Algorithm Library

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Algorithm Library by Liu Yang

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1 String

1.1 AhoCorasickAutomaton

```
const int maxn = "Edit";
struct AhoCorasickAutomaton {
 int son[maxn][26];
 int val[maxn];
 int fail[maxn];
 int tot;
 // Trie Tree 初始化
 void TrieInit() {
   tot = 0;
   memset(son, 0, sizeof(son));
   memset(val, 0, sizeof(val));
   memset(fail, 0, sizeof(fail));
 }
 // 计算字母下标
 int Pos(char x) { return x - 'a'; }
 // 向 Trie Tree 中插入 str 模式字符串
 void Insert(std::string str) {
   int cur = 0, Len = (int)str.length();
   for (int i = 0; i < Len; ++i) {
     int idx = Pos(str[i]);
     if (!son[cur][idx]) son[cur][idx] = ++tot;
     cur = son[cur][idx];
   }
   val[cur]++;
 }
 // Bfs 求得 Trie Tree 上失配指针
 void GetFail() {
   std::queue<int> que;
   for (int i = 0; i < 26; ++i) {
     if (son[0][i]) {
       fail[son[0][1]] = 0;
        que.push(son[0][i]);
     }
   }
   while (!que.empty()) {
     int cur = que.front(); que.pop();
     for (int i = 0; i < 26; ++i) {
        if (son[cur][i]) {
         fail[son[cur][i]] = son[fail[cur]][i];
         que.push(son[cur][i]);
       }
```

```
else son[cur][i] = son[fail[cur]][i];
     }
   }
 }
 // 询问 str 中出现的模式串数量
 int Query(std::string str) {
   int len = (int)str.length();
   int cur = 0, ret = 0;
   for (int i = 0; i < len; ++i) {
     cur = son[cur][Pos(str[i])];
     for (int j = cur; j && ~val[j]; j = fail[j]) {
       ret += val[j];
       val[j] = -1;
     }
   }
   return ret;
 }
};
1.2 KMP
// 对模式串 pattern 计算 next 数组
void KMPPre(std::string pattern, std::vector<int> &next) {
 int i = 0, j = -1;
 next[0] = -1;
 int len = (int)pattern.length();
 while (i != len) {
   if (j == -1 || pattern[i] == pattern[j]) next[++i] = ++j;
   else j = next[j];
}
// 优化对模式串 pattern 计算 next 数组
void PreKMP(std::string pattern, std::vector<int> &next) {
 int i, j;
 i = 0;
 j = next[0] = -1;
 int len = (int)pattern.length();
 while (i < len) {
   while (j != -1 && pattern[i] != pattern[j]) j = next[j];
   if (pattern[++i] == pattern[++j]) next[i] = next[j];
   else next[i] = j;
 }
}
// 利用预处理 next 数组计数模式串 pattern 在主串 main 中出现次数
int KMPCount(std::string pattern, std::string main) {
 int pattern_len = (int)pattern.length(), main_len = (int)main.length();
 std::vector<int> next(pattern_len + 1, 0);
```

```
//PreKMP(pattern, next);
 KMPPre(pattern, next);
  int i = 0, j = 0;
  int ret = 0;
 while (i < main_len) {</pre>
   while (j != -1 \&\& main[i] != pattern[j]) j = next[j];
   i++; j++;
   if (j >= pattern_len) {
     ret++;
      j = next[j];
   }
 }
 return ret;
}
1.3 Manacher
const int maxn = "Edit";
char convert_str[maxn << 1];</pre>
int len[maxn << 1];</pre>
// Manacher 算法求 str 字符串最长回文子串长度
int Manacher(char Str[]) {
  int L = 0, str_len = (int)strlen(Str);
  convert_str[L++] = '$'; convert_str[L++] = '#';
 for (int i = 0; i < str_len; ++i) {
    convert_str[L++] = Str[i];
    convert_str[L++] = '#';
 }
  int mx = 0, id = 0, ret = 0;
 for (int i = 0; i < L; ++i) {
   len[i] = mx > i ? std::min(len[2 * id - i], mx - i) : 1;
   while (convert_str[i + len[i]] == convert_str[i - len[i]]) len[i]++;
   if (i + len[i] > mx) {
     mx = i + len[i];
     id = i;
   }
   ret = std::max(ret, len[i] - 1);
 }
 return ret;
1.4 PalindromicTree
const int maxn = "Edit";
struct PalindromicTree {
  // 子节点记录数组
  int son[maxn][26];
```

```
// 失配指针 fail 数组
int fail[maxn];
// len[i]: 节点 i 表示的回文串长度 (一个节点表示一个回文串)
int len[maxn];
// cnt[i]: 节点 i 表示的本质不同的串的个数 (最后需要运行 Count() 函数才可求出正确结
→ 果)
int cnt[maxn];
// num[i]: 以节点 i 表示的最长回文串的最右端为回文串结尾的回文串个数
int num[maxn];
// 字符
int str[maxn];
// 新添加字符后最长回文串表示的节点
int last;
// 字符数量
int str_len;
// 节点数量
int tot;
// 新建节点
int NewNode(int x) {
 for (int i = 0; i < 26; ++i) son[tot][i] = 0;
 cnt[tot] = 0;
 num[tot] = 0;
 len[tot] = x;
 return tot++;
}
// 初始化
void Init() {
 tot = 0;
 NewNode(0); NewNode(-1);
 last = 0;
 str_len = 0;
 // 开头存字符集中没有的字符, 减少特判
 str[0] = -1;
 fail[0] = 1;
}
int GetFail(int x) {
 while (str[str_len - len[x] - 1] != str[str_len]) x = fail[x];
 return x;
}
void Add(int c) {
 c -= 'a';
 Str[++str_len] = c;
 int Cur = GetFail(last);
 if (!son[Cur][c]) {
   int New = NewNode(len[Cur] + 2);
```

```
fail[New] = son[GetFail(fail[Cur])][c];
      son[Cur][c] = New;
      num[New] = num[fail[New]] + 1;
   last = son[Cur][c];
    cnt[last]++;
 }
 void Count() {
   // 若 fail[v]=u,则 u 一定是 v 回文子串,所以双亲累加孩子的 cnt
   for (int i = tot - 1; i >= 0; --i) cnt[fail[i]] += cnt[i];
 }
};
1.5
    \operatorname{Trie}
const int maxn = "Edit";
struct Trie {
  int son[maxn][26];
  int tot;
 int cnt[maxn];
 void TrieInit() {
   tot = 0;
   memset(cnt, 0, sizeof(cnt));
   memset(son, 0, sizeof(son));
 }
 int Pos(char x) { return x - 'a'; }
 // 向 Trie Tree 中插入字符串 str
 void Insert(std::string str) {
   int cur = 0, len = (int)str.length();
