

# Tablica Fourierovih transformacija

inačica 6.0

	<b>CTFS</b> <i>Continuous Time Fourier Series</i>	<b>CTFT</b> <i>Continuous Time Fourier Transform</i>	<b>DTFT</b> <i>Discrete Time Fourier Transform</i>	<b>DTFS</b> <i>Discrete Time Fourier Series</i>
Transformacija:	$X(k) = \frac{1}{T_0} \int_{T_0} x(t) e^{-jk\omega_0 t} dt$	$X(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$	$X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x(n) e^{-j\omega n}$	$X(k) = \frac{1}{N} \sum_{n=0}^{N-1} x(n) e^{-jk\omega n}$
Inverzna transformacija:	$x(t) = \sum_{k=-\infty}^{\infty} X(k) e^{jk\omega_0 t}$	$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega$	$x(n) = \frac{1}{2\pi} \int_{-\pi}^{\pi} X(e^{j\omega}) e^{j\omega n} d\omega$	$x(n) = \sum_{k=0}^{N-1} X(k) e^{jk\omega n}$
Parsevalova relacija:	$E = \infty$ $P_x = \frac{1}{T_0} \int_{T_0}  x(t) ^2 dt = \sum_{k=-\infty}^{\infty}  X(k) ^2$	$E = \frac{1}{2\pi} \int_{-\infty}^{\infty}  X(j\omega) ^2 d\omega$	$E = \frac{1}{2\pi} \int_{-\pi}^{\pi}  X(e^{j\omega}) ^2 d\omega$	$E = \infty$ $P_x = \frac{1}{N} \sum_{k=0}^{N-1}  x(n) ^2 = \sum_{k=0}^{N-1}  X(k) ^2$
	KontPeriod → DiskSignal	KontSignal → KontSignal	DiskSignal → KontPeriod	DiskPeriod → DiskPeriod
Vremensko područje:	Kontinuiran	Kontinuiran	Diskretan	Diskretan
Frekvencijsko područje:	Diskretan	Kontinuiran	Kontinuiran	Diskretan

Vremensko područje	Frekvencijsko područje
Periodičan	Diskretan
Aperiodičan	Kontinuirani
Diskretan	Periodičan
Kontinuirani	Aperiodičan

	<b>FT</b> <i>Fourier Transform</i>	<b>FS</b> <i>Fourier Series</i>
Transformacija:	$X(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$	$X(k) = \frac{1}{T_0} \int_{T_0} x(t) e^{-jk\omega_0 t} dt$
Inverzna transformacija:	$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega$	$x(t) = \sum_{k=-\infty}^{\infty} X(k) e^{jk\omega_0 t}$
	$E = \frac{1}{2\pi} \int_{-\infty}^{\infty}  X(j\omega) ^2 d\omega$	$E = \infty$ $P = \sum_{k=-\infty}^{\infty}  X(k) ^2$

### CTFS

$$\text{sinc}(x) = \frac{\sin x}{x}$$

$$\text{sinc}(0) = 1$$

Pravokutan periodičan signal kojemu je osnovna komponenta simetrična s obzirom na ishodište:

$$X_k = X(k) = A \cdot \frac{\tau}{T} \text{sinc}\left(k\pi \cdot \frac{\tau}{T}\right)$$

$$X_0 = A \cdot \frac{\tau}{T}$$

# Svojstva transformacija

	CTFT	DTFT
Linearnost	$\alpha x(t) + \beta y(t) \xrightarrow{F} \alpha X(j\omega) + \beta Y(j\omega)$	$\alpha x(n) + \beta y(n) \xrightarrow{F} \alpha X(e^{j\omega}) + \beta Y(e^{j\omega})$
Vremenski pomak	$x(t - t_0) \xrightarrow{F} X(j\omega) e^{-j\omega t_0}$	$x(n - n_0) \xrightarrow{F} X(e^{j\omega}) e^{-j\omega n_0}$
Frekvencijski pomak	$x(t) e^{+j\omega_0 t} \xrightarrow{F} X(\omega - \omega_0)$	$x(n) e^{+j\omega_0 n} \xrightarrow{F} X(e^{j(\omega - \omega_0)})$
Vremensko skaliranje	$x(at) \xrightarrow{F} \frac{1}{ a } X\left(j\frac{\omega}{a}\right)$	
Frekvencijsko skaliranje	$\frac{1}{ a } x\left(\frac{t}{a}\right) \xrightarrow{F} X(ja\omega)$	
Konjugiranost	$x^*(t) \xrightarrow{F} X^*(-j\omega)$	$x^*(n) \xrightarrow{F} X^*(e^{-j\omega})$
Vremenska inverzija	$x(-t) \xrightarrow{F} X(-j\omega)$	$x(-n) \xrightarrow{F} X(e^{-j\omega})$
Dualnost	$X(jt) \xrightarrow{F} 2\pi x(-\omega) \qquad X(-jt) \xrightarrow{F} 2\pi x(\omega)$	
Konvolucija	$(x * y)(t) \xrightarrow{F} X(j\omega) Y(j\omega)$	$(x * y)(n) \xrightarrow{F} X(e^{j\omega}) Y(e^{j\omega})$
Množenje	$x(t) y(t) \xrightarrow{F} \frac{1}{2\pi} X(j\omega) * Y(j\omega)$	$x(n) y(n) \xrightarrow{F} \frac{1}{2\pi} X(e^{j\omega}) * Y(e^{j\omega})$
Parseval	$\int_{-\infty}^{\infty}  x(t) ^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty}  X(j\omega) ^2 d\omega$	$\sum_{n=-\infty}^{\infty}  x(n) ^2 = \frac{1}{2\pi} \int_{-\pi}^{\pi}  X(e^{j\omega}) ^2 d\omega$
Derivacija	$\frac{d^k}{dt^k} (x(t)) \xrightarrow{F} (j\omega)^k X(j\omega)$	$nx(n) \xrightarrow{F} \left( j \frac{dX(e^{j\omega})}{d\omega} \right)$
Modulacija	$x(t) \cos(\omega_0 t) \xrightarrow{F} \frac{1}{2} [X(j(\omega - \omega_0)) + X(j(\omega + \omega_0))]$	$x(n) \cos(\omega_0 n) \xrightarrow{F} \frac{1}{2} [X(e^{j(\omega - \omega_0)}) + X(e^{j(\omega + \omega_0)})]$
Integracija	$\int_{-\infty}^t x(\lambda) d\lambda \xrightarrow{F} \frac{X(j\omega)}{j\omega} + \pi X(0) \delta(\omega)$	