

### **CS5228: Knowledge Discovery and Data Mining**

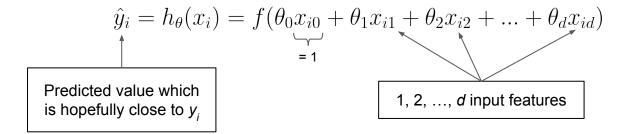
Lecture 8 — Recommender Systems

# **Course Logistics**



## Quick Recap — Linear Models

- Basic Assumption
  - Linear relationship between  $x_i$  and dependent variable  $y_i$

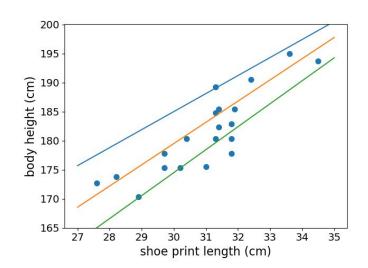


lacktriangle Learned parameters of model:  $heta=\{ heta_0, heta_1, heta_2,..., heta_d\},\; heta_i\in\mathbb{R}$ 

# **Quick Recap** — Linear Regression

• Find  $\theta$  that minimizes MSE loss L

$$L = \frac{1}{n} \sum_{i=1}^{n} (\hat{y}_i - y_i)^2$$
$$= \frac{1}{n} ||X\theta - y||^2$$



Solve using Normal Equation

$$\frac{\partial L}{\partial \theta} = \frac{2}{n} X^T (X\theta - y) \quad \Rightarrow \quad \frac{2}{n} X^T (X\theta - y) \stackrel{!}{=} \overrightarrow{0} \quad \Rightarrow \quad \theta = (X^T X)^{-1} X^T y$$

Solve using Gradient Descent

$$\nabla_{\theta} L = \frac{2}{n} X^T (X\theta - y) \quad \Rightarrow \quad \text{repeat:} \quad \theta \leftarrow \theta - (\eta \cdot \nabla_{\theta} L)$$

# **Quick Recap** — Logistic Regression

- Regression model for classification
  - Interpret  $\hat{y}$  as probability that x belongs to Class 1

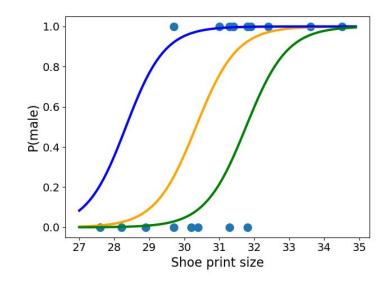
$$\hat{y} = h_{\theta}(x) = f(\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$

■ Minimize Cross-Entropy Loss L

$$L = -[y \log \hat{y} + (1 - y) \log (1 - \hat{y})]$$



$$\nabla_{\theta} L = \frac{1}{n} X^T (h_{\theta}(X) - y) \quad \Rightarrow \quad \text{repeat:} \quad \theta \leftarrow \theta - (\eta \cdot \nabla_{\theta} L)$$



## Quick Recap — Linear Models

### Polynomial Linear/Logistic Regression

- Data transformation to include polynomial terms of features
- No change of algorithms needed

$$X^{(1)} = \begin{bmatrix} 1 & x_1 \\ 1 & x_2 \\ \vdots & \vdots \\ 1 & x_n \end{bmatrix} \quad X^{(2)} = \begin{bmatrix} 1 & x_1 & x_1^2 \\ 1 & x_2 & x_2^2 \\ \vdots & \vdots & \vdots \\ 1 & x_n & x_n^2 \end{bmatrix} \quad X^{(3)} = \begin{bmatrix} 1 & x_1 & x_1^2 & x_1^3 \\ 1 & x_2 & x_2^2 & x_2^3 \\ \vdots & \vdots & \vdots & \vdots \\ 1 & x_n & x_n^2 & x_n^3 \end{bmatrix}$$

### Regularization to avoid overfitting

- lacktriangle Extend loss function to "punish" large values of heta
- Only minor changes to Normal Equation and calculation of Gradient

$$L = \frac{1}{n} ||X\theta - y||^2 + \sqrt{\frac{1}{n} ||\theta||_2^2}$$

## **Outline**

- Overview
  - Motivation
  - Naive / alternative approaches
- Content-based recommendation systems
  - Pairwise item-item similarity
  - User-item similarity
- Collaborative filtering (CF)
  - Memory-based CF
  - Model-based CF

## **Recommender Systems** — Motivation

- In the online world: information and item overload
  - Too many items: products, songs, movies, news articles, restaurants, etc.
  - More choices require better filters → recommendation engines