   for (int i = 0; i < len; ++i) {</pre>
      int idx = Pos(str[i]);
      if (!son[cur][idx]) son[cur][idx] = ++tot;
      cur = son[cur][idx];
      cnt[cur]++;
   }
 }
  // 查找字符串 str, 存在返回 true, 不存在返回 false
 bool Find(std::string str) {
   int cur = 0, len = (int)str.length();
   for (int i = 0; i < len; ++i) {
      int idx = Pos(str[i]);
      if (!son[cur][idx]) return false;
      cur = son[cur][idx];
   }
```

```
return true;
}

// 查询字典树中以 str 为前缀的字符串数量
int PathCnt(std::string str) {
   int cur = 0, len = (int)str.length();
   for (int i = 0; i < len; ++i) {
      int idx = Pos(Str[i]);
      if (!son[cur][idx]) return 0;
      cur = son[cur][idx];
   }
   return cnt[cur];
}
```

2 Math

```
2.1 Catalan
const int maxn = "Edit";
```

```
long long cat[maxn];

void GetCat() {
  memset(cat, 0, sizeof(cat));
  cat[0] = cat[1] = 1;
  for (int i = 2; i < maxn; ++i) cat[i] = cat[i - 1] * (4 * i - 2) / (i + 1);
}</pre>
```

2.2 CombinatorialNumber

```
const int mod = "Edit";
const int maxn = "Edit";

int c[maxn][maxn];

void GetC() {
    memset(c, 0, sizeof(c));
    c[0][0] = 1;
    for (int i = 1; i < maxn; ++i) {
        c[i][0] = 1;
        for (int j = 1; j <= i; ++j) {
            if (j == i) c[i][j] = 1;
            else c[i][j] = (c[i - 1][j - 1] + c[i - 1][j]) % mod;
        }
    }
}</pre>
```

2.3 Derangement

2.4 Euler

```
2.4.1 Euler
int GetPhi(int x) {
  int ret = x;
 for (int i = 2; i * i <= x; ++i) {
    if (!(x % i)) {
      ret = ret / i * (i - 1);
      while (!(x \% i)) x /= i;
 }
  if (x > 1) ret = ret / x * (x - 1);
 return ret;
}
2.4.2 Screen
const int maxn = "Edit";
int phi[maxn];
void GetPhi() {
  for (int i = 1; i < maxn; ++i) phi[i] = i;</pre>
 for (int i = 2; i < maxn; i += 2) phi[i] /= 2;
 for (int i = 3; i < maxn; i += 2)
    if (phi[i] == i)
      for (int j = i; j < maxn; j += i) phi[j] = phi[j] / i * (i - 1);
}
2.4.3 Sieve
const int maxn = "Edit";
bool is_prime[maxn];
int phi[maxn];
std::vector<int> prime;
void Sieve() {
  memset(is_prime, true, sizeof(is_prime));
 phi[1] = 1; is_prime[0] = is_prime[1] = false;
  for (long long i = 2; i < maxn; ++i) {
    if (is_prime[i]) {
      phi[i] = i - 1;
      prime.emplace_back(i);
    for (auto &p : prime) {
      if (p * i >= maxn) break;
      is_prime[i * p] = false;
      if (i % p == 0) {
```

phi[i * p] = phi[i] * p;

```
break;
      phi[i * p] = phi[i] * phi[p];
 }
}
2.5 FFT
const int maxn = "Edit";
const double pi = acos(-1.0);
// 复数
struct complex {
  double x, y;
  complex operator + (const complex &b) const {return complex {x + b.x, y + b.y};}
  complex operator - (const complex &b) const {return complex {x - b.x, y - b.y};}
  complex operator * (const complex &b) const {return complex {x * b.x - y * b.y, x
  \rightarrow * b.y + y * b.x};}
  complex operator / (const complex &b) const {
    double tmp = b.x * b.x + b.y * b.y;
    return complex \{(x * b.x + y * b.y) / tmp, (y * b.x - x * b.y) / tmp\};
 }
};
// 多项式系数数量
int n, m;
int 1;
int limit;
int r[maxn << 2];</pre>
// 快速傅里叶变换 (FFT)
void FFT(complex f[], int op) {
  for (int i = 0; i < limit; ++i) {</pre>
    if (i < r[i]) std::swap(f[i], f[r[i]]);</pre>
  for (int j = 1; j < limit; j <<= 1) {
    complex tmp = complex {cos(pi / j), op * sin(pi / j)};
    for (int k = 0; k < limit; k += (j << 1)) {
      complex Buffer = complex {1.0, 0.0};
      for (int l = 0; l < j; ++1) {
        complex tx = f[k + 1], ty = Buffer * f[k + j + 1];
        f[k + 1] = tx + ty;
        f[k + j + 1] = tx - ty;
        Buffer = Buffer * tmp;
      }
    }
 }
}
```

```
complex a[maxn], b[maxn];
// 多项式卷积计算
void Cal() {
  limit = 1; 1 = 0;
  while (limit \leq n + m) {
    limit <<= 1;
    1++;
  }
  for (int i = 0; i < limit; ++i) r[i] = (r[i >> 1] >> 1) | ((i & 1) << (1 - 1));
  FFT(a, 1);
  FFT(b, 1);
  for (int i = 0; i <= limit; ++i) a[i] = a[i] * b[i];</pre>
  FFT(a, -1);
2.6 Fibonacci
const int mod = "Edit";
struct matrix { long long mat[2][2]; };
matrix operator * (matrix &k1, matrix &k2) const {
  matrix ret;
  memset(ret.mat, 0, sizeof(ret.mat));
  for (int i = 0; i < 2; ++i) {
    for (int j = 0; j < 2; ++j) {
      for (int k = 0; k < 2; ++k) {
          ret.mat[i][j] = (ret.mat[i][j] + k1.mat[i][k] * k2.mat[k][j] % mod) %
           \hookrightarrow mod;
      }
    }
  }
  return ret;
}
// 矩阵快速幂
matrix operator ^ (matrix base, long long k) {
  matrix ret;
  memset(ret.mat, 0, sizeof(ret.mat));
  ret.mat[0][0] = ret.mat[1][1] = 1;
  while (k) {
    if (k & 1) ret = ret * base;
    base = base * base;
    k >>= 1;
  }
  return ret;
// 斐波那契数列中第 æ 项
```

```
long long Fib(long long x) {
  matrix base;
  base.mat[0][0] = base.mat[1][0] = base.mat[0][1] = 1;
 base.mat[1][1] = 0;
  return (base ^ x).mat[0][1];
}
2.7 Gauss
const int mod = "Edit";
void Gauss(std::vector<std::vector<long long>> &matrix) {
  int n = (int)matrix.size();
  for (int i = 0; i < n; ++i) {
