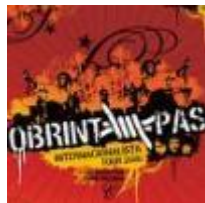


Skenirana rješenja

Prijenosne funkcije i a.-f. karakteristika: Zadaci sa rješenjima za vježbu

by:

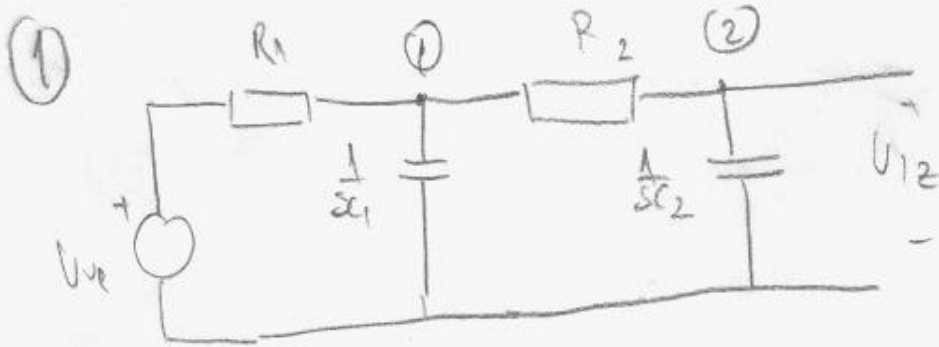
Limpus (... direktor svemira...)



Skenirao: Tywin



$$R_1 = R_2 = C_1 = C_2 = 1$$



$$(1) \quad U_1 \left(\frac{1}{R_1} + sC_1 + \frac{1}{R_2} \right) - U_2 \left(\frac{1}{R_2} \right) = \frac{U_{ve}}{R_1}$$

$$(2) \quad U_2 \left(\frac{1}{R_2} + sC_2 \right) - U_1 \left(\frac{1}{R_2} \right) = 0$$

$$(1) \quad U_1 (1+s+1) - U_2 = U_{ve} \quad \leftarrow$$

$$(2) \quad U_2 (1+s) - U_1 = 0 \rightarrow \boxed{U_1 = (s+1) U_2}$$

$$\Rightarrow U_2 [(s+1)(s+2)] - U_2 = U_{ve}$$

$$U_2 [s^2 + s + 2s + 2 - 1] = U_{ve}$$

$$\boxed{U_2 [s^2 + 3s + 1] = U_{ve}}$$

$$T(s) = \frac{U_{12}}{U_{ve}} = \frac{U_2}{U_{ve}} = \frac{\cancel{U_2}}{\cancel{U_2} [s^2 + 3s + 1]} = \frac{1}{s^2 + 3s + 1}$$

$$T(j\omega) = \frac{1}{- \omega^2 + 3j\omega + 1} = \frac{1}{1 - \omega^2 + 3j\omega}$$

$$|T(j\omega)| = \frac{1}{\sqrt{(1 - \omega^2)^2 + 9\omega^2}}$$

$$|T(j\omega)| = \frac{1}{\sqrt{(1-\omega^2)^2 + 9\omega^2}} \quad \text{①}$$

$$|T(0)| = 1$$

$$|T(\infty)| = 0$$

$$|T(1)| = \frac{1}{\sqrt{9}} = \frac{1}{3}$$



$$(2) R_1 = R_2 = 10 \text{ k}\Omega = 10 \cdot 10^3 \Omega$$

$$C_1 = C_2 = 1 \text{ mF} = 1 \cdot 10^{-3} \text{ F}$$

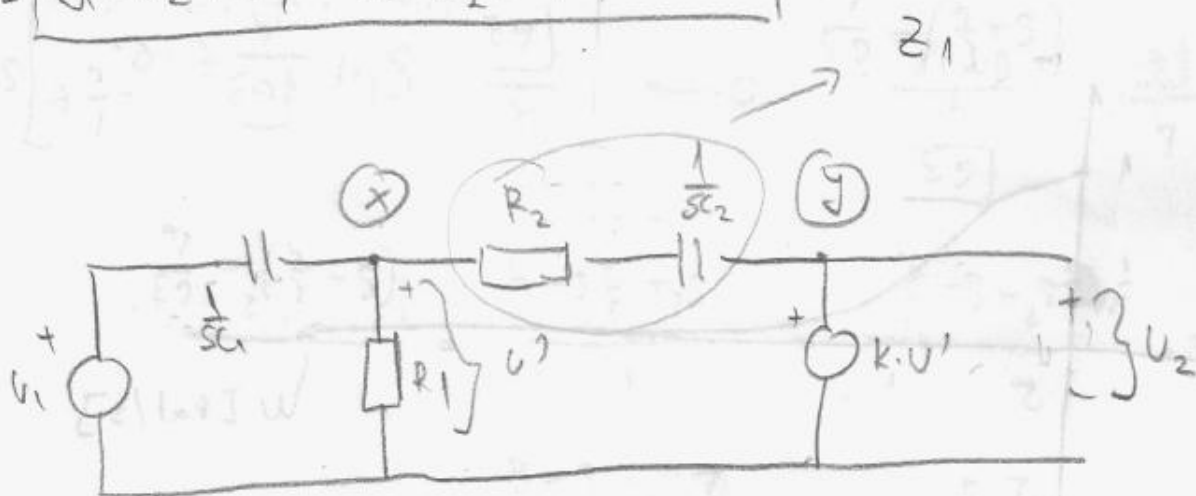
$$k = 2$$

$$\Rightarrow \omega_0 = 10^5 \text{ rad/s}, R_0 = 10^4 \text{ k}\Omega$$

$$\Rightarrow R_m = \frac{R}{R_0} = \frac{10^4}{10^4} = 1$$

$$\Rightarrow C_m = \omega_0 R_0 C_0 = 10^5 \cdot 10^4 \cdot 10^{-9} = 1$$

$$\Rightarrow R_1 = R_2 = 1, C_1 = C_2 = 1, k = 2$$



$$Z_1 = R_2 + \frac{1}{sC_2} = \frac{R_2 sC_2 + 1}{sC_2}$$

$$(1) U_x \left(sC_1 + R_1 + \frac{sC_2}{R_2 sC_2 + 1} \right) - U_y \left(\frac{sC_2}{R_2 sC_2 + 1} \right) = U_1 sC_1$$

$$(2) U_y = k \cdot U' \Rightarrow U_y = k \cdot U_x \Rightarrow \boxed{U_y = 2 \cdot U_x} \Rightarrow \boxed{U_x = \frac{U_y}{2}}$$

$$U_x \left(s+1 + \frac{s}{s+1} \right) - U_y \left(\frac{s}{s+1} \right) = U_1 s$$

$$U_x \left(\frac{s^2 + s + s + 1 + s}{s+1} \right) - U_y \left(\frac{s}{s+1} \right) = U_1 s$$

$$U_x \left(\frac{s^2 + 3s + 1}{s+1} \right) - U_y \left(\frac{s}{s+1} \right) = U_1 s \quad (5)$$

$$U_y \left(\frac{s^2 + 3s + 1}{2(s+1)} \right) - U_y \left(\frac{s}{s+1} \right) = U_1 s$$

$$U_y \left(\frac{s^2 + 3s + 1}{2(s+1)} - \frac{s}{s+1} \right) = U_1 s$$

$$U_y \left(\frac{s^2 + 3s + 1}{2(s+1)} \right) = U_1 s \Rightarrow U_1 = \frac{s^2 + 3s + 1}{2s(s+1)} U_y$$

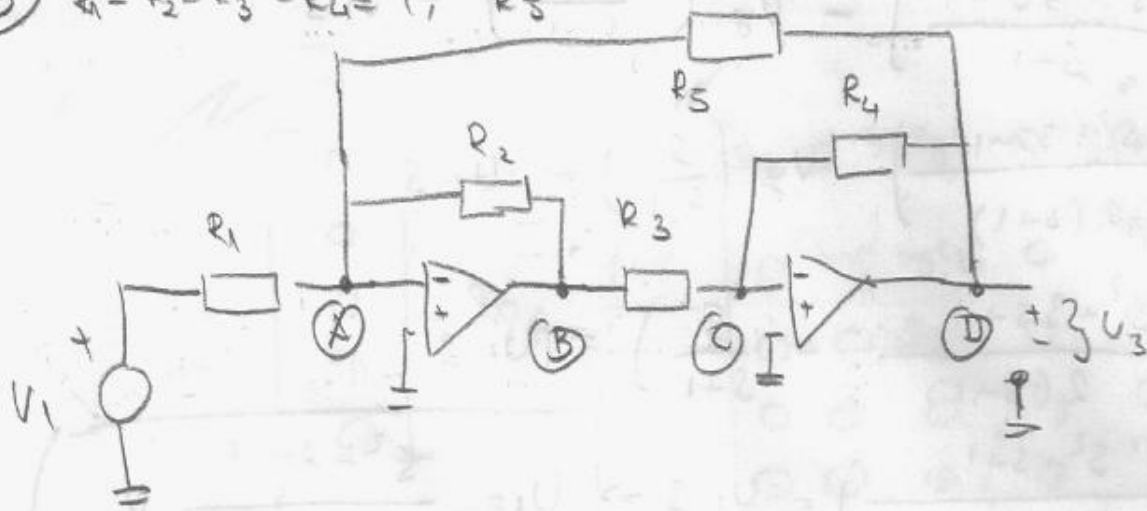
$$T(s) = \frac{U_2}{U_1} = \frac{U_y}{U_1} = \frac{2s(s+1)}{s^2 + 3s + 1}$$

POLY: $s^2 + 3s + 1 = 0 \Rightarrow s_{p1,2} = \frac{-1 \pm \sqrt{1-4}}{2} = -\frac{1}{2} \pm j\frac{\sqrt{3}}{2}$

NULE: $2s(s+1) = 0 \Rightarrow s_{01} = 0, s_{02} = -1$



③ $R_1 = R_2 = R_3 = R_4 = 1, R_5 = 2$



$$\Rightarrow (A) \quad U_A \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_5} \right) - U_B \left(\frac{1}{R_2} \right) - U_D \left(\frac{1}{R_5} \right) = \frac{V_1}{R_1}$$

$$(C) \quad U_C \left(\frac{1}{R_3} + \frac{1}{R_4} \right) - U_B \left(\frac{1}{R_3} \right) - U_D \left(\frac{1}{R_4} \right) = 0$$

$$\Rightarrow \boxed{U_A = U_C = 0}$$

$$\Rightarrow (A) \quad -U_B \left(\frac{1}{R_2} \right) - U_D \left(\frac{1}{R_5} \right) = \frac{V_1}{R_1}$$

$$(C) \quad -U_B \left(\frac{1}{R_3} \right) - U_D \left(\frac{1}{R_4} \right) = 0$$

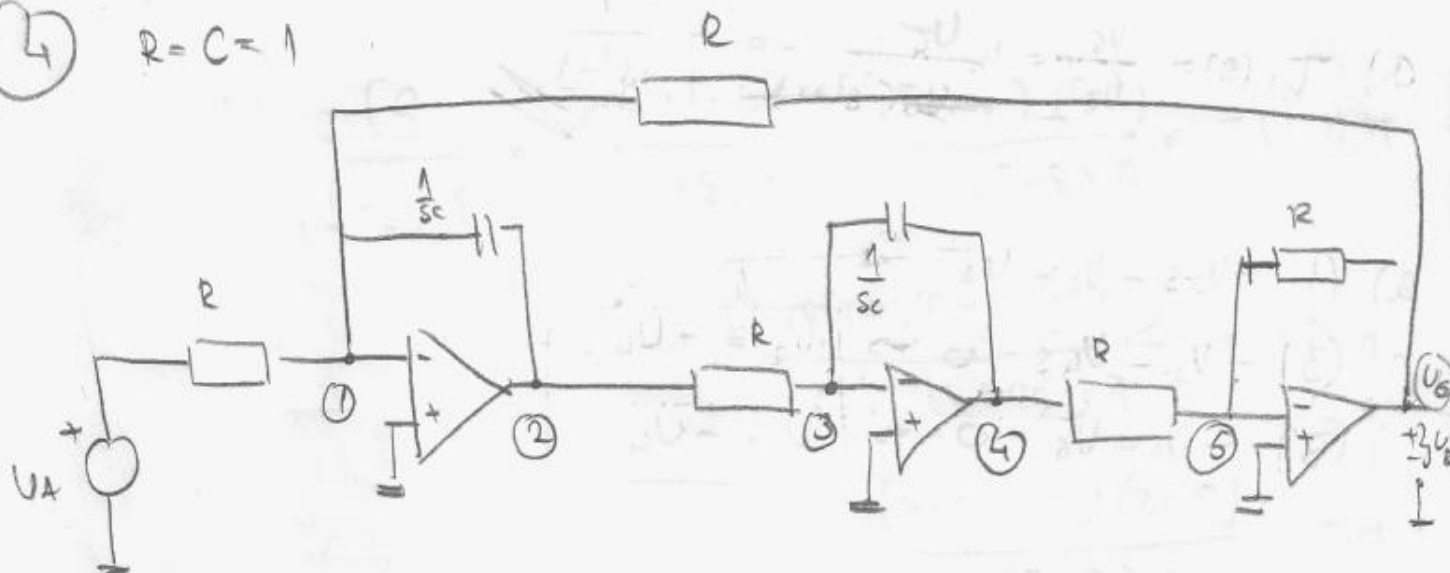
$$= U_B - \frac{1}{2} U_D = V_1 \quad \leftarrow$$

$$-U_B - U_D = 0 \Rightarrow \boxed{U_B = -U_D}$$

$$+ U_D - \frac{1}{2} U_D = V_1 \Rightarrow \boxed{U_1 = \frac{1}{2} U_D}$$

$$T(s) = \frac{U_3}{U_1} = \frac{U_D}{U_1} = \frac{U_D}{\frac{1}{2} U_D} = \frac{1}{\frac{1}{2}} = 2 //$$