User perspective	Provider perspective
Identify relevant items	Maximize sales / transactions
<ul> <li>Minimize effort (to find relevant items)</li> </ul>	<ul> <li>Maximize user engagement (e.g., to maximize ad revenue)</li> </ul>
Maximize satisfaction	Gain competitive advantage
<ul> <li>Optimize spending of money and attention</li> </ul>	

### **Editorial Recommendations**

- Recommendations by "experts"
  - Expert = person with expertise about item(s)
     (e.g., movie or restaurant critic, staff writers, journalists)
  - Objective, elaborate, trustworthy, credible (at least in an ideal world...)
  - Writing editorial recommendations is generally paid work

A Foodie's Guide to the Best Burgers in Singapore

### The best burgers in Singapore

15 Best Burgers In Singapore So Good, You Won't Stop At Just Bun

Burgers, burgers, burgers: The best to sink your teeth into whether dine-in or delivered

Best Burger Joints You Must Try in Singapore

**Snackdown review: The best burgers in Singapore** 

The best restaurants with burger delivery options in Singapore

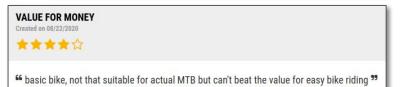
### **Peer Recommendations**

- Recommendations by normal users
  - Online word-of-mouth recommendations (however, users are typically strangers)
  - Common feature on shopping/booking sites
  - Typically subjective, short, biased
  - Many reviews per item create average view but represents again information overload



#### One of the best burgers in town

Food n drink above average. Service has much room for improvement. Ordered the beef burger which is huge n delicious. However the server failed to check for the preference on the done-ness of the patter.





28 May 2020

The product looks good and very difficult to tilt vertically otherwise it's a worth the money. Due to Circuit Breaker, the shipping took a Long time.

#### 5/5 Excellent

#### Verified traveller

Travelled with family, Travelled with group 25 Oct 2019

© Liked: Cleanliness, staff & service, amenities, property conditions & facilities

It was too crowded and busy hotel. Otherwise everything was good

#### \*\*\* A dream come true.

Reviewed in the United States on August 1, 2019

#### **Verified Purchase**

A lot of us thought we would never see all these characters in one movie, but these guys did it. And they gave us some of the best movies we know now. What a spectacular journey it was, starting with Iron Man and now here. Very well done everyone who was apart of it, and thank you.

### Manual Recommendations — Pros & Cons

#### Pros

- Semantically rich (ratings, plain text, images, videos, etc.)
- Explainability / Interpretability

#### Cons

- Manual effort What is the incentive for writing a review?
- Lack of personalization

### **Recommendation Fraud**

Online reviews 'used as blackmail'

How merchants use Facebook to flood Amazon with fake reviews

'Why I write fake online reviews'

Army of fake reviewers being built to dupe buyers, drive online sales

Spotify tests sponsorship of fullscreen album recommendations

Influencer Marketing Fraud: The Shady Side of Social Media

Can We Trust Social Media Influencers?

A new study analyses the murky world of fake Amazon reviews

### Buy Lazada Review - Votes - Sells

**How to Get Paid to Write Reviews** 

Threatening a business with a bad review is ugly bullying

Amazon's Fake Review Problem Is Getting Worse Amazon is filled with fake reviews and it's getting harder to spot them

# **Quick Quiz**



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# **Recommendations Simple Aggregations**

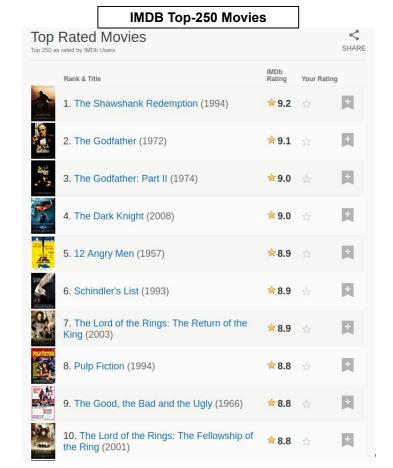
Rank items based on aggregated scores



#### **Rotten Tomatoes Top-100 Movies**

Movies with 40 or more critic reviews vie for their place in history at Rotten Tomatoes. Eligible movies are ranked based on their Adjusted Scores.

