

Chapter 4

The Semiconductor in Equilibrium

Review

Fermi–Dirac distribution

$$f_F(E) = \frac{1}{1 + \exp\left(\frac{E - EF}{kT}\right)}$$

if $E - EF \gg kT$
or $E - EF > 3kT$



Maxwell–Boltzmann approximation

$$f_F(E) = \exp\left(-\frac{E - EF}{kT}\right)$$

- 費米機率（Fermi-Dirac Probability）描述的是費米子（在半導體物理指的是電子）在特定能量下的佔有機率。
- 貹米能階（Fermi Level）是指在費米-狄拉克統計中，
 - 當溫度趨近於絕對零度時，電子的最高佔有能量水平。
 - 當溫度高於絕對零度時，它是所有能量狀態中，佔有機率為50%的那個能量水平。

Outline

4.1 Charge Carriers in Semiconductors

4.2 Dopant Atoms and Energy Levels

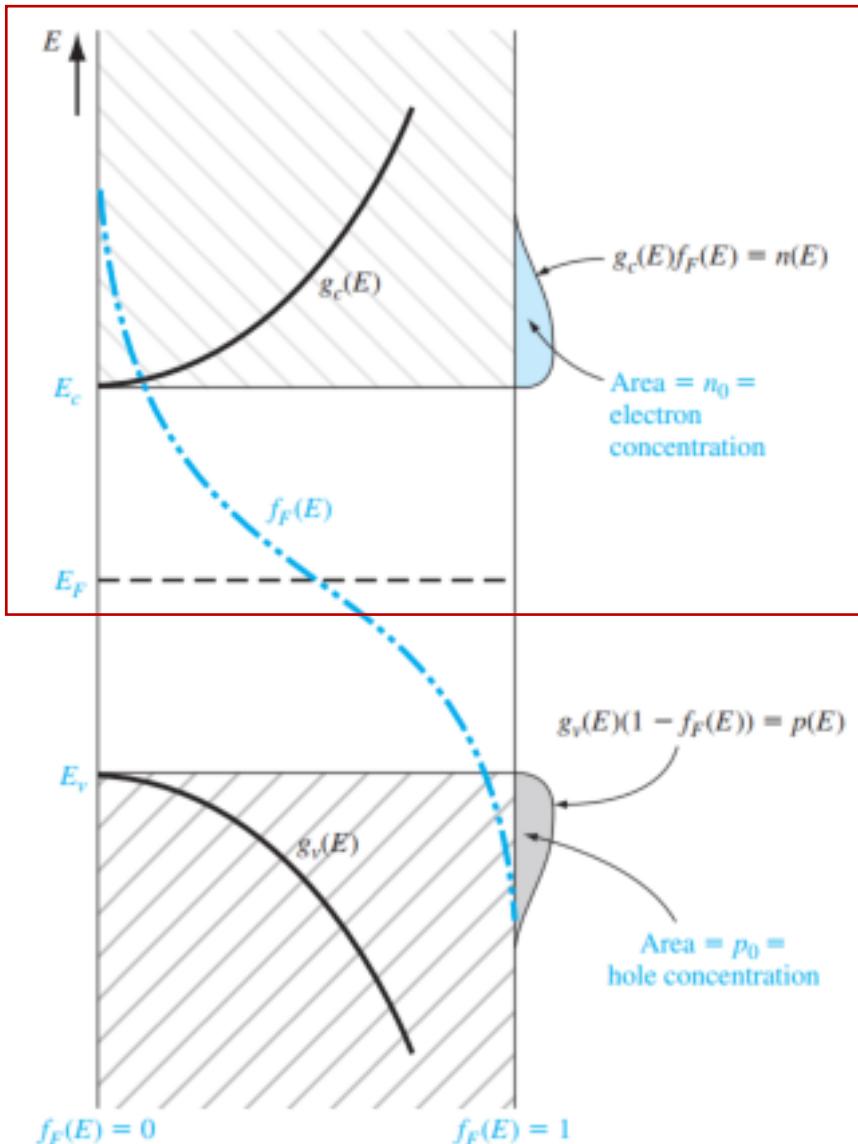
4.3 The Extrinsic Semiconductor

4.4 Statistics of Donors and Acceptors

4.5 Charge Neutrality

4.6 Position of Fermi Energy Level

平衡時電子濃度



Properties of the semiconductor at equilibrium

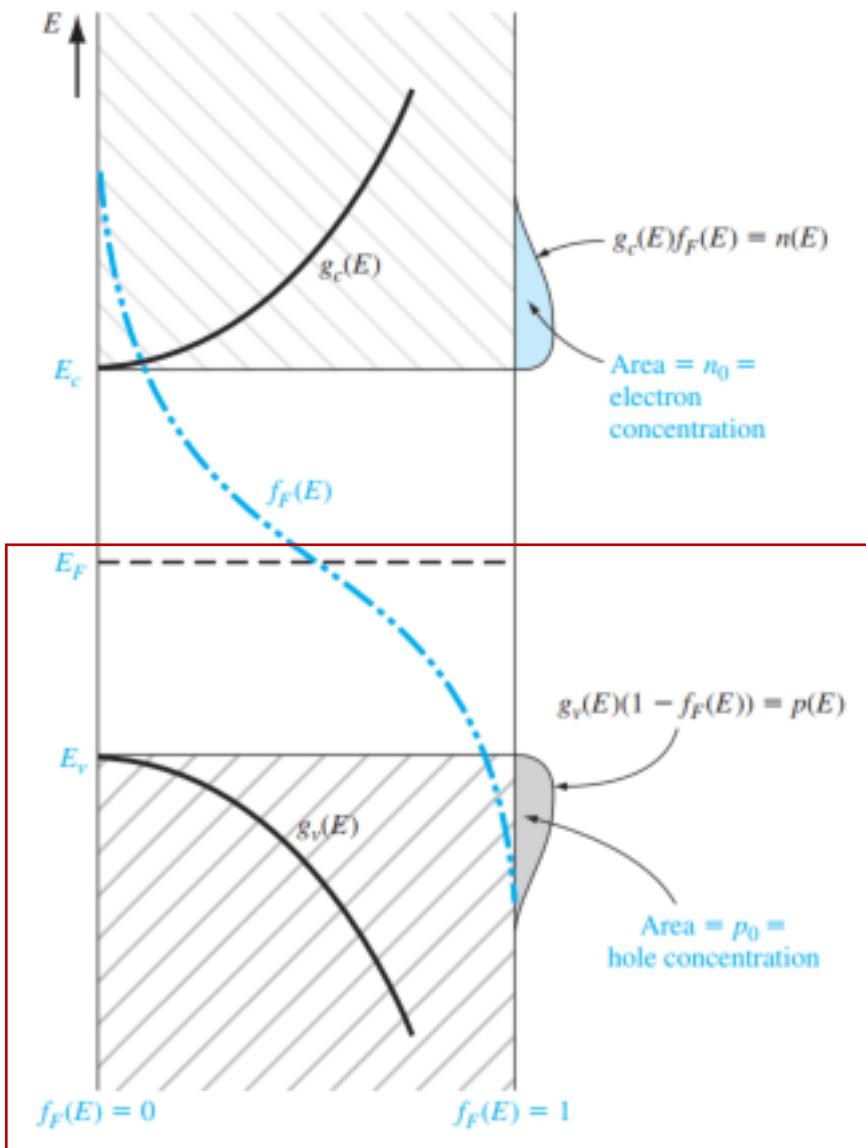
- Zero net energy transfer
- Zero net carrier transfer

$$n(E) = g_c(E) f_F(E)$$

$$n_o = \int_{E_c}^{\infty} g_c(E) f_F(E) dE$$

→ 單位體積中傳導帶電子的數量

平衡時電洞濃度

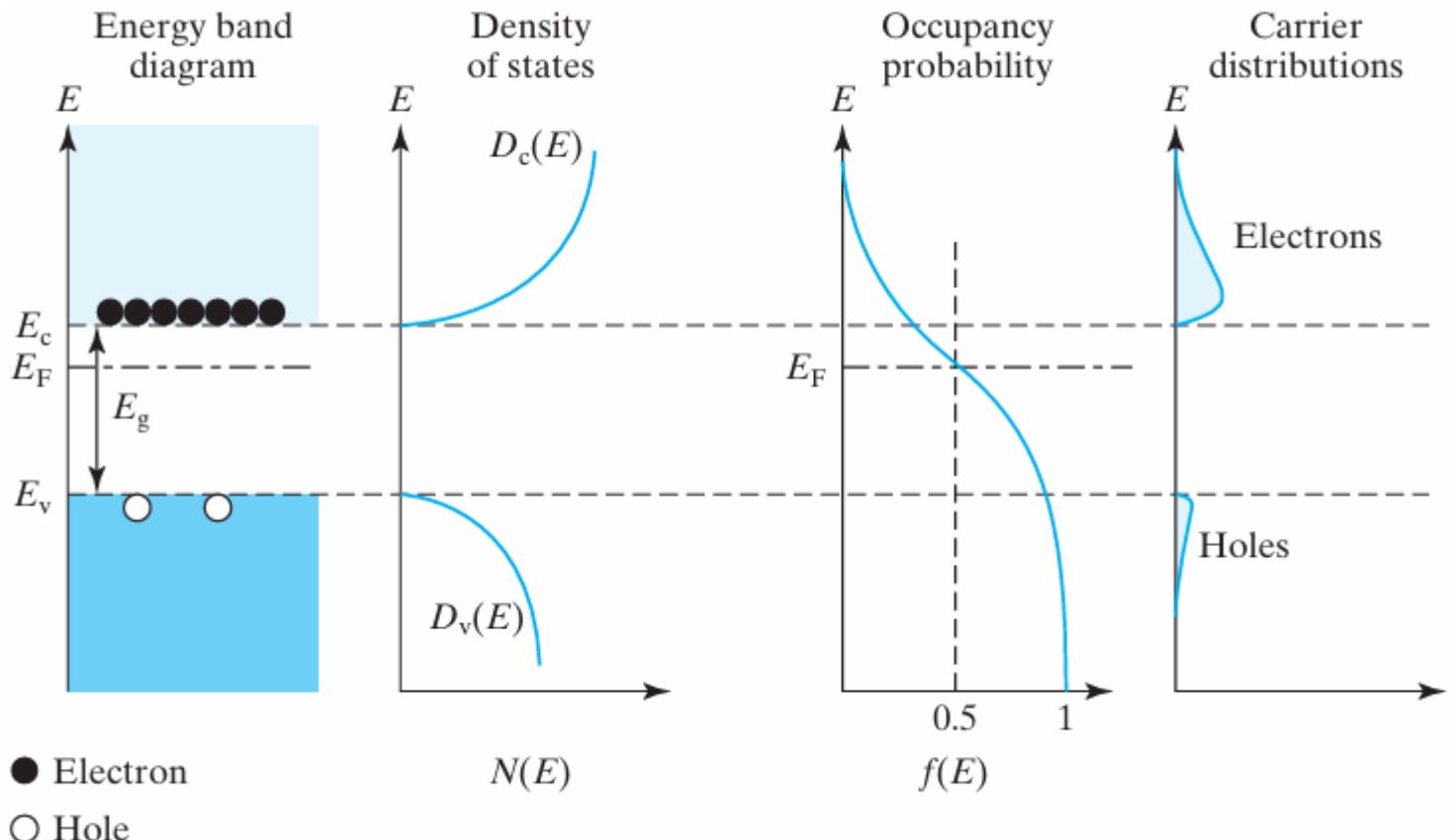


$$p(E) = g_v(E)[1 - f_F(E)]$$

$$p_o = \int_{-\infty}^{E_v} g_v(E)[1 - f_F(E)] dE$$

→ 單位體積中價帶電洞的數量

平衡時載子濃度



$$n_0 = \int_{E_c}^{\infty} n(E) dE = \int_{E_c}^{\infty} g_c(E) f_F(E) dE$$

$$g_c(E) = \frac{4\pi(2m_n^*)^{3/2}}{h^3} \sqrt{E - E_c}$$

$$f_F(E) = -\exp\left(\frac{E - EF}{kT}\right)$$

$$p_0 = \int_{-\infty}^{E_v} p(E) dE = \int_{-\infty}^{E_v} g_v(E) [1 - f_F(E)] dE$$

$$g_v(E) = \frac{4\pi(2m_p^*)^{3/2}}{h^3} \sqrt{E_v - E}$$

$$f_F(E) = -\exp\left(\frac{E - EF}{kT}\right)$$

平衡時電子與電洞濃度

N_c : The effective density of states function in the conduction band.

