$$H(s) = \int_{-\infty}^{\infty} h(t) e^{-st} dt$$

$$X(s) = \int_{-\infty}^{\infty} x(t) e^{-st} dt$$

72.11

$$X(t) = e^{-at} \mu(t)$$

$$X(s) = \int_{0}^{\infty} e^{-at} e^{-st} dt = \int_{0}^{\infty} e^{-t(s-a)} dt = \frac{(-1)}{s+a} e^{-t(s+a)} \Big|_{0}^{\infty} = \frac{(-1)}{s+a} \left(e^{-as(s+a)} - e^{-s} \right) = \frac{1}{s+a}$$

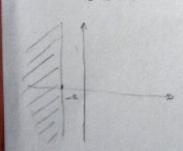
$$X(s) = \frac{1}{s+a}$$

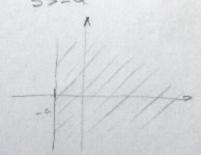
$$X(t) = -e^{-\alpha t} \mu(t)$$

$$X(s) = \int_{-\infty}^{\infty} e^{-\alpha t} e^{-st} dt = -\int_{-\infty}^{\infty} e^{t(-\alpha - s)} dt = \frac{-1}{-s - \alpha} e^{t(-\alpha - s)} \Big|_{-\infty}^{0} = \frac{1}{s + \alpha} \left(e^{\alpha} - e^{-\alpha t (s - \alpha)} \right) \Big|_{-\infty}^{\infty}$$

$$X(s) = \frac{1}{s + \alpha}$$

$$X(s) = \frac{1}{s + \alpha}$$





$$x(\xi) = \int_{0}^{\infty} x(\xi) e^{-s\xi} d\xi$$

$$x(\xi) = w(\xi) + y(\xi)$$

$$x(\xi) = \int_{0}^{\infty} f(\xi) e^{-s\xi} d\xi = 1$$

e-ot. +300 6 (s+a)4

sim ared potenoje X (m-1) - s red derivacje

y" (t) + 2 y'(t) + y(t) = n"(t) + n'(t) + n(t)

 $u(t) = \delta(t)$

4(0) = 4(0) = 0

 $y(t) \circ y(s) = sy(s) - y(s) = sy(s)$ $y'(t) \circ s^{2}y(s) - sy(s) - y'(s) = s^{2}y(s)$

u(t) 00 U(s)

ul(+) 0-0 sll(s) - U(0), = sl(s)

u* (+) 0 = s2U(s) - su(o) - U(o) = s2U(s)

 $s^{2}H(s) + 2sH(s) + H(s) = s^{2}H(s) + sU(s) + U(s)$ $H(s)(s^{2}+2s+1) = H(s)(s^{2}+s+1)$

 $U(s) = \frac{s^2 + s + 1}{s^2 + 2s + 1} U(s) = \frac{s^2 + s + 1}{s^2 + 2s + 1} = 1 + \frac{-s}{s^2 + 2s + 1} = 1 - \frac{s}{s^2 + 2s + 1}$

 $(s^2 + s + 1) : (s^2 + 2s + 1) = 1$ - $s^2 - 2s - 1$

 $\frac{S}{(S+1)^2} = \frac{A}{(S+1)} + \frac{\gamma_5}{(S+1)^2}$

 $\frac{5}{5^2 + 2s + 1} = \frac{5}{(5 + 1)^2}$

 $\frac{A_{s+1}}{(s^{2}+1)(s-1)^{3}} = \frac{A_{s+1}}{s^{2}+1} + \frac{C}{(s-1)} + \frac{D}{(s-1)^{2}} + \frac{E}{(s-1)^{3}}$ $= \frac{A}{s-2} + \frac{B}{(s-2)^{2}} + \frac{C_{s+1}}{s^{2}+1} + \frac{E_{s+1}}{(s^{2}+1)^{2}}$ $+ \frac{E_{s+1}}{(s^{2}+1)^{2}}$

