

# TP4 - Neighborhood Descriptors

NPM3D - M2 MVA

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## 1 CloudCompare Normals

**Q1.** Too small / too big radius leads to a bad estimation. The following figure shows four normal results calculated with radius in  $\{0.1, 0.5, 1.0, 3.0\}$ .

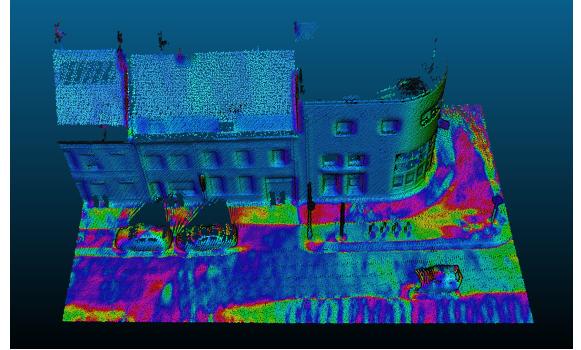
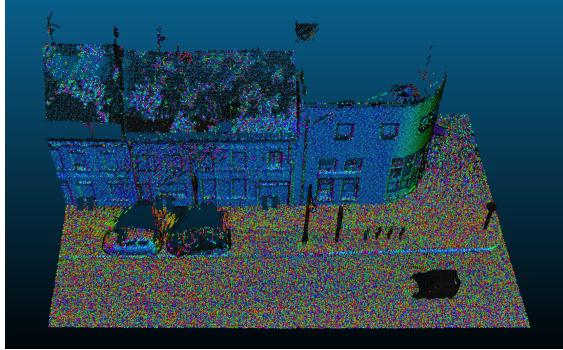


Figure 1: (a)  $r = 0.1$  (b)  $r = 0.5$

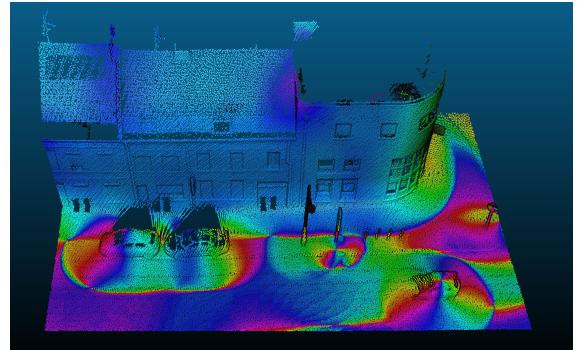
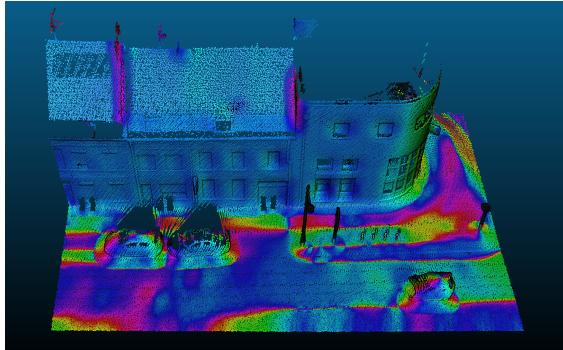


Figure 2: (c)  $r = 1$  (d)  $r = 3$

We observe that a too small radius makes the result noisy. Even two normals of close points might have a large angle. When the radius is large, the normal map is smooth but we loss some information especially on the borders. In our case,  $r = 1$  should be a good tradeoff.

**Q2.** A density-independent way to choose a proper radius is to estimate the average spacing. For a query point  $x$ , we find its 6 nearest neighbors and calculate the average distance  $\bar{d}$  from the point  $x$  to its neighbors. And then we can choose a radius proportional to  $\bar{d}$  (for instance,  $r = 3d$ ).

## 2 Local PCA

**Q3.** We use CloudCompare to visualize the computed normal map, and compare it to the one calculated by the software itself. The radius  $r$  is 1 for both calculations. Since the calculated normal map is unoriented, we use fast marching method to orient it.

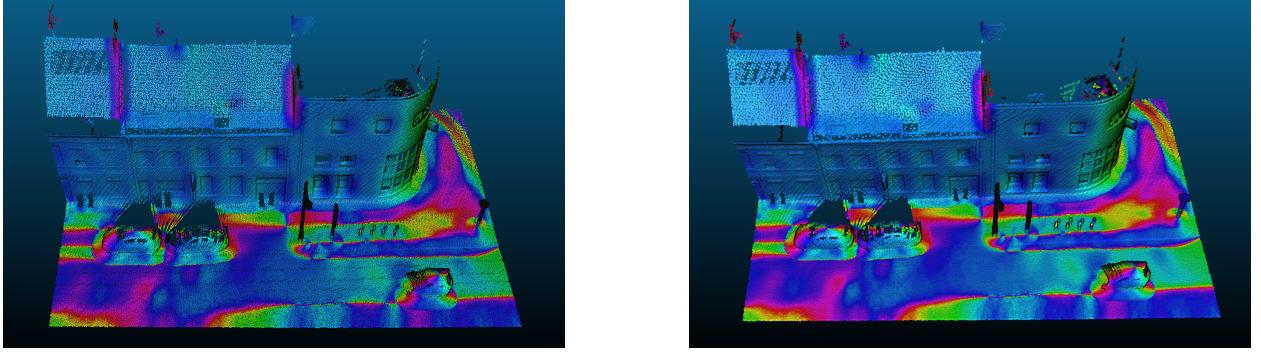


Figure 3: (a) CloudCompare (b) Neighbor PCA

We observe that the results are quite similar.

