Assignment setatives e formule Atoms (4) = { A, B, C} (ℓ, \mathfrak{I}) $(A \rightarrow \overline{\ell})$ $\vee \neg (\overline{\ell} \wedge B)$ $(\ell_2 \mathfrak{I})$ $\neg (A \rightarrow \neg B)$ $\wedge C$ μ(A):= 1 ́и(в);=Т 43 3 (7A N7B) → (AN7C) m(c):= T laa) CVB Does u = P1 ?. yes M = P2? Yes Is in cationable? yes, u = in Is ch valid? NO, let's show it. We need to haild ut such We need to make both (A>TB) and TCAR) To woke A => -1B folse we need Nor(A) =T To make 7 (CAB) false we need (CAB) Inve 10: m (B) = T 50 2t ble and Mo= {+,7, T} A formula lis valid if 7 l is vasely stible If The is satisfiable then I is not valid So for example: $\ell_1 = (A \Rightarrow 7B) V = (C \land B)$ $\neg \mathcal{L}_{1} = \neg ((A \rightarrow \neg B) \vee \neg (C \land B))$ Exmpe:

μ ≠ 4, iff μ(A) -μ(B) =1 41: A1B V2: (AVB) Л (CV-C) $M \nvDash \ell_2 : ff_M(A) = M(B) = L$ $\mu'(c)$ = \downarrow or $\mu'(c)$ = \uparrow There we not equivalent but equivatisfiable $(A_1 \vee \neg A_2) \wedge$ $(A_2 \vee \neg A_4) \wedge$ $(A_2 \vee \neg A_4)$ Exemple: You can think of this like a system of equations and everyone must be sztisfied. While for every close you must check any one literal because Another way of sceing CNF 15 seems it like e set of literals: { { A1 , 7 A2 } , { A3 , A1 , 7 A2 } , { A2 , 7 A4 } } let's consider (ArB) v(CrD) Represented 24 2 circuit $\psi' = (X_1 \hookrightarrow A \land B) \land (X_2 \hookleftarrow \land C \land D) \land (X_3 \hookleftarrow \land X_1 \lor X_2) \land (X_3 \smile \land X_2) \lor (X_3 \smile \land X_1 \lor X_2) \land (X_3 \smile \land X_1 \lor X_2) \lor (X_3 \smile \lor X_2$ q'is not caf quisatisfiable M(x3):= T this must be true to be against is falle either m(x1):= T or m(x2):=T If this is true then either X2 or x2 must be true $\mu' \models \varphi'$ Assume $\mu(x_1):=T$ then $\mu'(A):=T$ and $\mu(B):=T$ $\mu(x_1):=L$ then either $\mu'(C):=L$ or $\mu'(D)=L$ From M we can extratt: M(A):= T,M(B):= T,M(C):= 1, M(B):= 1 We have found on assignment that satisfy the Commute has

lests now build q" that will be CNF. q'=(x, c>AAB)A Where eve contints, not conjunctions. (x2 CND) n $(x_3 \leftarrow x_1 \lor x_2) \land$ el is aqui-shipple wit Let's begin to build 4": 7K, VA 1 (-x, v (AnB))/ $(x, \rightarrow (A_{\Lambda}B))_{\Lambda}$ 7 X1 VB 1 (7(AMB) V X1)n ((A1B) > x,) 1 7417B V X1 1 (-1 x2 V (C/D)) 1 (x2 -> ((10)) 7×2 VC 1 lx2√D ν (7(CAD) V K2) 1 (((np) -> k2) 1 7CV7DVX2 / (/3 => (x2 vx2)) ~ (7 Kz V (K1 V K2))1 (-, (m vx2) v x3) n ((x7 \x1) >> x3) ~ 7 X3 VK1 VK2 1 7 X1 VX3 N X_3 7 X2 V X3 1 The sormula does not blow up because you add a rarable sion the new clauses. And you keep equi-satisficulty by maintaining equishive between the branformations. " y is in CNF A > (B1c) A -1>0 V 7 A V (BNC) *1 $\mu \models q$ is such that: either $\mu(4) := L$ or $\mu(A) := T, \mu(B) := T, \mu(B)$ $\neg X_1 \lor B$ X_L Coo Bac 7 X, VC KZ CO JAVKI 7BV7C V X1 м(c):=T χ₂ 7×2 V 7A V X1 µ' = el is cul that A VK2 722 42 $\mu'(x_2):=T$ then either: $\mu(x_1):=1$ or $\mu'(x_2):=T$ ΧZ μ(x2):=+ iff μ(B):=+, μ(c):=+