$$\frac{S}{s^{2}+2s+1} = \frac{S}{(s+1)^{2}} = \frac{A}{(s+1)} + \frac{B}{(s+1)^{2}} = \frac{A(s+1)+B}{(s+1)^{2}} = \frac{SA+A+B}{(s+1)^{2}}$$

$$A = 1$$

$$A + B = 0 \Rightarrow B = -1$$

$$\frac{1}{1} - \frac{1}{12}$$

$$\frac{1}{s+1} = \frac{1}{(s+1)^2}$$

$$\frac{1}{s+1} = 0 e^{-t} \mu(t)$$

$$\frac{1}{(s+1)^2} = 0 t e^{-t} \mu(t)$$

$$X(s) = \frac{7s^2 - 5s - 6}{(s+1)(s-2)(s-1)}$$

$$X(s) = \frac{Cu}{s+1} + \frac{Cu}{s-2} + \frac{Cu}{s-1}$$

$$\frac{(s+1)^{2}(s-2)(s-1)}{s+1} = \frac{C_{11}}{s+1} + \frac{C_{12}}{(s+1)^{2}} + \frac{C_{21}}{s-2} + \frac{C_{31}}{s-1}$$

r-višestrukost pola

$$C_{11} = \frac{1}{(1-1)!} \lim_{s \to -1} \left[\frac{d^{1-1}}{ds^{1-1}} \left(s+1 \right)^{1} \frac{7s^{2} - 5s - 6}{(s+1)(s-2)(s-1)} \right]$$

=
$$\lim_{s \to -1} \left(\frac{7s^2 - 5s - 6}{(s-2)(s-1)} \right)$$

$$X(s) = \frac{1}{s+1} + \frac{4}{s-2} + \frac{2}{s-1}$$

$$\frac{1}{s+1} = 0 e^{-st} \mu(t)$$

$$4 \frac{1}{s-2} = 04e^{2t} \mu(t)$$

$$2 \frac{1}{s-1} = 002e^{t} \mu(t)$$

PI.

$$X(s) = \frac{s+1}{(s-1)^2 (s+2)}$$

$$= \frac{Cu}{(s-1)} + \frac{Cu}{(s-1)^2} + \frac{Cu}{s+2}$$

$$C_{21} = -\frac{1}{9}$$

$$C_{11} = \frac{1}{(2-1)!} \lim_{s \to 1} \left[\frac{d^{2-1}}{ds^{2-1}} \left(s - 1 \right)^{\frac{s}{2}} \frac{s+1}{(s+2)} \right]$$

=
$$\lim_{s \to 1} \left(\frac{d}{ds} \left(\frac{s+1}{s+2} \right) \right)$$

$$= \lim_{S \to 1} \left(\frac{S + 2 - (S + 1) \cdot 1}{(S + 2)^2} \right) = \frac{1}{9}$$

$$= \lim_{s \to 1} \frac{s+1}{s+2} = \frac{2}{3}$$

$$X(s) = \frac{1}{9} \cdot \frac{1}{s-1} + \frac{\varrho}{3} \cdot \frac{1}{(s-1)^2} - \frac{1}{9} \cdot \frac{1}{s+2}$$

6 = b'n - 6n'

$$X(s) = 1 - \frac{s}{(3+1)^2}$$

$$\frac{S}{(S+1)^2} = \frac{C_{11}}{S+1} + \frac{C_{12}}{(S+1)^2}$$

$$\chi(s) = \frac{s}{(s^2+1)(s-1)^2}$$

$$= \frac{s}{(s-j)(s+j)(s-1)^2} = \frac{C_{11}}{s-j} + \frac{C_{21}}{s+j} + \frac{C_{31}}{s-1} + \frac{C_{32}}{(s-1)^2}$$

$$C_u = \frac{1}{2j(j-1)^2} = \frac{1}{2(-1-2j+1)} = \frac{1}{-4j} \cdot \frac{1}{i} = \frac{1}{4i}$$

