

Say, we have algorithms for the same problem

Line by line analysis gives:

Algorithm A: $T(n) = 10 \cdot n^2 + 5$

Algorithm B: $T(n) = 100000 \cdot n + 100000$

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$n=1$ $T(1)=15$

$T(1)=200000$

$n=10$ $T(10)=1005$

$T(10)=1100000$

.....

$n=1000$ $T(1000)=1000005$

$T(1000)= 100000000+100000$

$n=100000$ (becoming larger than the second)

We can compare two functions based on order of growth

Asymptotic Analysis

Algorithms are compared based on n tends to infinity

Ignore constant terms from $T(n)$

Algorithm A: $T(n) \propto n^2 = O(n^2)$

Algorithm B: $T(n) \propto n = O(n)$

Big-oh notation: O

$T(n)=f(n)= 5n^2 + 10$

$g(n)= n^2$

$f(n) = O(g(n)) = O(n^2)?$

$f(n) \geq 0$ and $f(n) \leq c \cdot g(n)$

Find n_0 , for which above condition holds for all $n > n_0$

$f(n)= 5n^2 + 10 \leq 15n^2$

$5n^2 + 10 < 30n^2$ for all $n \geq 1$

$n_0=1, c=30$

$f(n)=O(n^2)$

$$f(n) \leq c \cdot n^2$$

$$T(n) \leq c \cdot g(n)$$

Limit method