    long long inv = Inv(matrix[i][i]);
    for (int j = i; j \le n; ++j) {
      matrix[i][j] = matrix[i][j] * inv % mod;
    }
    for (int j = 0; j < n; ++j) {
      if (j != i) {
        long long tmp = matrix[j][i];
        for (int k = i; k \le n; ++k) {
          matrix[j][k] = (matrix[j][k] - matrix[i][k] * tmp % mod + mod) % mod;
        }
     }
    }
 }
}
2.8 GeneratingFunction
const int maxn = "Edit";
int c1[maxn], c2[maxn];
void GetGeneratingFunction(int n) {
  for (int i = 0; i < maxn; ++i) {</pre>
    c1[i] = 1;
    c2[i] = 0;
  }
  // c1[i] 为 x~i 的系数
  // c2 为中间变量
  for (int i = 2; i <= n; ++i) {
    for (int j = 0; j \le n; ++j) {
      for (int k = 0; k + j \le n; k += i) {
        c2[j + k] += c1[i];
      }
    }
    for (int j = 0; j \le n; ++j) {
      c1[j] = c2[j];
```

```
c2[j] = 0;
   }
 }
}
2.9 InverseElement
2.9.1 ExtendGcd
const int mod = "Edit";
// 扩展欧几里得, a*x+b*y=d
long long ExtendGcd(long long a, long long b, long long &x, long long &y) {
  if (a == 0 \&\& b == 0) return -1;
 if (b == 0) {
   x = 1;
   y = 0;
   return a;
 long long d = ExtendGcd(b, a % b, y, x);
 y = a / b * x;
 return d;
}
// 逆元, ax = 1 \pmod{mod}
long long GetInv(long long a) {
 long long x, y;
 long long d = ExtendGcd(a, mod, x, y);
 if (d == 1) return (x % mod + mod) % mod;
 else return -1;
}
2.9.2 Factorial
const int mod = "Edit";
const int maxn = "Edit";
// fac: 阶乘, facinv: 阶乘逆元
long long fac[maxn], facinv[maxn];
void GetFacInv() {
 fac[0] = 0; fac[1] = 1;
 for (int i = 2; i < maxn; ++i) fac[i] = (fac[i - 1] * i) % mod;
 facinv[maxn - 1] = Pow(fac[maxn - 1], mod - 2);
 for (int i = maxn - 2; i \ge 0; --i) facinv[i] = (facinv[i + 1] * (i + 1)) % mod;
}
2.9.3 FermatLittleTheorem
const int mod = "Edit";
```

```
long long Inv(long long x) {
 return Pow(x, mod - 2);
2.9.4 Recursive
const int mod = "Edit";
const int maxn = "Edit";
long long inv[maxn];
// 递推求逆元
void GetInv() {
  inv[1] = 1;
 for (int i = 2; i < maxn; ++i) inv[i] = (mod - mod / i) * inv[mod % i] % mod;</pre>
}
2.10 Mobius
#include <bits/stdc++.h>
const int maxn = "Edit";
bool is_prime[maxn];
std::vector<int> prime;
int mu[maxn];
void Sieve() {
 memset(is_prime, true, sizeof(is_prime));
 mu[1] = 1; is_prime[0] = is_prime[1] = false;
 for (int i = 2; i < maxn; ++i) {</pre>
    if (is_prime[i]) {
      prime.emplace_back(i);
     mu[i] = -1;
   }
   for (auto &p : prime) {
      if (p * i >= maxn) break;
      is_prime[i * p] = false;
      if (i % p == 0) {
       mu[i * p] = 0;
        break;
     mu[i * p] = -mu[i];
   }
 }
}
2.11 NimGame
// ret 不为零则先手赢, 否则为后手赢
bool GetNim(std::vector<int> arr) {
```

```
int ret = 0;
 for (auto &v : arr) ret ^= v;
 return ret != 0;
2.12 Polynomial
const int mod = "Edit";
// 多项式求值(低次在前)
long long F(long long x, std::vector<long long> &coef) {
 long long ret = 0;
 for (int i = (int)coef.size() - 1; ~i; --i) {
   ret = (ret * x + coef[i]) \% mod;
 }
 return ret;
2.13 Prime
2.13.1 PrimeFactor
const int maxn = "Edit"
bool is_prime[maxn];
vector<int> prime_fac[maxn];
void GetPrimeFac() {
 memset(is_prime, true, sizeof(is_prime));
 for (long long i = 2; i < maxn; ++i) {
   if (is_prime[i]) {
      prime_fac[i].push_back(i);
      for (long long j = i + i; j < maxn; ++j) {
        is_prime[j] = false;
        prime_fac[j].push_back(i);
   }
 }
  is_prime[1] = false;
2.13.2 SieveOfEratosthenes
const int maxn = "Edit";
bool is_prime[maxn];
std::vector<int> prime
void Sieve() {
 memset(is_prime, true, sizeof(is_prime));
  is_prime[0] = is_prime[1] = false;
```

```
for (long long i = 2; i < maxn; ++i) {
    if (is_prime[i]) prime.emplace_back(i);
    for (auto &p : prime) {
      if (p * i >= maxn) break;
      is_prime[i * p] = false;
    }
 }
}
2.14 QuickPow
const int mod = "edit";
long long Mul(long long x, long long y) {
 long long ret = 0;
 while (y) {
    if (y) ret = (ret + x) \% mod;
    x = (x + x) \% mod;
    y >>= 1;
 }
 return ret;
}
long long Pow(long long x, long long n) {
 long long ret = 1;
 while (n) {
    if (n & 1) ret = (ret * x) % mod;
    x = x * x \% mod;
    n >>= 1;
 }
 return ret;
}
2.15 Stirling
const double pi = acos(-1.0);
const double e = 2.718281828459;
int GetStirling(int x) {
  if (x <= 1) return 1;
 return (int)ceil(log10(2 * pi * x) / 2 + x * log10(x / e));
}
```

3 DataStructure

3.1 BinaryIndexedTree

```
#define lowbit(x) (x \mathcal{B}(-x))
const int maxn = "Edit";
struct BitTree {
  int arr[maxn];
 void Update(int x, int v) {
    while (x < maxn) {</pre>
      arr[x] += v;
      x += lowbit(x);
    }
  }
  int GetSum(int x) {
    int ans = 0;
    while (x > 0) {
      ans += arr[x];
      x = lowbit(x);
 }
};
3.2 DfsOrder
std::vector<std::vector<int>> g;
int dfs_clock;
std::vector<int> in, out;
// Dfs 序
void DfsOrder(int cur, int pre) {
  in[cur] = ++dfs_clock;
 for (auto &it : g) {
    if (it == pre) continue;
    DfsOrder(it, cur);
 }
  out[cur] = dfs_clock;