Rank	Rating	Title	No. of Reviews
1.	96%	Black Panther (2018)	516
2.	94%	Avengers: Endgame (2019)	531
3.	93%	Us (2019)	536
4.	97%	Toy Story 4 (2019)	445
5.	99%	Lady Bird (2017)	394
6.	100%	Citizen Kane (1941)	94
7.	97%	Mission: Impossible - Fallout (2018)	430
8.	98%	The Wizard of Oz (1939)	120
9.	96%	The Irishman (2019)	441
10.	96%	BlacKkKlansman (2018)	438



## Simple Aggregations — Pros & Cons

#### Pros

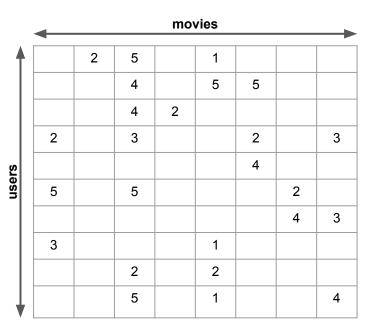
- Relatively easy to compute (typically weighted aggregated based on different factors)
- Typically good/safe recommendations (particularly for new/unknown users)

#### Cons

- Requires sufficient number of ratings per items
- High risk of popularity bias; lack of diversity ("rich get richer" effects, "few get richer" effects)
- Lack of personalization

### **Personalized Recommendations**

- Users have different preference that define the relevance of items
  - Preferences = interests, likings, needs, wants, desires, etc.
  - Relevant items = items that match users' preferences best
- Basic setup
  - Set of users  $U = \{u_1, u_2, ..., u_n\}$
  - Set of items  $V = \{v_1, v_2, ..., v_m\}$
  - Rating matrix *R* with |*U*| rows and |*V*| columns
  - Matrix element  $R_{uv}$ : u's rating of v (e.g., 1-5 stars, binary 0/1)



### Personalized Recommendations — Core Tasks



### Infer missing values $\hat{R}_{uv}$

- In practice, mainly interested in high values
- Algorithmic component of recommender systems
- Wide range of existing approaches



#### **Evaluation: How good are the recommendations?**

• Compare  $\hat{R}_{uv}$  with true  $R_{uv}$  from test set

## **Collecting Ratings**

- Explicit
  - Ask/invite/encourage users to rate items
  - Pay users to rate items (e.g., crowdsourcing)
- Implicit derive ratings from users' behavior, e.g.:
  - Product bought
  - Video watched
  - Article read
  - Link clicked
  - **...**

→ High ratings

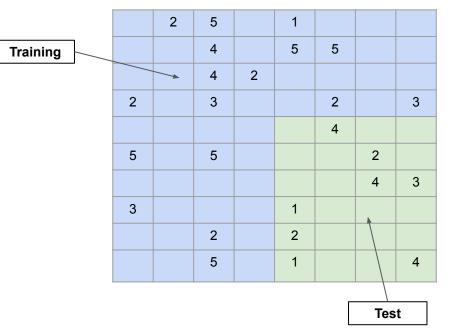
(But how to get low ratings?)

Key challenge: Rating matrix R is in practice very sparse!

## **Evaluation**

- Split R into training and test set
- Performance metrics
  - Root Mean Squared Error (for numerical ratings)

$$\sqrt{\frac{1}{|S|}\sum_{(u,v)\in S} \left(\widehat{R}_{uv} - R_{uv}\right)^2}$$
 Set of (u, v) pairs in test set



- Precision, Recall, F1 score, etc.

  (TP, TN, FP, FN for binary ratings or binary recommendation after converting numerical ratings)
- Precision@k, Recall@k (precision and recall w.r.t. to the top-k highest predicted ratings)
- $\blacksquare$  Compare rankings induced by  $\widehat{R}_{uv}$  and  $R_{uv}$  with  $(u,v)\in S$  (also consider the order of the top-k highest ratings)

## **Recommendations Using Association Rules**

### User preferences & likings

- Items: movies, songs, books, etc.
- Transaction: viewing/listening/reading history

### Interesting rules (movies):

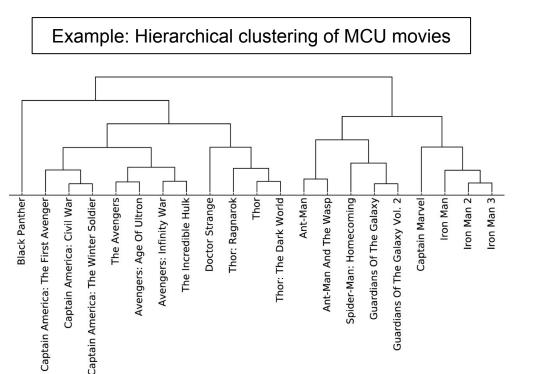
- Viewer who watched movies {a, b} also watched movies {x, y}
- Example: {Jaws} → {It}

#### Limitations

- Basic AR algorithm ignores ratings
- Popularity bias: user with very unique tastes likely to get subpar recommendations

TID	Items
1	Jaws, Halloween, Scream, It
2	Alien, Jaws, Scream, It
3	Tenet, Inception, Interstellar
4	Jaws, Halloween, It
5	Alien, Tenet Jaws, It

# **Recommendations Using Clustering**



### Approach

- Cluster movies based on "useful" features (genre, director, writer, length, ...)
- Recommend movies from clusters with movies a user has rated highly