$$c_{2x} = \frac{-1}{-2j(-j-1)^2} = \frac{1}{2(-1+2j+1)} = -\frac{1}{4}j$$

$$C_{32} = \lim_{s \to 1} \left[\frac{s}{s^2 + 1} \right] = \frac{1}{2}$$

$$= \frac{1}{4} \frac{1}{s - 1} - \frac{1}{4} \frac{1}{s + 1} + \frac{1}{2} \frac{1}{(s - 1)^2}$$

$$= \frac{1}{4} e^{3t} - \frac{1}{4} e^{-1t} + \frac{1}{2} e^{t} \cdot t$$

$$= \frac{1}{4} e^{3t} - \frac{1}{4} e^{-1t} + \frac{1}{2} e^{t} \cdot t$$

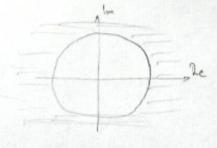
$$= \frac{1}{4} e^{3t} + \frac{1}{4} e^{-1t} + \frac{1}{2} e^{t} \cdot t$$

$$= -\frac{1}{2} e^{3t} (t) \mu(t) + \frac{1}{2} e^{t} t \mu(t)$$

PRIMIER 1.

$$X(n) = L^n \mu(n)$$

$$X(2) = \sum_{m=0}^{\infty} \lambda^m \pm^m = \sum_{m=0}^{\infty} \left(\frac{1}{2}\right)^m = \frac{1}{1 - \frac{1}{2}} = \frac{1}{2 - \lambda}$$



$$\mu(-n-1) = \begin{cases} 1, & n \le -1 \\ 0, & n > -1 \end{cases}$$

$$-n-1 \ge 0$$

$$n < -1$$

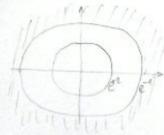
$$\times (z) = -\frac{t-1}{\sum_{t=0}^{t-1}} \int_{-t}^{-t} z^{t} = -\sum_{t=0}^{\infty} \left(\frac{z}{z}\right)^{t} = -\sum_{t=0}^{\infty} \left(\frac{z}{z}\right)^{t} + 1$$

$$H(z) = \frac{(e^{-2} - e^{-1}) z}{(z - e^{-2}) (z - e^{-1})}$$

$$H_{\star}(z) = \frac{H(z)}{z} = \frac{e^{-2} - e^{-1}}{(z - e^{-2})(z - e^{-1})}$$

$$H_{\lambda}(\pm) = \frac{1}{2 - e^{-2}} - \frac{1}{2 - e^{-1}}$$

$$\mu(z) = \frac{z}{z - e^2} - \frac{z}{z - e^{-1}}$$

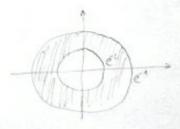


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$$\mathcal{Z}^{-1}(H_{\lambda}(z)) = \frac{A}{z - e^{-z}} + \frac{B}{z - e^{-1}}$$

$$\frac{A(z-e^{-1})+B(z-e^{-2})}{(z-e^{-2})(z-e^{-1})} =$$

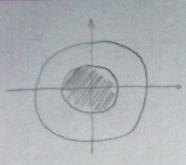
$$Z(A+B) + (-Ae^{A} - Be^{-2}) = e^{-2} - e^{-1}$$



|天| イ|ヤロ

$$h(n) = e^{-2n}\mu(n) - (-e^{-n}\mu(n-1))$$

 $h(n) = e^{-2n}\mu(n) + e^{-n}\mu(-n-1)$



12/4

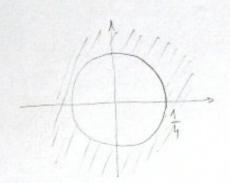
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$$h(n) = -e^{-2n}\mu(n-1) + e^{-n}\mu(-n-1)$$

