, sigma):
24     input_name = input_image
25     input_image = io.imread(input_image + ".tiff")
26
27     # input_image = ada.adaptive_11810818(input_image, 3, 30)
28
29     m, n = input_image.shape
30     # input_image = np.pad(input_image, ((0, m), (0, n)))
31     # m, n = input_image.shape
32
33     filter = undergo(0.1, 0.1, m, n, 1)
34     inverse_filter = np.reciprocal(filter)
```

```
    g = ee.gaussian_filter(m, n, sigma)

    input_image = np.fft.fft2(input_image)
    input_image = np.fft.fftshift(input_image)

    input_image = input_image * inverse_filter * g
    # input_image = input_image * inverse_filter

    input_image = np.fft.ifftshift(input_image)
    output_image = np.real(np.fft.ifft2(input_image))

    return output_image


def wiener_filter_11810818(input_image, sigma, k):
    input_image = io.imread(input_image + ".tiff")
    # input_image = ada.adaptive_11810818(input_image, 3, 30)
    m, n = input_image.shape
    # input_image = np.pad(input_image, ((0, m), (0, n)))
    # m, n = input_image.shape

    g = ee.gaussian_filter(m, n, sigma)
    filter = undergo(0.1, 0.1, m, n, 1)

    # f = ((1/filter)*(filter*np.conj(filter)/(filter*np.conj(filter) +
    ↪  k))) * g
    # f = ((filter * np.conj(filter) / (filter * np.conj(filter) + k)))

    buf = filter * np.conj(filter)
    f = buf / (filter * (buf + k)) * g

    input_image = np.fft.fft2(input_image)
    input_image = np.fft.fftshift(input_image)

    output_image = input_image * f

    output_image = np.fft.ifftshift(output_image)
    output_image = np.fft.ifft2(output_image)
    output_image = np.real(output_image)

    return output_image


def test_image():
    test = np.ones([100, 100])*255
    test[49:51, 49:51] = [[0, 0], [0, 0]]

```

```
    mplimg.imsave("test_input.png",
                  test,
                  cmap=cm.gray)

    filter = undergo(0.1, 0.1, 100, 100, 1)
    test = np.fft.fftshift(np.fft.fft2(test))
    test = test * filter
    test = np.fft.ifft2(np.fft.fftshift(test))
    test = np.abs(test)

    mplimg.imsave("test_input_burl.png",
                  np.real(test),
                  cmap=cm.gray)

    buf = filter * np.conj(filter)
    f = buf / (filter * (buf + 0.000000025))

    test = np.fft.fftshift(np.fft.fft2(test))
    test = test * f
    test = np.fft.ifft2(np.fft.ifftshift(test))

    mplimg.imsave("test_input_restore_winber.png",
                  np.real(test),
                  cmap=cm.gray)



def denoise1():
    for input_name in ["Q6_3_2", "Q6_3_3"]:
        output_image =
        ↪  ee.adaptive_filter(io.imread(str(input_name)+".tiff"), 3,
        ↪  30)
        print("Finish denoise 1 " + str(input_name))
        output_image = ee.adaptive_filter(output_image, 3, 30)
        print("Finish denoise 2 " + str(input_name))
        output_image = ee.adaptive_filter(output_image, 3, 30)
        print("Finish denoise 3 " + str(input_name))
        output_image = ee.adaptive_filter(output_image, 3, 30)
        mplimg.imsave(str(input_name) + ".png",
                      output_image,
                      cmap=cm.gray)
    print("Finish denoise " + str(input_name))


def denoise2():
    for input_name in ["Q6_3_3"]:
        output_image =
        ↪  ee.adaptive_filter(io.imread(str(input_name)+".tiff"), 3,
        ↪  30)
```

