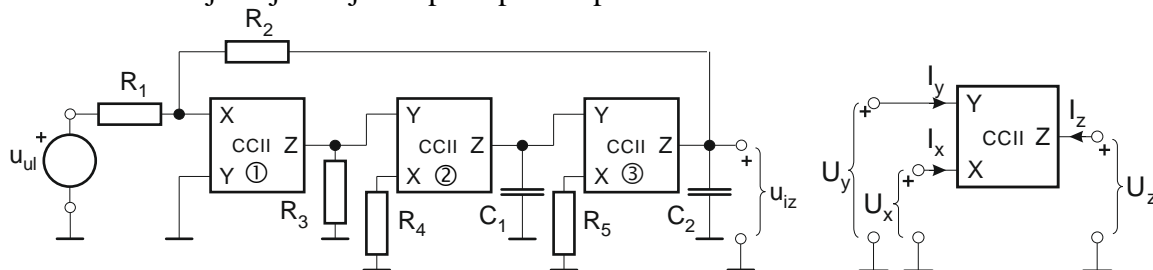
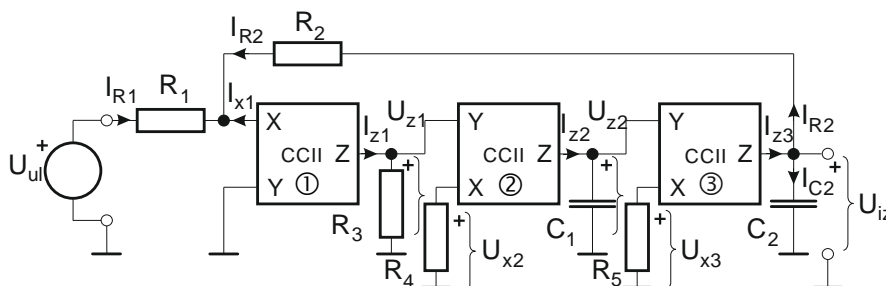


ZAVRŠNI ISPIT IZ ELEKTRIČNIH KRUGOVA 2016-2017 – Rješenja

1. Za električni krug prikazan slikom izračunati valni oblik napona $u_{iz}(t)$ za $t > 0$ kao odziv, ako je zadana pobuda $u_{ul}(t) = \delta(t)$ [V], a početni naponi na kapacitetima su jednaki nula. Zadane su normalizirane vrijednosti elemenata $R_1=1, R_2=1, R_3=1, R_4=1, R_5=1, C_1=1, C_2=1$. Za strujni prijenosnik druge generacije (CCII) vrijede slijedeće definicijske jednadžbe: $u_x=u_y, i_y=0, i_z=i_x$ uz referentna usmjerenja struja i napona prilaza prikazana na slici.



Rješenje:



a) Za prvi CCII vrijedi: **(1 bod)**

$$U_{z1} = I_{z1} \cdot R_3, I_{y1} = 0, U_{x1} = 0, U_{y1} = 0,$$

$$I_{z1} = I_{x1} = -(I_{R1} + I_{R2}) = -\left(\frac{U_{ul}}{R_1} + \frac{U_{iz}}{R_2}\right) \Rightarrow U_{z1} = -U_{ul} \frac{R_3}{R_1} - U_{iz} \frac{R_3}{R_2}$$

b) Za drugi CCII vrijedi: **(1 bod)**

$$U_{z2} = I_{z2} \cdot \frac{1}{sC_1}, I_{y2} = 0, U_{x2} = U_{y2} = U_{z1}, I_{z2} = I_{x2} = \frac{U_{x2}}{R_4} \Rightarrow U_{z2} = U_{z1} \frac{1}{sR_1C_1}$$

c) Za treći CCII vrijedi: **(1 bod)**

$$I_{z3} = I_{C2} + I_{R2} = U_{iz} sC_2 + \frac{U_{iz}}{R_2} = U_{iz} \left(sC_2 + \frac{1}{R_2} \right) \Rightarrow U_{iz} = \frac{I_{z3}}{sC_2 + 1/R_2}$$

$$I_{z3} = I_{x3} = \frac{U_{x3}}{R_5} = \frac{U_{y3}}{R_5} = \frac{U_{z2}}{R_5} \Rightarrow U_{iz} = \frac{1}{R_5} \cdot \frac{1}{sC_2 + 1/R_2} \cdot U_{z2}$$

d) Nakon sređivanja do sada napisanih izraza: **(1 bod)**

$$U_{iz} = -\frac{1}{R_5} \cdot \frac{1}{sC_2 + 1/R_2} \cdot \frac{1}{sR_1C_1} \cdot \left(U_{ul} \frac{R_3}{R_1} + U_{iz} \frac{R_3}{R_2} \right)$$