}
3.3 FunctionalSegmentTree
const int maxn = "Edit";
struct FuncSegTree {
  int tot;
  int rt[maxn];
  int lson[maxn << 5], rson[maxn << 5];</pre>
  int cnt[maxn << 5];</pre>
```

```
int Build(int 1, int r) {
   int o = ++tot, m = (1 + r) >> 1;
   cnt[o] = 0;
   if (1 != r) {
      lson[o] = Build(1, m);
      rson[o] = Build(m + 1, r);
   }
   return o;
  int Modify(int prev, int 1, int r, int v) {
   int o = ++tot, m = (1 + r) >> 1;
   lson[o] = lson[prev];
   rson[o] = rson[prev];
   cnt[o] = cnt[prev] + 1;
   if (1 != r) {
      if (v \le m) lson[o] = Modify(lson[o], l, m, v);
      else rson[o] = Modify(rson[o], m + 1, r, v);
   }
   return o;
 }
 // 区间 [u+1,v] 静态第 k 小
  int Query(int u, int v, int l, int r, int k) {
   if (1 == r) return 1;
   int m = (1 + r) >> 1;
   int num = cnt[lson[v]] - cnt[lson[u]];
   if (num >= k) return Query(lson[u], lson[v], l, m, k);
   return Query(rson[u], rson[v], m + 1, r, k - num);
 }
 // 区间 [u+1,v] 内 [s,t] 数量
 int Query(int u, int v, int s, int t, int l, int r) {
   if (s <= 1 && t >= r) return cnt[v] - cnt[u];
    int m = (1 + r) >> 1, ret = 0;
   if (s <= m) ret += Query(lson[u], lson[v], s, t, 1, m);</pre>
   if (t > m) ret += Query(rson[u], rson[v], s, t, m + 1, r);
   return ret;
 }
};
3.4 Hash
template <typename type>
struct Hash {
    int size;
   vector<int> arr;
   Hash(const vector<type> &v) {
```

```
arr.assign(v.begin(), v.end());
      sort(arr.begin(), arr.end());
      arr.erase(unique(arr.begin(), arr.end()), arr.end());
      size = arr.size();
   int Get(type k) {
      return lower_bound(arr.begin(), arr.end(), k) - arr.begin();
   }
};
3.5 LCA
3.5.1 DFS+ST
const int maxn = "Edit";
struct edge { int v, c, next; };
edge edges[maxn << 1];</pre>
int head[maxn];
int tot;
void AddEdge(int u, int v, int c) {
  edges[tot] = (edge){v, c, head[u]};
 head[u] = tot++;
}
// 节点深度
int rmq[maxn << 1];</pre>
// 深搜遍历顺序
int vertex[maxn << 1];</pre>
// 节点在深搜中第一次出现的位置
int first[maxn];
int fa[maxn];
int dis[maxn];
int lca_tot;
// 最小值对应下标
int dp[maxn << 1][20];</pre>
// rmg 初始化
void Work(int n) {
 for (int i = 1; i <= n; ++i) dp[i][0] = i;
 for (int j = 1; (1 << j) <= n; ++j) {
   for (int i = 1; i + (1 << j) - 1 <= n; ++i) {
      dp[i][j] = rmq[dp[i][j-1]] < rmq[dp[i+(1 << (j-1))][j-1]] ? dp[i][j-1]
      \rightarrow 1] : dp[i + (1 << (j - 1))][j - 1];
   }
 }
```

```
}
// 深搜
void Dfs(int cur, int pre, int dep) {
  vertex[++lca_tot] = cur;
 first[cur] = lca_tot;
 rmq[lca_tot] = dep;
 fa[cur] = pre;
 for (int i = head[cur]; ~i; i = edges[i].next) {
    if (edges[i].v == pre) continue;
   dis[edges[i].v] = dis[cur] + edges[i].c;
   Dfs(edges[i].v, cur, dep + 1);
   vertex[++lca_tot] = cur;
   rmq[lca_tot] = dep;
 }
}
// rmg 查询
int Query(int 1, int r) {
  if (1 > r) swap(1, r);
 int len = (int)\log 2(r - 1 + 1);
 return rmq[dp[l][len]] \le rmq[dp[r - (1 << len) + 1][len]] ? dp[l][len] : dp[r -
  \rightarrow (1 << len) + 1][len];
}
// LCA 初始化
void Init(int rt, int num) {
 memset(dis, 0, sizeof(dis));
 lca_tot = 0;
 Dfs(rt, 0, 0);
 fa[1] = 0;
 Work(2 * num - 1);
}
// 查询节点 w v 的距离
int GetDis(int u, int v) { return dis[u] + dis[v] - 2 * dis[LCA(u, v)]; }
// 查询节点 u, v 的最近公共祖先 (LCA)
int GetLCA(int u, int v) { return vertex[Query(first[u], first[v])]; }
3.5.2 Multiplication
const int maxn = "Edit";
int n, k;
std::vector<int> g[maxn];
void AddEdge(int u, int v) {
 g[u].push_back(v);
 g[v].push_back(u);
```

```
}
int anc[maxn][25];
int dep[maxn];
void Dfs(int u, int prev, int depth) {
  anc[u][0] = prev; dep[u] = depth;
  for (auto &v : g[u]) {
    if (v == prev) continue;
    Dfs(v, u, depth + 1);
 }
}
void Init(int rt) {
 Dfs(rt, 0, 1);
 for (int j = 1; j < k; ++j) {
    for (int i = 1; i <= n; ++i) {
      anc[i][j] = anc[anc[i][j - 1]][j - 1];
    }
 }
}
void Swim(int &u, int h) {
  for (int i = 0; h > 0; ++i) {
    if (h & 1) u = anc[u][i];
    h >>= 1;
  }
}
int Query(int u, int v) {
  if (dep[u] < dep[v]) std::swap(u, v);</pre>
 Swim(u, dep[u] - dep[v]);
  if (u == v) return u;
 for (int i = k - 1; i \ge 0; --i) {
    if (anc[u][i] != anc[v][i]) {
      u = anc[u][i];
      v = anc[v][i];
    }
  }
  return anc[u][0];
3.5.3 Tarjan
const int maxn = "Edit";
int pre[maxn << 2];</pre>
struct edge { int v, next; };
edge g[maxn << 2];</pre>
int head[maxn];
```

```
int tot;
struct query { int q, next, index; };
query qg[maxn << 2];
int qhead[maxn];
int qtot;
int vis[maxn];
int anc[maxn];
int ans[maxn];
int Find(int x) { return pre[x] == x ? x : pre[x] = Find(pre[x]); }
void Union(int x, int y) { pre[Find(x)] = Find(y); }
void AddEdge(int u, int v) {
 g[tot] = edge {v, head[u]};
 head[u] = tot++;
}
// 添加询问
void AddQuery(int u, int v, int index) {
  qg[qtot] = query {v, qhead[u], index};
 qhead[u] = qtot++;
 qg[qtot] = query {u, qhead[v], index};
 qhead[v] = qtot++;
}
// 初始化
void Init() {
 tot = 0;
 memset(head, -1, sizeof(head));
 qtot = 0;