#### Limitations

- Find good feature in practice very difficult (we come back to that)
- Unsystematic: no well-defined process to pick recommendations

# **Recommendations Using Regression (or Classification)**

- Example approach: Linear Regression
  - Independent variable: movie features
  - Dependent variable: user rating
- → Build a linear regression model for each users

- Limitations
  - Requires good features for each item
  - Cold-start problem: requires a lot of user ratings to build a good model

Rated movies of an individual user

original	powerful	absorbing	comical	romantic	 Rating
0.20	0.95	0.80	0.00	0.10	 4.5
0.80	0.25	0.50	0.50	0.75	 4.0
0.05	0.2	0.20	0.95	0.90	 2.0
0.60	0.20	0.80	0.00	0.85	 3.5
0.90	0.95	0.90	0.10	0.40	 5.0
0.45	0.50	0.20	0.60	0.30	 2.0
0.10	0.40	0.55	0.90	0.30	 2.5
0.75	0.50	0.50	0.40	0.40	 3.5
0.80	0.80	0.85	0.10	0.10	 4.5

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## **Content-Based Recommender System**

#### Intuition

- Recommend item *v* to user *u* that are similar to *v* and *u* has rated highly
- Examples: movies of the same genre, songs from the same artist, articles about the same topic, products with similar features, etc.
- Basic requirement: item profiles = feature vector for each item, e.g.:
  - Movie: genre, director, writer, cast, length, year, ...
  - Product: type, brand, price, weight, color, ...
  - Article: set of (important) words / tf-idf vector / ...

# **Running Example**

#### MovieLens dataset

■ Items: Movies of different genres

■ Features: 20 genres (incl. "uncategorized")

■ Ratings: 1-5 stars (incl. half stars)

#### Numbers for "Small" dataset

■ 610 users, 9,742 movies

■ ~100k ratings → sparsity: ~1.7%

	comedy	action	romance	drama	fantasy	thriller	
Clueless	1	0	1	0	0	0	
Heat	0	1	0	0	0	1	
Bad Boys	1	1	0	1	0	1	
Leon	0	1	0	1	0	1	
Alice	1	0	1	1	1	0	
Jarhead	0	1	0	1	0	0	
Rocky	0	0	0	1	0	0	
Big	1	0	1	1	1	0	
Krull	0	1	0	0	1	0	

	<b>V</b> <sub>1</sub>	v <sub>2</sub>	<b>V</b> <sub>3</sub>	<b>V</b> <sub>4</sub>	<b>v</b> <sub>5</sub>	<b>v</b> <sub>6</sub>	<b>v</b> <sub>7</sub>	<b>v</b> <sub>8</sub>	
u <sub>1</sub>	3.0					4.5			
u <sub>2</sub>	3.5	5.0						2.0	
u <sub>3</sub>				3.0		5.0			
u <sub>4</sub>		4.5	2.0				2.0		
u <sub>5</sub>	3.5		2.5						
u <sub>6</sub>					3.0			3.0	
u <sub>7</sub>					3.5	3.0			
u <sub>8</sub>			2.0				3.0	3.0	
u <sub>9</sub>	5.0				4.5				

Source: MovieLens Dataset

# Simple Approach — Pairwise Item Similarity

- Pairwise item similarity sim(x,y)
  - x, y feature vectors of movies
  - Common metric: cosine similarity

$$sim(x, y) = \cos(\theta) = \frac{x \cdot y}{\|x\| \|y\|}$$

sim(Heat, Heat) = 1.0 sim(Heat, Clueless) = 0.0 sim(Heat, Bad Boys) = 0.77 sim(Heat, Jarhead) = 0.33sim(Heat, Alice) = 0.0

- Limitation: Requires reference item, e.g.:
  - Movie(s) the user was most recently watching
  - Movie(s) the user has rated the highest
  - Movie(s) the user is currently browsing

#### Similar titles you might also like What is this?

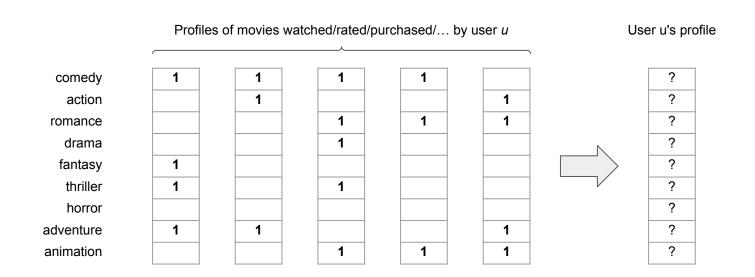


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  - **■** User-item similarity
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### **User-Item Similarities**