N_v : The effective density of states function in the valence band.

電子濃度 $n = \frac{2(2\pi m_n^* kT)^{3/2}}{h^3} \exp\left(-\frac{E_c - E_F}{kT}\right) = N_c \exp\left(-\frac{E_c - E_F}{kT}\right)$

電洞濃度 $p = \frac{2(2\pi m_p^* kT)^{3/2}}{h^3} \exp\left(-\frac{E_F - E_v}{kT}\right) = N_v \exp\left(-\frac{E_F - E_v}{kT}\right)$

	$N_c (\text{cm}^{-3})$	$N_v (\text{cm}^{-3})$	m_n^*/m_0	m_p^*/m_0
Silicon	2.8×10^{19}	1.04×10^{19}	1.08	0.56
Gallium arsenide	4.7×10^{17}	7.0×10^{18}	0.067	0.48
Germanium	1.04×10^{19}	6.0×10^{18}	0.55	0.37

	Ge	Si	GaAs
$\mu_n (\text{cm}^2/\text{V}\cdot\text{s})$	3900	1400	8500
$\mu_p (\text{cm}^2/\text{V}\cdot\text{s})$	1900	470	400

Example 4.1

Objective: Calculate the probability that a quantum state in the conduction band at $E = E_c + kT/2$ is occupied by an electron, and calculate the thermal-equilibrium electron concentration in silicon at $T = 300$ K.

Assume the Fermi energy is 0.25 eV below the conduction band. The value of N_c for silicon at $T = 300$ K is $N_c = 2.8 \times 10^{19} \text{ cm}^{-3}$ (see Appendix B).

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$$n = \frac{2(2\pi m_n^* kT)^{3/2}}{h^3} \exp\left(-\frac{E_c - E_F}{kT}\right) = 2.8 \times 10^{19} \exp\left(-\frac{0.25}{0.0259}\right) = 1.8 \times 10^{15} \text{ cm}^{-3}$$

Example 4.2

Objective: Calculate the thermal-equilibrium hole concentration in silicon at $T = 400$ K.

Assume that the Fermi energy is 0.27 eV above the valence-band energy. The value of N_v for silicon at $T = 300$ K is $N_v = 1.04 \times 10^{19} \text{ cm}^{-3}$. (See Appendix B)

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$$p = \frac{2(2\pi m_p^* kT)^{3/2}}{h^3} \exp\left(-\frac{E_F - E_v}{kT}\right) = 1.04 \times 10^{19} \exp\left(-\frac{0.27}{0.0259}\right)$$

$$p = 1.04 \times 10^{19} \times \left(\frac{400}{300}\right)^{3/2} \exp\left[-\frac{0.27}{0.0259(400/300)}\right] = 6.43 \times 10^{15} \text{ cm}^{-3}$$

平衡時載子濃度(未摻雜半導體)

對一本質半導體(intrinsic semiconductor)而言，電子濃度必等於電洞濃度，因為一顆電子跳上去傳導帶，即產生一顆電洞在價帶。

$$\begin{cases} n_i = N_c \exp\left(-\frac{E_c - E_F}{kT}\right) \\ p_i = N_v \exp\left(-\frac{E_F - E_v}{kT}\right) \end{cases}$$

$$E_f = E_{fi}$$

$$E_{fi} \approx \frac{E_c + E_v}{2}$$

Table 4.2 | Commonly accepted values of n_i at $T = 300$ K

Silicon	$n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$
Gallium arsenide	$n_i = 1.8 \times 10^6 \text{ cm}^{-3}$
Germanium	$n_i = 2.4 \times 10^{13} \text{ cm}^{-3}$

$$\left. \begin{array}{l} n_i p_i = N_c N_v \exp(-E_g / kT) \\ n_i^2 = N_c N_v \exp(-E_g / kT) \end{array} \right\} n_0 = ni = p_0 = p_i$$

Example 4.3

Objective: Calculate the intrinsic carrier concentration in silicon at $T = 250$ K and at $T = 400$ K.

The values of N_c and N_v for silicon at $T = 300$ K are $2.8 \times 10^{19} \text{ cm}^{-3}$ and $1.04 \times 10^{19} \text{ cm}^{-3}$, respectively. Both N_c and N_v vary as $T^{3/2}$. Assume the bandgap energy of silicon is 1.12 eV and does not vary over this temperature range.

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The values of N_c and N_v for silicon at $T = 300$ K are $2.8 \times 10^{19} \text{ cm}^{-3}$ and $1.04 \times 10^{19} \text{ cm}^{-3}$, respectively. Both N_c and N_v vary as $T^{3/2}$. Assume the bandgap energy of silicon is 1.12 eV and does not vary over this temperature range.

$$n_i^2 = N_c N_v \exp\left(-\frac{E_g}{kT}\right) \quad N_c, N_v \propto T^{3/2}$$

$$250\text{k} : n_i^2 = 2.8 \times 10^{19} \times 1.04 \times 10^{19} \times \left(\frac{250}{300}\right)^3 \times \exp\left(-\frac{1.12}{0.0259(250/300)}\right) = 4.9 \times 10^{15}$$

$$n_i = 7.0 \times 10^7$$

$$400\text{k} : n_i^2 = 2.8 \times 10^{19} \times 1.04 \times 10^{19} \times \left(\frac{400}{300}\right)^3 \times \exp\left(-\frac{1.12}{0.0259(400/300)}\right) = 5.67 \times 10^{24}$$

$$n_i = 2.38 \times 10^{12}$$

Example

EXAMPLE 1-4 Carrier Concentrations

QUESTION: What is the hole concentration in an N-type semiconductor with 10^{15}cm^{-3} of donors?

SOLUTION: For each ionized donor, an electron is created. Therefore $n = 10^{15}\text{cm}^{-3}$.

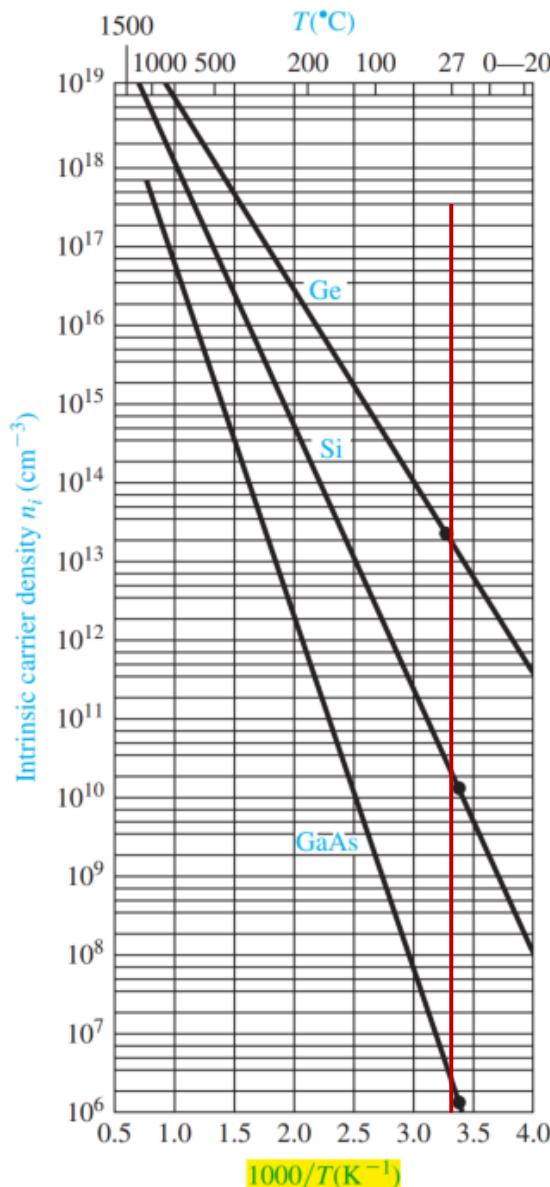
$$p = \frac{n_i^2}{n} \approx \frac{10^{20} \text{ cm}^{-3}}{10^{15} \text{ cm}^{-3}} = 10^5 \text{ cm}^{-3}$$

With a modest temperature increase of 60°C , n remains the same at 10^{15}cm^{-3} , while p increases by about a factor of 2300 because n_i^2 increases according to Eq. (1.8.12).

QUESTION: What is n if $p = 10^{17}\text{cm}^{-3}$ in a P-type silicon wafer?

$$\textbf{SOLUTION: } n = \frac{n_i^2}{p} = \frac{10^{20}}{10^{17}} = 10^3 \text{ cm}^{-3}$$

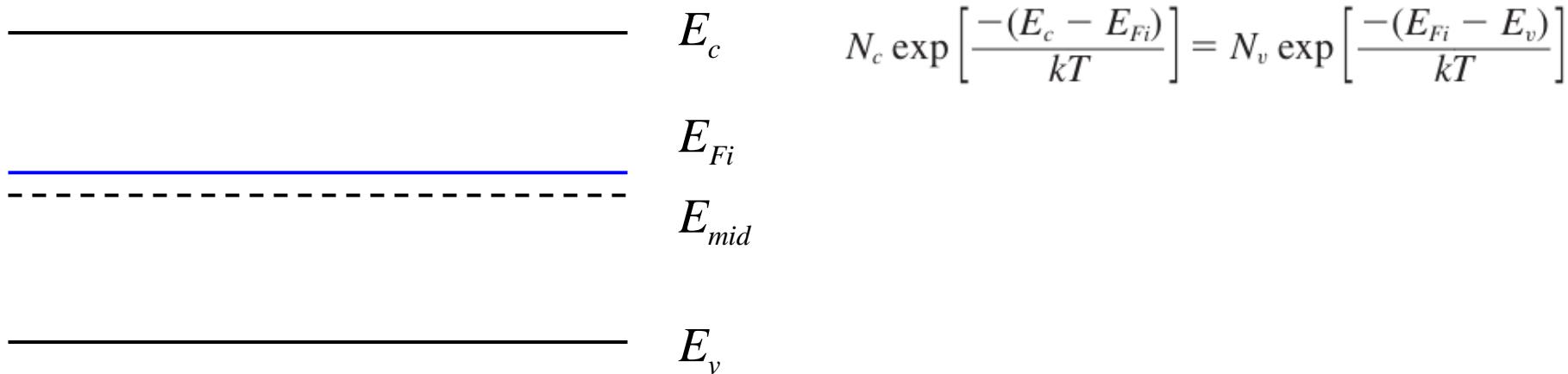
載子濃度與溫度關係 (本質半導體)



$$\frac{1000}{T} = 3.33 \Rightarrow T = 300$$

$$\frac{1000}{T} = 4 \Rightarrow T = 250$$

費米能階位置 (本質半導體)



$$n = p \Rightarrow E_{Fi} - E_{mid} = \frac{1}{2} kT \ln\left(\frac{N_v}{N_c}\right) = \frac{3}{4} kT \ln\left(\frac{m_p^*}{m_n^*}\right)$$

常溫時 E_{Fi} 幾乎位於 E_c 和 E_v 的中央位置

Example 4.4

Objective: Calculate the position of the intrinsic Fermi level with respect to the center of the bandgap in silicon at $T = 300$ K.