④ $R = C = 1$



$$(1) U_1 \left(\frac{1}{R} + sC + \frac{1}{R} \right) - U_2(sC) - U_6 \left(\frac{1}{R} \right) = \frac{U_A}{R}$$

$$(3) U_3 \left(\frac{1}{R} + sC \right) - U_2 \left(\frac{1}{R} \right) - U_4(sC) = 0$$

$$(5) U_5 \left(\frac{1}{R} + \frac{1}{R} \right) - U_4 \left(\frac{1}{R} \right) - U_6 \left(\frac{1}{R} \right) = 0$$

$$\Rightarrow \boxed{U_1 = U_3 = U_5 = 0}$$

$$(1) -U_2(sC) - U_6 \left(\frac{1}{R} \right) = \frac{U_A}{R}$$

$$(3) -U_2 \left(\frac{1}{R} \right) - U_4 sC = 0$$

$$(5) -U_4 \left(\frac{1}{R} \right) - U_6 \left(\frac{1}{R} \right) = 0$$

$$(1) -U_2 s - U_6 = U_A$$

$$(3) -U_2 - U_4 s = 0 \quad \leftarrow$$

$$(5) -U_4 - U_6 = 0 \Rightarrow \boxed{U_4 = -U_6}$$

$$(3) \Rightarrow -U_2 + U_6 s = 0 \Rightarrow \boxed{U_2 = U_6 s}$$

$$-U_6 s^2 - U_6 = U_A \Rightarrow \boxed{U_A = -U_6 (s^2 + 1)}$$

$$a) T_1(s) = \frac{U_6}{U_A} = \frac{U_6}{-U_6(s^2+1)} = -\frac{1}{s^2+1}$$

a) (1) $-U_2 s - U_6 = U_A$ ← T_1

(3) $-U_2 - U_4 s = 0 \Rightarrow U_2 = -U_4 s$

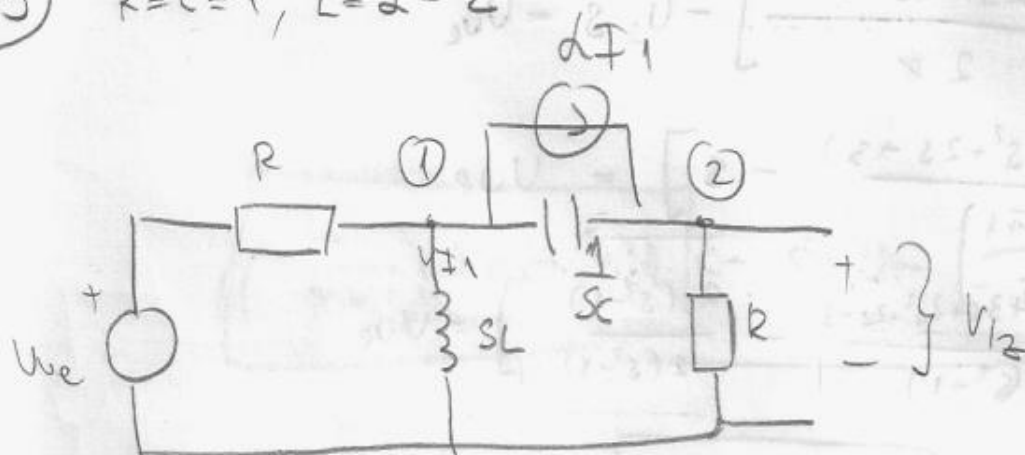
(5) $-U_4 - U_6 = 0 \Rightarrow U_6 = -U_4$

$$(1) U_4 s^2 + U_4 = U_A$$

$$U_4 (s^2+1) = U_A$$

$$T(s) = \frac{U_4}{U_A} = \frac{U_4}{U_4 (s^2+1)} = \frac{1}{s^2+1}$$

⑤ $R=C=1, L=2=2$



$$(1) U_1 \left(\frac{1}{R} + \frac{1}{SL} + sC \right) - U_2 (sC) = \frac{U_{ve}}{R} - 2I_1$$

$$(2) U_2 \left(sC + \frac{1}{R} \right) - U_1 (sC) = 2I_1$$

$$(3) I_1 = \frac{U_1}{SL}$$

$$(1) U_1 \left(1 + \frac{1}{2s} + s \right) - U_2 s = U_{ve} - 2 \left(\frac{U_1}{2s} \right)$$

$$(2) U_2 (s + 1) - U_1 s = 2 \left(\frac{U_1}{2s} \right)$$

$$(1) U_1 \left(\frac{2s+1+2s^2}{2s} \right) - U_2 s = U_{ve} - \frac{U_1}{s}$$

$$(2) U_2 (s+1) - U_1 s = \frac{U_1}{s} \Rightarrow U_2 (s+1) = U_1 \left(\frac{1}{s} + s \right)$$

$$\Rightarrow U_2 (s+1) = U_1 \left(\frac{s^2+1}{s} \right) \Rightarrow \boxed{U_1 = U_2 \left[\frac{s(s+1)}{s^2+1} \right]}$$

$$(1) U_1 \left(\frac{2s^2+2s+1}{2s} + \frac{1}{s} \right) - U_2 s = U_{ve}$$

$$U_1 \left(\frac{2s^2+2s+3}{2s} \right) - U_2 s = U_{ve}$$

$$U_2 \left[\frac{8(s+1)}{s^2+1} - \frac{2s^2+2s+3}{2 \cdot 8} \right] - U_2 s = U_{ve}$$

$$U_2 \left[\frac{(s+1)(2s^2+2s+3)}{2(s^2+1)} - s \right] = U_{ve}$$

$$U_2 \left[\frac{2s^3+2s^2+3s+2s+3}{2(s^2+1)} - \frac{2s(s^2+1)}{2(s^2+1)} \right] = U_{ve}$$

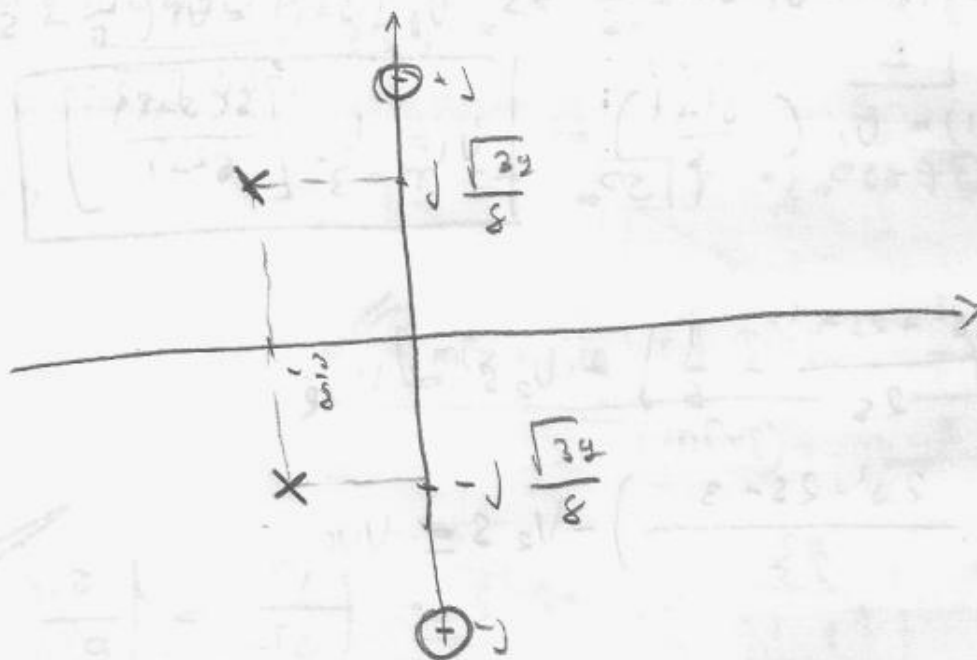
$$U_2 \left[\frac{\cancel{2s^3} + 4s^2 + 5s + 3 - 2s^3 - 2s}{2(s^2+1)} \right] = U_{ve}$$

$$U_2 \left(\frac{4s^2 + 3s + 3}{2(s^2+1)} \right) = U_{ve}$$

$$T(s) = \frac{U_{ve}}{U_{ve}} = \frac{U_2}{U_{ve}} = \frac{2(s^2+1)}{4s^2+3s+3}$$

$$\text{Polovi: } 4s^2+3s+3=0 \rightarrow s_{p1,2} = \frac{-3 \pm \sqrt{9-48}}{8} = -\frac{3}{8} \pm j \frac{\sqrt{39}}{8}$$

$$\text{Nule: } 2(s^2+1)=0 \rightarrow s^2+1=0 \rightarrow \boxed{s_{o1,2} = \pm j}$$



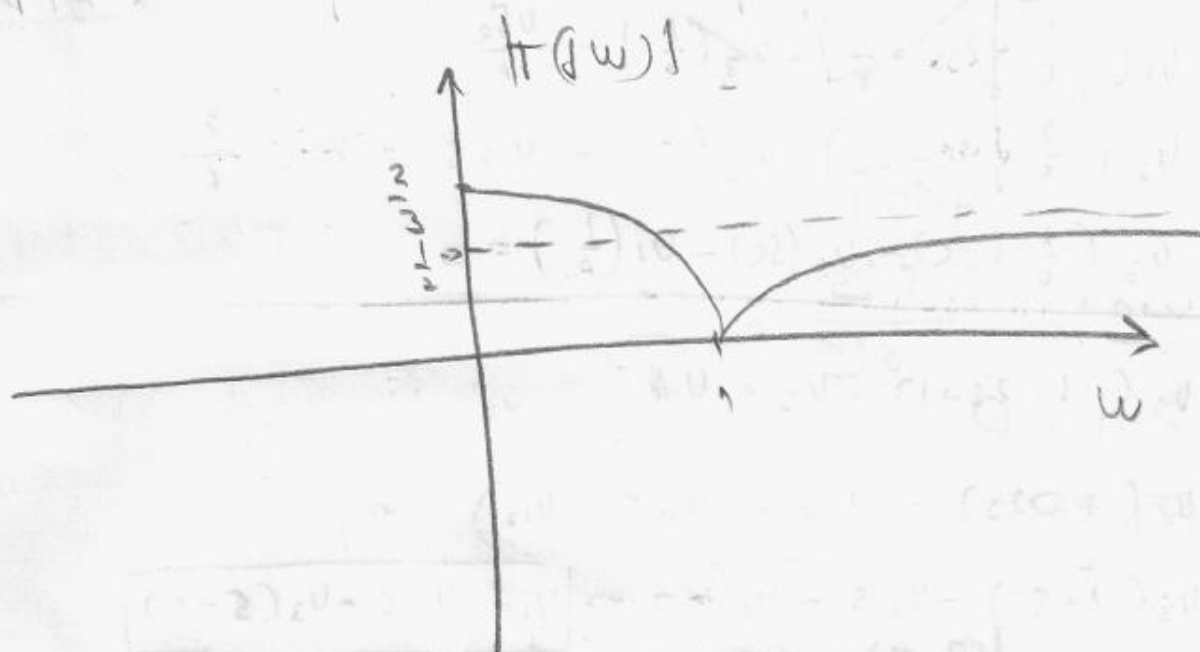
$$T(j\omega) = \frac{2(1-\omega^2)}{-4\omega^2 + 3j\omega + 3} = 2 \frac{(1-\omega^2)}{(3-4\omega^2) + 3j\omega}$$

$$|T(j\omega)| = 2 \frac{\sqrt{(1-\omega^2)^2}}{\sqrt{(3-4\omega^2)^2 + 9\omega^2}}$$