- Needed: user profiles = feature vector for each user
  - Requirement: same shape as item profiles to calculate similarities
  - Approach: user profile = "some aggregate" over item profiles rated by the user

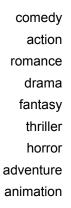


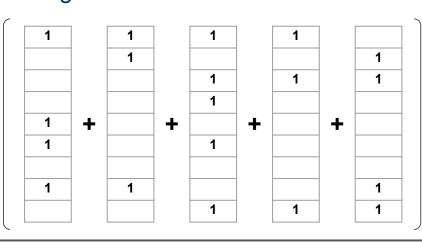
## **User-Item Similarities** — **Binary Utility Matrix**

- $R_{uv} \in \{0, 1\}$  for example,  $R_{uv} = 1$  if
  - User u bought movie v
  - User u watched movie v

Implicit rating that *u* like *v* (no explicit ratings available here; but also no implicit dislikes!)

#### Simple Average







#### User u's profile

4/5 = <b>0.8</b>
2/5 = <b>0.4</b>
3/5 = <b>0.6</b>
1/5 = <b>0.2</b>
1/5 = <b>0.2</b>
2/5 = <b>0.4</b>
0/5 = <b>0.0</b>
3/5 = 0.6
3/5 <b>= 0.6</b>

## User-Item Similarities — Real-Valued Utility Matrix

- $R_{uv} \in \mathbb{R}$  for example,  $R_{uv} \in \{1.0, 1.5, 2.0, 2.5, ..., 5.0\}$  star rating
  - Explicit rating of user *u* for movie *v*
  - Important: semantic interpretation ratings express both likes and dislikes (despite all ratings positive)
  - Use rating as weights for features for a weighted aggregation

comedy	1	1	1	1	
action		1			1
romance			1	1	1
drama			1		
fantasy	1				
thriller	1		1		
horror					
adventure	1	1			1
animation			1	1	1
u's ratings	1.5	2.0	4.5	5.0	4.0

#### Intuition

- The user likes romantic and animated movies
- The user dislikes fantasy and adventure movies

## User-Item Similarities — Real-Valued Utility Matrix

- Step 1: Normalize ratings
  - Subtract average user rating from each movie rating
  - Converts ratings into positive (liked) and negative (disliked) scale
  - Distinguishes "generous" users (mostly rate highly and a 3.0 is a low rating) from more "grumpy" users (mostly rate low and a 3.0 is a high rating)

comedy	1	1	1	1	
action		1			1
romance			1	1	1
drama			1		
fantasy	1				
thriller	1		1		
horror					
adventure	1	1			1
animation			1	1	1

Average user rating

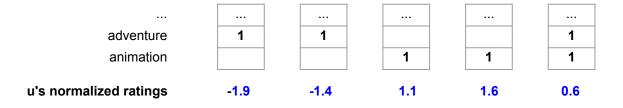
$$\frac{1.5 + 2.0 + 4.5 + 5.0 + 4.0}{5} = 3.4$$

1.6

0.6

## User-Item Similarities — Real-Valued Utility Matrix

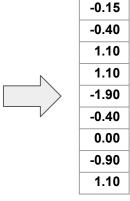
- Step 2: Calculate weighted features for user profile
  - The weights are the normalized weights



$$w_{adventure} = \frac{1 \cdot (-1.9) + 1 \cdot (-1.4) + 1 \cdot 0.6}{3} = -0.9$$

$$w_{animation} = \frac{1 \cdot 1.1 + 1 \cdot 1.6 + 1 \cdot 0.6}{3} = 1.1$$





comedy
action
romance
drama
fantasy
thriller
horror
adventure
animation

# **Quick Quiz**



### **User-Item Similarities**

- Pairwise item similarity sim(u,v)
  - *u* user profile; v item profile
  - Suitable metric: cosine similarity (note that user and item profiles can have different magnitudes)
- $\rightarrow$  Recommend items  $v_i$  to user u with max. similarities  $sim(u,v_i)$
- Practical considerations
  - Top k most similar items always the same  $\rightarrow$  add some randomization for diversity (the set of top k most similar items might only change over time if the user rates more items)
  - Top k most similar items might include items the user has already rated  $\rightarrow$  remove those items (in practice, recommending known items not uncommon e.g., YouTube recommendations)
  - More sophisticated ways to aggregate item profiles to user profiles conceivable (for example: ignore underrepresented features, e.g., if a user rated only one comedy movie)

## Content-Based Recommender System — Pros & Cons

#### Pros

- Recommendations for user *u* do not depend on other users (this also allows for good recommendations for users with very unique tastes)
- Recommendations can also include new or unpopular items (i.e., with no or very view ratings)
- Good explainability (features that had most effect on the high similarity)