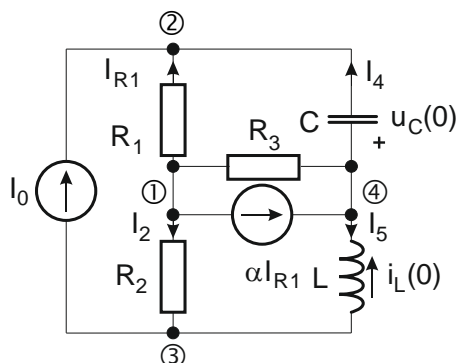
e) Uz uvrštene vrijednosti elemenata: **(1 bod)**

$$U_{iz} = -\frac{1}{s+1} \cdot \frac{1}{s} \cdot (U_{ul} + U_{iz}) \Rightarrow U_{iz} \left(1 + \frac{1}{s+1} \cdot \frac{1}{s} \right) = -\frac{1}{s+1} \cdot \frac{1}{s} \cdot U_{ul} \Rightarrow$$

$$U_{iz} \frac{s^2 + s + 1}{s(s+1)} = -\frac{1}{s(s+1)} U_{ul} \Rightarrow U_{iz}(s) = -\frac{1}{s^2 + s + 1} U_{ul}(s); U_{ul}(s) = 1 \Rightarrow$$

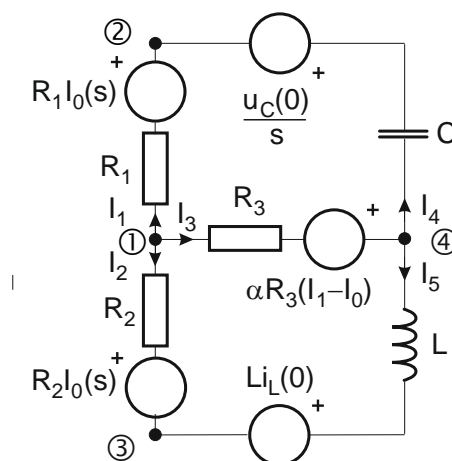
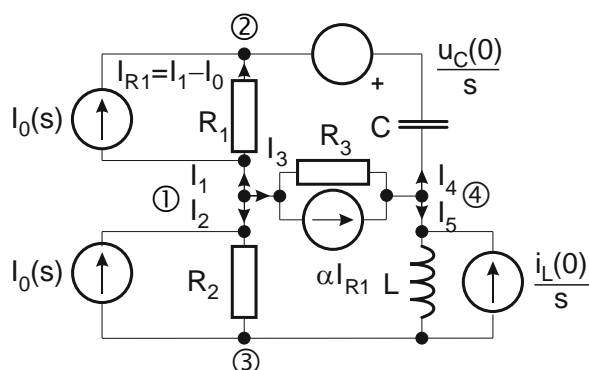
$$U_{iz}(s) = -\frac{1}{s^2 + s + 1} = -\frac{2}{\sqrt{3}} \cdot \frac{\sqrt{3}/2}{(s+1/2)^2 + (\sqrt{3}/2)^2} \Rightarrow u_{iz}(t) = -\frac{2\sqrt{3}}{3} \cdot e^{-\frac{t}{2}} \cdot \sin\left(\frac{\sqrt{3}}{2}t\right) \cdot S(t)$$

2. Zadan je električni krug prema slici. Poštujući oznake čvorišta i grana nacrtati pripadni orijentirani graf i napisati spojnu matricu \mathbf{S} . Napisati naponsko-strujne jednadžbe grana u matricnom obliku te ispisati matricu impedancija grana \mathbf{Z}_b i vektor početnih uvjeta i nezavisnih izvora grana \mathbf{U}_{0b} . Matrica \mathbf{Z}_b mora biti regularna. Napisati temeljni sustav jednadžbi petlji, odnosno odrediti matrice impedancija petlji \mathbf{Z}_p i vektor početnih uvjeta i nezavisnih izvora petlji \mathbf{U}_{0p} .



Rješenje: Posmicanje strujnog izvora i primjena Laplaceove transformacije **(1 bod)**

Da bismo na ispravan način postavili naponsko strujne jednadžbe grana, moramo paziti da nakon transformacije (posmicanja strujnog izvora) mreža ostane ista i da naponsko strujni odnosi unutar mreže ostanu nepromijenjeni. Odnosno, moramo paziti kako ćemo označiti pojedine struje grana.