$$|T(0)| = 2 \frac{1}{\sqrt{3^2}} = \frac{2}{3}$$

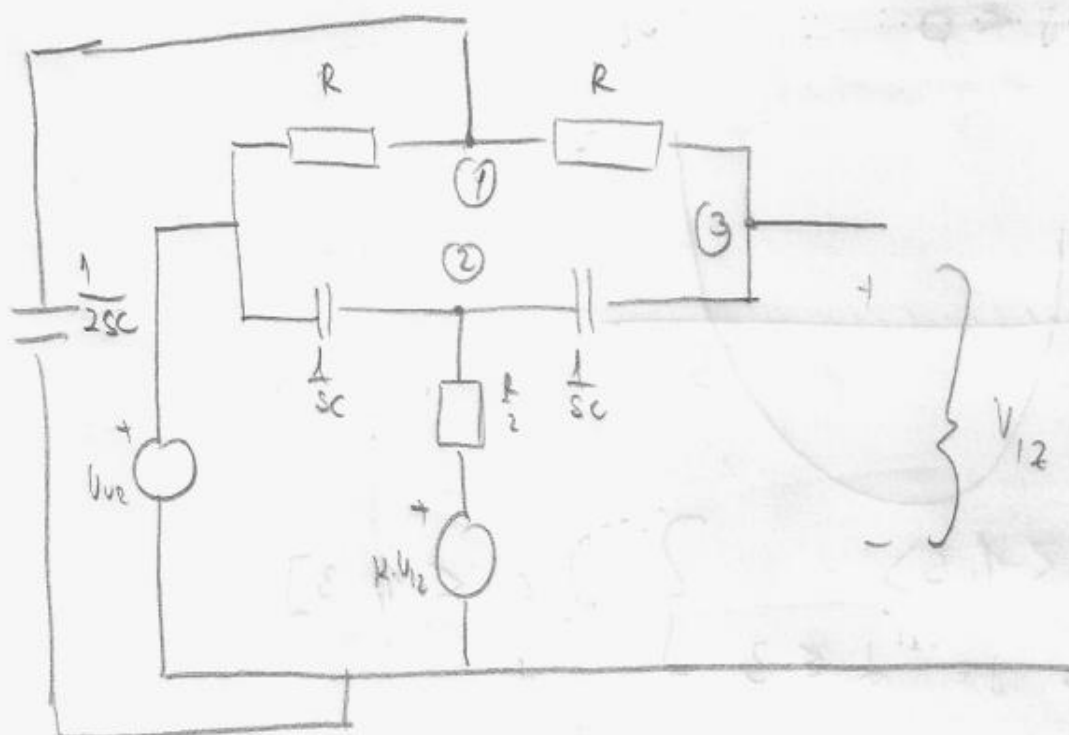
$$|T(\infty)| = 2 \frac{1}{4} = \frac{1}{2}$$

$$|T(1)| = 0$$



⑥

$$R=C=1, k=\frac{3}{2}$$



$$① \quad U_1 \left(\frac{1}{2} + 2s + \frac{1}{2} \right) - U_3 \left(\frac{1}{2} \right) = \frac{U_{ve}}{2}$$

$$② \quad U_2 \left(s + \frac{2}{2} + s \right) - U_3 (s) = k \cdot U_3 \cdot \frac{2}{2} + U_{ve} s$$

$$③ \quad U_3 \left(s + \frac{1}{2} \right) - U_2 (s) - U_1 \left(\frac{1}{2} \right) = 0$$

$$① \quad U_1 (2 + 2s) - U_3 = U_{ve}$$

$$② \quad U_2 (2 + 2s) - U_3 s = 3U_3 + U_{ve} s$$

$$③ \quad U_3 (s + 1) - U_2 s - U_1 = 0 \rightarrow U_1 = U_3 (s + 1) - U_2 s$$

$$U_2 (2 + 2s) = 3U_3 + sU_3 + U_{ve} s$$

$$U_1 (2 + 2s) = U_3 (s + 3) + U_{ve} s \rightarrow U_2 = U_3 \frac{s + 3}{2(s + 1)} + U_{ve} \frac{s}{2(s + 1)}$$

$$[V_3(s+1) - V_2s] 2(s+1) - V_3 = U_{ve}$$

$$V_3 2(s+1)^2 - V_2 2s(s+1) - V_3 = U_{ve}$$

$$V_3 [2(s^2+2s+1) - 1] - V_2 [2s(s+1)] = U_{ve}$$

$$V_3 [2s^2+4s+1] - \left[V_3 \frac{s+3}{2s+1} + U_{ve} \frac{s}{2s+1} \right] \cdot 2s(s+1) = U_{ve}$$

$$V_3 [2s^2+4s+1] - V_3 s(s+3) - U_{ve} s^2 = U_{ve}$$

$$V_3 \left[\frac{2s^3+4s^2+3}{s} - \frac{s^2(s+3)}{s} \right] = U_{ve} (s^2+1)$$

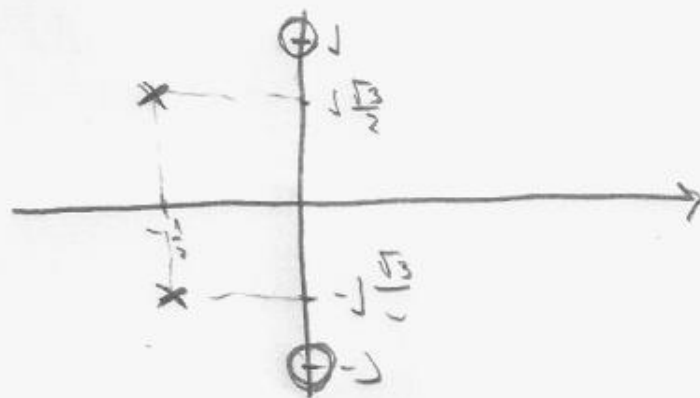
$$V_3 \left(\frac{2s^3+4s^2+3-s^3-3s^2}{s} \right) \cdot \frac{1}{s^2+1} = U_{ve}$$

$$U_{ve} = V_3 \left(\frac{s^3+s^2+3}{s(s^2+1)} \right) = V_3 \frac{s^2+s+1}{s^2+1}$$

$$T(s) = \frac{V_3}{U_{ve}} = \frac{s^2+1}{s^2+s+1}$$

POLovi: $s^2+s+1=0 \rightarrow s_{p1,2} = -\frac{1}{2} \pm j \frac{\sqrt{3}}{2}$

NOLE: $s^2+1=0 \rightarrow s_{o1,2} = \pm j$



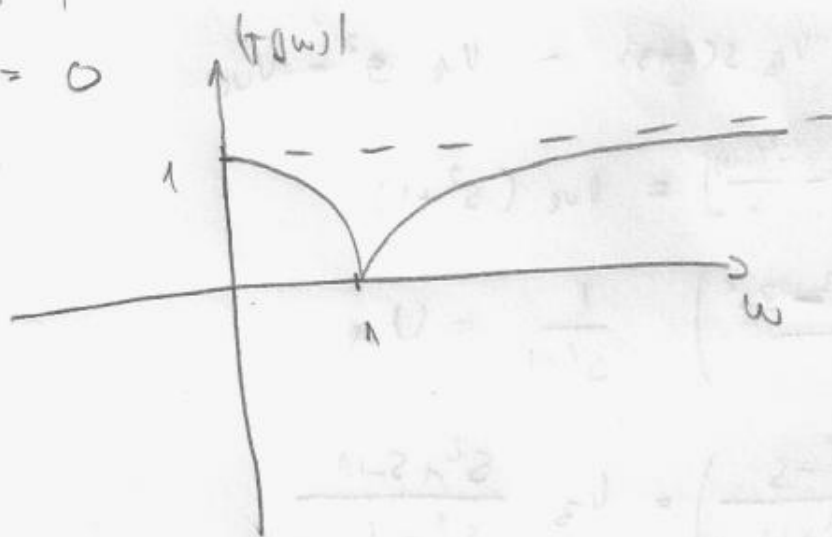
$$T(s) = \frac{s^2 + 1}{s^2 + s + 1}$$

$$T(j\omega) = \frac{1 - \omega^2}{1 - \omega^2 + j\omega} \Rightarrow |T(j\omega)| = \frac{|1 - \omega^2|}{\sqrt{(1 - \omega^2)^2 + \omega^2}}$$

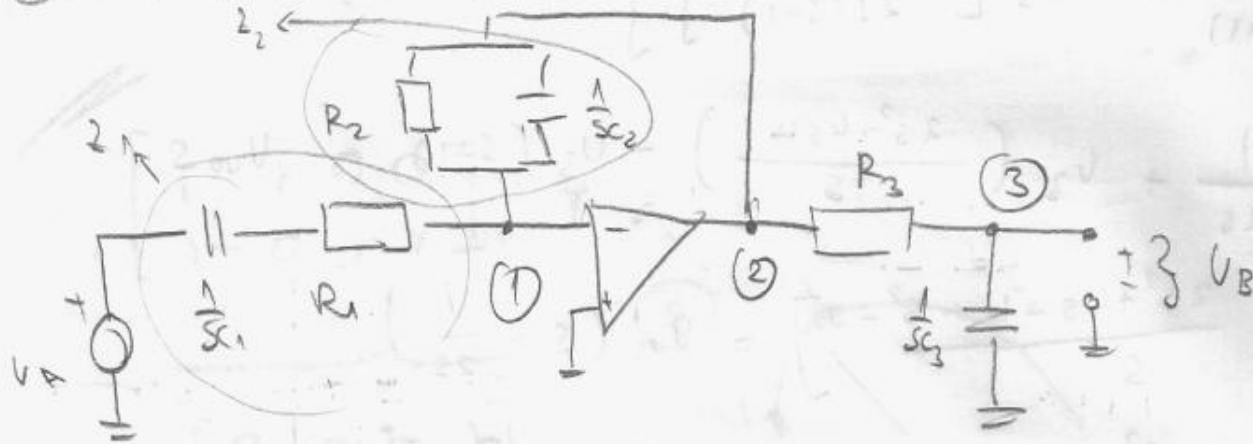
$$T(0) = 1$$

$$|T(\infty)| = 1$$

$$|T(1)| = 0$$



⑦ $R_1 = R_2 = R_3 = 1$, $C_1 = 1$, $C_2 = \frac{1}{2}$, $C_3 = 2$



$$Z_1 = \frac{1}{s_1} + R_1 = \frac{1 + R_1 s_1}{s_1}$$

$$Z_2 = \left(\frac{1}{R_2} + s_2 \right)^{-1} = \left(\frac{1 + R_2 s_2}{R_2} \right)^{-1} \Rightarrow Z_2 = \frac{R_2}{1 + R_2 s_2}$$

$$\textcircled{1} \quad V_1 \left(\frac{s_1}{1 + R_1 s_1} + \frac{1 + R_2 s_2}{R_2} \right) - V_2 \left(\frac{1 + R_2 s_2}{R_2} \right) = V_A \frac{s_1}{1 + R_1 s_1}$$

$$\textcircled{3} \quad V_3 \left(\frac{1}{R_3} + s_3 \right) - V_2 \left(\frac{1}{R_3} \right) = 0$$

$$\Rightarrow V_1 = 0$$

$$\textcircled{1} \quad -V_2 \left(\frac{1 + \frac{1}{2}s}{1} \right) = V_A \frac{s}{1 + s} \quad \leftarrow$$

$$\textcircled{3} \quad V_3 (1 + 2s) - V_2 = 0 \Rightarrow \boxed{V_3 (2s + 1) = V_2}$$

$$\textcircled{1} \quad -V_3 (2s + 1) \left(\frac{\frac{2 + s}{2}}{1} \right) = V_A \frac{s}{s + 1}$$

$$-V_3 \frac{(2s + 1)(s + 2)}{2} = V_A \frac{s}{s + 1} \Rightarrow \boxed{V_A = - \frac{(s + 2)(2s + 1)(s + 1)}{2s} V_3}$$

$$T(s) = \frac{U_3}{U_4} = \frac{2s}{(s+2)(s+1)(2s+1)} \quad (8)$$

$$\Rightarrow \text{Poles: } s+2=0 \rightarrow s_{p1} = -2$$

$$s+1=0 \rightarrow s_{p2} = -1$$

$$2s+1=0 \rightarrow s_{p3} = -\frac{1}{2}$$

$$\text{NULE: } s_{0,1} = 0$$

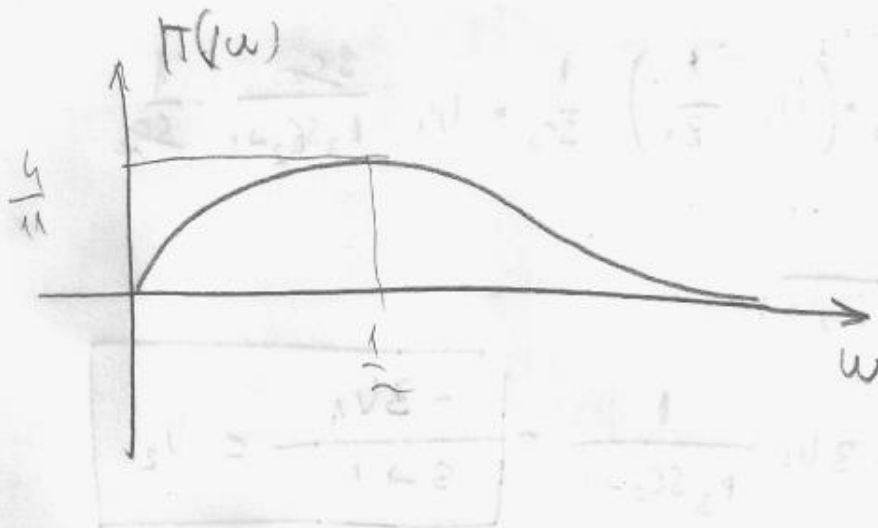
$$s_{0,2} = \infty, s_{0,3} = \infty$$



$$T(j\omega) = \frac{-2j\omega}{(2+j\omega)(1+j\omega)(1+2j\omega)} \Rightarrow |T(j\omega)| = \frac{|-2j\omega|}{\sqrt{[(1)(1)(1)]^2}}$$

