

Part 2

a)

tetraMultiple(n)

if (n == 0 or n == 1 or n == 2)

return 0

if (n == 3)

return 1

return (tetraMultiple(n-1) + tetraMultiple(n-2) + tetraMultiple(n-3) + tetraMultiple(n-4))

tetraRecursive(n, a, b, c, d)

if (n == 0)

Return a

If (n == 1)

return b

if (n == 2)

Return c

If (n== 3)

return a + b+ c + d

return tetraRecursive(n-1,a+b+c+d, a, b, c)

tetraLinear(n)

return tetraRecursive(n,0,0,0,1)

c)

Linear:

No branching. Parameters a,b,c,d are incremented and returned upon reaching base case.

Since parameters are incremented with each call, repeated calculations are not a problem.

Algorithm essentially performs $n - 2$ recursive calls, so algorithm is $O(n)$

Multiple:

Branching due to 4 recursive calls each time (if not at base case). Tree-like structure emerges from drawing execution diagram, and it can be seen that 4^n function calls occur at most. So this algorithm is $O(4^n)$. Issue with this algorithm is the repetition of subproblems. Eg. $T(n)$ will call $T(n-1)$, $T(n-2)$, $T(n-3)$ and $T(n-4)$, and these functions will call the other functions again (eg $T(n-1)$ will call $T(n-2)$ again and so on).