(1 bod)

Naponsko-strujne jednadžbe grana:

$$U_1 = I_1 \cdot R_1 - I_0 \cdot R_1$$

$$U_2 = I_2 \cdot R_2 + I_0 \cdot R_2$$

$$U_3 = -I_1 \cdot \alpha R_3 + I_3 \cdot R_3 + I_0 \cdot \alpha R_3$$

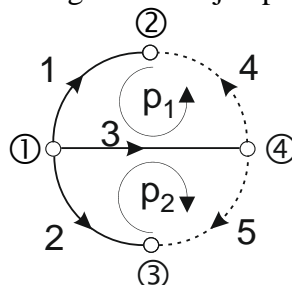
$$U_4 = I_4 \cdot \frac{1}{sC} + \frac{u_C(0)}{s}$$

$$U_5 = I_5 \cdot sL + Li_L(0)$$

Spojna matrica:

$$\mathbf{S} = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} (p_1) \\ (p_2) \end{matrix} & \begin{bmatrix} -1 & 0 & 1 & 1 & 0 \\ 0 & -1 & 1 & 0 & 1 \end{bmatrix} \end{matrix}$$

Orijentirani graf i temeljne petlje:



Naponsko-strujne relacije grana u matričnom obliku: $\mathbf{U}_b = \mathbf{Z}_b \cdot \mathbf{I}_b + \mathbf{U}_{0b}$

$$\underbrace{\begin{bmatrix} U_1 \\ U_2 \\ U_3 \\ U_4 \\ U_5 \end{bmatrix}}_{\mathbf{U}_b} = \underbrace{\begin{bmatrix} R_1 & 0 & 0 & 0 & 0 \\ 0 & R_2 & 0 & 0 & 0 \\ -\alpha R_3 & 0 & R_3 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{sC} & 0 \\ 0 & 0 & 0 & 0 & sL \end{bmatrix}}_{\mathbf{Z}_b} \cdot \underbrace{\begin{bmatrix} I_1 \\ I_2 \\ I_3 \\ I_4 \\ I_5 \end{bmatrix}}_{\mathbf{I}_b} + \underbrace{\begin{bmatrix} -I_0 R_1 \\ I_0 R_2 \\ \alpha R_3 I_0 \\ \frac{u_c(0)}{s} \\ Li_L(0) \end{bmatrix}}_{\mathbf{U}_{0b}} \quad (1 \text{ bod})$$

Matrica \mathbf{Z}_b je regularna, jer nema niti jedan stupac niti redak jednak nuli. Temeljni sustav jednadžbi petlji u matričnom obliku: $\mathbf{Z}_p \cdot \mathbf{I}_p = \mathbf{U}_{0p}$, gdje su (matrice \mathbf{Z}_p i \mathbf{U}_{0p}):

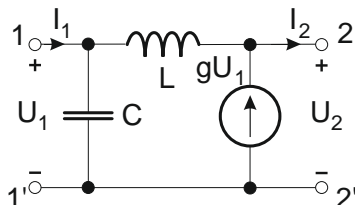
$$\mathbf{Z}_p = \mathbf{S} \cdot \mathbf{Z}_b \cdot \mathbf{S}^T = \begin{bmatrix} -1 & 0 & 1 & 1 & 0 \\ 0 & -1 & 1 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} R_1 & 0 & 0 & 0 & 0 \\ 0 & R_2 & 0 & 0 & 0 \\ -\alpha R_3 & 0 & R_3 & 0 & 0 \\ 0 & 0 & 0 & \frac{1}{sC} & 0 \\ 0 & 0 & 0 & 0 & sL \end{bmatrix} \cdot \mathbf{S}^T =$$

$$= \begin{bmatrix} -R_1 - \alpha R_3 & 0 & R_3 & \frac{1}{sC} & 0 \\ -\alpha R_3 & -R_2 & R_3 & 0 & sL \end{bmatrix} \cdot \begin{bmatrix} -1 & 0 \\ 0 & -1 \\ 1 & 1 \\ 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} R_1 + \alpha R_3 + R_3 + \frac{1}{sC} & R_3 \\ \alpha R_3 + R_3 & R_2 + R_3 + sL \end{bmatrix} \quad (1 \text{ bod})$$

$$\mathbf{U}_{0p} = -\mathbf{S} \cdot \mathbf{U}_{0b} = -\begin{bmatrix} -1 & 0 & 1 & 1 & 0 \\ 0 & -1 & 1 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} -I_0 R_1 \\ I_0 R_2 \\ \alpha R_3 I_0 \\ \frac{u_c(0)}{s} \\ Li_L(0) \end{bmatrix} = -\begin{bmatrix} I_0 R_1 + \alpha R_3 I_0 + \frac{u_c(0)}{s} \\ -I_0 R_2 + \alpha R_3 I_0 + Li_L(0) \end{bmatrix} \quad (1 \text{ bod})$$

$$\text{Rješenje: } \mathbf{Z}_p \cdot \mathbf{I}_p = \mathbf{U}_{0p} \Rightarrow \mathbf{I}_p = \begin{bmatrix} I_{p1} \\ I_{p2} \end{bmatrix}$$