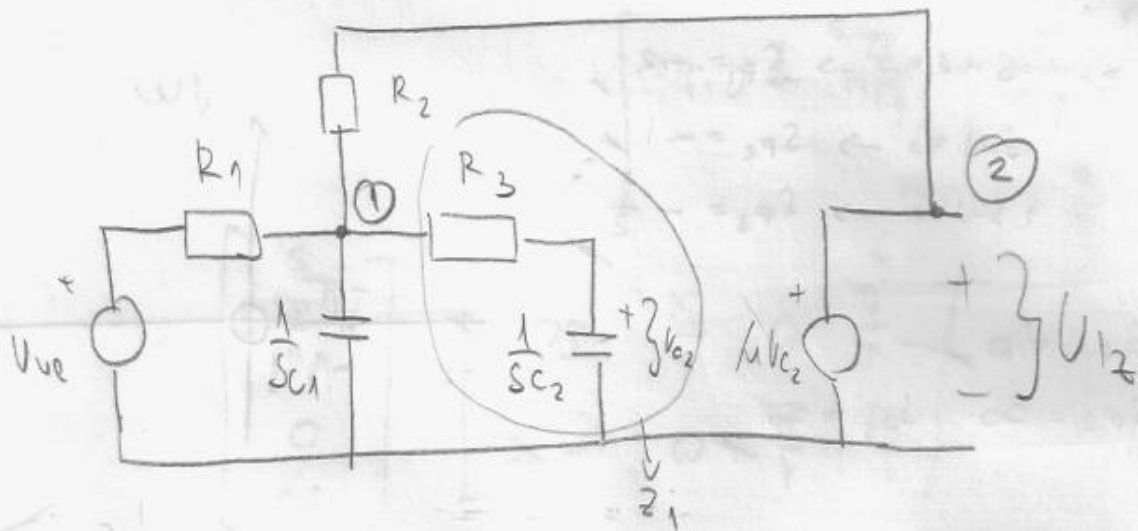
$$|T(0)| = 0$$

$$|T(\infty)| = 0$$



$$\frac{1+2}{1+2} = 1$$

⑧ $R_1 = R_2 = \frac{1}{2}, R_3 = C_1 = C_2 = 1, \mu = -3$



$$Z_1 = R_3 + \frac{1}{s_2} = \frac{R_3 s_2 + 1}{s_2}$$

① $V_1 \left(\frac{1}{R_1} + \frac{1}{R_2} + s_1 + \frac{s_2}{R_3 s_2 + 1} \right) - V_2 \left(\frac{1}{R_2} \right) = \frac{V_{u1}}{R_1}$

② $V_2 = \mu V_{C_2}$

③ $V_{C_2} = I_x \cdot \frac{1}{s_2} = \left(V_1 \cdot \frac{1}{Z_1} \right) \cdot \frac{1}{s_2} = V_1 \cdot \frac{s_2}{R_3 s_2 + 1} \cdot \frac{1}{s_2}$

$$\Rightarrow V_{C_2} = V_1 \cdot \frac{1}{R_3 s_2 + 1}$$

$$\Rightarrow \textcircled{2} V_2 = \mu V_{C_2} = -3 V_1 \cdot \frac{1}{R_3 s_2 + 1} = \boxed{\frac{-3 V_1}{s + 1} = V_2}$$

$$\Downarrow$$

$$\boxed{V_1 = -V_2 \frac{s+1}{3}}$$

$$\textcircled{1} U_1 \left(2 + 2 \rightarrow s + \frac{s}{s+1} \right) - 2U_2 = 2U_{ve}$$

$$U_1 \left[\frac{4(s+1) + s(s+1) + s}{s+1} \right] - 2U_2 = 2U_{ve}$$

$$+ U_2 \left(\frac{s+1}{3} \cdot \frac{4s+4+s^2+s+5}{(s+1)} \right) - 2U_2 = 2U_{ve}$$

$$- U_2 \left(\frac{s^2+6s+4}{3} + 2 \right) = 2U_{ve}$$

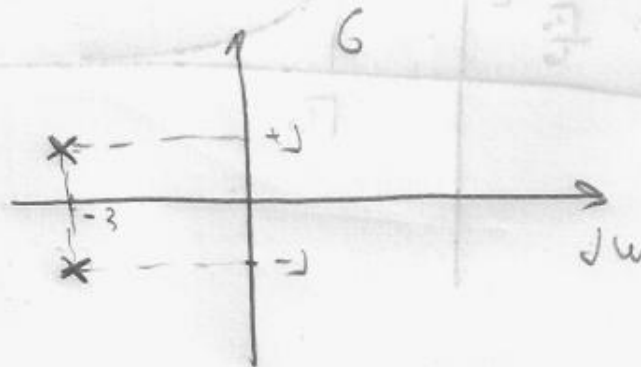
$$- U_2 \left[\frac{s^2+6s+4+6}{3} \right] = 2U_{ve} \Rightarrow -U_2 \left[\frac{s^2+6s+10}{3} \right] = U_{ve}$$

$$T(s) = \frac{U_2}{U_{ve}} = \frac{-6}{s^2+6s+10}$$

$$\Rightarrow \text{Polovi: } s^2+6s+10=0 \Rightarrow s_{p1,2} = \frac{-6 \pm \sqrt{36-40}}{2} = \frac{-6 \pm j2}{2}$$

$$\Rightarrow s_{p1,2} = -3 \pm j$$

$$s_{01,2} = \infty$$



$$T(s) = \frac{-6}{s^2 + 6s + 10}$$

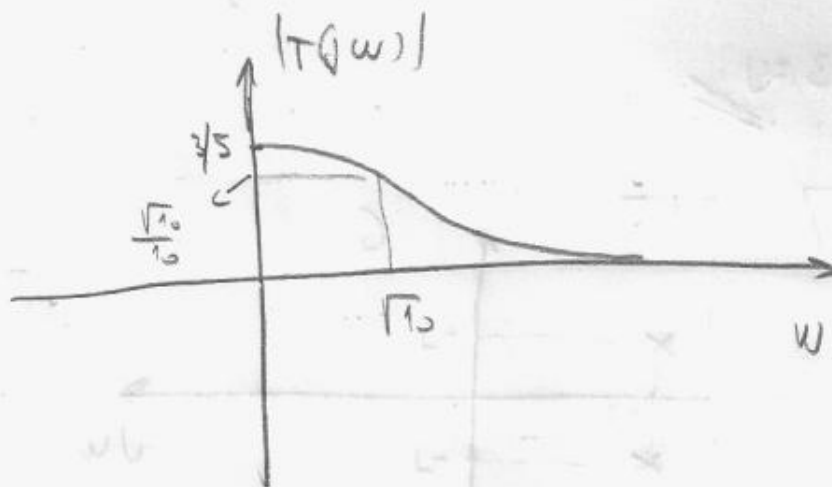
$$T(j\omega) = \frac{-6}{- \omega^2 + 6j\omega + 10} = \frac{-6}{10 - \omega^2 + 6j\omega}$$

$$|T(j\omega)| = \frac{|-6|}{\sqrt{(10 - \omega^2)^2 + 36\omega^2}} = \frac{6}{\sqrt{(10 - \omega^2)^2 + 36\omega^2}}$$

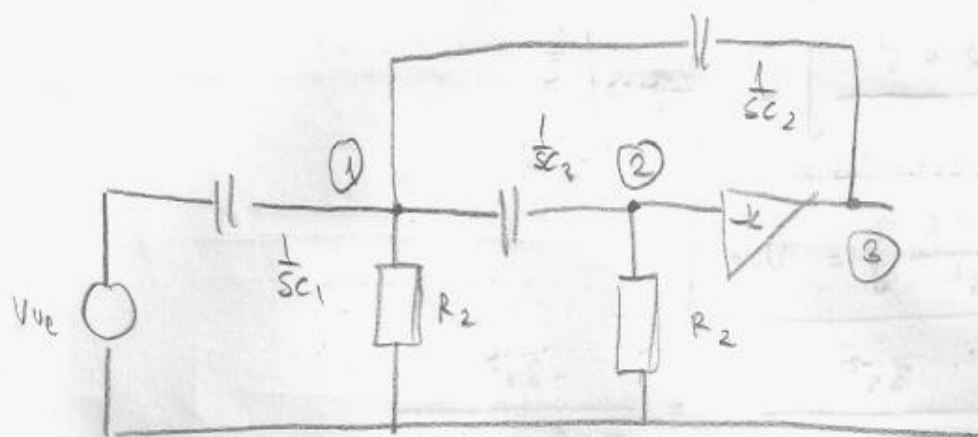
$$|T(0)| = \frac{6}{10} = \frac{3}{5}$$

$$|T(\infty)| = 0$$

$$|T(\sqrt{10})| = \frac{6}{\sqrt{360}} = \frac{6}{6\sqrt{10}} = \frac{\sqrt{10}}{10}$$



(9) $R_1 = R_2 = C_3 = 1, C_1 = C_2 = \frac{1}{2}, |k| = 3$



$$(1) U_1 \left(sC_1 + \frac{1}{R_2} + sC_2 + sC_3 \right) - U_2 (sC_3) - U_3 (sC_2) = U_{ue} sC_1$$

$$(2) U_2 \left(sC_3 + \frac{1}{R_2} \right) - U_1 (sC_3) = 0$$

$$(3) U_3 = -k \cdot U_2 \Rightarrow U_3 = -3 U_2 \Rightarrow \boxed{U_2 = -\frac{1}{3} U_3}$$

$$(1) U_1 \left(\frac{s}{2} + 1 + \frac{s}{2} + s \right) - U_2 s - U_3 \frac{s}{2} = \frac{U_{ue}}{2} \cdot s$$

$$(2) U_2 (s+1) - U_1 s = 0$$

$$(1) U_1 (2s+1) - U_2 s - U_3 \frac{s}{2} = \frac{U_{ue}}{2} \cdot s$$

$$(2) U_1 s = U_2 (s+1) \Rightarrow U_1 = U_2 \frac{s+1}{s} = \boxed{-U_3 \frac{s+1}{3s} = U_1}$$

$$(1) -U_3 \frac{s+1}{3s} (2s+1) + U_2 \frac{s}{3} - U_2 \frac{s}{2} = \frac{U_{ue}}{2} \cdot s$$

$$U_3 \left[\frac{-(s+1)(2s+1)}{3s} + \frac{s}{3} - \frac{s}{2} \right] = \frac{U_{ue}}{2} \cdot s$$

$$U_3 \left[\frac{-(2s^2 + s + 2s + 1)}{3s} + \frac{2s - 3s}{6} \right] = \frac{U_{ue}}{2} \cdot s$$

$$-U_3 \left[\frac{2s^2 + 3s + 1}{3s} + \frac{s}{6} \right] = \frac{U_{ve}}{2} \cdot s$$

$$-U_3 \left[\frac{4s^2 + 6s + 2 + s^2}{6s} \right] = \frac{U_{ve}}{2} \cdot s \cdot \frac{2}{s}$$

$$\boxed{-U_3 \left[\frac{5s^2 + 6s + 2}{3s^2} \right] = U_{ve}}$$

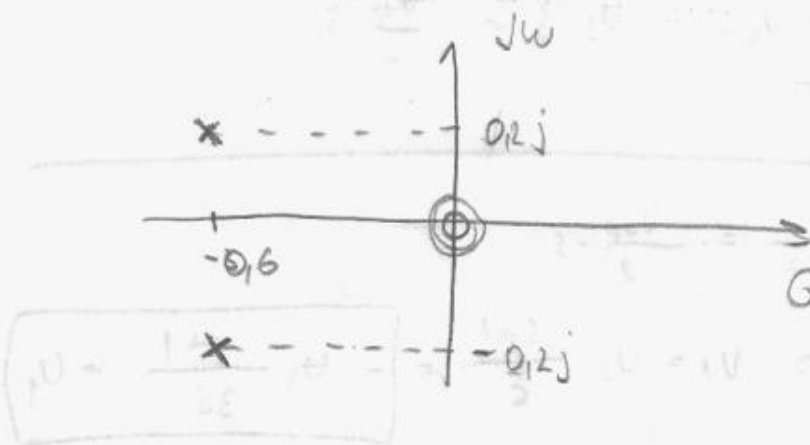
$$T(s) = \frac{U_3}{U_{ve}} = - \frac{3s^2}{5s^2 + 6s + 2} = \frac{-3s^2}{5s^2 + 6s + 2}$$

Polovi:

$$5s^2 + 6s + 2 = 0 \Rightarrow s_{1,2} = \frac{-6 \pm \sqrt{36 - 40}}{2} = \frac{-6 \pm 2j}{10} = \underline{\underline{-0,6 \pm 0,2j}}$$