 memset(qhead, -1, sizeof(qhead));
 memset(vis, false, sizeof(vis));
 memset(pre, -1, sizeof(pre));
 memset(anc, 0, sizeof(anc));
 for (int i = 0; i <= n; ++i) pre[i] = i;
}
// LCA 离线 Tarjan 算法
void Tarjan(int u) {
  anc[u] = u;
 vis[u] = true;
 for (int i = head[u]; ~i; i = g[i].next) {
   if (vis[g[i].v]) continue;
   Tarjan(g[i].v);
   Join(u, g[i].v);
   anc[Find(u)] = u;
 }
 for (int i = qhead[u]; ~i; i = qg[i].next) {
```

```
if (vis[qg[i].q]) ans[qg[i].index] = anc[Find(qg[i].q)];
 }
}
3.6
    MultipleTree
  BZOJ 3196 (线段树套伸展树)
  1. 查询 k 在区间内的排名
  2. 查询区间内排名为 k 的值
  3. 修改某一位值上的数值
  4. 查询 k 在区间内的前驱 (前驱定义为小于 x, 且最大的数)
  5. 查询 k 在区间内的后继 (后继定义为大于 x, 且最小的数)
#include <bits/stdc++.h>
using namespace std;
const int inf = 2147483647;
const int maxn = 5e4 + 5;
const int maxm = maxn * 25;
int n;
int arr[maxn];
namespace SplayTree {
  int rt[maxm], tot;
  int fa[maxm], son[maxm][2];
  int val[maxm], cnt[maxm];
  int sz[maxm];
  void Push(int o) { sz[o] = sz[son[o][0]] + sz[son[o][1]] + cnt[o]; }
 bool Get(int o) { return o == son[fa[o]][1]; }
  void Clear(int o) { son[o][0] = son[o][1] = fa[o] = val[o] = sz[o] = cnt[o] = 0;
  → }
  void Rotate(int o) {
    int p = fa[o], q = fa[p], ck = Get(o);
    son[p][ck] = son[o][ck ^ 1];
   fa[son[o][ck ^ 1]] = p;
   son[o][ck ^ 1] = p;
   fa[p] = o; fa[o] = q;
   if (q) son[q][p == son[q][1]] = o;
   Push(p); Push(o);
  }
 void Splay(int &root, int o) {
   for (int f = fa[o]; (f = fa[o]); Rotate(o))
     if (fa[f]) Rotate(Get(o) == Get(f) ? f : o);
   root = o;
```

```
}
void Insert(int &root, int x) {
  if (!root) {
    val[++tot] = x;
    cnt[tot]++;
    root = tot;
    Push(root);
    return;
  }
  int cur = root, f = 0;
  while (true) {
    if (val[cur] == x) {
      cnt[cur]++;
      Push(cur); Push(f);
      Splay(root, cur);
      break;
    }
    f = cur;
    cur = son[cur][val[cur] < x];</pre>
    if (!cur) {
      val[++tot] = x;
      cnt[tot]++;
      fa[tot] = f;
      son[f][val[f] < x] = tot;
      Push(tot); Push(f);
      Splay(root, tot);
      break;
    }
  }
}
int GetRank(int &root, int x) {
  int ans = 0, cur = root;
  while (cur) {
    if (x < val[cur]) {</pre>
      cur = son[cur][0];
      continue;
    ans += sz[son[cur][0]];
    if (x == val[cur]) {
      Splay(root, cur);
      return ans;
    }
    if (x > val[cur]) {
      ans += cnt[cur];
      cur = son[cur][1];
    }
  }
```

```
return ans;
}
int GetKth(int &root, int k) {
  int cur = root;
  while (true) {
    if (son[cur][0] \&\& k \le sz[son[cur][0]]) cur = son[cur][0];
    else {
      k -= cnt[cur] + sz[son[cur][0]];
      if (k <= 0) return cur;</pre>
      cur = son[cur][1];
    }
  }
}
int Find(int &root, int x) {
  int ans = 0, cur = root;
  while (cur) {
    if (x < val[cur]) {</pre>
      cur = son[cur][0];
      continue;
    ans += sz[son[cur][0]];
    if (x == val[cur]) {
      Splay(root, cur);
      return ans + 1;
    }
    ans += cnt[cur];
    cur = son[cur][1];
  }
}
int GetPrev(int &root) {
  int cur = son[root][0];
  while (son[cur][1]) cur = son[cur][1];
  return cur;
}
int GetPrevVal(int &root, int x) {
  int ans = -inf, cur = root;
  while (cur) {
    if (x > val[cur]) {
      ans = max(ans, val[cur]);
      cur = son[cur][1];
      continue;
    cur = son[cur][0];
  }
  return ans;
}
```

```
int GetNext(int &root) {
  int cur = son[root][1];
  while (son[cur][0]) cur = son[cur][0];
  return cur;
}
int GetNextVal(int &root, int x) {
  int ans = inf, cur = root;
  while (cur) {
    if (x < val[cur]) {</pre>
      ans = min(ans, val[cur]);
      cur = son[cur][0];
      continue;
    }
    cur = son[cur][1];
  }
  return ans;
}
void Delete(int &root, int x) {
  Find(root, x);
  if (cnt[root] > 1) {
    cnt[root]--;
    Push(root);
    return;
  }
  if (!son[root][0] && !son[root][1]) {
    Clear(root);
    root = 0;
    return;
  }
  if (!son[root][0]) {
    int cur = root;
    root = son[root][1];
    fa[root] = 0;
    Clear(cur);
    return;
  }
  if (!son[root][1]) {
    int cur = root;
    root = son[root][0];
    fa[root] = 0;
    Clear(cur);
    return;
  int p = GetPrev(root), cur = root;
  Splay(root, p);
  fa[son[cur][1]] = p;
  son[p][1] = son[cur][1];
```

```
Clear(cur);
    Push(root);
  }
};
namespace SegTree {
  int tree[maxn << 2];</pre>
  void Build(int o, int 1, int r) {
    for (int i = 1; i <= r; ++i) SplayTree::Insert(tree[o], arr[i - 1]);</pre>
    if (l == r) return;
    int m = (1 + r) >> 1;
    Build(o << 1, 1, m);
    Build(o << 1 | 1, m + 1, r);
  }
  void Modify(int o, int 1, int r, int 11, int rr, int u, int v) {
    SplayTree::Delete(tree[o], u); SplayTree::Insert(tree[o], v);
    if (l == r) return;
    int m = (1 + r) >> 1;
    if (ll <= m) Modify(o << 1, 1, m, ll, rr, u, v);</pre>
    if (rr > m) Modify(o << 1 | 1, m + 1, r, ll, rr, u, v);
  }
  int QueryRank(int o, int l, int r, int ll, int rr, int v) {