3. Za četveropol prikazan slikom izračunati prijenosne $[a]$ -parametre i napisati matricu $[a]$ -parametara. Pomoću poznatih $[a]$ -parametara izračunati naponsku prijenosnu funkciju četveropola $T(s)=U_2(s)/U_1(s)$ te ulaznu impedanciju $Z_{ul1}(s)=U_1(s)/I_1(s)$ ako je na izlaznom prilazu (2–2') spojen otpor R . Da li je četveropol: a) recipročan, b) simetričan ? Obrazložiti odgovor. Zadane su normalizirane vrijednosti elemenata $R=1, L=1, C=1$ i parametar $g=1$.



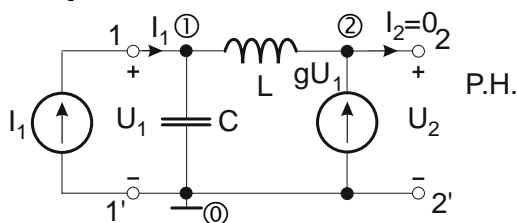
Rješenje:

$[a]$ -parametri:

$$U_1 = A \cdot U_2 + B \cdot I_2$$

$$I_1 = C \cdot U_2 + D \cdot I_2$$

$$\underline{I_2 = 0} \quad A = \left. \frac{U_1}{U_2} \right|_{I_2=0} \quad C = \left. \frac{I_1}{U_2} \right|_{I_2=0}$$



$$(1) \quad U_1 \left(\frac{1}{sL} + sC \right) - U_2 \frac{1}{sL} = I_1$$

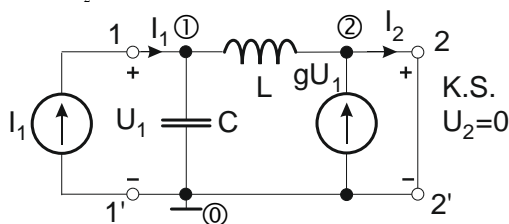
$$(2) \quad -U_1 \frac{1}{sL} + U_2 \frac{1}{sL} = gU_1$$

$$(2) \Rightarrow \left(g + \frac{1}{sL} \right) U_1 = \frac{1}{sL} U_2 \Rightarrow U_1 = \frac{1}{gsL+1} U_2 \Rightarrow A = \frac{U_1}{U_2} = \frac{1}{gsL+1}$$

$$(2) \rightarrow (1) \Rightarrow U_2 \frac{1}{gsL+1} \left(\frac{1}{sL} + sC \right) - U_2 \frac{1}{sL} = I_1 \Rightarrow C = \frac{I_1}{U_2} = \frac{1}{gsL+1} \left(\frac{1}{sL} + sC \right) - \frac{1}{sL}$$

$$C = \frac{\left(\frac{1}{sL} + sC \right) - \frac{1}{sL} (gsL+1)}{gsL+1} = \frac{sC - g}{gsL+1}$$

$$\underline{U_2 = 0} \quad B = \left. \frac{U_1}{I_2} \right|_{U_2=0} \quad D = \left. \frac{I_1}{I_2} \right|_{U_2=0}$$



$$(1) U_1 \left(\frac{1}{sL} + sC \right) - U_2 \frac{1}{sL} = I_1$$

$$(2) -U_1 \frac{1}{sL} + U_2 \frac{1}{sL} = gU_1 - I_2$$

$$U_2 = 0 \quad (1) \Rightarrow U_1 \left(\frac{1}{sL} + sC \right) = I_1$$

$$(2) \Rightarrow -U_1 \frac{1}{sL} = gU_1 - I_2 \Rightarrow I_2 = U_1 \left(g + \frac{1}{sL} \right) \Rightarrow B = \frac{U_1}{I_2} = \frac{1}{g + 1/(sL)} = \frac{sL}{gsL + 1}$$

$$(2) \rightarrow (1) \Rightarrow I_2 \frac{sL}{gsL + 1} \left(\frac{1}{sL} + sC \right) = I_1 \Rightarrow D = \frac{I_1}{I_2} = \frac{sL}{gsL + 1} \left(\frac{1}{sL} + sC \right) = \frac{1 + s^2 LC}{gsL + 1}$$

$$[a] = \frac{1}{gsL + 1} \begin{bmatrix} 1 & sL \\ sC - g & s^2 LC + 1 \end{bmatrix} = \frac{1}{s + 1} \begin{bmatrix} 1 & s \\ s - 1 & 1 + s^2 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix}$$

(3 boda)

