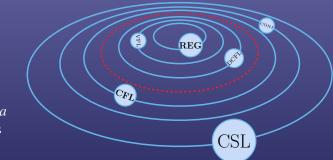


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Pushdown Machines: Visible and Not



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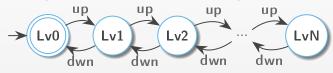
Lecture Outline



Finite Automata is Enough?

Real-world machines are finite. Do finite models suffice?

Recall "elevator automaton" with a unique final state on the "ground floor", breaking if asked to reach an non-existing floor:



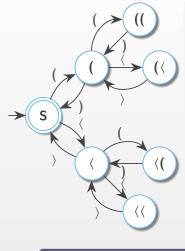
"up" and "dwn" instructions can be interpreted wrt a parentheses structure. That is, parsing string "((" we move to Lv2, and "(()())" returns us to Lv1.

Real-world nesting depth is limited (even in Lisp-like languages), and linear blow-up in state size seems satisfactory.

Until we decide to use several sorts of brackets...



Myhill-Nerode Congruence for Many-Sorted Brackets



Congruence Table

8. 1101100 111010								
		ε)	\rangle))	$\rangle)$	\rangle	$\rangle \rangle$
	ε	+	-	-	-	-	-	-
	(_	+	-	-	-	-	-
	<	_	-	+	-	-	-	-
	((_	-	-	+	-	-	-
	((_	_	_	- - - + -	+	-	-
	((_	-	-	-	-	+	-
	$\langle \langle$	_	-	-	_	-	-	+

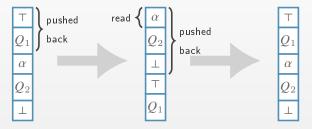
- *N*-depth balanced sequences of 2 sorts of brackets $\Rightarrow 2^{N+1} 1$ states in a min NFA.
- *N*-depth balanced sequences of *K* sorts of brackets $\Rightarrow \frac{K^{N+1}-1}{K-1}$ states in a min <u>NFA</u>.

Finite automata cannot track nested structures efficiently.



Memoising Counters via Additional Memory

 Queue as a memory — can be considered as an additional tape with the write access, since it can be "re-rolled" to any wanted position with no memory loss.



• Stack as a memory — information given in Q_1 cannot be stored except in states when α is read. More restrictive, natural for tracking nested structures.