The density of states effective carrier masses in silicon are $m_n^* = 1.08m_0$ and $m_p^* = 0.56m_0$.

Example 4.4

Objective: Calculate the position of the intrinsic Fermi level with respect to the center of the bandgap in silicon at $T = 300$ K.

The density of states effective carrier masses in silicon are $m_n^* = 1.08m_0$ and $m_p^* = 0.56m_0$.

$$E_{Fi} - E_{\text{midgap}} = \frac{3}{4} kT \ln\left(\frac{m_p^*}{m_n^*}\right) = \frac{3}{4} (0.0259) \ln\left(\frac{0.56}{1.08}\right)$$

$$E_{Fi} - E_{\text{midgap}} = -0.0128 \text{ eV} = -12.8 \text{ meV}$$

Example

EXAMPLE 1-3 Finding the Fermi Level in Si

Where is E_F located in the energy band of silicon, at 300K with $n = 10^{17}\text{cm}^{-3}$? And for $p = 10^{14}\text{cm}^{-3}$?

SOLUTION: From Eq. (1.8.5)

$$E_c - E_F = kT \cdot \ln(N_c/n) \\ = 0.026 \ln(2.8 \times 10^{19}/10^{17}) \\ \equiv 0.146 \text{ eV}$$

Therefore, E_F is located at 146 meV below E_c , as shown in Fig. 1-22a.

For $p = 10^{14} \text{ cm}^{-3}$, from Eq. (1.8.8),

$$E_F - E_v = kT \cdot \ln(N_v/p) \\ = 0.026 \ln(1.04 \times 10^{19}/10^{14}) \\ \equiv 0.31 \text{ eV}$$

Therefore E_F is located at 0.31 eV above E_v .

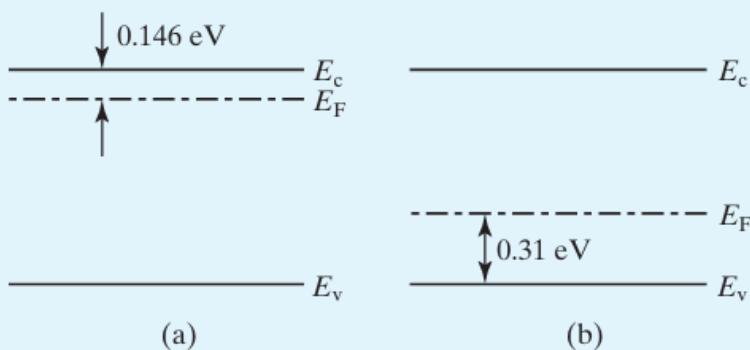
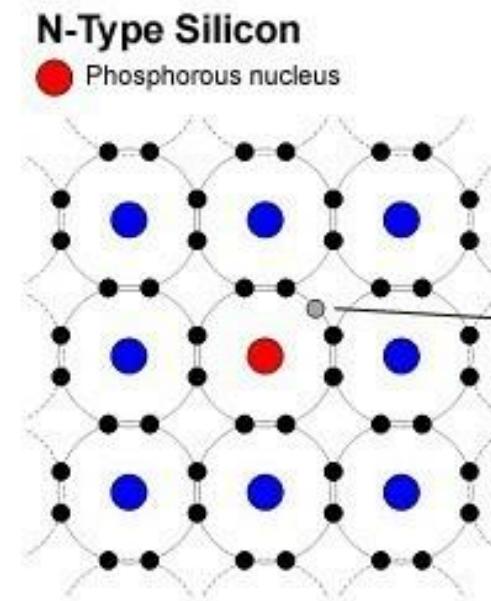
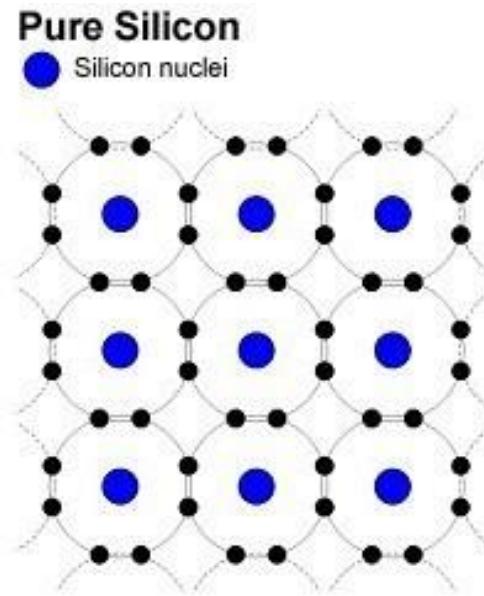


FIGURE 1-22 Location of E_F when $n = 10^{17} \text{ cm}^{-3}$ (a), and $p = 10^{14} \text{ cm}^{-3}$ (b).

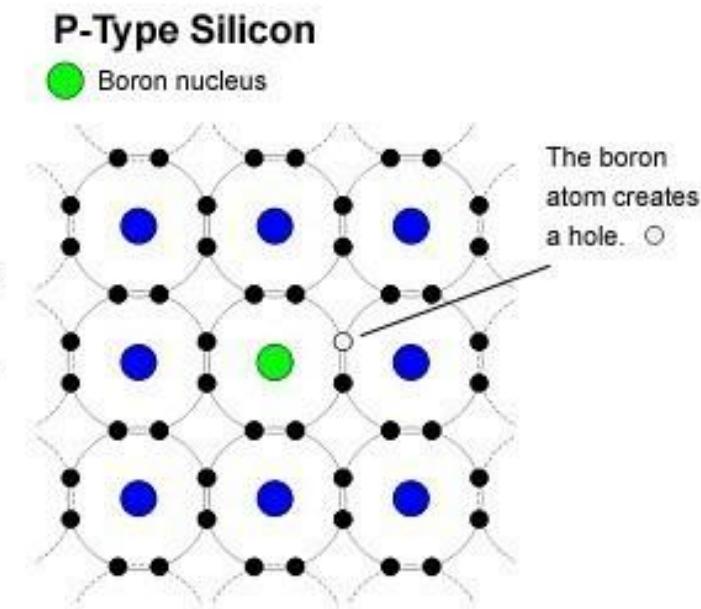
異質半導體(摻雜)

An extrinsic semiconductor:

A semiconductor in which controlled amounts of specific **dopant** or **impurity atoms** have been added so that **the thermal-equilibrium electron and hole concentrations are different from the intrinsic carrier concentration.**



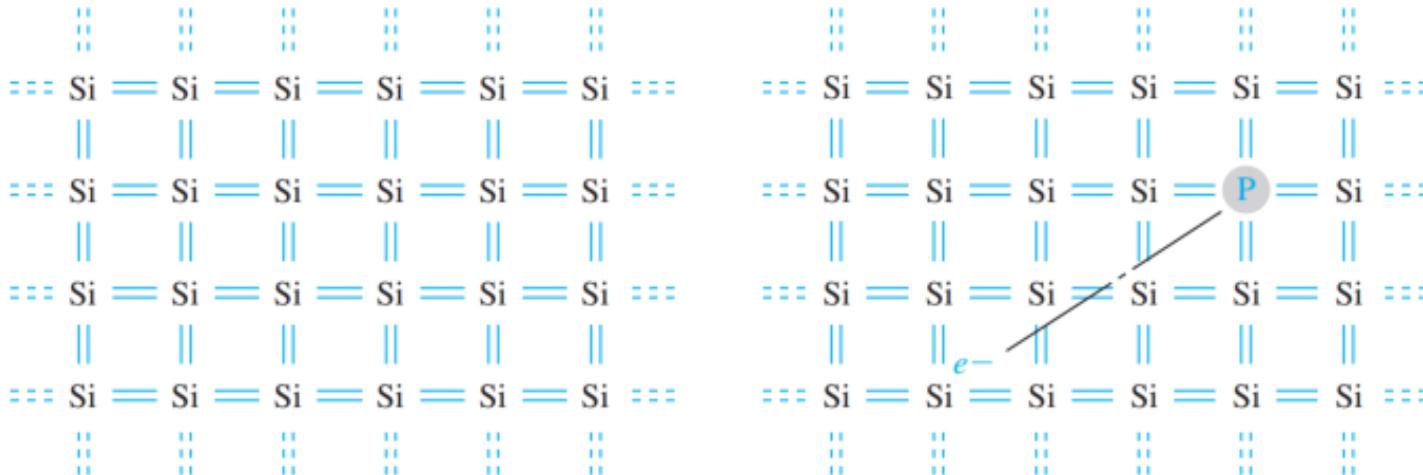
The phosphorous atom creates an extra electron.



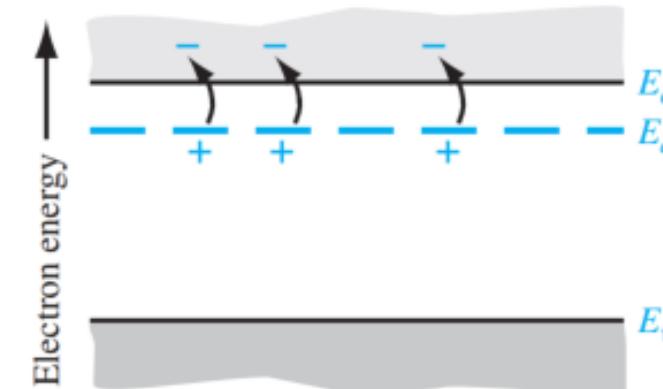
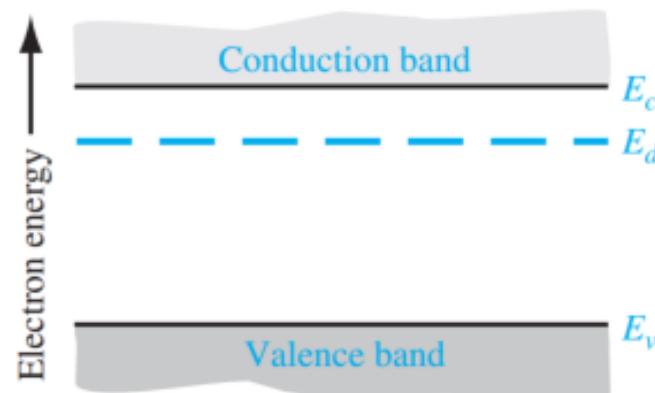
The boron atom creates a hole.

Qualitative Description for Donor

The atom donates an electron to the CB is called a donor impurity atom.