Prijenosna funkcija napona:

$$T(s) = \frac{U_2(s)}{U_1(s)} = \frac{Z_2}{AZ_2 + B} = \frac{s + 1}{s + 1} = 1$$

Ulazna impedancija u četveropol zaključen s otporom R :

$$Z_{ul}(s) = \frac{U_1(s)}{I_1(s)} = \frac{AZ_2 + B}{CZ_2 + D} = \frac{s + 1}{s - 1 + s^2 + 1} = \frac{s + 1}{s(s + 1)} = \frac{1}{s}$$

(1 bod)

Odgovori na pitanja:

a) Četveropol nije električki recipročan jer sadrži naponsko ovisni strujni izvor i vrijedi da je:

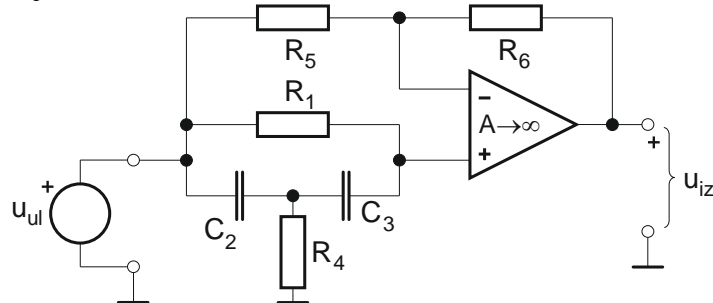
$$|a| = AD - BC = \frac{1 + s^2 - s(s - 1)}{(s + 1)^2} = \frac{1 + s}{(s + 1)^2} = \frac{1}{s + 1} \neq 1;$$

b) Četveropol nije električki simetričan jer se parametri A i D razlikuju:

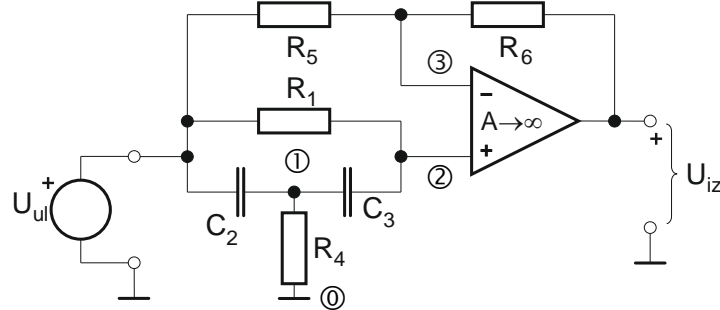
$$A = \frac{1}{s + 1} \neq D = \frac{s^2 + 1}{s + 1}$$

(1 bod)

4. Zadan je aktivni-RC električni filter prikazan slikom s normaliziranim vrijednostima elemenata $R_1=1$, $C_2=1$, $C_3=1$, $R_4=1$, te $R_5=1$, $R_6=2$. a) Izračunati njegovu naponsku prijenosnu funkciju $T(s)=U_{iz}(s)/U_{ul}(s)$. O kojem se tipu filtra radi (NP, VP, PP ili PB)? b) Usporedbom s odgovarajućim općim oblikom prijenosne funkcije filtra 2. stupnja izračunati vrijednost parametara k , ω_p , ω_z , q_p . c) Prikazati raspored polova i nula u kompleksnoj ravnini. d) Nacrtati amplitudno-frekvencijsku karakteristiku.



Rješenje: Laplaceova transformacija i jednačbe čvorišta:



Metoda napona čvorišta:

$$(1) U_1 \left(sC_2 + sC_3 + \frac{1}{R_4} \right) - U_2 sC_3 = U_{ul} sC_2 / R_4$$

$$(2) -U_1 sC_3 + U_2 \left(\frac{1}{R_1} + sC_3 \right) = U_{ul} \frac{1}{R_1} / sC_3$$

$$(3) U_3 \left(\frac{1}{R_5} + \frac{1}{R_6} \right) = U_{ul} \frac{1}{R_5} + U_{iz} \frac{1}{R_6} / R_5 R_6$$

$$(4) A(U_2 - U_3) = U_{iz} \Rightarrow U_2 = U_3 \quad (A \rightarrow \infty)$$

Slijedi postepeno računanje korak po korak

$$(3) \Rightarrow U_3 (R_5 + R_6) = U_{ul} R_6 + U_{iz} R_5 \Rightarrow U_3 = U_{ul} \frac{R_6}{R_5 + R_6} + U_{iz} \frac{R_5}{R_5 + R_6}; \text{ Uz oznaku } \alpha = \frac{R_5}{R_5 + R_6} \Rightarrow$$