    if (ll <= l && rr >= r) return SplayTree::GetRank(tree[o], v);
    int m = (1 + r) >> 1, ans = 0;
    if (ll <= m) ans += QueryRank(o << 1, 1, m, ll, rr, v);
    if (rr > m) ans += QueryRank(o << 1 | 1, m + 1, r, 11, rr, v);
    return ans;
  }
  int QueryPrev(int o, int l, int r, int ll, int rr, int v) {
    if (ll <= l && rr >= r) return SplayTree::GetPrevVal(tree[o], v);
    int m = (1 + r) >> 1, ans = -inf;
    if (ll <= m) ans = max(ans, QueryPrev(o << 1, 1, m, ll, rr, v));
    if (rr > m) ans = max(ans, QueryPrev(o << 1 | 1, m + 1, r, ll, rr, v));
    return ans;
  }
  int QueryNext(int o, int l, int r, int ll, int rr, int v) {
    if (ll <= l && rr >= r) return SplayTree::GetNextVal(tree[o], v);
    int m = (l + r) >> 1, ans = inf;
    if (ll <= m) ans = min(ans, QueryNext(o << 1, 1, m, ll, rr, v));
    if (rr > m) ans = min(ans, QueryNext(o << 1 | 1, m + 1, r, 11, rr, v));
    return ans;
  }
  int QueryKth(int 11, int rr, int v) {
```

```
int 1 = 0, r = 1e8 + 10;
    while (1 < r) {
      int m = ((1 + r) >> 1) + 1;
      if (QueryRank(1, 1, n, ll, rr, m) < v) l = m;</pre>
      else r = m - 1;
    }
    return 1;
 }
};
int main() {
  ios::sync_with_stdio(false);
  cin.tie(nullptr); cout.tie(nullptr);
  int m; cin >> n >> m;
  for (int i = 0; i < n; ++i) cin >> arr[i];
  SplayTree::tot = 0;
  SegTree::Build(1, 1, n);
  for (int i = 0, op, l, r, pos, k; i < m; ++i) {
    cin >> op;
    if (op == 1) {
      cin >> 1 >> r >> k;
      cout << SegTree::QueryRank(1, 1, n, 1, r, k) + 1 << endl;</pre>
    else if (op == 2) {
      cin >> 1 >> r >> k;
      cout << SegTree::QueryKth(1, r, k) << endl;</pre>
    }
    else if (op == 3) {
      cin >> pos >> k;
      SegTree::Modify(1, 1, n, pos, pos, arr[pos - 1], k);
      arr[pos - 1] = k;
    }
    else if (op == 4) {
      cin >> 1 >> r >> k;
      cout << SegTree::QueryPrev(1, 1, n, 1, r, k) << endl;</pre>
    }
    else if (op == 5) {
      cin >> 1 >> r >> k;
      cout << SegTree::QueryNext(1, 1, n, 1, r, k) << endl;</pre>
    }
  }
  return 0;
3.7 SegmentTree
```

3.7.1 AreaCombination

```
// HDU 1542 矩形面积并
#include <bits/stdc++.h>
```

```
typedef double db;
const int maxn = 1e2 + 5;
const db eps = 1e-9;
int Sgn(db k) { return fabs(k) < eps ? 0 : (k < 0 ? -1 : 1); }</pre>
int Cmp(db k1, db k2) { return Sgn(k1 - k2); }
struct seg {
  db 1, r, h;
  int flag;
};
bool operator < (seg &k1, seg &k2) { return Cmp(k1.h, k2.h) < 0; }
std::vector<seg> segs;
std::vector<db> pos;
int BinarySearch(db k) {
  int ret = (int)pos.size() - 1, 1 = 0, r = (int)pos.size() - 1;
  while (1 <= r) {
    int m = (1 + r) >> 1;
    if (Cmp(pos[m], k) >= 0) {
      ret = m;
      r = m - 1;
    }
    else l = m + 1;
  }
  return ret;
struct node {
  int 1, r, cnt;
  db len;
};
node seg_tree[maxn << 4];</pre>
void Pull(int o) {
  if (seg_tree[o].cnt) seg_tree[o].len = pos[seg_tree[o].r + 1] -
  → pos[seg_tree[o].1];
  else if (seg_tree[o].l == seg_tree[o].r) seg_tree[o].len = 0.0;
  else seg_tree[o].len = seg_tree[o << 1].len + seg_tree[o << 1 | 1].len;</pre>
void Build(int 1, int r, int o) {
  seg_tree[o].1 = 1; seg_tree[o].r = r;
  seg_tree[o].cnt = 0; seg_tree[o].len = 0.0;
  if (1 == r) return;
  int Mid = (1 + r) >> 1;
  Build(1, Mid, o << 1);
  Build(Mid + 1, r, o << 1 | 1);
```

```
Pull(o);
}
void Update(int 1, int r, int v, int o) {
  if (1 <= seg_tree[o].1 && r >= seg_tree[o].r) {
   seg_tree[o].cnt += v;
   Pull(o);
   return;
 }
  int Mid = (seg_tree[o].l + seg_tree[o].r) >> 1;
  if (r <= Mid) Update(1, r, v, o << 1);</pre>
 else if (1 > Mid) Update(1, r, v, o << 1 | 1);
 else {
   Update(1, Mid, v, o << 1);</pre>
   Update(Mid + 1, r, v, o << 1 | 1);
 }
 Pull(o);
}
int cas;
int n;
db x1, y1, x2, y2;
db ans;
int main() {
  while (~scanf("%d", &n) && n) {
    segs.clear(); pos.clear();
   for (int i = 0; i < n; ++i) {
      scanf("%lf%lf%lf", &x1, &y1, &x2, &y2);
      segs.push_back((seg)\{x1, x2, y1, 1\});
      segs.push_back((seg)\{x1, x2, y2, -1\});
      pos.push_back(x1); pos.push_back(x2);
   }
   std::sort(segs.begin(), segs.end());
    std::sort(pos.begin(), pos.end(), [\&](db k1, db k2) { return Cmp(k1, k2) < 0;}
    → });
    int cur = 1;
   for (int i = 1; i < (int)pos.size(); ++i)</pre>
      if (Cmp(pos[i], pos[i - 1]) != 0)
        pos[cur++] = pos[i];
   pos.erase(pos.begin() + cur, pos.end());
   Build(0, (int)pos.size(), 1);
   ans = 0.0;
   for (int i = 0; i < (int)segs.size() - 1; ++i) {</pre>
      int 1 = BinarySearch(segs[i].1), r = BinarySearch(segs[i].r);
      Update(l, r - 1, segs[i].flag, 1);
      ans += (segs[i + 1].h - segs[i].h) * seg_tree[1].len;
   printf("Test case #%d\n", ++cas);
```

```
printf("Total explored area: %.2lf\n\n", ans);
 }
 return 0;
}
3.7.2 AreaXorCombination
// CodeForces GYM 101982 F 矩形面积异或并
#include <bits/stdc++.h>
std::vector<int> x;
int Get(int k) { return std::lower_bound(x.begin(), x.end(), k) - x.begin(); }