#### Cons

- Cold-start problem: How to build a profile for new users? (naive approach: recommend generally popular items to new users)
- Finding good features (and values!) for items a non-trivial tasks (Question: Are genres a good feature set to represent movies?)
- Overspecialization: By default, no recommendations outside a user's profile (in practice: add some randomization into the recommendation process)

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### **Collaborative Filtering**

- Idea: Utilize the opinions of others
  - Recommend items that other user with similar tastes/preferences/needs have liked
  - Does not require item or user-specific features
- Two perspectives
  - User-based two users are similar if they rated the same items similarly
  - Item-based two items are similar if they are equally rated by users

### User-Based CF — Calculating Similarities

- Example: movie ratings
  - How much might Bob like the movie "Heat"?

	Clueless	Heat	Jarhead	Big	Rocky
Alice	2	4	5	0	1
Bob	1	???	4	0	2
Claire	1	0	4	3	0
Dave	5	1	2	0	5
Erin	1	5	3	0	3

- Intuitions given the dataset
  - Alice and Bob have similar tastes, so Bob might rate "Heat" similar to Alice
  - Claire and Bob have similar tastes, but Claire has not rated "Heat"
  - Dave and Bob have very different tastes, so Dave's opinion about "Heat" shouldn't matter (if anything, it should an indicator that Bob will like "Heat"; usually not relevant in practice)
- → How can we capture and quantify these intuitions?

### **User-Based CF** — Calculating Similarities

- Represent all users by their rating vectors v
  - Rows of rating matrix

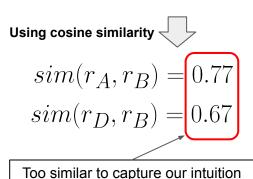
$$r_A = (2, 4, 5, 0, 1)^T$$

$$r_B = (1, 0, 4, 0, 2)^T$$

$$r_C = (1, 0, 4, 3, 0)^T$$

$$r_D = (5, 1, 2, 0, 5)^T$$

$$r_E = (1, 5, 3, 0, 3)^T$$



	Clueless	Heat	Jarhead	Big	Rocky
Alice	2	4	5	0	1
Bob	1	???	4	0	2
Claire	1	0	4	3	0
Dave	5	1	2	0	5
Erin	1	5	3	0	3

#### **Problem**

- Missing values (0) are treated as negative
- All ratings are positive values
- → No explicit notion of dissimilarity (only less or more similar)

## User-Based CF — Calculating Similarities

- Idea: Normalize rating vectors
  - Mean-centering subtract row mean from each rating vector
  - Missing values (0) now represent the average rating
  - Bad ratings (i.e., below average) now represented by negative values

	Clueless	Heat	Jarhead	Big	Rocky
Alice	2-3 = <b>-1</b>	4-3 = <b>1</b>	5-3 <b>= 2</b>	0	1-3 = <b>-2</b>
Bob	1-2.33 = <b>-1.33</b>	???	4-2.33 <b>= 1.67</b>	0	2-2.33 = <b>-0.33</b>
Claire	1-2.67 = <b>-1.67</b>	0	4-2.67 <b>= 1.33</b>	3-2.67 <b>= 0.33</b>	0
Dave	5-3.25 <b>= 1.75</b>	1-3.25 <b>= -2.25</b>	2-3.25 = <b>-1.25</b>	0	5-3.25 <b>= 1.75</b>
Erin	1-3 = <b>-2</b>	5-3 <b>= 2</b>	3-3 <b>= 0</b>	0	3-3 <b>= 0</b>

$$\Rightarrow sim(r_A, r_B) = 0.78$$
$$sim(r_D, r_B) = -0.65$$

Cosine similarity between mean-centered vectors → Pearson Correlation Coefficient

### **User-Based CF** — **Predicting Ratings**

- $\hat{R}_{uv}$  = weighted average of ratings from similar users
  - N set of k users most similar to u who have already rated item v

$$\widehat{R}_{uv} = \frac{\sum_{w \in N} sim(u, w) \cdot R_{wv}}{\sum_{w \in N} sim(u, w)}$$

- For the example
  - With k = 2

$$\widehat{R}_{Bob,Heat} = rac{\overbrace{0.78 \cdot 4 + 0.44 \cdot 5}^{ ext{Alice}}}{0.78 + 0.44} = 4.3$$

	Clueless	Heat	Jarhead	Big	Rocky
Alice	2	4	5	0	1
Bob	1	???	4	0	2
Claire	1	0	4	3	0
Dave	5	1	2	0	5
Erin	1	5	3	0	3

### **Item-Based CF**

- Analog to user-based approach
  - For an item *v*, find the most similar items (2 items are similar, if their ratings across all users are similar)
  - $\hat{R}_{uv}$  = weighted average of ratings of similar items
  - M set of k items most similar to v who have already been rated by u

$$\widehat{R}_{uv} = \frac{\sum_{i \in M} sim(i, v) \cdot R_{ui}}{\sum_{i \in M} sim(i, v)}$$

**Note:** Recall that in content-based recommender systems, measuring the similarity between items relied on item profiles / feature vectors. In case of item-item CF, the rating vector of an item represents its profile.