```
126         print("Finish denoise 1 " + str(input_name))
127         output_image = ee.adaptive_filter(output_image, 3, 30)
128         print("Finish denoise 2 " + str(input_name))
129         output_image = ee.adaptive_filter(output_image, 3, 30)
130         print("Finish denoise 3 " + str(input_name))
131         output_image = ee.adaptive_filter(output_image, 3, 30)
132         print("Finish denoise 4 " + str(input_name))
133         output_image = ee.adaptive_filter(output_image, 3, 30)
134         print("Finish denoise 5 " + str(input_name))
135         output_image = ee.adaptive_filter(output_image, 3, 30)
136         mplimg.imsave(str(input_name) + ".png",
137                       output_image,
138                       cmap=cm.gray)
139     print("Finish denoise " + str(input_name))
140
141
142 def run():
143     for input_image in ["Q6_3_3"]:
144         for sigma in [1, 10, 50, 100]:
145             output_name = "plots/" + str(input_image) +
                ↪  "_radially_limited_" + str(sigma) + ".png"
146             output_image =
                ↪  radially_limited_inverse_filtering_11810818(input_image,
                ↪  sigma)
147             mplimg.imsave(output_name,
148                           output_image,
149                           cmap=cm.gray)
150         print("Finish processing radially limited filtering")
151
152         for sigma in [1, 10, 20, 30, 40, 50]:
153             for K in [0.25, 0.0025, 0.000025]:
154                 output_name = "plots/" + str(input_image) + "_wiener_" +
                    ↪  str(sigma) + "_" + str(K) + ".png"
155                 output_image = wiener_filter_11810818(input_image,
                    ↪  sigma, K)
156                 mplimg.imsave(output_name,
157                               output_image,
158                               cmap=cm.gray)
159         print("Finish processing wiener filtering")
160
161
162 if __name__ == '__main__':
163     test_image()
164     # run()
165     # denoise2()
```

```python
'''
Library USE for EE326 2021
'''

import numpy as np
from skimage import io, data
import math
from scipy import interpolate
import matplotlib.pyplot as plt
from numba import njit,prange

# General

def format_image(input_image):
    output_image = input_image
    output_image -= np.min(output_image)
    output_image = (output_image/np.max(output_image))*255
    return output_image

# LAB 4

def convolution_3x3(input_image, operator_3x3):
    col, row = input_image.shape
    output_image = np.zeros([col, row])
    input_image = np.pad(input_image, 1)
    for i in range(0, col):
        for j in range(0, row):
            for i2 in range(3):
                for j2 in range(3):
                    output_image[i, j] += input_image[i+i2, j+j2] *
                     ↪  operator_3x3[i2, j2]

    return output_image


def sobel_filter(input_image):

    operator1 = np.array([[-1, -2, -1], [0, 0, 0], [1, 2, 1]])
    operator2 = np.array([[-1, 0, 1], [-2, 0, 2], [-1, 0, 1]])

    output_image1 = convolution_3x3(input_image, operator1)
    output_image2 = convolution_3x3(input_image, operator2)
    #
    # output_image1 = np.clip(output_image1, 0, 255)
    # output_image2 = np.clip(output_image2, 0, 255)

    output_image = output_image1 + output_image2 # + input_image
```

```
    # output_image = np.clip(output_image, 0, 255)

    output_image = output_image.astype(np.uint8)

    return output_image


def zero_padding(input_image, P, Q):
    output_image = np.zeros([P, Q])

    return output_image


def denoise_filter(input_image, n_size, mode):
    output_image = np.zeros(input_image.shape, dtype=np.uint8)

    m, n = input_image.shape

    for i in range(m):
        for j in range(n):
            step = (int)((n_size - 1) / 2)
            pixels = np.zeros(n_size * n_size)

            for i2 in range(n_size):
                for j2 in range(n_size):
                    if i - step + i2 >= 0 \
                            and i - step + i2 < input_image.shape[0] \
                            and j - step + j2 >= 0 \
                            and j - step + j2 < input_image.shape[0]:
                        pixels[j2 * n_size + i2] = input_image[i - step
                         ↪  + i2, j - step + j2]

            pixels = np.sort(pixels)

            if(mode == "max"):
                output_image[i, j] = pixels[pixels.shape[0]-1]
            elif(mode == "medium"):
                output_image[i, j] = pixels[(int)((n_size * n_size + 1)
                 ↪  / 2)]
            elif(mode == "min"):
                output_image[i, j] = pixels[0]
            elif(mode == "average"):
                output_image[i, j] = np.average(pixels)
            elif(mode == "smart"):
                have_normal_pixel = 0
                for pixel in pixels:
                    if(pixel < 250 and pixel > 5):
```