struct SegTree {
 struct node {
   int v, lazy;
   node() { v = lazy = 0; }
 };
 node Unite(const node &k1, const node &k2) {
   node ans;
   ans.v = k1.v + k2.v;
   return ans;
 }
 void Pull(int o) { tree[o] = Unite(tree[o << 1], tree[o << 1 | 1]); }</pre>
 void Push(int o, int 1, int r) {
   int m = (1 + r) >> 1;
   if (tree[o].lazy != 0) {
      tree[o << 1].v = x[m] - x[l - 1] - tree[o << 1].v;
      tree[o << 1 | 1].v = x[r] - x[m] - tree[o << 1 | 1].v;
      tree[o << 1].lazy ^= 1;</pre>
      tree[o << 1 | 1].lazy ^= 1;
      tree[o].lazy = 0;
   }
 }
 int n;
 std::vector<node> tree;
 void Build(int o, int 1, int r) {
   if (l == r) return;
   int m = (1 + r) >> 1;
   Build(o << 1, 1, m);
   Build(o << 1 | 1, m + 1, r);
   Pull(o);
 }
 SegTree(int _n): n(_n) {
```

```
tree.resize(n << 2);</pre>
   Build(1, 1, n);
  }
 void Modify(int o, int 1, int r, int 11, int rr) {
    if (ll <= l && rr >= r) {
      tree[o].v = x[r] - x[1 - 1] - tree[o].v;
      tree[o].lazy ^= 1;
      return;
   Push(o, 1, r);
   int m = (1 + r) >> 1;
   if (ll <= m) Modify(o << 1, 1, m, ll, rr);
   if (rr > m) Modify(o << 1 | 1, m + 1, r, ll, rr);
   Pull(o);
  }
  void Modify(int ll, int rr) { Modify(1, 1, n, ll, rr); }
 node Query(int o, int 1, int r, int 11, int rr) {
    if (l1 <= 1 && rr >= r) return tree[o];
   Push(o, 1, r);
   int m = (1 + r) >> 1;
   node ans;
   if (ll <= m) ans = Unite(ans, Query(o << 1, 1, m, ll, rr));
   if (rr > m) ans = Unite(ans, Query(o << 1 | 1, m + 1, r, ll, rr));
   Pull(o);
   return ans;
 }
 node Query() { return Query(1, 1, n, 1, n); }
};
struct seg { int 1, r, h, flag; };
bool operator < (seg k1, seg k2) {return k1.h < k2.h;}</pre>
std::vector<seg> s;
int main() {
 std::ios::sync_with_stdio(false);
 std::cin.tie(nullptr); std::cout.tie(nullptr);
 int n; std::cin >> n;
 for (int i = 0, x1, y1, x2, y2; i < n; ++i) {
    std::cin >> x1 >> y1 >> x2 >> y2;
   if (x1 > x2) std::swap(x1, x2);
   if (y1 > y2) std::swap(y1, y2);
   x.emplace_back(x1); x.emplace_back(x2);
   s.emplace_back((seg){x1, x2, y1, 1});
    s.emplace_back((seg)\{x1, x2, y2, -1\});
 }
  sort(s.begin(), s.end());
  sort(x.begin(), x.end());
```

```
x.erase(unique(x.begin(), x.end()), x.end());
 SegTree tree((int)x.size());
  long long ans = 0;
  for (int i = 0, 1, r; i < (int)s.size() - 1; ++i) {
    1 = Get(s[i].1), r = Get(s[i].r);
    tree.Modify(l + 1, r);
    ans += (long long)tree.Query().v * (s[i + 1].h - s[i].h);
  }
  std::cout << ans << '\n';
  return 0;
}
3.7.3 MergeSegmentTree
// BZ0J2212: 交换左右子树后最小逆序对
#include <bits/stdc++.h>
const int maxn = 1e7 + 5;
template <typename t>
inline bool Read(t &ret) {
  char c; int sgn;
  if (c = getchar(), c == EOF) return false;
 while (c != '-' \&\& (c < '0' || c > '9')) c = getchar();
  sgn = (c == '-') ? -1 : 1;
 ret = (c == '-') ? 0 : (c - '0');
 while (c = getchar(), c >= '0' && c <= '9') ret = ret * 10 + (c - '0');
 ret *= sgn;
 return true;
struct node {
  int sz, lson, rson;
 node() \{sz = lson = rson = 0;\}
};
int n;
int tot;
node tree[maxn];
long long ans1, ans2;
long long ans;
int Build(int 1, int r, int c) {
  tree[++tot].sz = 1;
  if (1 == r) return tot;
  int m = (1 + r) >> 1, o = tot;
  if (c <= m) tree[o].lson = Build(1, m, c);</pre>
 else tree[o].rson = Build(m + 1, r, c);
 return o;
}
```

```
int Merge(int 1, int r, int x, int y) {
  if (!x || !y) return x + y;
 if (1 == r) {
   tree[++tot].sz = tree[x].sz + tree[y].sz;
   return tot;
 }
 ans1 += 111 * tree[tree[x].rson].sz * tree[tree[y].lson].sz;
 ans2 += 111 * tree[tree[x].lson].sz * tree[tree[y].rson].sz;
 int m = (1 + r) >> 1, o = ++tot;
 tree[o].lson = Merge(1, m, tree[x].lson, tree[y].lson);
 tree[o].rson = Merge(m + 1, r, tree[x].rson, tree[y].rson);
 tree[o].sz = tree[x].sz + tree[y].sz;
 return o;
}
int Dfs() {
  int c = 0; Read(c);
  if (c) return Build(1, n, c);
  int o = Merge(1, n, Dfs(), Dfs());
 ans += std::min(ans1, ans2);
 ans1 = ans2 = 0;
 return o;
int main() {
 Read(n);
 Dfs();
 printf("%lld", ans);
 return 0;
}
3.7.4 SegmentTree
// 求和线段树
template <typename type>
struct SegTree {
 struct node {
   type v, lazy;
   node() { v = lazy = 0; }
 };
  int n;
  std::vector<node> tree;
 node Unite(const node &k1, const node &k2) {
   node ret;
   ret.v = k1.v + k2.v;
   return ret;
```

```
}
void Pull(int o) { tree[o] = Unite(tree[o << 1], tree[o << 1 | 1]); }</pre>
void Push(int o, int 1, int r) {
  int m = (1 + r) >> 1;
  if (tree[o].lazy != 0) {
    tree[o << 1].v += (m - 1 + 1) * tree[o].lazy;</pre>
    tree[o << 1 | 1].v += (r - m) * tree[o].lazy;</pre>
    tree[o << 1].lazy += tree[o].lazy;</pre>
    tree[o << 1 | 1].lazy += tree[o].lazy;</pre>
    tree[o].lazy = 0;
  }
}
template <typename t>
void Build(int o, int 1, int r, const std::vector<t> &v) {
  if (1 == r) {
    tree[o].v = v[1 - 1];
    return;
  }
  int m = (1 + r) >> 1;