# **Item-Based CF** — **Example**

### Calculate mean-centered rating vectors (here: columns of rating matrix)

$$v_C = (0, -1, -1, 3, -1)^T$$

$$v_H = (0.67, 0, 0, -2.33, 1.67)^T$$

$$v_J = (1.4, 0.4, 0.4, -1.6, -0.6)^T$$

$$v_B = (0, 0, 0, 0, 0)^T$$

$$v_R = (-1.75, -0.75, 0, 2.25, 0.25)^T$$

	Clueless	Heat	Jarhead	Big	Rocky
Alice	2	4	5	0	1
Bob	1	???	4	0	2
Claire	1	0	4	3	0
Dave	5	1	2	0	5
Erin	1	5	3	0	3

# Calculate distances between "Heat" and all other movies Bob has already rated

$$sim(v_H, v_C) = -0.85$$
$$sim(v_H, v_J) = 0.55$$

$$sim(v_H, v_R) = -0.69$$

Even for k=2, there is only 1 movie with a positive Pearson correlation coefficient

$$\widehat{R}_{uv} = \overbrace{\frac{0.55 \cdot 4}{0.55}}^{\text{Jarhead}} = 4$$

### Collaborative Filtering — User-Based vs. Item-Based

- In theory: user-based and item-based are dual approaches
- In practice: item-based typically outperforms user-based
  - Items are "simpler" than users
  - Items can be more easily described
  - User can have very varied tastes

→ Item-item similarity typically more meaningful

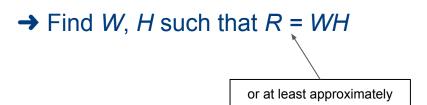
### **Outline**

- Overview
  - Motivation
  - Naive / alternative approaches
- Content-based recommendation systems
  - Pairwise item-item similarity
  - User-item similarity
- Collaborative filtering (CF)
  - Memory-based CF
  - Model-based CF

### **Model-Based Collaborative Filtering**

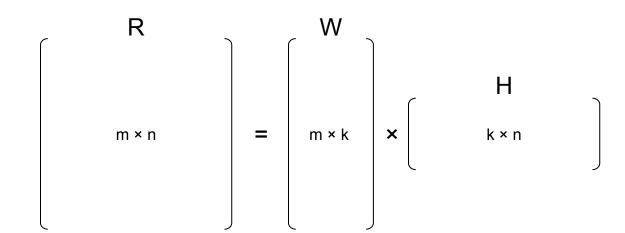
- Latent factor models
  - Latent representation: k-dimensional vector for each user u and item v
  - Learn latent representations from the data (in contrast to content-based systems where feature vectors are constructed)
  - lacktriangle Estimate unknown ratings  $\widehat{R}_{uv} = w_u^T h_v$

- Approach: Matrix Factorization
  - Put all user vectors into a matrix *W*
  - Put all item vector into a matrix *H*



## **Matrix Factorization** — Basic Setup

- Given: ratings matrix R
  - m number of users |W|
  - n number of items |H|



- Hyperparameter k
  - Size of latent representations

# Finding Matrices W, H

• Minimize loss function

$$L = \sum_{R_{uv}>0} e_{uv} = \sum_{R_{uv}>0} (R_{uv} - \widehat{R}_{uv})^2 = \sum_{R_{uv}>0} (R_{uv} - w_u^T h_v)^2$$

→ with regularization:

$$L = \sum_{P} (R_{uv} - w_u^T h_v)^2 + \lambda (\|w_u\|^2 + \|h_v\|^2)$$

### Using Gradient Descent

Calculate gradients

$$\frac{\partial e_{uv}}{\partial w_u} = -2(R_{uv} - w_u^T h_v) h_v + 2\lambda w_u$$

$$\frac{\partial e_{uv}}{\partial h_v} = -2(R_{uv} - w_u^T h_v) w_u + 2\lambda h_v$$

#### Update rules



$$w_u \leftarrow w_u - \eta \frac{\partial e_{uv}}{\partial w_u}$$

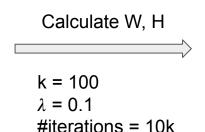
$$h_v \leftarrow h_v - \eta \frac{\partial e_{uv}}{\partial h_v}$$