NULI:

$$-3s^2 = 0 \Rightarrow s_{0,1,2} = 0$$



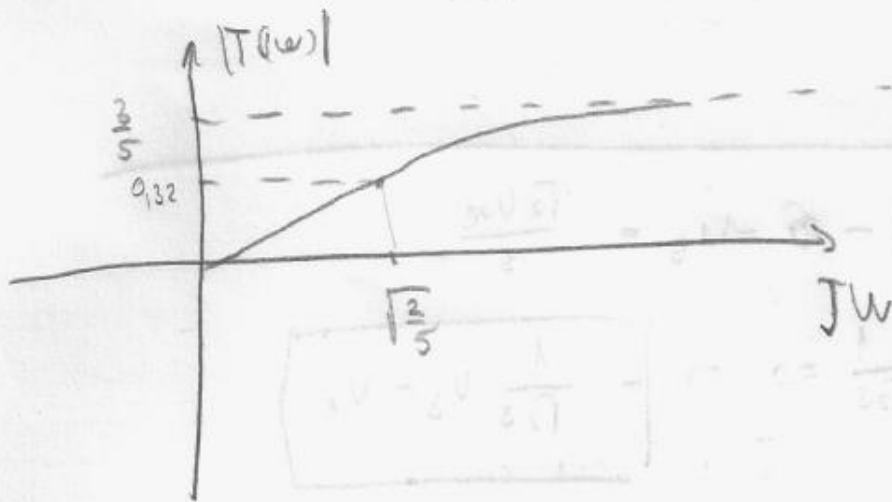
$$T(j\omega) = \frac{3\omega^2}{-5\omega^2 + 6j\omega + 2} = \frac{3\omega^2}{(2-5\omega^2) + 6j\omega}$$

$$|T(j\omega)| = \frac{3\omega^2}{\sqrt{(2-5\omega^2)^2 + 36\omega^2}}$$

$$|T(0)| = 0$$

$$|T(\infty)| = \frac{3}{5}$$

$$|T(\frac{\sqrt{2}}{5})| = \frac{\frac{6}{5}}{\sqrt{36 \cdot \frac{2}{5}}} = \frac{\frac{6}{5}}{\sqrt{\frac{72}{5}}} = \frac{1}{5} \cdot \frac{\sqrt{5}}{\sqrt{2}} = \frac{\sqrt{5}}{5\sqrt{2}} = \frac{\sqrt{10}}{10} = 0.32$$



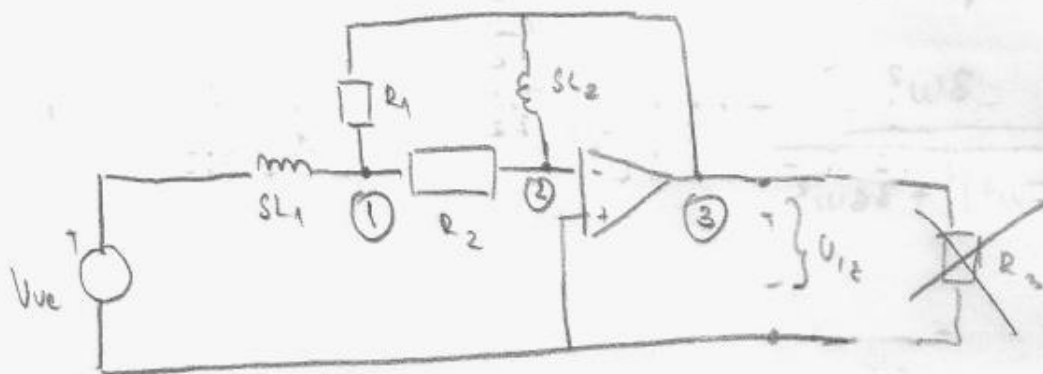
$$2V \cdot \frac{5}{2} = 2V - \left(\frac{25 + 5}{2} \right) V \quad (1)$$

$$2V \cdot \frac{5}{2} = 2V - 2V \left(\frac{25 + 5}{2} \right) \frac{1}{25}$$

$$2V \cdot \frac{5}{2} = \left[1 - \frac{25 + 5}{25} \right] 2V =$$

$$\frac{5}{2} \cdot 2V \mid 2V \cdot \frac{5}{2} = \left[\frac{5 - 25 + 5}{25} \right] 2V =$$

⑩ $R_1 = R_2 = R_3 = 1$, $L_1 = \frac{1}{\sqrt{2}}$, $L_2 = \sqrt{2}$



$$\textcircled{1} U_1 \left(\frac{1}{SL_1} + \frac{1}{R_2} + \frac{1}{R_1} \right) - U_2 \frac{1}{R_2} - U_3 \frac{1}{R_1} = \frac{U_{ue}}{SL_1}$$

$$\textcircled{2} U_2 \left(\frac{1}{SL_2} + \frac{1}{R_2} \right) - U_1 \left(\frac{1}{R_2} \right) - U_3 \left(\frac{1}{SL_2} \right) = 0$$

$$\Rightarrow U_2 = 0$$

$$\textcircled{1} U_1 \left(\frac{\sqrt{2}}{s} + 1 + 1 \right) - 0 - U_3 = \frac{\sqrt{2} U_{ue}}{s}$$

$$\textcircled{2} 0 - U_1 - U_3 \frac{1}{\sqrt{2}s} \Rightarrow \boxed{-\frac{1}{\sqrt{2}s} U_3 = U_1}$$

$$\textcircled{1} U_1 \left(\frac{\sqrt{2} + 2s}{s} \right) - U_3 = \frac{\sqrt{2}}{s} U_{ue}$$

$$-\frac{1}{\sqrt{2}s} \left(\frac{\sqrt{2} + 2s}{s^2} \right) U_3 - U_3 = \frac{\sqrt{2}}{s} U_{ue}$$

$$-U_3 \left[\frac{\sqrt{2} + 2s}{\sqrt{2}s^2} + 1 \right] = \frac{\sqrt{2}}{s} U_{ue}$$

$$-U_3 \left[\frac{\sqrt{2} + 2s + \sqrt{2}s^2}{\sqrt{2}s^2} \right] = \frac{\sqrt{2}}{s} U_{ue} \quad \bigg/ \cdot \frac{s}{\sqrt{2}}$$

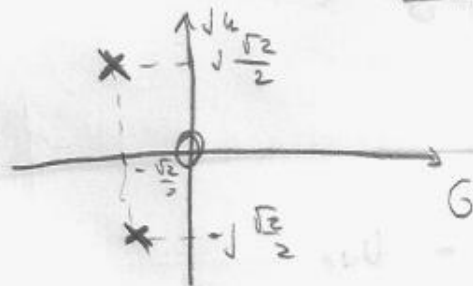
$$U_{ve} = -U_3 \left[\frac{\sqrt{2}s^2 + 2s + \sqrt{2}}{2s} \right]$$

$$T(s) = \frac{U_3}{U_{ve}} = - \frac{2s}{\sqrt{2}s^2 + 2s + \sqrt{2}} \cdot \frac{\frac{\sqrt{2}}{\sqrt{2}}}{\frac{\sqrt{2}}{\sqrt{2}}} = - \frac{2\sqrt{2}s}{2s^2 + 2\sqrt{2}s + \sqrt{2}}$$

$$T(s) = \frac{-\sqrt{2}s}{s^2 + \sqrt{2}s + 1}$$

Polevi: $s_{1,2} = \frac{-\sqrt{2} \pm \sqrt{2 - 4}}{2} = -\frac{\sqrt{2}}{2} \pm j\frac{\sqrt{2}}{2}$

NULE: $-\sqrt{2}s = 0 \rightarrow \boxed{s_{01} = 0}, \boxed{s_{02} = \infty}$



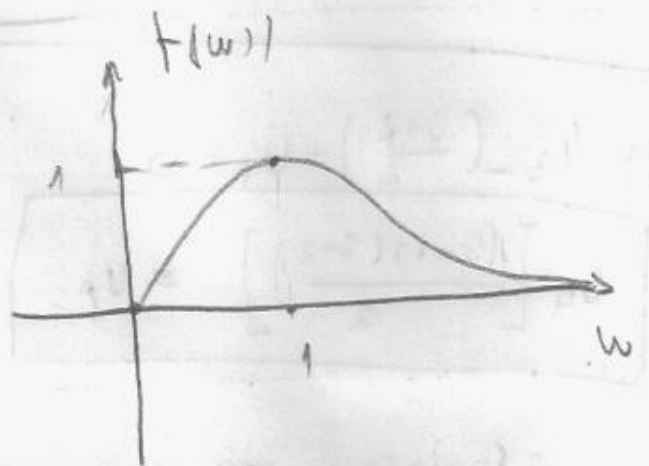
$$T(j\omega) = \frac{-\sqrt{2}j\omega}{-\omega^2 + \sqrt{2}j\omega + 1} = \frac{-j\sqrt{2}\omega}{(1 - \omega^2) + j\sqrt{2}\omega}$$

$$|T(j\omega)| = \frac{\sqrt{2}\omega}{\sqrt{(1 - \omega^2)^2 + 2\omega^2}}$$

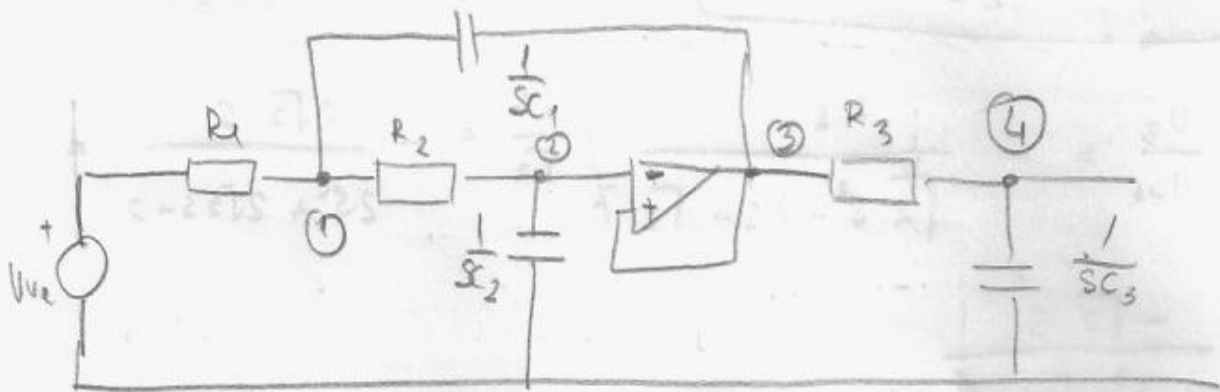
$$|T(0)| = 0$$

$$|T(\infty)| = 0$$

$$|T(1)| = \frac{\sqrt{2}\omega}{\sqrt{2}\omega} = 1$$



(11) $R_1 = R_2 = R_3 = 1, C_1 = 2, C_2 = \frac{1}{2}$



$$(1) U_1 \left(\frac{1}{R_1} + \frac{1}{R_2} + sC_1 \right) - U_2 \left(\frac{1}{R_2} \right) - U_3 (sC_1) = \frac{U_{we}}{R_1}$$

$$(2) U_2 \left(sC_2 + \frac{1}{R_2} \right) - U_1 \left(\frac{1}{R_2} \right) = 0$$

$$(4) U_4 \left(\frac{1}{R_3} + sC_3 \right) - U_3 \left(\frac{1}{R_3} \right) = 0$$

$$\rightarrow U_2 = U_3$$

$$(1) U_1 (1 + 1 + 2s) - U_3 - U_3 s = U_{we}$$

$$(2) U_3 \left(\frac{s}{2} + 1 \right) - U_1 = 0$$

$$(4) U_4 (s+1) - U_3 = 0 \Rightarrow U_3 = U_4 (s+1)$$

$$(2) U_3 \left(\frac{s+2}{2} \right) - U_1 = 0$$

$$U_4 \left[\frac{(s+1)(s+2)}{2} \right] = U_1$$

$$(1) U_4 \left[\frac{(s+1)(s+2) \cdot 2(s+1)}{2} \right] - U_4 (s+1) (1+2s) = U_{we}$$

$$U_4 [(s+1)^2 (s+2)] - U_4 (s+1) (2s+1) = U_{we}$$

$$U_u [(s+1) [(s+1)(s+2) - 2s-1]] = U_{ue} \quad (1)$$

$$U_u [(s+1) (s^2 + s + 2s + 2 - 2s - 1)] = U_{ue}$$

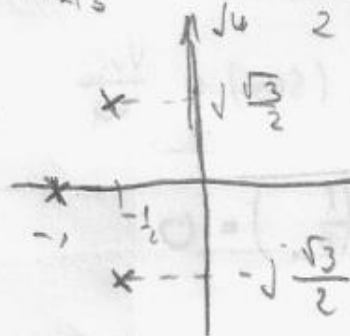
$$U_u [(s+1) (s^2 + s + 1)] = U_{ue}$$

$$T(s) = \frac{U_u}{U_{ue}} = \frac{1}{(s+1)(s^2+s+1)} = \frac{1}{s^3+s^2+s+s^2+s+1} = \frac{1}{s^3+2s^2+2s+1}$$

$$\text{Pole: } (s+1) = 0 \Rightarrow \boxed{s_1 = -1}$$

$$s^2 + s + 1 = 0 \Rightarrow s_{2,3} = \frac{-1 \pm \sqrt{1-4}}{2} = -\frac{1}{2} \pm j\frac{\sqrt{3}}{2}$$

$$\text{NUCLE: } s_{0,1,2} = \infty$$

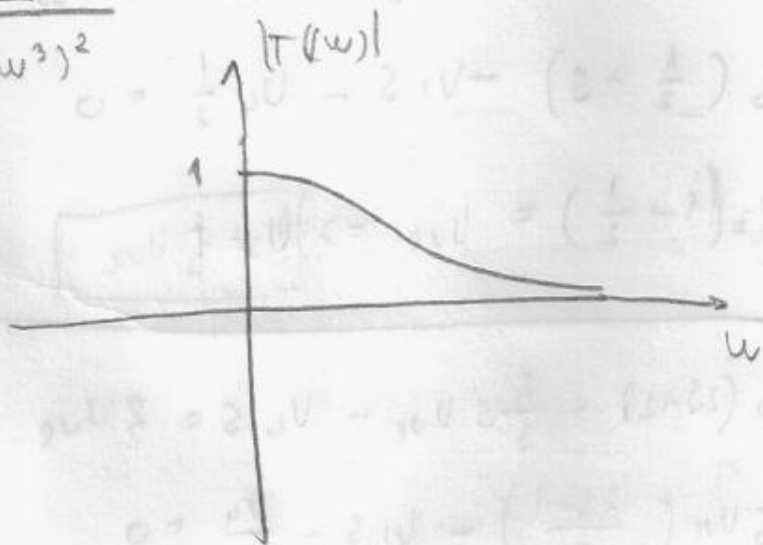


$$T(j\omega) = \frac{1}{-j\omega^3 - 2\omega^2 + 2j\omega + 1} = \frac{1}{1 - 2\omega^2 + j(2\omega - \omega^3)}$$