```
                        have_normal_pixel = 1
                if(have_normal_pixel):
                    selected = (int)(pixels.shape[0]/2)
                    while(pixels[selected] < 5):
                        selected = selected + 1
                    while(pixels[selected] > 250):
                        selected = selected - 1
                    output_image[i, j] = pixels[selected]
                else:
                    output_image[i, j] = np.average(pixels)



    return output_image

# LAB 5


def extract_result_eastsouth(input_image):
    x, y = input_image.shape
    output_image = input_image[int(x/2):x, int(y/2):y]

    return output_image


def extract_result_westnorth(input_image):
    x, y = input_image.shape
    output_image = input_image[0:int(x/2), 0:int(y/2)]

    return output_image


def zero_padding_DFT(input_image, P, Q):
    m, n = input_image.shape

    output_image = np.zeros([P, Q])
    output_image[0:m, 0:n] = input_image

    return output_image


def zero_padding_DFT(input_image):
    m,n = input_image.shape

    P = 2*m
    Q = 2*n

```

```
    output_image = np.zeros([P, Q])
    output_image[0:m, 0:n] = input_image

    return output_image


def centering(size):
    m, n = size
    centering_matrix = np.ones(size)
    mul1 = 1
    for i in range(m):
        mul2 = mul1
        for j in range(n):
            centering_matrix[i, j] = centering_matrix[i, j] * mul2
            mul2 *= -1
        mul1 *= -1
    return centering_matrix

@njit
def generating_from_spatial_filter(input_filter, P, Q):
    output_filter = np.zeros(P, Q)

    return output_filter


def gaussian_filter(a, b, sigma):
    x, y = np.meshgrid(np.linspace(0, a-1, a), np.linspace(0, b-1, b))
    x = x - a/2
    y = y - b/2
    d = x * x + y * y
    g = np.exp(-(d / (2.0 * sigma ** 2)))
    # g = g/np.sum(g)
    return g


def butterworth_filter(b, a, center, n, sigma):
    cx, cy = center
    x, y = np.meshgrid(np.linspace(0, a - 1, a), np.linspace(0, b - 1,
     ↪  b))
    x = x - cx
    y = y - cy
    d = np.sqrt(x * x + y * y) + 0.1
    h = 1/(1+(sigma/d)**(-2*n))
    return h


# LAB 6
```

```
@njit(parallel=True)
def adaptive_filter(input_image, n_size, smax):
    output_image = np.zeros(input_image.shape, dtype=np.uint8)
    m, n = input_image.shape

    for i in prange(m):
        for j in prange(n):
            n_size_2 = n_size

            while True:
                step = (int)((n_size_2 - 1) / 2)
                pixels = np.zeros(n_size_2 * n_size_2)

                for i2 in range(n_size_2):
                    for j2 in range(n_size_2):
                        if i - step + i2 >= 0 \
                                and i - step + i2 < input_image.shape[0]
                                 ↪  \
                                and j - step + j2 >= 0 \
                                and j - step + j2 <
                                 ↪  input_image.shape[0]:
                            pixels[j2 * n_size_2 + i2] = input_image[i -
                             ↪  step + i2, j - step + j2]

                pixels_sorted = np.sort(pixels)
                med = (int)((n_size_2 * n_size_2-1)/2)
                a1 = pixels_sorted[med] - pixels_sorted[0]
                a2 = pixels_sorted[med] - pixels_sorted[n_size_2 *
                 ↪  n_size_2-1]
                if(a1>0 and a2<0):
                    b1 = input_image[i, j] - pixels_sorted[0]
                    b2 = input_image[i, j] - pixels_sorted[n_size_2 *
                     ↪  n_size_2-1]
                    if(b1>0 and b2<0):
                        output_image[i, j] = pixels[med]
                    else:
                        output_image[i, j] = pixels_sorted[med]
                    break
                else:
                    if(n_size_2 < smax):
                        n_size_2 += 2
                    else:
                        output_image[i, j] = pixels_sorted[med]
                        break

    return output_image
```