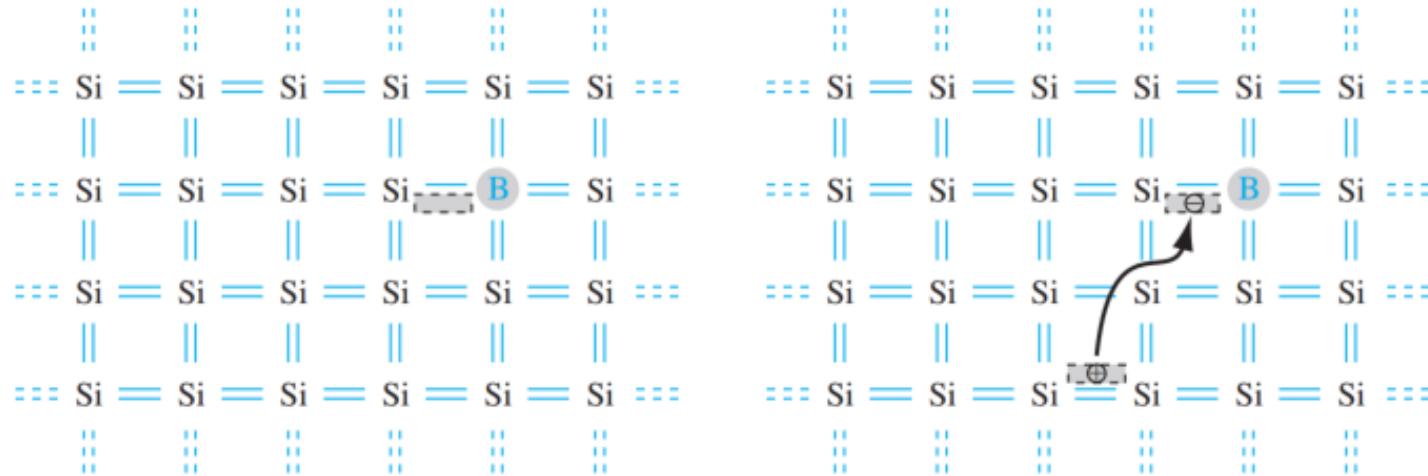


Donor energy level

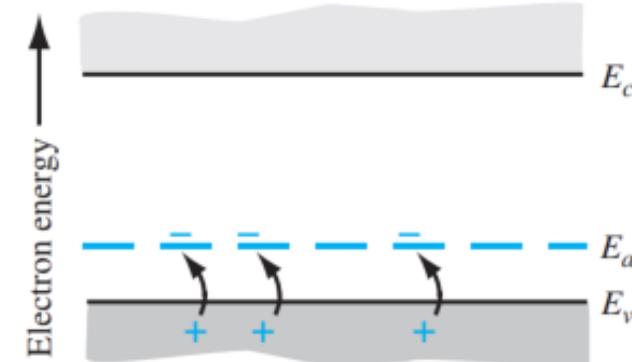
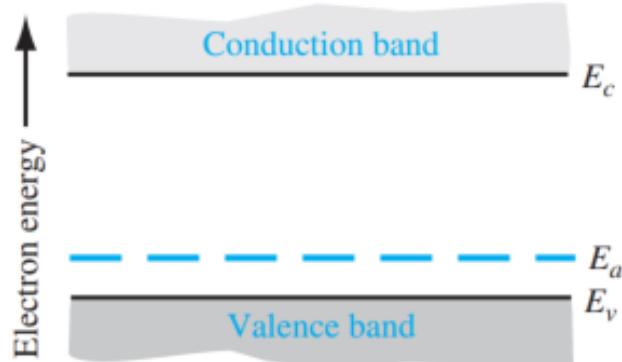


Qualitative Description for Acceptor

The atom accepts an electron from the VB is called an acceptor impurity atom.



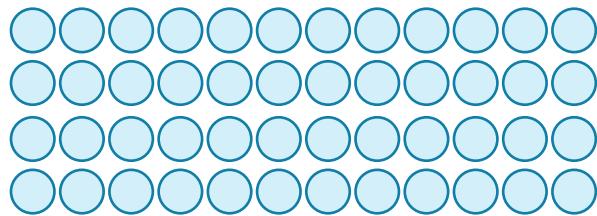
Acceptor energy level



摻雜濃度

Intrinsic semiconductor

本質半導體、無摻雜半導體

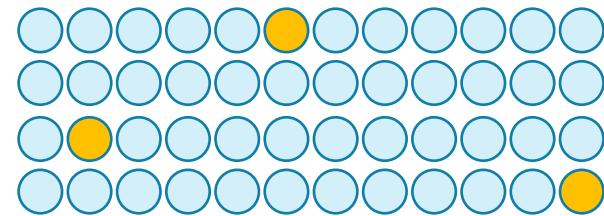


矽濃度: $\sim 10^{22}$ (cm^{-3})

電子濃度: $\sim 10^{12}$ (cm^{-3})

Extrinsic semiconductor

異質半導體、摻雜半導體

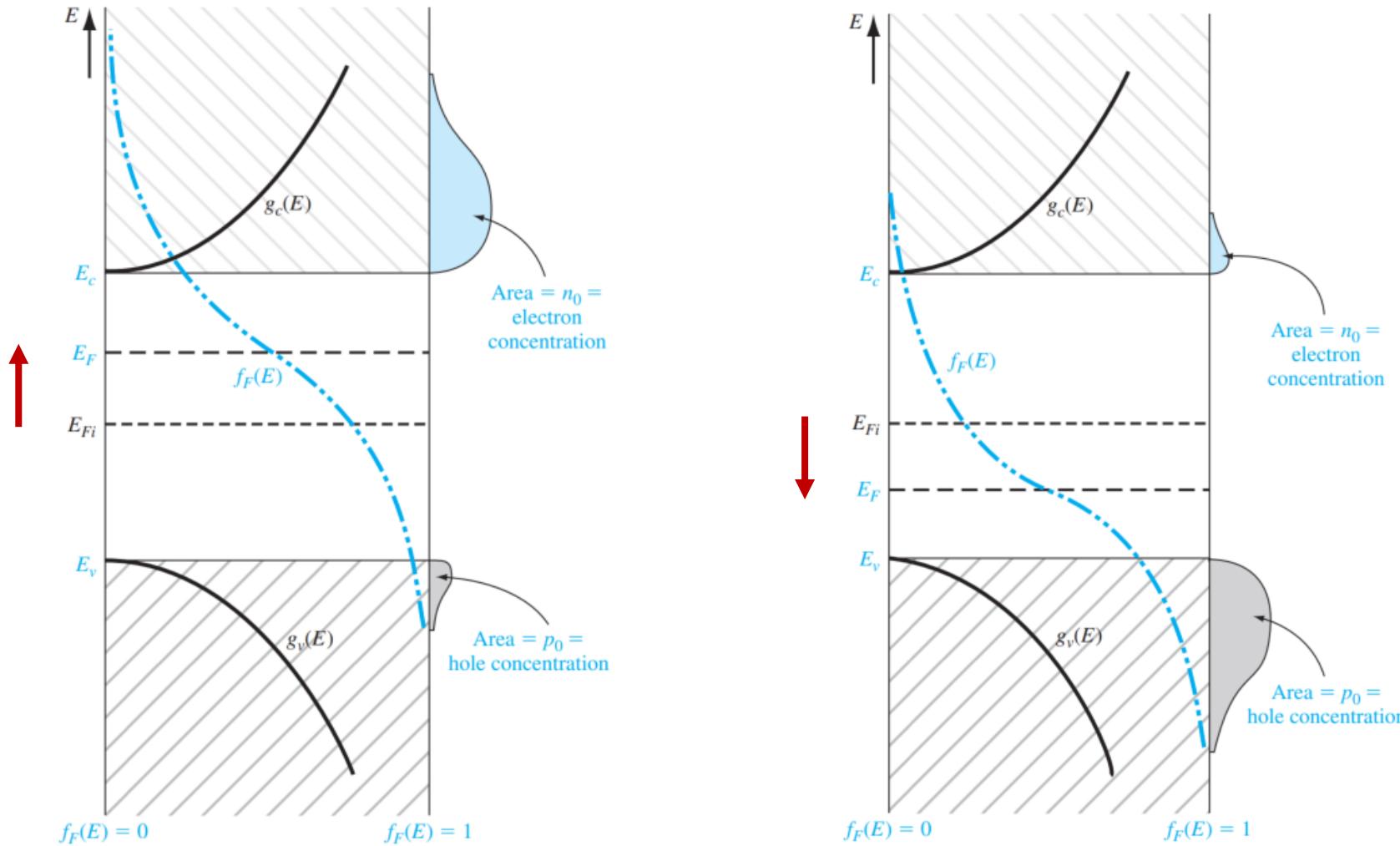


輕度摻雜: $10^{15}\text{-}10^{18}$ (cm^{-3})

重度摻雜: $>10^{19}$ (cm^{-3})

平衡時載子濃度(摻雜半導體)

摻雜會改變費米能階的位置



平衡時載子濃度(輕度摻雜半導體)

對輕度摻雜之半導體，公式依然適用

形式1

$$n_o = N_c \exp\left(-\frac{E_c - E_F}{kT}\right)$$

形式2

$$n_o = n_i \exp\left(\frac{E_F - E_{Fi}}{kT}\right)$$

$$p_o = N_v \exp\left(-\frac{E_F - E_v}{kT}\right)$$

$$p_o = p_i \exp\left(-\frac{E_F - E_{Fi}}{kT}\right)$$

$$n_o p_o = n_i p_i = n_i^2 \quad \text{但} \quad n_o \neq p_o$$

Example 4.5

Objective: Calculate the thermal equilibrium concentrations of electrons and holes for a given Fermi energy.

Consider silicon at $T = 300$ K so that $N_c = 2.8 \times 10^{19} \text{ cm}^{-3}$ and $N_v = 1.04 \times 10^{19} \text{ cm}^{-3}$. Assume that the Fermi energy is 0.25 eV below the conduction band. If we assume that the bandgap energy of silicon is 1.12 eV, then the Fermi energy will be 0.87 eV above the valence band.

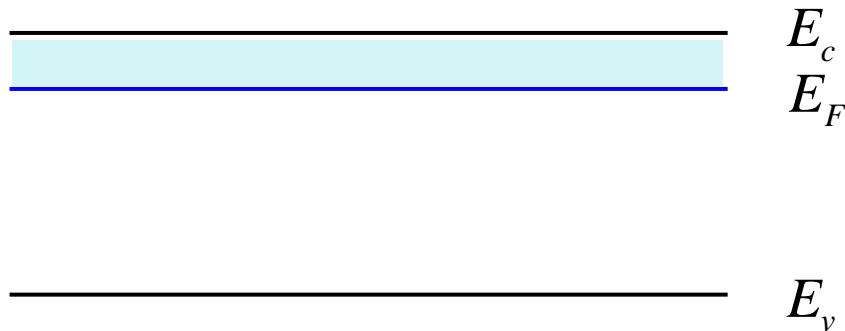
$$n_o = N_c \exp\left(-\frac{E_c - E_F}{kT}\right) = 2.8 \times 10^{19} \exp\left(-\frac{0.25}{0.0259}\right) = 1.8 \times 10^{15}$$

$$p_o = N_v \exp\left(-\frac{E_F - E_v}{kT}\right) = 1.04 \times 10^{19} \exp\left(-\frac{0.87}{0.0259}\right) = 2.7 \times 10^4$$