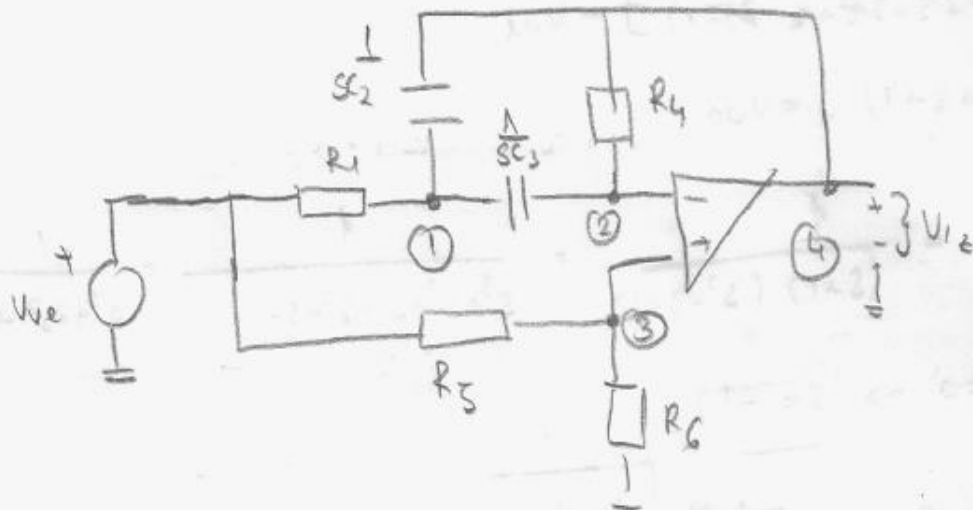
$$|T(j\omega)| = \frac{1}{\sqrt{(1-2\omega^2)^2 + (2\omega - \omega^3)^2}}$$

$$|T(\omega)| = 1$$

$$|T(\infty)| = 0$$



(12) $R_1 = \frac{1}{2}$, $R_4 = R_6 = 2$, $R_3 = C_2 = C_3 = 1$



$$(1) U_1 \left(\frac{1}{R_1} + sC_2 + sC_3 \right) - U_2 (sC_3) - U_4 (sC_2) = \frac{U_{ve}}{R_1}$$

$$(2) U_2 \left(\frac{1}{R_4} + sC_3 \right) - U_1 (sC_3) - U_4 \left(\frac{1}{R_4} \right) = 0$$

$$(3) U_3 \left(\frac{1}{R_6} + \frac{1}{R_5} \right) = \frac{U_{ve}}{R_5}$$

$$\Rightarrow U_2 = U_3$$

$$(1) U_1 (2 + s + s) - U_3 s - U_4 s = 2 U_{ve}$$

$$(2) U_3 \left(\frac{1}{2} + s \right) - U_1 s - U_4 \frac{1}{2} = 0$$

$$(3) U_3 \left(1 + \frac{1}{2} \right) = U_{ve} \Rightarrow \boxed{U_3 = \frac{2}{3} U_{ve}}$$

$$(1) U_1 (2s + 2) - \frac{2}{3} s U_{ve} - U_4 s = 2 U_{ve}$$

$$(2) \frac{2}{3} U_{ve} \left(\frac{2s + 1}{2} \right) - U_1 s - \frac{U_4}{2} = 0$$

$$U_1 s = \frac{2s + 1}{3} U_{ve} - \frac{U_4}{2} \Rightarrow \boxed{U_1 = \frac{2s + 1}{3s} U_{ve} - \frac{1}{2s} U_4}$$

$$\left[\frac{(2s+1)}{3s} U_{ve} - \frac{1}{2s} U_u \right] 2(s+1) - U_u s = \frac{(6+2s)}{3} U_{ve}$$

$$\frac{2(s+1)(2s+1)}{3s} U_{ve} - \frac{s+1}{s} U_u - U_u s = \frac{(6+2s)}{3} U_{ve}$$

$$-U_u \left(\frac{s+1}{s} + s \right) = \left[\frac{6+2s}{3} - \frac{2(2s^2+s+2s+1)}{3s} \right] U_{ve}$$

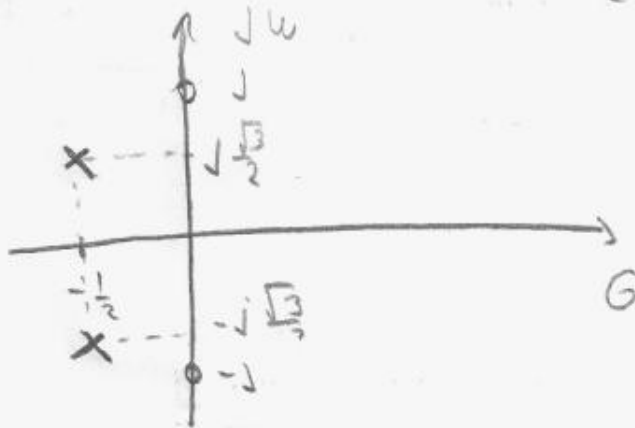
$$-U_u \left(\frac{s^2+s+1}{s} \right) = \left[\frac{6s+2s^2-4s^2-6s-2}{3s} \right] U_{ve}$$

$$+U_u \left(\frac{s^2+s+1}{s} \right) = \frac{2(s^2+1)}{3s} U_{ve}$$

$$U_{ve} = \frac{3(s^2+s+1)}{2(s^2+1)} U_u \Rightarrow T(s) = \frac{U_u}{U_{ve}} = \frac{2}{3} \cdot \frac{s^2+1}{s^2+s+1}$$

$$\Rightarrow \text{NULE: } s^2+1=0 \Rightarrow s_{0,1} = \pm j$$

$$\Rightarrow \text{POLE: } s^2+s+1=0 \Rightarrow s_{p1,2} = \frac{-1 \pm \sqrt{1-4}}{2} = -\frac{1}{2} \pm j\frac{\sqrt{3}}{2}$$



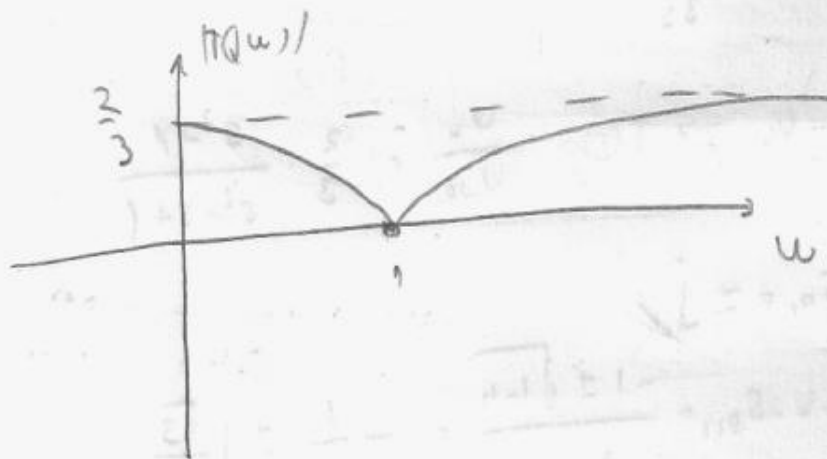
$$T(j\omega) = \frac{2}{3} \frac{1-\omega^2}{(1-\omega^2) + j\omega}$$

$$|T(j\omega)| = \frac{2}{3} \frac{|1-\omega^2|}{\sqrt{(1-\omega^2)^2 + \omega^2}}$$

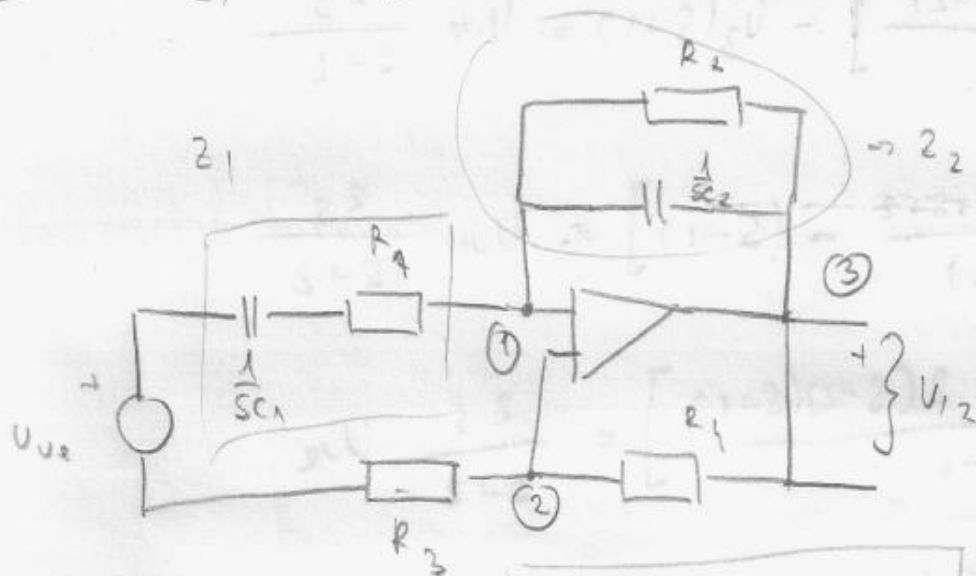
$$|T(0)| = \frac{2}{3}$$

$$|T(\infty)| = \frac{2}{3}$$

$$|T(1)| = 0$$



(13) $R_1 = \frac{1}{2}, R_2 = R_3 = R_4 = C_1 = C_2 = 1$



$$Z_1 = \left(\frac{1}{sC_1} + R_4 \right) = \frac{1 + R_4 sC_1}{sC_1} = Z_1$$

$$Z_2 = \left(sC_2 + \frac{1}{R_2} \right)^{-1} = \left(\frac{R_2 sC_2 + 1}{R_2} \right)^{-1} = \frac{R_2}{R_2 sC_2 + 1} = Z_2$$

$$(1) U_1 \left(\frac{sC_1}{1 + R_4 sC_1} + \frac{R_2 sC_2 + 1}{R_2} \right) - U_3 \left(\frac{R_2 sC_2 + 1}{R_2} \right) = U_{ve} \frac{sC_1}{1 + R_4 sC_1}$$

$$(2) U_2 \left(\frac{1}{R_3} + \frac{1}{R_4} \right) - U_3 \left(\frac{1}{R_4} \right) = 0$$

$$(3) U_2 = U_1$$

$$(1) U_2 \left(\frac{s}{1 + \frac{s}{2}} + \frac{s+1}{1} \right) - U_3 \left(\frac{s+1}{1} \right) = U_{ve} \frac{s}{1 + \frac{1}{2}s}$$

$$(2) U_2 (1+1) - U_3 = 0 \Rightarrow 2U_2 = U_3 \Rightarrow U_2 = \frac{U_3}{2}$$

$$(1) U_2 \left[\frac{2s}{s+2} + (s+1) \right] - U_3 (s+1) = U_{ve} \frac{2s}{s+2}$$

$$\frac{U_2}{2} \left[\frac{2s + (s+1)(s+2)}{s+2} \right] - U_3(s+1) = U_{ve} \frac{2s}{s+2}$$

$$U_3 \left(\frac{2s + s^2 + 2s + s + 2}{2(s+2)} - (s+1) \right) = U_{ve} \frac{2s}{s+2}$$

$$U_3 \left(\frac{s^2 + 5s + 2 - 2(s+2)(s+1)}{2(s+2)} \right) = \frac{2s}{s+2} U_{ve}$$

$$U_3 \left(\frac{s^2 + 5s + 2 - 2(s^2 + 3s + 2)}{2(s+2)} \right) = \frac{2s}{s+2} U_{ve}$$

$$U_3 \left(\frac{s^2 + 5s + 2 - 2s^2 - 6s - 4}{2(s+2)} \right) = \frac{2s}{s+2} U_{ve}$$