$$U_3 = U_{ul} (1 - \alpha) + U_{iz} \alpha; \text{ Zajedno sa (4) } \Rightarrow U_2 = U_3 = U_{ul} (1 - \alpha) + U_{iz} \alpha$$

$$(2) \Rightarrow U_1 = U_2 \left(\frac{1}{sC_3 R_1} + 1 \right) - U_{ul} \frac{1}{sC_3 R_1}$$

$$(1) \Rightarrow U_1 (sR_4 C_2 + sR_4 C_3 + 1) - U_2 R_4 sC_3 = U_{ul} R_4 sC_2; (2) \rightarrow (1) \text{ (rješavamo se } U_1) \Rightarrow$$

$$\left[U_2 \left(\frac{1}{sC_3 R_1} + 1 \right) - U_{ul} \frac{1}{sC_3 R_1} \right] (sR_4 C_2 + sR_4 C_3 + 1) - U_2 R_4 sC_3 = U_{ul} R_4 sC_2$$

$$U_2 \left(\frac{1}{sC_3 R_1} + 1 \right) (sR_4 C_2 + sR_4 C_3 + 1) - U_2 R_4 sC_3 = U_{ul} \frac{1}{sC_3 R_1} (sR_4 C_2 + sR_4 C_3 + 1) + U_{ul} R_4 sC_2 / sC_3 R_1$$

$$\begin{aligned}
U_2(sC_3R_1+1)(sR_4C_2+sR_4C_3+1)-U_2R_1R_4s^2C_3^2 &= U_{ul}(s^2R_1C_2C_3R_4+sR_4C_2+sR_4C_3+1) \\
U_2(s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1) &= U_{ul}(s^2R_1C_2C_3R_4+sR_4C_2+sR_4C_3+1) \\
[U_{ul}(1-\alpha)+U_{iz}\alpha](s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1) &= U_{ul}(s^2R_1C_2C_3R_4+sR_4C_2+sR_4C_3+1) \\
U_{iz}\alpha(s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1) &= \\
U_{ul}(s^2R_1C_2C_3R_4+sR_4C_2+sR_4C_3+1)-U_{ul}(1-\alpha)(s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1) &= \\
U_{iz}\alpha(s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1) &= \\
U_{ul}(s^2R_1C_2C_3R_4+sR_4C_2+sR_4C_3+1)-U_{ul}(s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1)+ & \\
+U_{ul}\alpha(s^2R_1C_2C_3R_4+sC_3R_1+sR_4C_2+sR_4C_3+1) & \\
T(s) = \frac{U_{iz}(s)}{U_{ul}(s)} = \frac{s^2R_1C_2C_3R_4+s\left[C_3R_1\left(1-\frac{1}{\alpha}\right)+R_4C_2+R_4C_3\right]+1}{s^2R_1C_2C_3R_4+s(C_3R_1+R_4C_2+R_4C_3)+1}
\end{aligned}$$

Konačno je:

$$T(s) = \frac{U_{iz}(s)}{U_{ul}(s)} = \frac{s^2 + s \frac{C_3R_1(1-1/\alpha) + R_4C_2 + R_4C_3}{R_1C_2C_3R_4} + \frac{1}{R_1C_2C_3R_4}}{s^2 + s \frac{C_3R_1 + R_4C_2 + R_4C_3}{R_1C_2C_3R_4} + \frac{1}{R_1C_2C_3R_4}} = \frac{s^2 + 1}{s^2 + 3s + 1} \quad (2 \text{ boda})$$

Usporedbom s odgovarajućim općim oblikom prijenosne funkcije filtra 2. stupnja izračunati parametre k , ω_p , q_p , ω_z .

$$T(s) = \frac{U_{iz}(s)}{U_{ul}(s)} = k \cdot \frac{s^2 + \omega_z^2}{s^2 + (\omega_p/q_p)s + \omega_p^2} \Rightarrow \omega_p = \omega_z = 1, \quad q_p = \frac{1}{3}, \quad k = 1$$

-o kojem se tipu filtra radi (NP, VP, PP ili PB)? \Rightarrow PB (1 bod)

Raspored polova i nula u kompleksnoj ravnini: (1 bod)

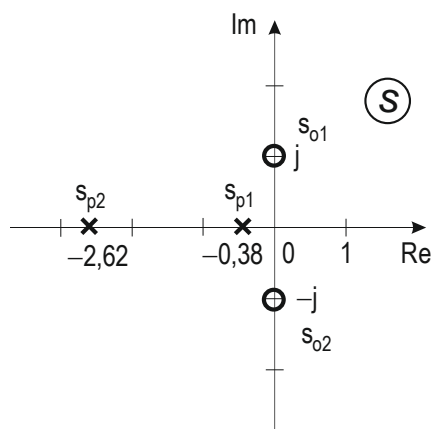
$$\text{Nule } s^2 + 1 = 0 \Rightarrow s_{o1,2} = \pm j$$

$$\text{Polovi } s^2 + 3s + 1 = 0 \Rightarrow s_{p1,2} = -\frac{3}{2} \pm \sqrt{\frac{9}{4} - 1} = -\frac{3}{2} \pm \frac{\sqrt{5}}{2}; \quad s_{p1} = -0,381966; \quad s_{p2} = -2,61803.$$