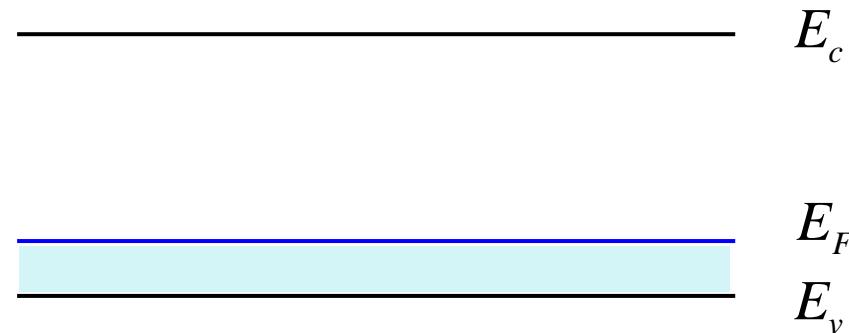
公式適用範圍

以能帶的角度來看：

$$E_c - E_F > 3kT$$



$$E_F - E_v > 3kT$$

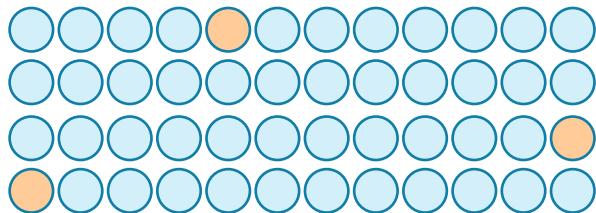


費米能階不可以太靠近導帶，
否則公式失效。

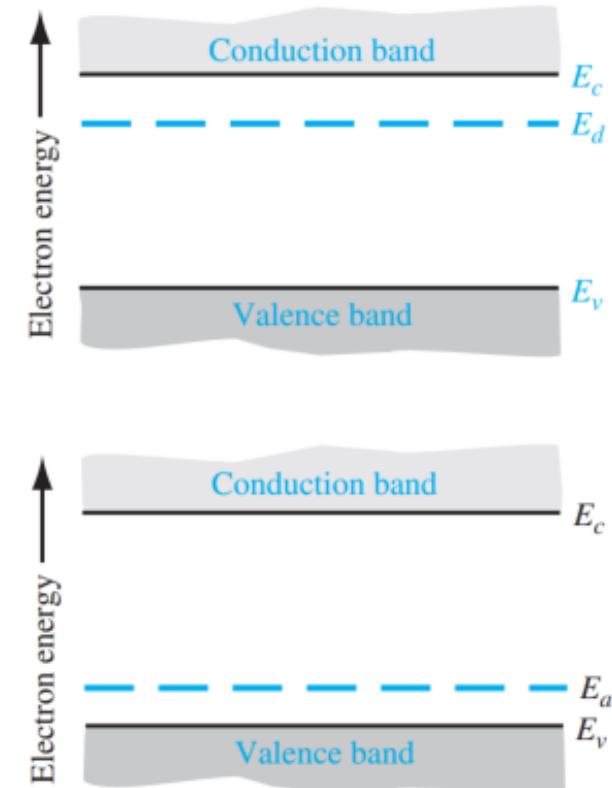
費米能階不可以太靠近價帶，
否則公式失效。

Nondegenerate Semiconductors

If the doping level is **low**, the dopant atoms are spread far enough apart so that there is no interaction between donor electrons or acceptor holes.

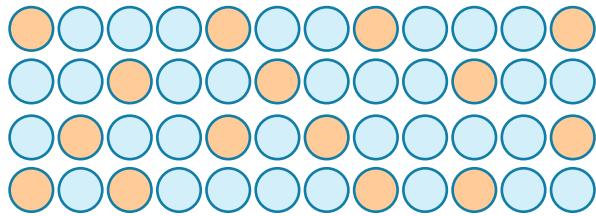


參雜濃度低
雜質原子距離很遠
可忽略交互作用
波函數不重疊
不形成能帶
 $E_c - E_F > 3kT$ 法則仍適用



Degenerate Semiconductors

If the doping level is **high**, the dopant atoms are close enough so that the donor electron or acceptor holes will begin to interact, and an impurity energy band will be formed.



參雜濃度高

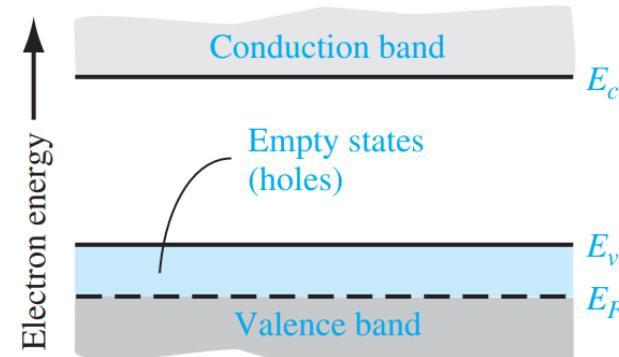
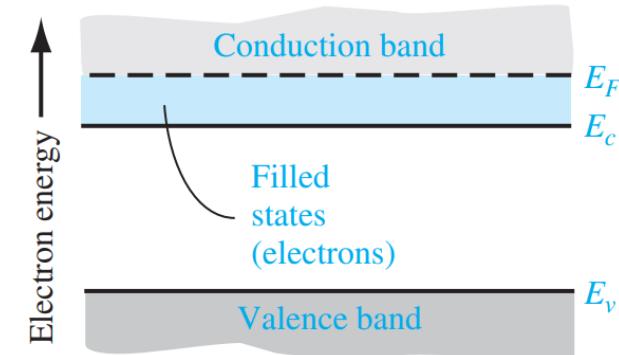
雜質原子距離很近

不可忽略交互作用

波函數重疊

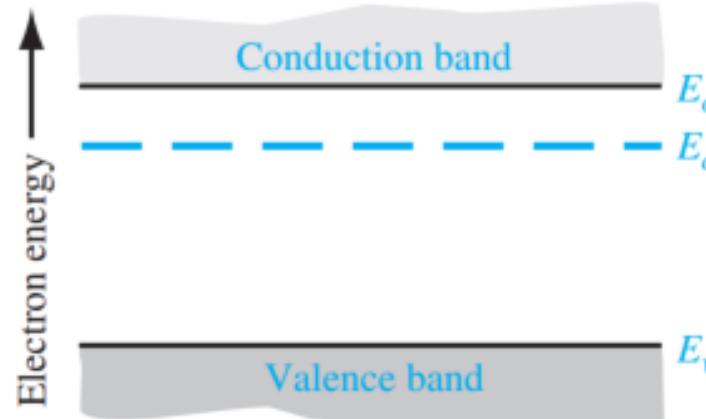
形成能帶

$E_c - E_F < 3kT$ 法則不適用



離子化 Ionization

$$f_F(E) = \frac{1}{1 + \exp\left(\frac{E - E_f}{kT}\right)}$$

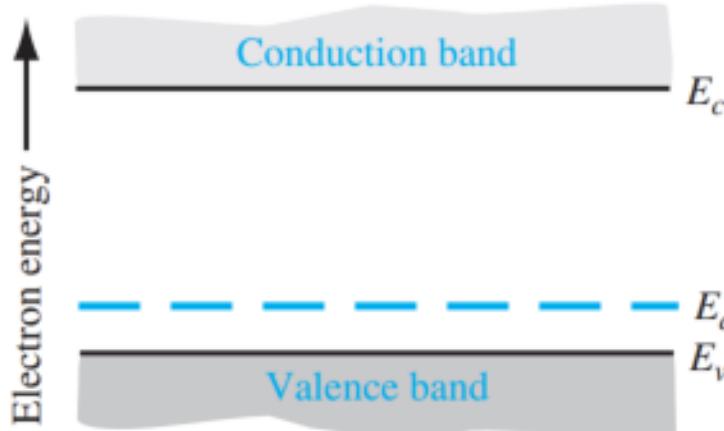


未離子化濃度

donor 摻雜濃度

$$\frac{n_d}{N_d} = \frac{1}{1 + \frac{1}{2} \exp\left(\frac{E_d - E_F}{kT}\right)}$$

$$n_d = N_d - N_d^+$$



未離子化濃度

Acceptor 摻雜濃度

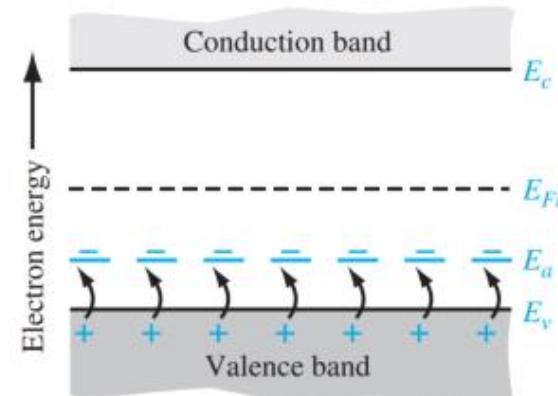
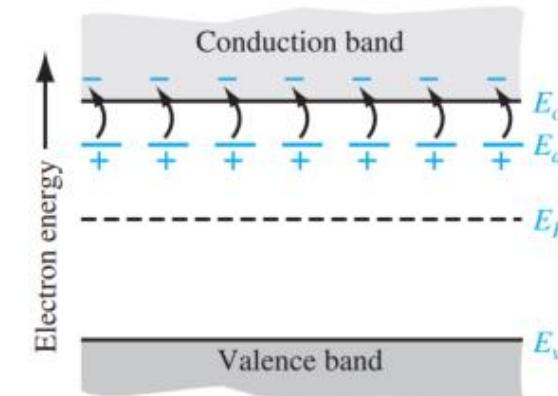
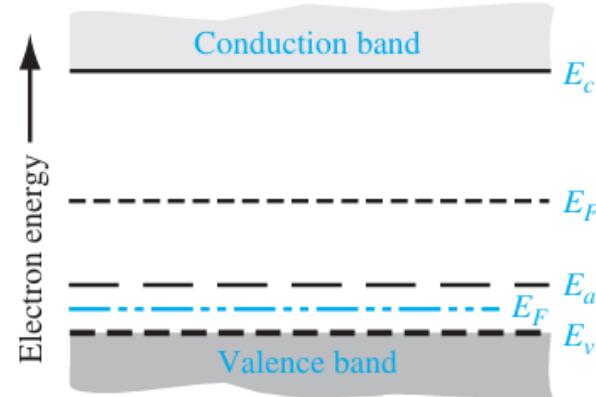
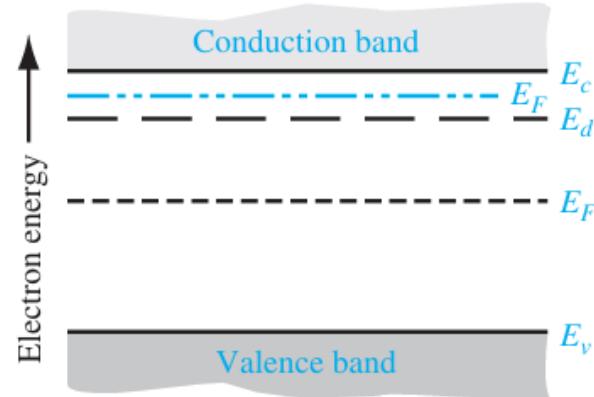
$$\frac{p_a}{N_a} = \frac{1}{1 + \frac{1}{4} \exp\left(\frac{E_F - E_a}{kT}\right)}$$