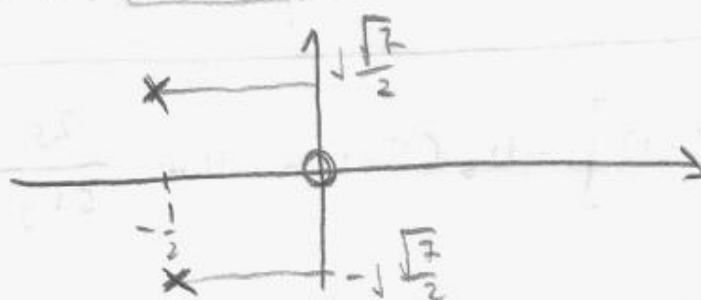
$$U_3 \frac{-s^2 - s - 2}{2(s+2)} \cdot \frac{s+2}{2s} = U_{ve}$$

$$U_3 = \frac{-(s^2 + s + 2)}{4s} = U_{ve}$$

$$T(s) = \frac{U_3}{U_{ve}} = \frac{-4s}{s^2 + s + 2}$$

$$\text{Polovi: } s^2 + s + 2 = 0 \Rightarrow s_{p1,2} = \frac{-1 \pm \sqrt{1-8}}{2} = -\frac{1}{2} \pm j\sqrt{\frac{7}{2}}$$

$$\text{NULE: } \boxed{s_1 = 0}, \boxed{s_2 = \infty}$$



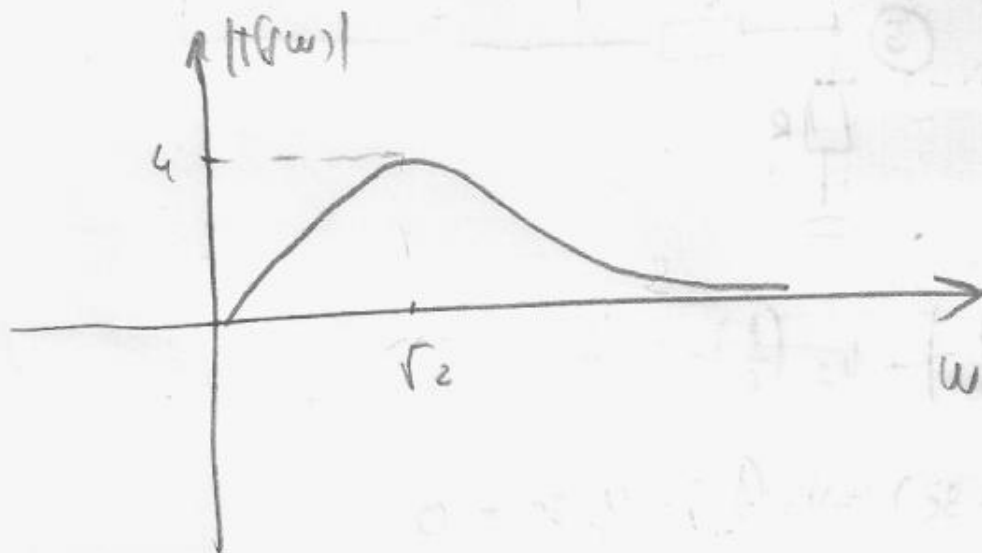
$$T(j\omega) = \frac{-4j\omega}{(2-\omega^2) + j\omega}$$

$$|T(j\omega)| = \frac{4\omega}{\sqrt{(2-\omega^2)^2 + \omega^2}}$$

$$|T(0)| = 0$$

$$|T(\infty)| = 0$$

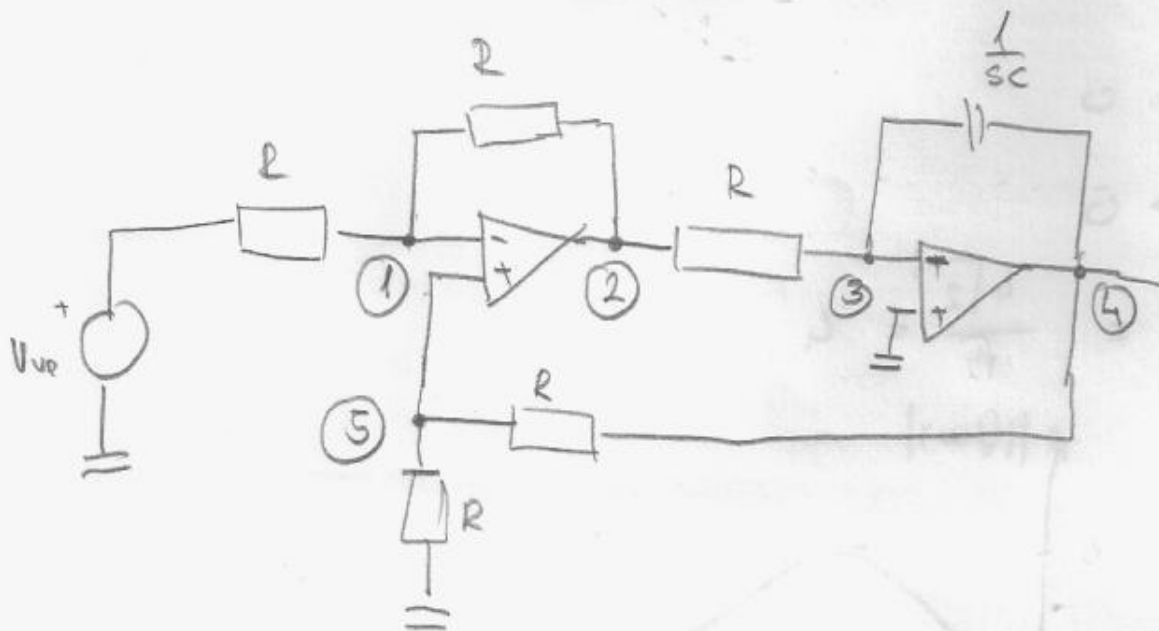
$$|T(\sqrt{2})| = \frac{4\sqrt{2}}{\sqrt{2}} = 4$$



14) NEMAJ BAŠ VOLJE ZA DVO, PA RECIMO SLJEDIOCI

$$R = C = 1$$

$$\Rightarrow T(s) = \frac{1}{s+1} \quad (\text{KAD SE UVRSTI } R=C=1 \text{ U } R_0)$$



$$\textcircled{1} \quad U_1 \left(\frac{1}{R} + \frac{1}{R} \right) - U_2 \left(\frac{1}{R} \right) = \frac{U_{ve}}{R}$$

$$\textcircled{3} \quad U_3 \left(\frac{1}{R} + sC \right) - U_2 \left(\frac{1}{R} \right) - U_4 sC = 0$$

$$\textcircled{5} \quad U_5 \left(\frac{1}{R} + \frac{1}{R} \right) - U_4 \left(\frac{1}{R} \right) = 0$$

$$\Rightarrow U_1 = U_5, \quad U_3 = 0$$

$$\textcircled{1} \quad 2U_1 - U_2 = U_{ve} \quad \leftarrow$$

$$\textcircled{3} \quad -U_2 - U_4 s = 0 \Rightarrow U_2 = -sU_4$$

$$\textcircled{5} \quad 2U_1 - U_4 = 0 \Rightarrow U_1 = \frac{1}{2} U_4$$

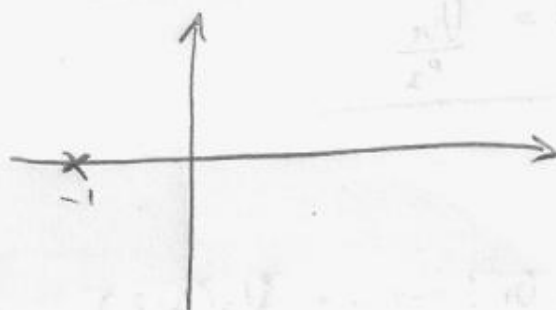
$$U_H + S U_H = U_{ve}$$

$$U_{ve} = U_H (S+1)$$

$$T(s) = \frac{U_H}{U_{ve}} = \frac{1}{s+1}$$

Pole: $s+1=0 \Rightarrow \boxed{s_{p1} = -1}$

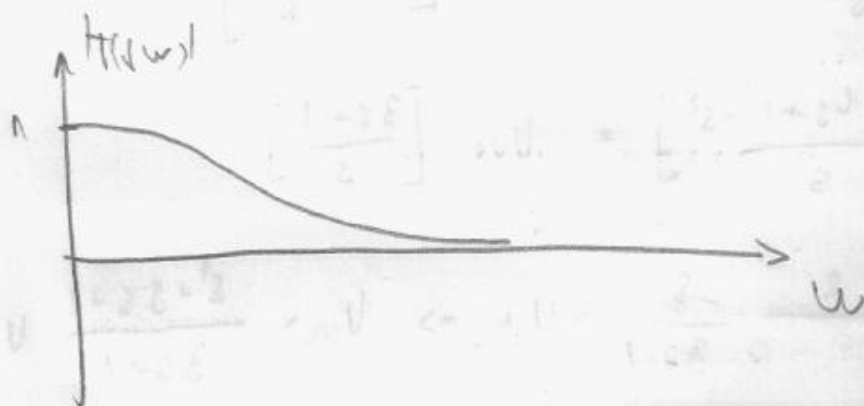
NULE: $\boxed{s_0 = \infty}$



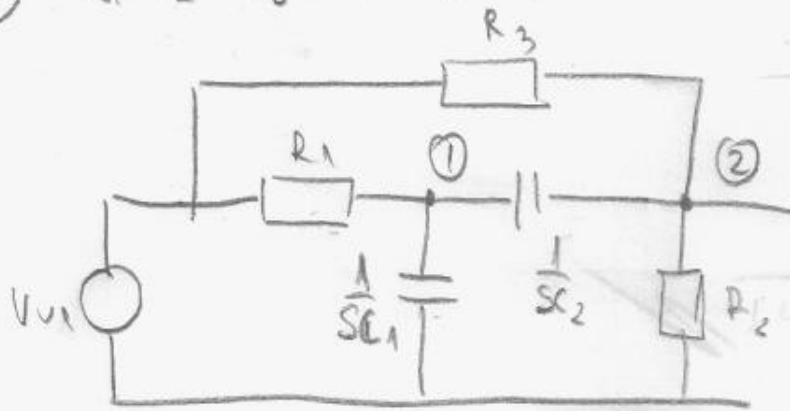
$$T(j\omega) = \frac{1}{1+j\omega} \Rightarrow |T(j\omega)| = \frac{1}{\sqrt{1+\omega^2}}$$

$$|T(0)| = 1$$

$$|T(\infty)| = 0$$



15) $R_1 = R_2 = R_3 = C_1 = C_2 = 1$



$$① \quad U_1 \left(\frac{1}{R_1} + sC_1 + sC_2 \right) - U_2 sC_2 = \frac{U_{ve}}{R_1}$$

$$② \quad U_2 \left(sC_2 + \frac{1}{R_2} + \frac{1}{R_3} \right) - U_1 (sC_2) = \frac{U_{ve}}{R_3}$$

$$① \quad U_1 (1 + s + s) - U_2 s = U_{ve}$$

$$② \quad U_2 (s + 2) - U_1 s = U_{ve} \Rightarrow \underbrace{U_1 s - U_{ve} + U_2 (s + 2)}_{U_1 = -\frac{U_{ve}}{s} + U_2 \frac{s+2}{s}}$$

$$① \quad \left[\frac{U_{ve}}{s} - U_2 \frac{s+2}{s} \right] (2s+1) - U_2 s = U_{ve}$$

$$U_2 \left[\frac{(s+2)(2s+1)}{s} - U_2 s \right] = U_{ve} \left[1 + \frac{(2s+1)}{s} \right]$$

$$U_2 \left[\frac{2s^2 + s + 4s + 2 - s^2}{s} \right] = U_{ve} \left[\frac{3s+1}{s} \right]$$

$$U_2 \frac{s^2 + 5s + 2}{s} \cdot \frac{s}{3s+1} = U_{ve} \Rightarrow U_{ve} = \frac{s^2 + 5s + 2}{3s+1} U_2$$

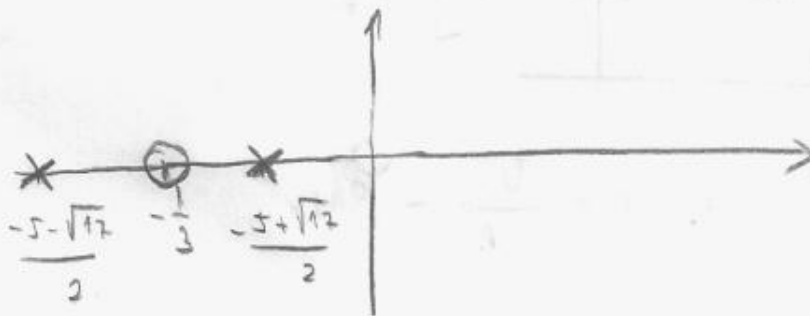
$$T(s) = \frac{U_2}{U_{ve}} = \frac{3s+1}{s^2 + 5s + 1}$$

POLY:

$$s^2 + 5s + 2 = 0 \Rightarrow s_{p1,2} = \frac{-5 \pm \sqrt{25 - 8}}{2} = \frac{-5 \pm \sqrt{17}}{2}$$