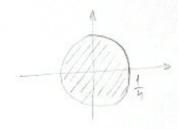
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$$H(z) = \frac{1}{4-z^{-1}} = \frac{1}{4-\frac{1}{2}} = \frac{z}{4z-1} - \frac{1}{4} = \frac{z}{z-\frac{1}{4}}$$

L= 1/4 h



$$\mathcal{J}_{1}\left(n\right)=\frac{1}{4}\cdot\left(\frac{1}{4}\right)^{n}\cdot\mu\left(n\right)$$



$$f_{N}(n) = \frac{1}{4} \cdot \left(-\frac{1}{4}\right)^{N} M(-N-1)$$

$$H(e^{i\omega}) = \frac{1}{4 - e^{-i\omega}} = \frac{1}{4 - \cos(\omega) + i\sin(\omega)}$$

$$|H(e^{iw})| = \frac{1}{\sqrt{17 - 8\cos(w)}}$$



$$\times (n-j) \circ = \exists i (x(z) + \underbrace{\exists}_{n=j}^{2} \cdot x(m) \neq x^{-m})$$
 $\times (n+j) \circ = \exists i (x(z) + \underbrace{\exists}_{n=0}^{2} \cdot x(m) \neq x^{-m})$

PRINTER.

$$X(\pm) = \frac{1}{1-0.75\pm^{-1}} = \frac{2}{2-0.75}$$

$$\chi(z) = \sum_{m=0}^{\infty} \chi(m) z^{-m} = \chi(0) + \chi(1) z^{-1} + \chi(2) z^{-2} + \chi(3) z^{-3} + \dots$$

$$\frac{2:(2-0.75)=(1+0.752)^{2}+0.562^{2}+...}{-2-0.75}$$

$$\frac{-2-0.75}{-0.75}=0.562^{-1}$$

$$0.562^{-1}$$

0,75 ". µ(n)

$$\times (\forall) = \frac{2^2}{(z-1)(z-2)(z-3)}$$

$$\frac{A}{(z-1)} + \frac{B}{(z-2)} + \frac{C}{(z-3)} =$$

$$X_{A}(\mp) = \frac{X(\mp)}{\mp}$$

$$Z^{-1} \left\{ X_{A}(\mp)^{2} \right\}$$

$$C_{*}[= \frac{1}{(r-1)!} \lim_{x \to R_{A}} \left[\frac{d^{r-1}}{d \pm^{r} i} \left(\left(\pm - P_{*} \right)^{r} X_{A}(\mp) \right) \right]$$

$$y'(t) + y(t) = \mu(t)$$

$$SY(s) - Y(o) + Y(s) = U(s)$$

$$U(s)(s+1) = U(s) + y(o)$$

$$Y(s) = \frac{1}{s+1} U(s) + \frac{2}{s+1}$$

$$H(s)$$

PRIMIER

$$X(\pm) = \frac{10 \pm^{3} - 37 \pm^{2} + 24 \pm 18}{2(\pm - 3)^{2}}$$

$$X_{1}(\pm) = \frac{10 \pm^{3} - 37 \pm^{2} + 24 \pm 18}{2^{2}(\pm - 3)^{2}}$$

$$= \frac{C_{11}}{\pm} + \frac{C_{12}}{\pm^{2}} + \frac{C_{21}}{\pm^{2}} + \frac{C_{22}}{(2 - 3)^{2}}$$

$$C_{11} = \frac{1}{(2 - 1)!} \lim_{Z \to 0} \left\{ \frac{d}{d \pm} \left[\pm^{2}, \frac{10 \pm^{3} - 37 \pm^{2} + 24 \pm 18}{2^{2}(\pm - 3)^{2}} \right] \right\}$$

$$C_{11} = \frac{1}{4}$$
 $C_{12} = \frac{1}{2}$
 $C_{21} = \frac{1}{2}$
 $C_{22} = \frac{1}{2}$
 $\frac{1}{2} + \frac{2}{2} + \frac{5}{2} + \frac{1}{(2-3)^2}$