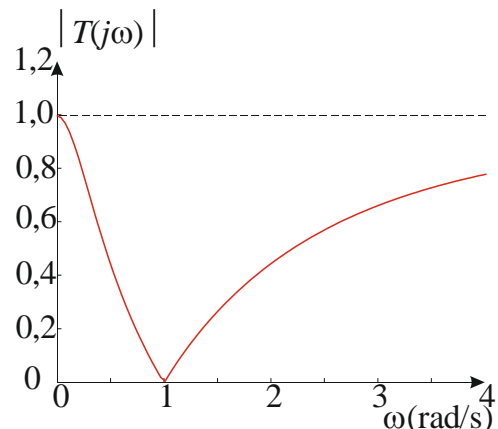
Amplitudno-frekvencijska (A-F) karakteristika (1 bod)

$$s = j\omega \Rightarrow T(j\omega) = \frac{-\omega^2 + 1}{-\omega^2 + 3 \cdot j\omega + 1} \Rightarrow |T(j\omega)| = \frac{|1 - \omega^2|}{\sqrt{(1 - \omega^2)^2 + (3 \cdot \omega)^2}}$$

Karakteristične točke A-F karakteristike $|T(j0)| = 1$; $|T(j1)| = 0$; $|T(j\infty)| = 1$.

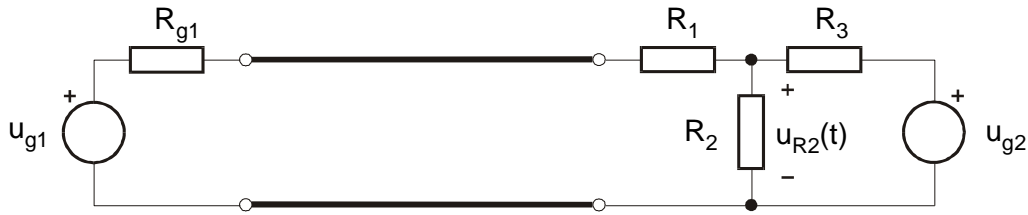


Raspored nula i polova u s -ravnini



Amplitudno frekvencijska karakteristika

5. Zadana je linija s primarnim parametrima $R=0,8\Omega/\text{km}$, $G=12,5\text{mS}/\text{km}$, $L=1,6\mu\text{H}/\text{km}$ i $C=25\text{nF}/\text{km}$. Duljina linije je 10km. Unutrašnji otpori generatora prilagođeni su zrcalnoj impedanciji linije. Zadano je: $R_1=4\Omega$, $R_2=6\Omega$, $u_{g1}(t)=u_{g2}(t)=4S(t)$. Koliki je R_3 ? Odrediti i nacrtati $u_{R2}(t)$ (primijeniti postupak superpozicije).



Rješenje: Ispitajmo da li vrijedi $\frac{R}{L} = \frac{G}{C}$ odnosno $\frac{0,8}{1,6 \cdot 10^{-6}} = \frac{12,5 \cdot 10^{-3}}{25 \cdot 10^{-9}}$. Vrijedi! \Rightarrow

To je linija bez distorzije. Računamo sekundarne parametre po pojednostavljenim formulama

$$Z_0 = \sqrt{\frac{L}{C}} = \sqrt{\frac{1,6 \cdot 10^{-6}}{25 \cdot 10^{-9}}} = \sqrt{64} = 8\Omega$$

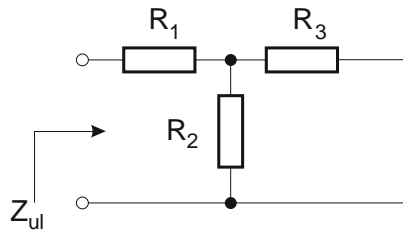
$$\gamma = \sqrt{RG} + s\sqrt{LC} = \sqrt{0,8 \cdot 12,5 \cdot 10^{-3}} + s\sqrt{1,6 \cdot 10^{-6} \cdot 25 \cdot 10^{-9}} = 0,1 + s \cdot 0,2 \cdot 10^{-6}$$

(1 bod)

Metoda superpozicije:

a) izvor $u_{g2}(t)$ isključen

$R_{g1} = 8\Omega$ zbog prilagođenja.

