

InsertionSort: left shift until correct $\rightarrow O(n^2)$

Mergesort: two sub-array to sort(divide&conquer) $\rightarrow O(n \log n)$

BinarySearch: start search from the middle, then middle again \rightarrow

$$T(n) \leq T(n/2) + O(1) = O(\log n)$$

Quicksort: use pivot to sort, move pivot in the middle at end. \rightarrow Best:

$$T(n) = 2T(n/2) + \Theta(n) \rightarrow O(n \log n), \text{ Worst: } O(n^2)$$

BFS: $G=(V,E)$: G for graph, V for nodes, E for edges. Search all nodes in a layer before going to the next. $\rightarrow O(n + E)$, n for V

DFS: Search according to depth first, touch the button then traceback. $\rightarrow O(n + E)$

Dijkstra: greedy alg for calculate the shortest path using graph. \rightarrow

$$T(n) = O(n \log n + m \log n) = O(m \log n), m = V + E, n = V$$

Huffman: compress document using Binary Tree, most frequent word put in forward to get less bit. $\rightarrow O(n \log n)$

SegmentedLeastSquares: fit a curve containing several pieces of line (dynamic programming). $\rightarrow O(n^2)$

Sequence Alignment: find the most similarity of two sentence with least error(dynamic programming). \rightarrow Two for loops: $O(nm)$

Upper: Big $O \leq$, **Lower:** Big $\Omega \geq$, **Tight:** Big $\Theta =$, little o $<$, little w $>$

$$\log n < n < n \log n < n^2 < 2^n < 3^n < n^n$$

Simple path for distinct nodes; **Simple cycle** for distinct paths; **Strongly Connect Components(SCC)** for bidirectional node.

$$\text{Recursive Fibonacci: } T(n) = O(1) + T(n-1) + T(n-2) = \Omega(2^n/2)$$

$$\text{Non-recursive Fib: } T(n) = O(n)$$

$$\text{Fib mul add: } T(n) = O(\log n)$$

BFS_CutNode: find node v between s and t which will destroy all s-t path if v is deleted. $\rightarrow O(n + E)$

Graph_isOdd: find if a directed graph G has an odd-length cycle. $\rightarrow O(V^2)$

WaterPouringBFS: two bottles with capacity X and Y with initial water x and y. Find possible or not that A liters water should in any bottle. $\rightarrow O(n^2)$

2SAT: find if there has the specific node and its negation in a same SCC, if yes, it is not Boolean satisfiable. $\rightarrow O(n + m)$, for n numbers of variables and m number of clauses.

Recursive: call function repeatedly; **Iterative:** Use (for) loop

Master Theorem: For a $T(n) = aT(n/b) + f(n)$, where $f(n) = \Theta/O/\Omega(n^c)$. If $c < 2$, $T(n) = \Theta(n^2)$; if $c = 2$, $T(n) = \Theta(n^2 \cdot \log(n))$; if $c > 2$, $T(n) = \Theta(f(n))$