$$p_a = N_a - N_a^-$$

離子化與溫度變化

絕對溫度 K	攝氏溫度 °C	游離率
50	-223	4%
100	-173	88.4%
200	-73	99%
300	23	99.6%

幾乎全部游離

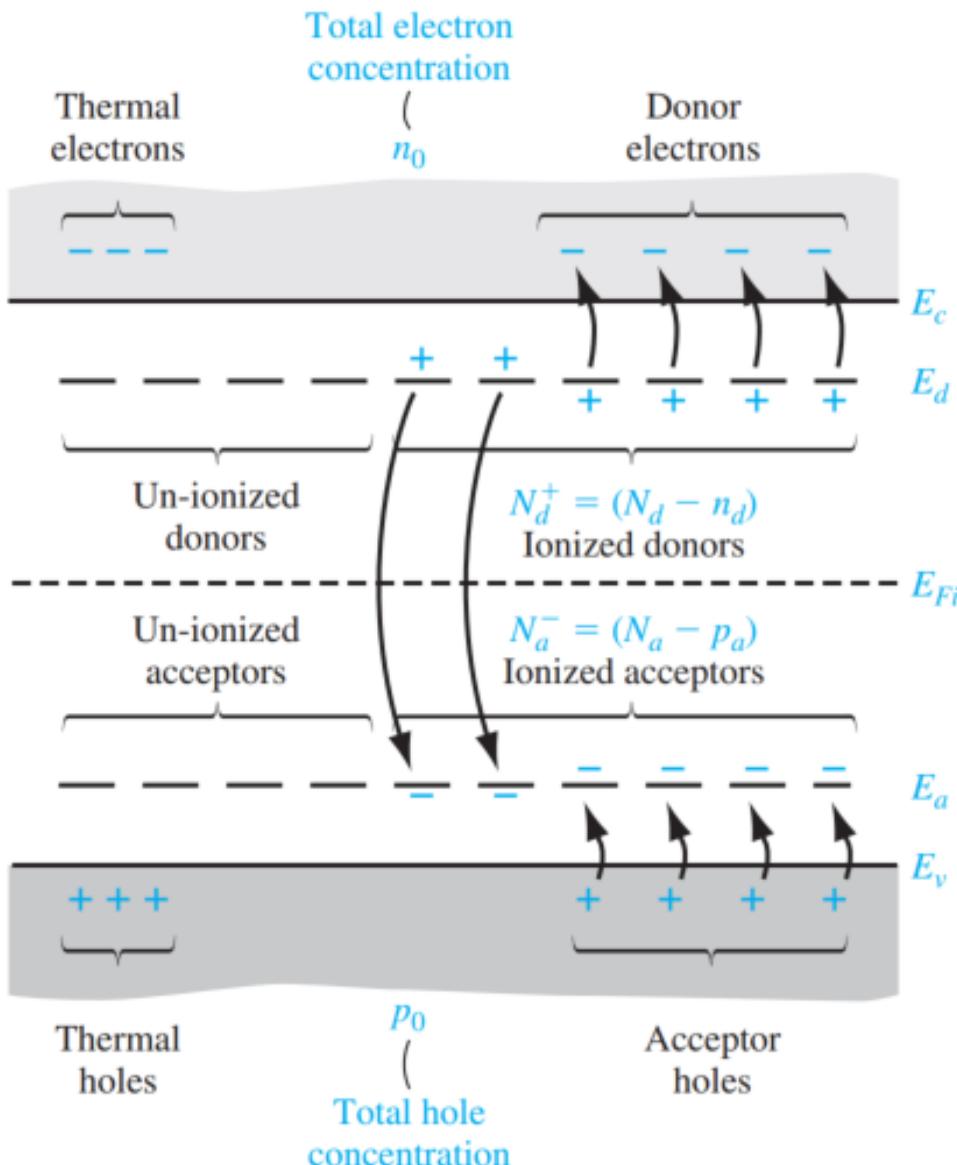


互補半導體 Compensated Semiconductor

在同一區域內同時摻雜了 donor 和 acceptor.

- n-type compensated semiconductor $N_d > N_a$
- p-type compensated semiconductor $N_d < N_a$
- Completely compensated semiconductor $N_d = N_a$

電中性原理



整塊材料的淨電荷量必須是零

$$n_0 + N_a^- = p_0 + N_d^+$$

$$n_0 + (N_a - p_a) = p_0 + (N_d - n_d)$$

假設完全游離 $\Rightarrow n_d \approx 0, p_a \approx 0$

$$n_0 + N_a = p_0 + N_d$$

$$n_0 + N_a = \frac{n_i^2}{n_0} + N_d$$

$$n_0^2 - (N_d - N_a)n_0 - n_i^2 = 0$$

電中性原理

傳導帶電子

$$n_0 = \frac{N_d - N_a}{2} + \sqrt{\left(\frac{N_d - N_a}{2}\right)^2 + n_i^2}$$

價帶電洞

$$p_0 = \frac{N_a - N_d}{2} + \sqrt{\left(\frac{N_a - N_d}{2}\right)^2 + n_i^2}$$

公式解：

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Silicon	$n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$
Gallium arsenide	$n_i = 1.8 \times 10^6 \text{ cm}^{-3}$
Germanium	$n_i = 2.4 \times 10^{13} \text{ cm}^{-3}$

Example 4.9

Objective: Determine the thermal-equilibrium electron and hole concentrations in silicon at $T = 300$ K for given doping concentrations. (a) Let $N_d = 10^{16} \text{ cm}^{-3}$ and $N_a = 0$. (b) Let $N_d = 5 \times 10^{15} \text{ cm}^{-3}$ and $N_a = 2 \times 10^{15} \text{ cm}^{-3}$.

Recall that $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ in silicon at $T = 300$ K.

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Recall that $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$ in silicon at $T = 300$ K.

$$n_0 = \frac{N_d - N_a}{2} + \sqrt{\left(\frac{N_d - N_a}{2}\right)^2 + n_i^2} = \frac{10^{16}}{2} + \sqrt{\left(\frac{10^{16}}{2}\right)^2 + (1.5 \times 10^{10})^2} \approx 10^{16}$$

$$p_0 = \frac{n_i^2}{n_0} = \frac{(1.5 \times 10^{10})^2}{10^{16}} = 2.25 \times 10^4$$

Example 4.10

Objective: Calculate the thermal-equilibrium electron and hole concentrations in germanium for a given doping concentration.

Consider a germanium sample at $T = 300$ K in which $N_d = 2 \times 10^{14} \text{ cm}^{-3}$ and $N_a = 0$. Assume that $n_i = 2.4 \times 10^{13} \text{ cm}^{-3}$.

Example 4.10

Objective: Calculate the thermal-equilibrium electron and hole concentrations in germanium for a given doping concentration.

Consider a germanium sample at $T = 300$ K in which $N_d = 2 \times 10^{14} \text{ cm}^{-3}$ and $N_a = 0$. Assume that $n_i = 2.4 \times 10^{13} \text{ cm}^{-3}$.

$$n_0 = \frac{2 \times 10^{14}}{2} + \sqrt{\left(\frac{2 \times 10^{14}}{2}\right)^2 + (2.4 \times 10^{13})^2} \approx 2.028 \times 10^{14}$$

$$p_0 = \frac{n_i^2}{n_0} = \frac{(2.4 \times 10^{13})^2}{2.028 \times 10^{14}} = 2.84 \times 10^{12}$$

Example 4.11

Objective: Calculate the thermal-equilibrium electron and hole concentrations in a compensated p-type semiconductor.

Consider a silicon semiconductor at $T = 300$ K in which $N_a = 10^{16} \text{ cm}^{-3}$ and $N_d = 3 \times 10^{15} \text{ cm}^{-3}$. Assume $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$.

Example 4.11

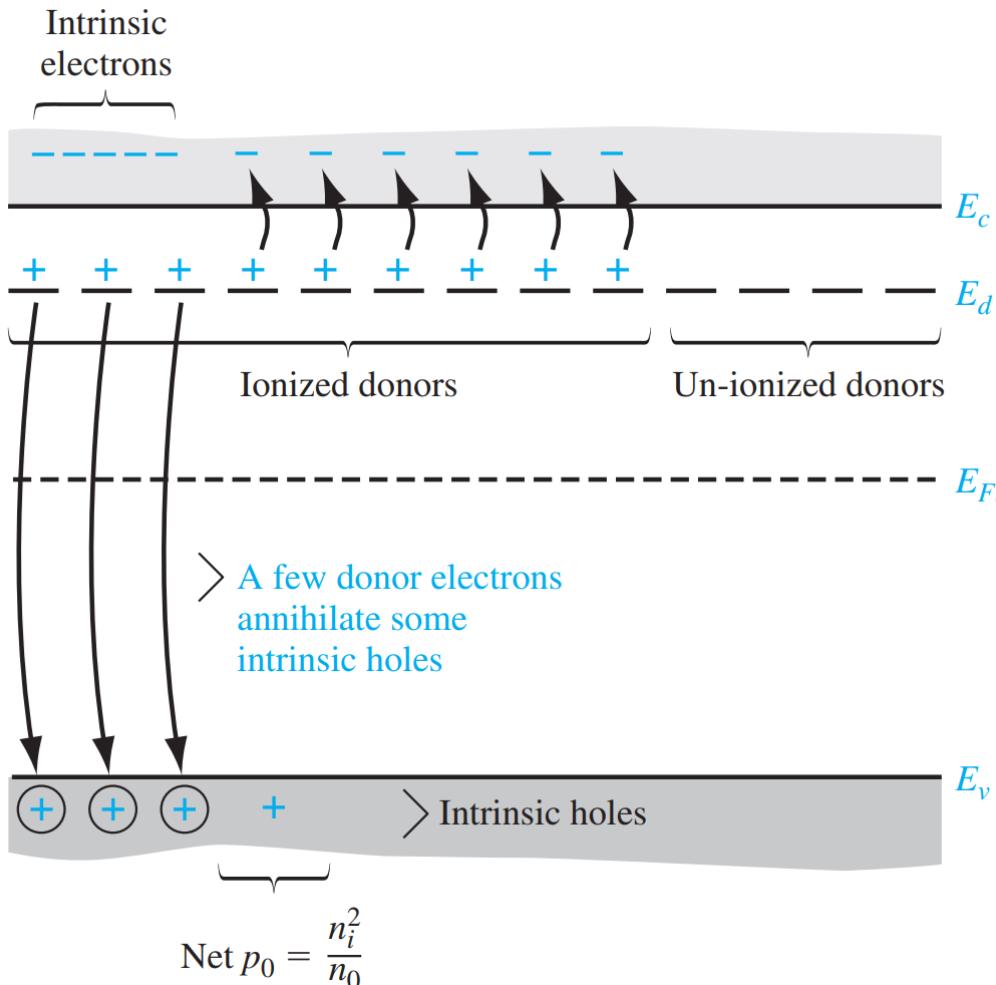
Objective: Calculate the thermal-equilibrium electron and hole concentrations in a compensated p-type semiconductor.