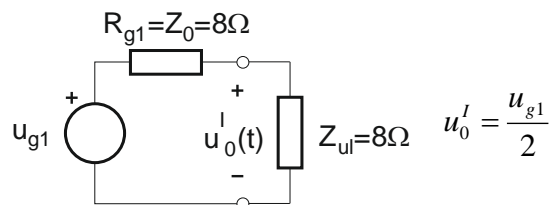
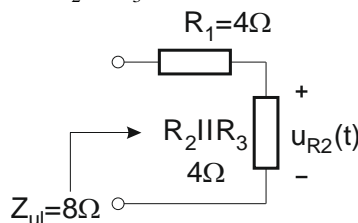


$$Z_{ul} = 8\Omega = R_1 + \frac{R_2 R_3}{R_2 + R_3} \Rightarrow Z_{ul}(R_2 + R_3) = (R_2 + R_3)R_1 + R_2 R_3$$

$$\Rightarrow Z_{ul}R_2 + Z_{ul}R_3 = R_1R_2 + (R_1 + R_2)R_3 \Rightarrow Z_{ul}R_3 - (R_1 + R_2)R_3 = R_1R_2 - Z_{ul}R_2 \Rightarrow$$

$$R_3 = \frac{R_1R_2 - Z_{ul}R_2}{Z_{ul} - (R_1 + R_2)} = \frac{4 \cdot 6 - 8 \cdot 6}{8 - (4 + 6)} = \frac{-24}{-2} = 12\Omega$$

$$R_2 \parallel R_3 = \frac{R_2 R_3}{R_2 + R_3} = \frac{6 \cdot 12}{6 + 12} = 4\Omega$$

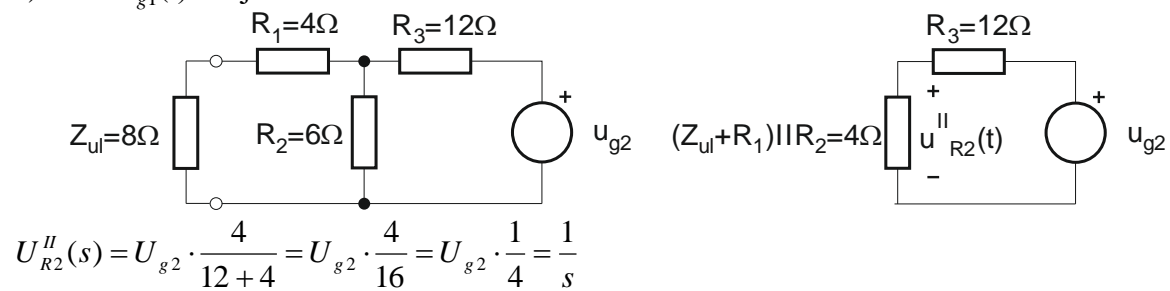


$$g_1 = \gamma \cdot l_1 = (0,1 + s \cdot 0,2 \cdot 10^{-6}) \cdot 10 = 1 + s \cdot 2 \cdot 10^{-6}$$

$$U'_{R2}(s) = \frac{U_{g1}}{2} \cdot \frac{1}{2} \cdot e^{-1} \cdot e^{-s \cdot 2 \cdot 10^{-6}} = \frac{1}{s} e^{-1} \cdot e^{-s \cdot 2 \cdot 10^{-6}}$$

(2 boda)

b) izvor $u_{g1}(t)$ isključen

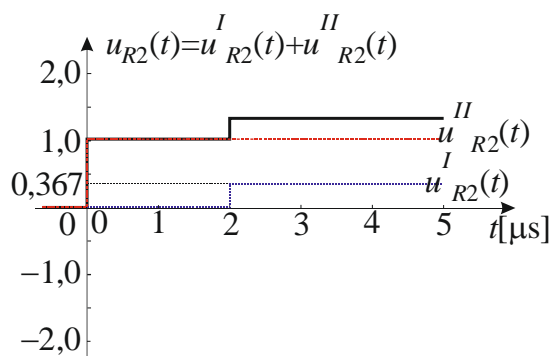


(1 bod)

c) ukupan napon na R_2 :

$$U_{R2}(s) = U_{R2}^I(s) + U_{R2}^{II}(s) = \frac{1}{s} e^{-1} \cdot e^{-s \cdot 2 \cdot 10^{-6}} + \frac{1}{s}$$

$$u_{R2}(t) = u_{R2}^I(t) + u_{R2}^{II}(t) = \frac{1}{e} S(t - 2 \cdot 10^{-6}) + S(t) = 0,367879 \cdot S(t - 2 \cdot 10^{-6}) + S(t)$$



(1 bod)