NULE:

$$3s + 1 = 0 \Rightarrow s_n = -\frac{1}{3}, \quad s_{n2} = \infty$$

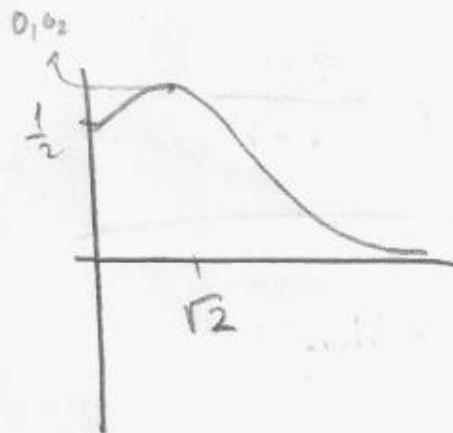


$$T(j\omega) = \frac{1 + 3j\omega}{(2 - \omega^2) + 5j\omega} \Rightarrow |T(j\omega)| = \frac{\sqrt{1 + 9\omega^2}}{\sqrt{(2 - \omega^2)^2 + 25\omega^2}}$$

$$|T(0)| = \frac{1}{2}$$

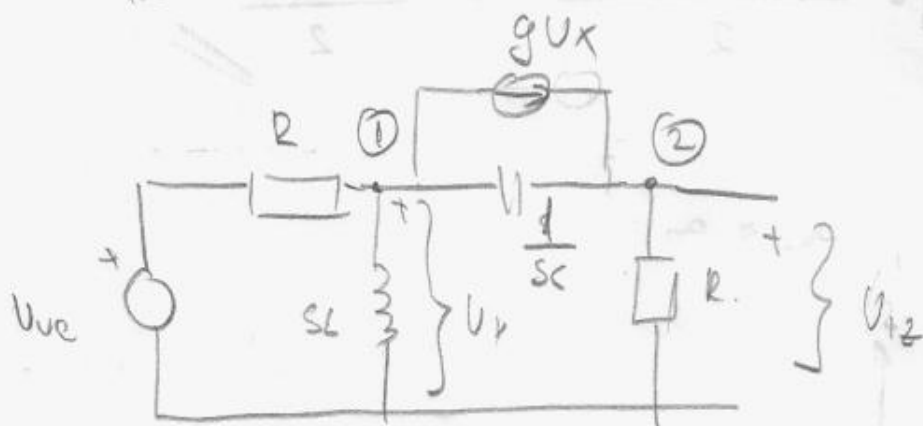
$$|T(\infty)| = 0$$

$$|T(\sqrt{2})| = \frac{\sqrt{19}}{5\sqrt{2}} = 0,62$$



⑫ $R=C=1, L=g=2$

$u_1(t) = 10 \cos t$



① $U_1 \left(\frac{1}{R} + \frac{1}{sL} + sC \right) - U_2 sC = \frac{U_{ve}}{R} - g U_x$

② $U_2 \left(sC + \frac{1}{R} \right) - U_1 (sC) = g U_x$

③ $U_x = U_1$

① $U_1 \left(1 + \frac{1}{2s} + s \right) - U_2 s = U_{ve} - 2 U_1$

② $U_2 (s + 1) - U_1 s = 2 U_1$

① $U_1 \left(\frac{2s^2 + 2s + 1}{2s} + 2 \right) - U_2 s = U_{ve}$

② $\Rightarrow U_2 (s + 1) = U_1 (s + 2) \Rightarrow U_1 = U_2 \frac{s + 1}{s + 2}$

$U_2 \left(\frac{s + 1}{s + 2} \cdot \frac{2s^2 + 2s + 1 + 4s}{2s} \right) - U_2 s = U_{ve}$

$U_2 \left(\frac{(s + 1)(2s^2 + 6s + 1)}{2s(s + 2)} - \frac{2s^2(s + 2)}{2s(s + 2)} \right) = U_{ve}$

$$U_{ve} = U_2 \left[\frac{2s^3 + 6s^2 + s + 2s^3 + 6s + 1 - 2s^3 - 4s^2}{2s(s+2)} \right] \quad (51)$$

$$U_{ve} = U_2 \left[\frac{4s^2 + 7s + 1}{2s(s+2)} \right] \rightarrow T(s) = \frac{U_2}{U_{ve}} = \frac{2s(s+2)}{4s^2 + 7s + 1}$$

$$T(s) = \frac{2s^2 + 4s}{4s^2 + 7s + 1} \rightarrow T(j\omega) = \frac{-2\omega^2 + 4j\omega}{-4\omega^2 + 7j\omega + 1} = \frac{4j\omega - 2\omega^2}{(1 - 4\omega^2) + 7j\omega}$$

$$\Rightarrow U_{ve} = 10 \cos t = 10 \angle 0^\circ \Rightarrow \omega = 1$$

$$T(j.1) = \frac{j4 - 2}{-3 + 7j} = \frac{4,47 \angle 116,56^\circ}{7,61 \angle 113,15^\circ} = 0,587 \angle 3,37^\circ$$

$$T(j.1) = 0,587 \angle 3,37^\circ$$

$$T(j.1) = \frac{U_{12}}{U_{ve}} \Rightarrow U_{12} = T(j.1) \cdot U_{ve} = 0,587 \angle 3,37^\circ \cdot 10 \angle 0^\circ$$

$$U_{12} = 5,87 \angle 3,37^\circ = 5,87 \cos(t + 3,37^\circ)$$

$$(17) \quad x(t) = s(t) \Rightarrow X(s) = \frac{1}{s}$$

$$g(t) = e^{-3t} \cosh(2t) \cdot s(t) \Rightarrow Y(s) = \frac{(s+3)}{(s+3)^2 - 4}$$

$$Y(s) = \frac{s+3}{s^2+6s+9-4} = \frac{s+3}{s^2+6s+5}$$

$$T(s) = \frac{Y(s)}{X(s)} = \frac{s+3}{s^2+6s+5} \cdot \frac{s}{1} = \frac{s^2+3s}{s^2+6s+5}$$

$$T(j\omega) = \frac{-\omega^2 + 3j\omega}{(5-\omega^2) + 6j\omega}$$

$$x_1(t) = 2 \cos(3t + 45^\circ) = 2 \angle 45^\circ \Rightarrow \omega = 3$$

$$T(j.3) = \frac{-9 + 9j}{-4 + 18j} = \frac{12,73 \angle 133^\circ}{18,44 \angle 102,53^\circ} = 0,69 \angle 32,47^\circ$$

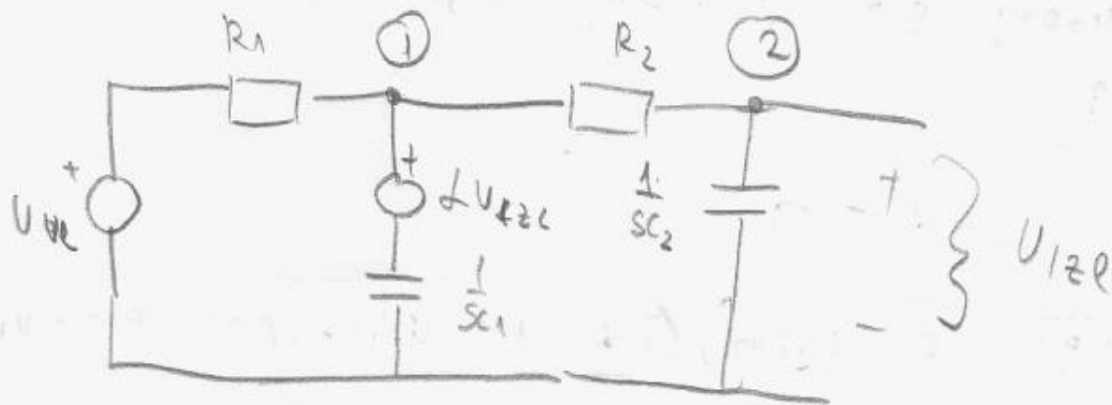
$$T(j.3) = \frac{Y(t)}{X(t)} \Rightarrow Y(t) = T(j.3) \cdot X(t)$$

$$y(t) = 0,69 \angle 32,47^\circ \cdot 2 \angle 45^\circ = 1,38 \angle 77,47^\circ$$

$$y(t) = 1,38 \cos(3t + 77,47^\circ)$$

(18) i (19)

$$R_1 = R_2 = C_1 = C_2 = 1$$



$$(1) \quad U_1 \left(\frac{1}{R_1} + sC_1 + \frac{1}{R_2} \right) - U_2 \left(\frac{1}{R_2} \right) = \frac{U_{ve}}{R_1} + L U_{12} \cdot sC_1$$

$$(2) \quad U_2 \left(\frac{1}{R_2} + sC_2 \right) - U_1 \left(\frac{1}{R_2} \right) = 0$$

$$(1) \quad U_1 (1 + s + 1) - U_2 = U_{ve} + s L U_2$$

$$(2) \quad U_2 (1 + s) - U_1 = 0 \Rightarrow U_1 = U_2 (s + 1)$$

$$(1) \quad U_2 [(s+1)(s+2)] - U_2 \xrightarrow{L} U_0 = U_{ve}$$

$$U_2 [s^2 + 2s + s + 2 - 1 - 2] = U_{ve}$$

$$U_{ve} = U_2 (s^2 + 3s + 1 - 2s) = U_2 [s^2 + (3-2)s + 1]$$

$$T(s) = \frac{U_2}{U_{ve}} = \frac{1}{s^2 + (3-2)s + 1}$$

$$s^2 + (3-\alpha)s + 1 = 0$$

⇒ Polovi MORAJU BITI U LIJEVOJ POLUPRAVNINI

TJ.

$$s^2 + (3-\alpha)s + 1 \leq 0$$

⇒ DA BI Polovi BILI LIJEVO, $(3-\alpha)$ mora uvijek biti pozitivno

$$3-\alpha \geq 0 \Rightarrow \alpha \geq -3 \Rightarrow \boxed{\alpha \leq 3}$$

$$\Rightarrow s^2 + (3-\alpha)s + 1 = 0$$

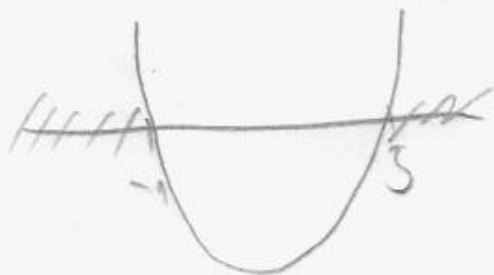
$$s_{1,2} = \frac{-(3-\alpha) \pm \sqrt{(3-\alpha)^2 - 4}}{2}$$

⇒ DA BI RJ. BILA REALNA $(3-\alpha)^2 - 4 \geq 0$

$$9 - 6\alpha + \alpha^2 - 4 \geq 0 \Rightarrow \alpha^2 - 6\alpha + 5 \geq 0$$

$$\alpha^2 - 6\alpha + 5 = 0 \Rightarrow \alpha_{1,2} = \frac{6 \pm \sqrt{36-20}}{2} = \frac{6 \pm 4}{2}$$

$$\alpha_1 = 5, \alpha_2 = 1$$



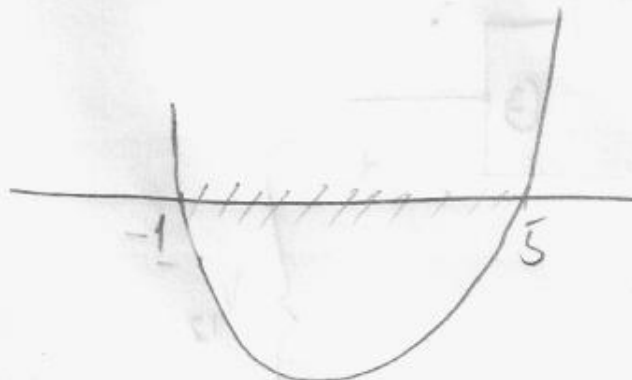
$$\alpha \in [-\infty, 1] \cup [5, \infty]$$

⇒ Ali, kako vidjeti $\alpha \leq 3$

$$\boxed{\alpha \leq 1}$$

→ DA BI POLOVI BILI KOMPLEKSNI: $\frac{5}{2} = 3, 1 = 1 - 3$

$$L^2 - 6L + 5 < 0$$



$$L \in (-1, 5)$$

$$\left. \begin{array}{l} L \in (-1, 5) \\ \text{ALI KAKO JE } L \leq 3 \end{array} \right\} L \in (-1, 3]$$

ALI KAKO JE $L \leq 3$

$$\frac{10V}{s} = \left(\frac{1}{s} \right) 5V - \left(\frac{1}{s} + 2s + \frac{1}{s} \right) 10 \quad (1)$$

$$25V = \frac{5}{s} 10V - \left(2s + \frac{2}{s} + 2s \right) 10 \quad (2)$$

$$0 = \left(\frac{1}{s} \right) 10 - \left(2s + \frac{2}{s} \right) 10 = \left(\frac{1}{s} - 2s - \frac{2}{s} \right) 10 \quad (3)$$

$$10V = 10V - (2s + \frac{2}{s}) 10 \quad (4)$$

$$25V = 5V - (2s + \frac{2}{s}) 10 \quad (5)$$

$$25V = 5V - (2s + \frac{2}{s}) 10 \quad (6)$$

$$25V = 5V - (2s + \frac{2}{s}) 10$$

$$\frac{2}{(1+2)s} 10V = \frac{5-2}{(1+2)s} 10V = 3V = 25V - (2s + \frac{2}{s}) 10 = (25-2s-\frac{20}{s}) 10$$