EXAMPLE FOR subsumed rule: 4: (AVB) ~ ___ 41:= (AVB) ~ (7BVC)A (7BVC) (AVBVC) becase AUB = AVBVC AUB Subsumes AUBUC EXHIPE P= { { A, B, C3, { ¬A, B3, { B, ¬C3}} Assign (A, 4) { {B}, 7 C} = first constraints on he removed hereve is or Assign (7A, e) = { [B, c], {B, 7c}} qut cle V Vecl Assign(V, e) somme CL lv CL/{-1/3 Resolution exemple 4: {{7A, B, (}} 4: {{B, (}} {7B,C3 {A,7C3} 7 AVBV AV 7C BV CV-7C lexemple e: Resolve Y = [\ 7 A , B, 7 C \ TAVBUTE AVD (1/2) AND $\{A, n\}$ BV7CV70 (20) (whether { nA, nB, C3 5 A, B, 7DSS TAVIBUC AUD
TBUCVO (3,2) TAVIBUL HURVID (3,a) , 7 BVB, V CV 7D

Y1:= {{ B, 74,0}, BV76 0 7BV6 VD 7 CVCVD -> laublayy {B,7C,70} BUTCUTD TBUCUD No simplification possible to resolve B 7CUCUDVID - tailology y", {{ rever puro}}, {rever puro}} Europe of elporethm. e={{A,B}, {A, nB, {7A,B}, {7A, rB}} 41= [[B], [-B]] Unit liked propyrtion on B Q4: {{?} Ell contains Vin empty change phis unit eso is q 9: (TAUBUC) MIRDUC) M(TBUTC) M(AUMBUTC) Assign (B, e) Assign (7B, C) CA7CA(AV7C) (TA VC)
| pue liter on A 7 (A V 7 C) eapty forms (SAT) on lead tool M(B):= 1 M(A):= 1 M(C):= undef () n A unszt DPU builds a satisfying assignment. SAT builds a partial assignment

I function yubol n-place x is a variable round-> f(x) yround of (s) s is a constant 0-ruy funtion following of (f(x)) 7- place P predicite symbol a producte symbol z-phice P(x); P(f(x)) P(S) } ill z tomic Q(xs) Q(f(x),s), Q(s,s)) Examples of WPFs Atoms eve predictes and arguments of predictes are terms. Forevery han & (x,51) Fx. Q (x, x(x1) } does Q(x,x) n P(f(x)) not dosed Vx. Vy. (P(x,y) -> }y Q(y)) En (1.de 32 (2) 1) f:= 7x.7y. P(f(x,y), z) Fid iff Fify P(K(dr,y),z) for some 2,6D(drEN) iff FI P(x(d1,d2),2) for some d7,d2 ED(d1,d2 EN) iff $(g(x)(d_1d_2),g(z)) \in g(P)$ (· (d₁,d₂), 2) ∈ ≤

2) This one it's not true in any case because I can find a counterwoodel. q': \frac{1}{2} \left\{ \text{p(\frac{1}{2}\text{p(\frac{1}\ FI P iff for my two dy, dz + M I have that dredz implies dredz hulif I doose dred and dredz I see that our but 140 =) coule model. 3) Vx. Vy. Vz. (((P(x,y) nP(y,x)) -) P(x, Z)) diedz j dzedz but We can try to deck it do, do, do EN such that diedz? No, there has Fight when the interpretation subilises of. 39) Let 1 the K this 25 c finite Domain I is such that F_I V_X . Person(x) It is such that I I

D; s finite

y(lesson) = D If the domain is limbe then at a centain point there would be no way of choosing fither or mother of some dements. Example Vx, 4x, 3, Vx3. Vx4. ((x,x2, 4, x3,x4) form without grantifier with x1,x2, e,x3, x4 free worlds A model for l' 15 one where: - given any choice of x, - given any choice of kz - there exists a choice for y such that given my choice for x3, x4 the formulz is true

So have the formula transformed in Swolen would be: Yr. Yx2. Yx3. Yx4 of (x1, X2, f(x1, X2), x3, x4) The order is important so your choice for y depends on your choice of x, 1x2. 50 y becomes 2 function of x, and xz. Exercise, Yx. (Rx) -> 147. Zy. (R(x,7) NQ(x,4)))) NNF Yx. (-> P(x) v]z. Yy (-R(x,7)v-Q(x,y))) PNF $\forall x, \exists z. \forall y. (\neg P(x) \lor \neg R(x,z) \lor \neg Q(x,y))$ CNF with one dose or pNF with 3 lerus. ∀x. ∀y. (¬P(x) v¬ R(x, f(x)) v ¬ Q(x,y)) € The advintage of SNE is that has only universally quantifiers. DH: { z, y(f) 2),y(f)(g(f)(2))...} }-> This is the domain for the precious formule.