Consider a silicon semiconductor at $T = 300$ K in which $N_a = 10^{16} \text{ cm}^{-3}$ and $N_d = 3 \times 10^{15} \text{ cm}^{-3}$. Assume $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$.

$$p_0 = \frac{N_a - N_d}{2} + \sqrt{\left(\frac{N_a - N_d}{2}\right)^2 + n_i^2} = \frac{7 \times 10^{15}}{2} + \sqrt{\left(\frac{7 \times 10^{15}}{2}\right)^2 + (1.5 \times 10^{10})^2} \approx 7 \times 10^{15}$$

$$n_0 = \frac{n_i^2}{p_0} = \frac{(1.5 \times 10^{10})^2}{7 \times 10^{15}} = 3.21 \times 10^4$$

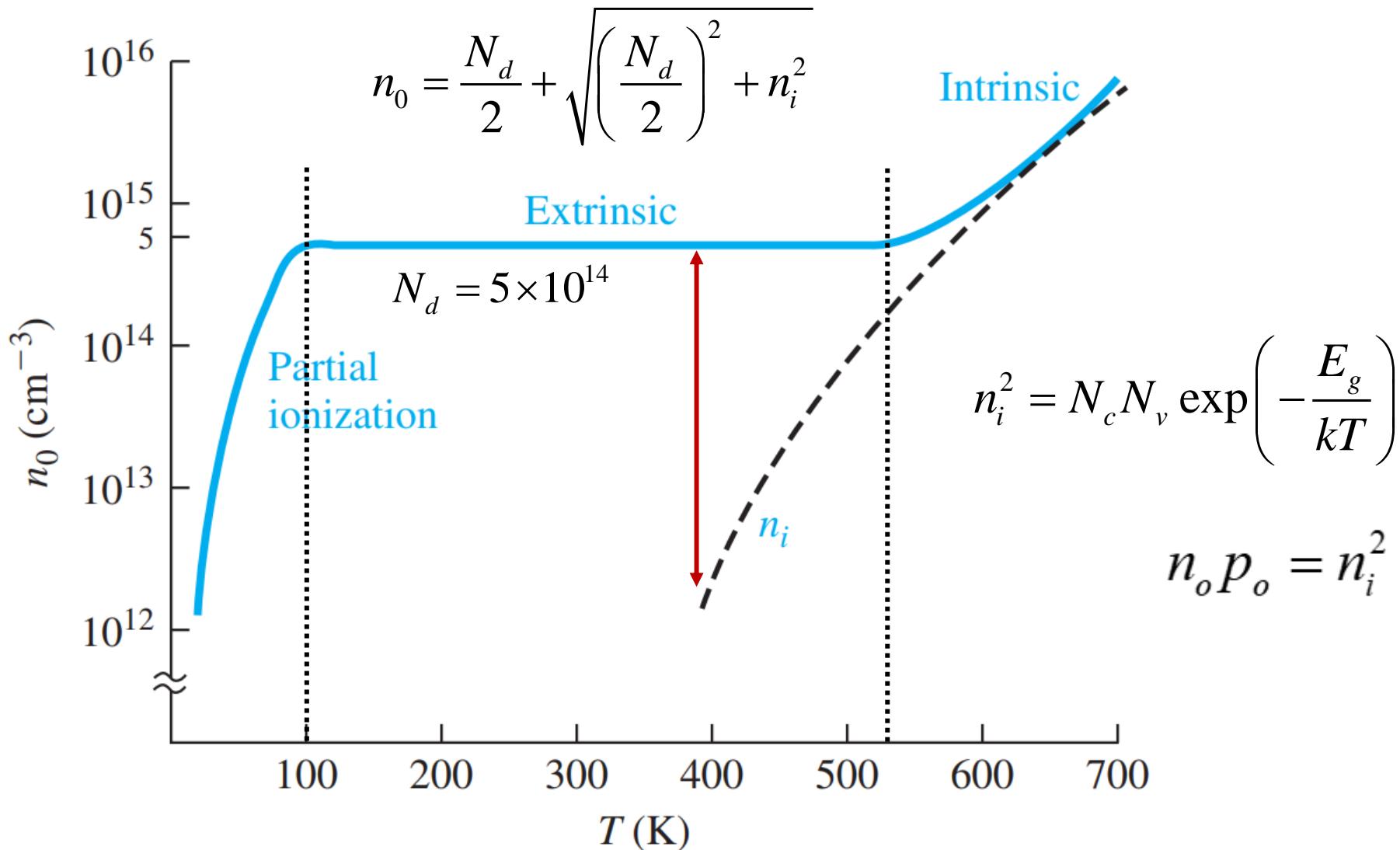
載子重新分布 Redistribution



- 傳導帶電子因N型摻雜而增加。
- 價帶電洞因N型摻雜而減少
- 因大部分電子跳上傳導帶，少部分跳到價帶並填入電洞

$$n_o p_o = n_i^2 \Rightarrow p_o = \frac{n_i^2}{n_o}$$

載子濃度與溫度關係 (n-type uncompensated)



載子濃度與溫度關係

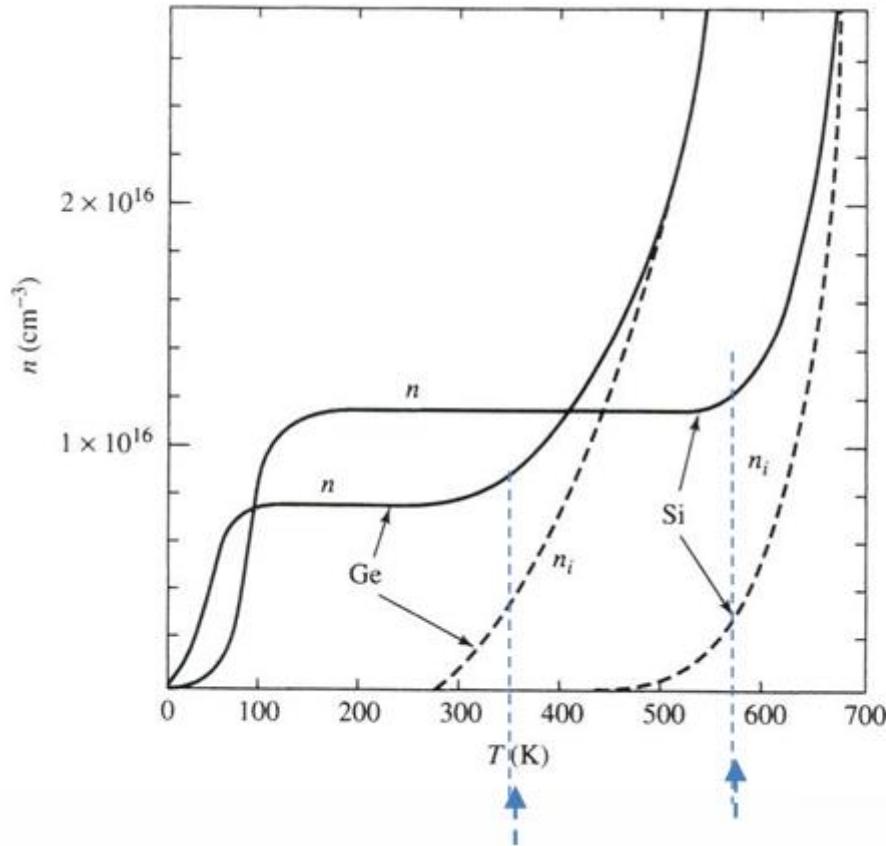
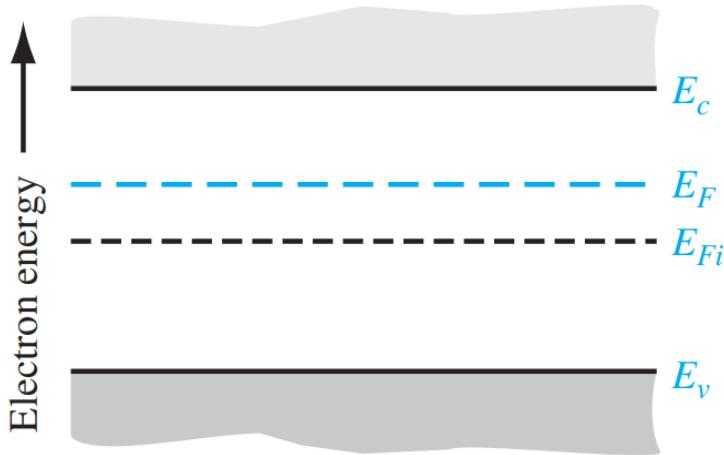
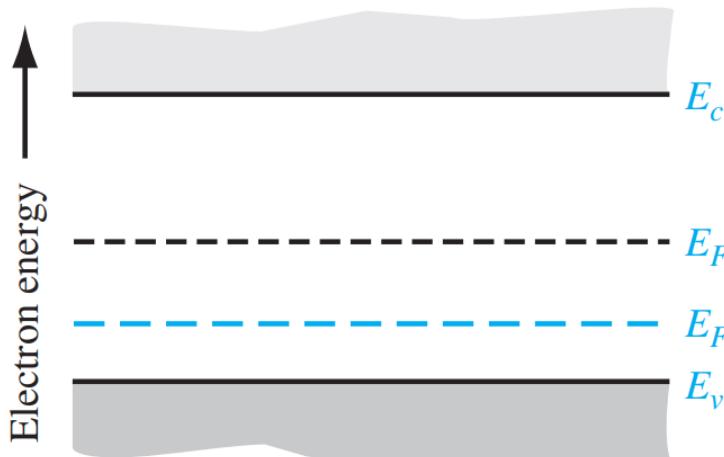


FIGURE 1.9 Electron concentration versus temperature for two n -type doped semiconductors: (a) Silicon doped with 1.15×10^{16} arsenic atoms cm^{-3} [1], (b) Germanium doped with 7.5×10^{15} arsenic atoms cm^{-3} [2].

費米能階位置 (輕度摻雜和完全游離)

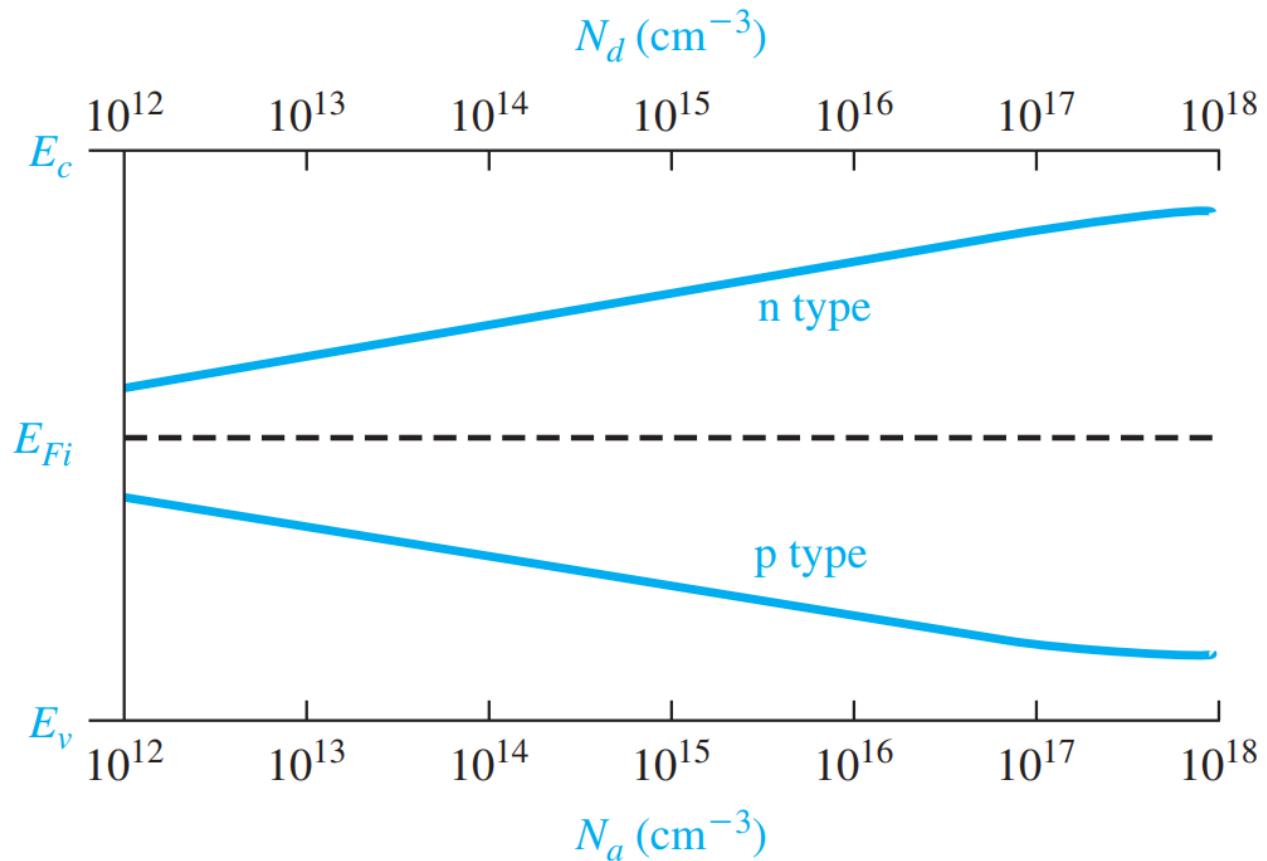


$$\left\{ \begin{array}{l} E_c - E_F \approx kT \ln \left(\frac{N_c}{N_d} \right) \\ E_F - E_{Fi} \approx kT \ln \left(\frac{N_d}{n_i} \right) \end{array} \right.$$



$$\left\{ \begin{array}{l} E_F - E_v \approx kT \ln \left(\frac{N_v}{N_a} \right) \\ E_{Fi} - E_F \approx kT \ln \left(\frac{N_a}{p_i} \right) \end{array} \right.$$