**Q4.** Since eigenvectors are all normalized to have norm 1. One method to evaluate the normal estimation is to visualize the vector field  $v_3 \vec{n}_3$ . The length of the vector represents its neighborhood's variance along this direction. If we consider a point on a plane, the length of its normal should be near 0.

**Q5.** The intuition of the four features are:

- Verticality: compare the local normal vector to the vertical vector.
- Linearity: is defined as  $1 - \frac{\lambda_2}{\lambda_1}$ . We can consider a point on a line, the eigenvalues should be  $\{1, 0, 0\}$  ideally. So if  $\lambda_2$  is much smaller than  $\lambda_1$ , its linearity will be close to 1.
- Planarity: is defined as  $\frac{\lambda_2 - \lambda_3}{\lambda_1}$ . We can consider a point on a plane, the eigenvalues should be  $\{0.5, 0.5, 0\}$  ideally. Thus when  $\lambda_3$  is tiny and  $\lambda_2$  is close to  $\lambda_1$ , the planarity is close to 1.
- Sphericity: is defined as  $\frac{\lambda_3}{\lambda_1}$ . We can consider a point on a sphere, the eigenvalues should be  $\{\frac{1}{3}, \frac{1}{3}, \frac{1}{3}\}$  ideally. When  $\lambda_3$  is close to  $\lambda_1$ , the sphericity is close to 1.

In the following graph we show the four features of the point cloud: verticality, linearity, planarity and sphericity.

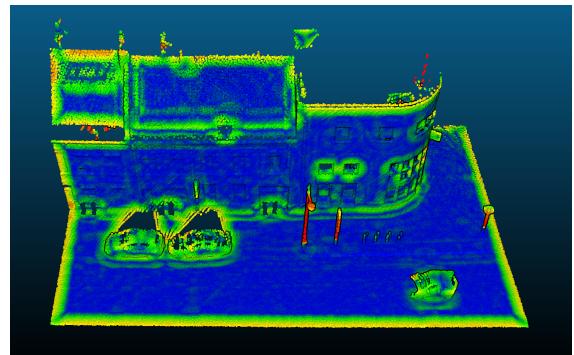
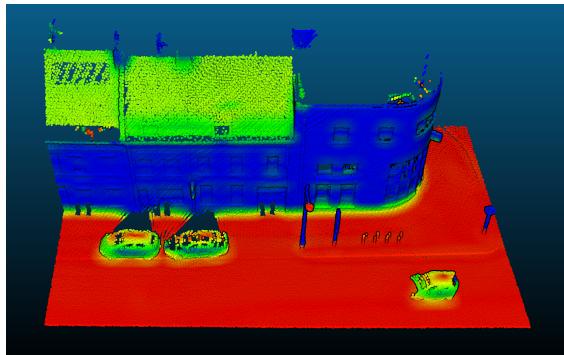


Figure 4: (a) Verticality (b) Linearity

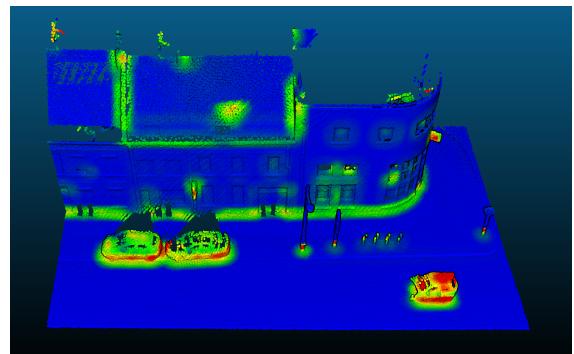
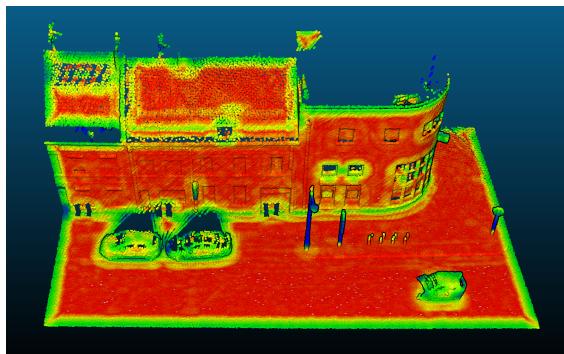


Figure 5: (c) Planarity (d) Sphericity