## Finding Matrices W, H — Algorithm

```
Input: rating matrix R^{(m \times n)}, latent vector size k, #iterations T
Initialization: W^{(m \times k)}, H^{(k \times n)} with values 0..1
for 1 to T
      for all u, v with R_{uv} > 0
            w_u \leftarrow w_u + \eta [2(R_{uv} - w_u^T h_v)h_v - 2\lambda w_u]
             h_v \leftarrow h_v + \eta [2(R_{uv} - w_u^T h_v)w_u - 2\lambda h_h]
return W, H
```

## Finding Matrices W, H — Example

	V <sub>1</sub>	V <sub>2</sub>	<b>v</b> <sub>3</sub>	V <sub>4</sub>	<b>v</b> <sub>5</sub>	<b>v</b> <sub>6</sub>	V <sub>7</sub>
u <sub>1</sub>	4	0	0	5	1	0	0
u <sub>2</sub>	5	5	4	0	0	0	0
u <sub>3</sub>	0	0	0	2	4	5	0
u <sub>4</sub>	0	3	0	0	0	0	3



	V <sub>1</sub>	<b>v</b> <sub>2</sub>	<b>v</b> <sub>3</sub>	V <sub>4</sub>	<b>V</b> <sub>5</sub>	<b>v</b> <sub>6</sub>	<b>V</b> <sub>7</sub>
u <sub>1</sub>	3.9	3.5	3.4	4.8	1	2.4	3.1
u <sub>2</sub>	4.9	4.8	4	3.7	3.2	5.3	4.4
u <sub>3</sub>	3.4	3.3	3.6	2	3.8	4.9	3.9
$u_{\scriptscriptstyle{4}}$	3.1	2.9	3.2	2.5	2.3	3.8	3

 $W \cdot H$ 

### Effects of regularization

- Increase  $\lambda$ : worse fit of known ratings, "smoother" values for all ratings
- Decrease  $\lambda$ : better fit of known ratings, more "extreme" values of unknown ratings

### Collaborative Filtering — Pros & Cons

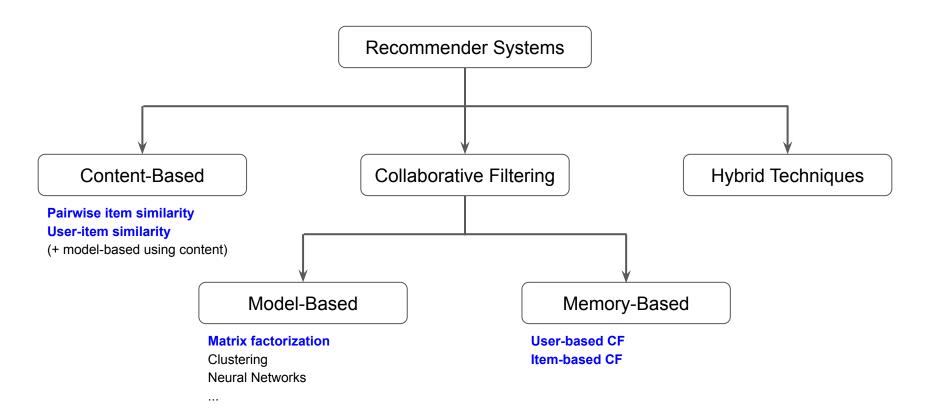
#### Pros

- No need to find and create good features (such as genres for movies)
- Intuitive approach

#### Cons

- Similarity calculations rely on sufficient number of ratings
- Cold-start problem in case of new users or items
- Popularity bias: user with very unique tastes likely to get subpar recommendations (because even the k most similar users will not be truly very similar)
- Naive implementation very expensive: Finding k most similar users/items ∈ O(|R|) (optimization techniques needed: e.g. clustering of users/items to limit search space)

### **Recommender Systems — Summary**



# **Quick Quiz**



# **Quick Quiz**



### The Dangers of (Over-)Personalization

• 2 infamous side-effects

(particularly when recommending news or social media posts)

- Filter bubbles
- **■** Echo chambers
- Core problems
  - No incentive for service providers to ensure (sufficient) diversity
  - Users do not know what content is shown and why (or why not!)

### Why is TikTok creating filter bubbles based on your race?

How social media filter bubbles and algorithms influence the election

When Algorithms Decide Whose Voices Will Be Heard

Social Media Giants Support Racial Justice. Their Products Undermine It.

Facebook reportedly ignored its own research showing algorithms divided users

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### **Summary**

- Recommender systems
  - More specifically: personalized recommender systems
  - Integral component of many online platforms
  - User: find relevant items + providers: present relevant items
  - BUT: risk of over-personalized recommendations
- Implementing recommender systems
  - Wide range of data mining techniques applicable
  - No "one-size-fits-all" solutions
  - In practice, hybrid approaches most successful

# **Solutions to Quick Quizzes**