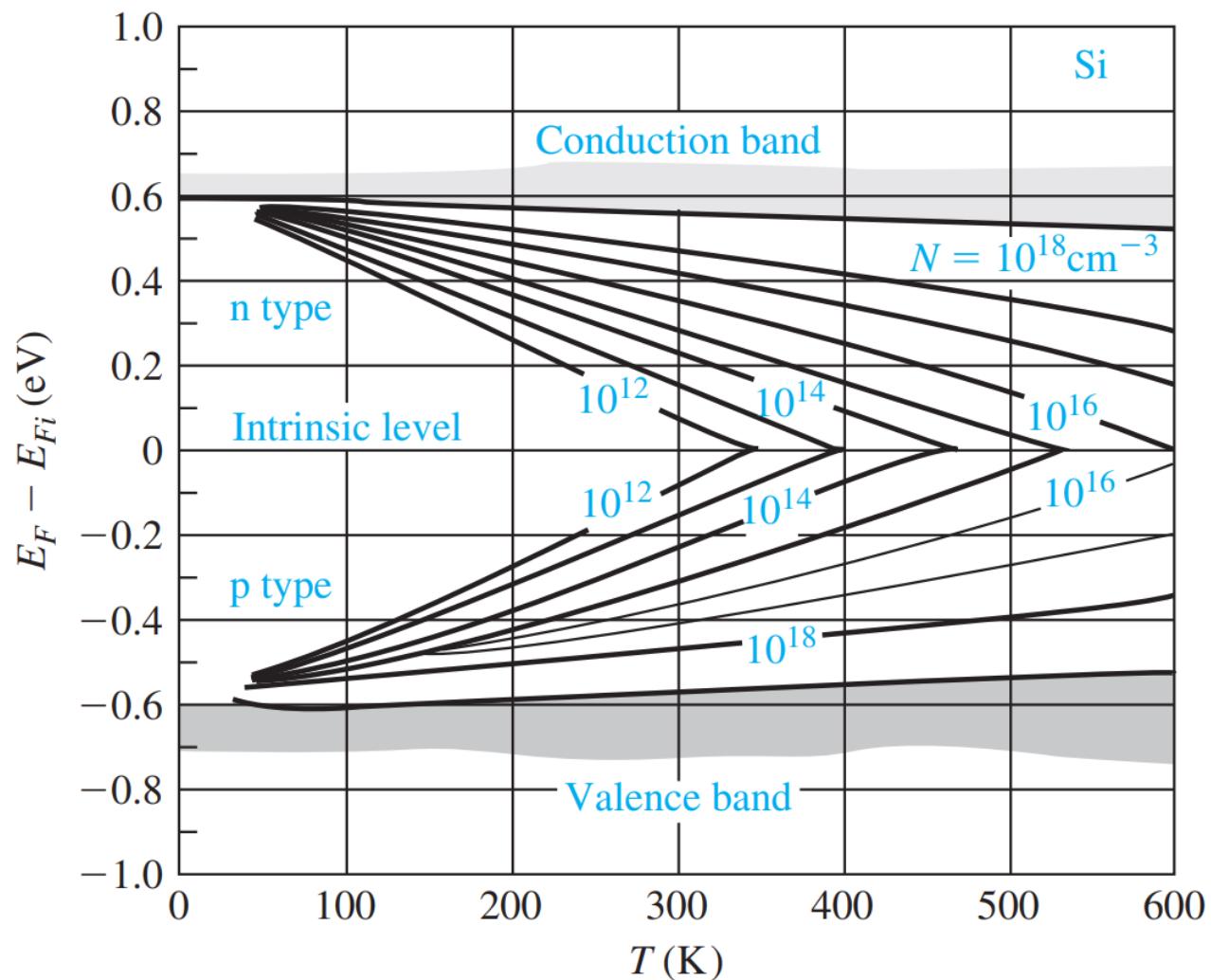
費米能階位置與摻雜濃度之關係



$$E_F - E_{Fi} = kT \ln\left(\frac{N_d}{n_i}\right)$$

$$E_{Fi} - E_F = kT \ln\left(\frac{N_a}{p_i}\right)$$

費米能階位置與溫度之關係

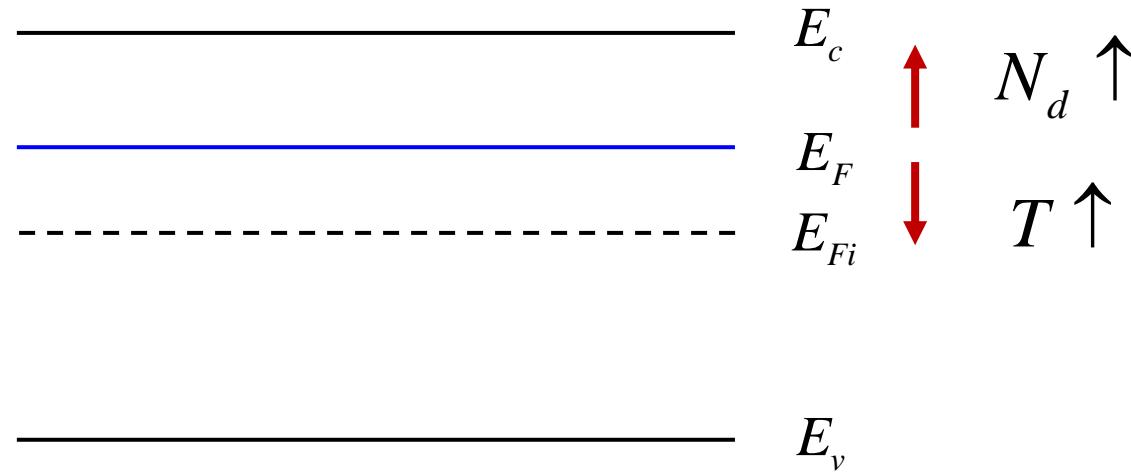


$$n_i = N_c \exp\left(-\frac{E_c - E_F}{kT}\right)$$

$$E_F - E_{Fi} = kT \ln\left(\frac{N_d}{n_i}\right)$$

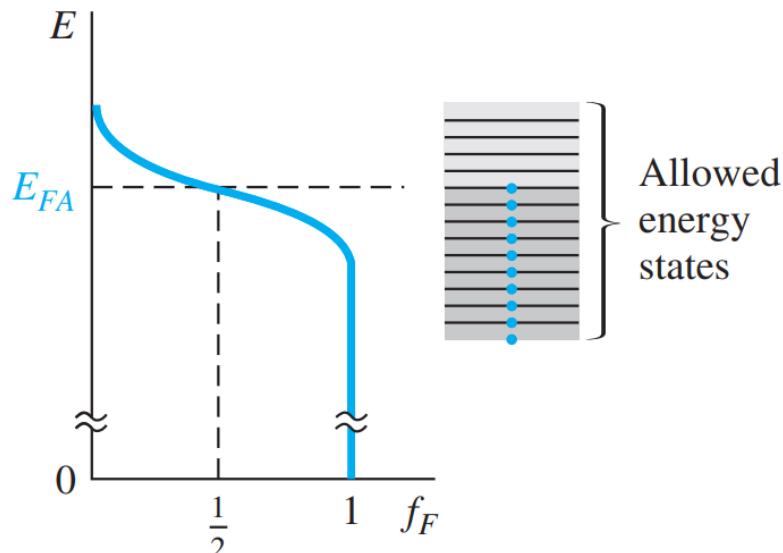
$$E_{Fi} - E_F = kT \ln\left(\frac{N_a}{p_i}\right)$$

費米能階位置總結

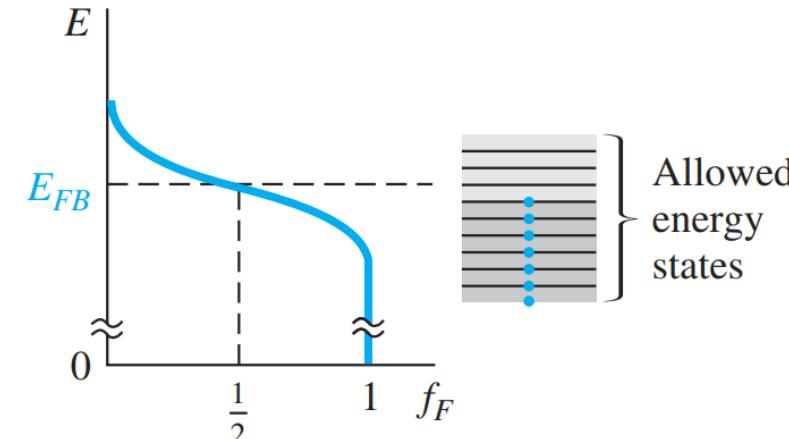


- 摻雜濃度愈高，費米能階往導帶靠
- 溫度愈高，費米能階往中線(本質費米能階)靠

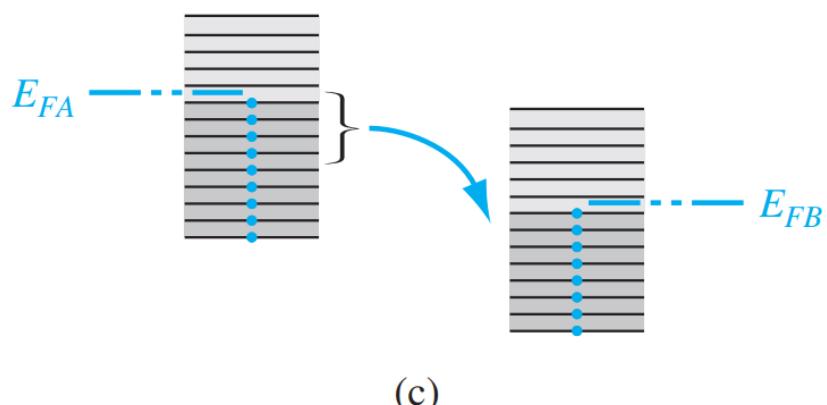
平衡時的P-N接面



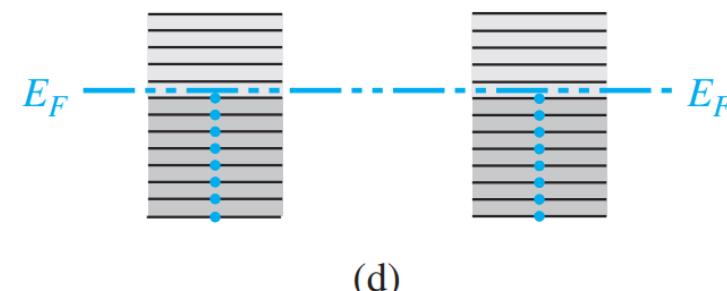
(a)



(b)



(c)



(d)