  Build(o << 1, 1, m, v);
  Build(o << 1 | 1, m + 1, r, v);
  Pull(o);
}
template <typename t>
SegTree(const std::vector<t> &v) {
  n = v.size();
  tree.resize((n \ll 2) + 1);
  Build(1, 1, n, v);
}
template <typename t>
void Modify(int o, int 1, int r, int 11, int rr, t v) {
  if (11 <= 1 && rr >= r) {
    tree[o].v += (r - 1 + 1) * v;
    tree[o].lazy += v;
    return;
  }
  Push(o, 1, r);
  int m = (1 + r) >> 1;
  if (ll <= m) Modify(o << 1, 1, m, ll, rr, v);
  if (rr > m) Modify(o << 1 | 1, m + 1, r, ll, rr, v);
  Pull(o);
}
template <typename t>
void Modify(int ll, int rr, t v) { Modify(1, 1, n, ll, rr, v); }
```

```
node Query(int o, int 1, int r, int 11, int rr) {
   if (ll <= l && rr >= r) return tree[o];
   Push(o, 1, r);
   int m = (1 + r) >> 1;
   node ret;
   if (ll <= m) ret = Unite(ret, Query(o << 1, 1, m, ll, rr));
   if (rr > m) ret = Unite(ret, Query(o << 1 | 1, m + 1, r, ll, rr));</pre>
   return ret;
 node Query(int 11, int rr) { return Query(1, 1, n, 11, rr); }
};
3.8 SparseTable
template <typename type>
struct SparseTable {
 std::vector<std::vector<type>> max, min;
 STTable(const std::vector<type> &arr) {
   int n = (int)arr.size(), m = log2(n) + 1;
   max = min = std::vector<std::vector<type>>(n, std::vector<type>(m, 0));
   for (int i = 0; i < n; ++i) max[i][0] = min[i][0] = arr[i];
   for (int j = 1; j < m; ++j) {
     for (int i = 0; i + (1 << j) - 1 < n; ++i) {
        \max[i][j] = std::\max(\max[i][j-1], \max[i+(1 << (j-1))][j-1]);
       min[i][j] = std::min(min[i][j-1], min[i+(1 << (j-1))][j-1]);
     }
   }
 type QueryMax(int 1, int r) {
   int k = log2(r - 1 + 1);
   return std::max(max[1][k], max[r - (1 << k) + 1][k]);
 }
 type QueryMin(int 1, int r) {
   int k = log2(r - 1 + 1);
   return std::min(min[l][k], min[r - (1 << k) + 1][k]);
 }
};
3.9 SplayTree
const int inf = "Edit"
const int maxn = "Edit";
struct SplayTree {
 int rt, tot;
 int fa[maxn], son[maxn][2];
```

```
int val[maxn], cnt[maxn];
int sz[maxn];
void Push(int o) { sz[o] = sz[son[o][0]] + sz[son[o][1]] + cnt[o]; }
bool Get(int o) { return o == son[fa[o]][1]; }
void Clear(int o) { son[o][0] = son[o][1] = fa[o] = val[o] = sz[o] = cnt[o] = 0;
→ }
void Rotate(int o) {
  int p = fa[o], q = fa[p], ck = Get(o);
  son[p][ck] = son[o][ck ^ 1];
  fa[son[o][ck ^ 1]] = p;
  son[o][ck ^ 1] = p;
  fa[p] = o; fa[o] = q;
  if (q) son[q][p == son[q][1]] = o;
  Push(p); Push(o);
}
void Splay(int o) {
  for (int f = fa[o]; f = fa[o], f; Rotate(o))
    if (fa[f]) Rotate(Get(o) == Get(f) ? f : o);
  rt = o;
}
void Insert(int x) {
  if (!rt) {
    val[++tot] = x;
    cnt[tot]++;
    rt = tot;
    Push(rt);
    return;
  }
  int cur = rt, f = 0;
  while (true) {
    if (val[cur] == x) {
      cnt[cur]++;
      Push(cur); Push(f);
      Splay(cur);
      break;
    }
    f = cur;
    cur = son[cur][val[cur] < x];</pre>
    if (!cur) {
      val[++tot] = x;
      cnt[tot]++;
      fa[tot] = f;
      son[f][val[f] < x] = tot;
```

```
Push(tot); Push(f);
      Splay(tot);
      break;
    }
  }
}
int GetRank(int x) {
  int ans = 0, cur = rt;
  while (true) {
    if (x < val[cur]) cur = son[cur][0];</pre>
    else {
      ans += sz[son[cur][0]];
      if (x == val[cur]) {
        Splay(cur);
        return ans + 1;
      }
      ans += cnt[cur];
      cur = son[cur][1];
    }
  }
}
int GetKth(int k) {
  int cur = rt;
  while (true) {
    if (son[cur][0] \&\& k \le sz[son[cur][0]]) cur = son[cur][0];
      k -= cnt[cur] + sz[son[cur][0]];
      if (k <= 0) return cur;</pre>
      cur = son[cur][1];
    }
  }
}
// after insert, before delete
int GetPrev() {
  int cur = son[rt][0];
  while (son[cur][1]) cur = son[cur][1];
  return cur;
}
int GetNext() {
  int cur = son[rt][1];
  while (son[cur][0]) cur = son[cur][0];
  return cur;
}
void Delete(int x) {
```

```
GetRank(x);
   if (cnt[rt] > 1) {
      cnt[rt]--;
      Push(rt);
      return;
   }
   if (!son[rt][0] && !son[rt][1]) {
      Clear(rt);
      rt = 0;
      return;
   }
   if (!son[rt][0]) {
      int cur = rt;
      rt = son[rt][1];
      fa[rt] = 0;
      Clear(cur);
      return;
   }
   if (!son[rt][1]) {
      int cur = rt;
      rt = son[rt][0];
      fa[rt] = 0;
      Clear(cur);
      return;
   }
   int p = GetPrev(), cur = rt;
   Splay(p);
   fa[son[cur][1]] = p;
    son[p][1] = son[cur][1];
   Clear(cur);
   Push(rt);
  }
};
3.10 SplayTreeArray
const int inf = "Edit"
const int maxn = "Edit";
struct SplayTree {
  // rt:Splay Tree 根节点
  int rt;
  // son[i][0]:i 节点的左孩子, son[i][0]:i 节点的右孩子
 int son[maxn][2];
  // fa[i]:i 节点的父节点
  int fa[maxn];
  // val[i]:i 节点的权值
  int val[maxn];
  // sz[i]: 以 i 节点为根的 Splay Tree 的节点数 (包含自身)
  int sz[maxn];
```

```
// 惰性标记数组
bool lazy[maxn];
void Push(int o) { sz[o] = sz[son[o][0]] + sz[son[o][1]] + 1; }
void Pull(int o) {
  if (lazy[o]) {
   std::swap(son[o][0], son[o][1]);
   if (son[o][0]) lazy[son[o][0]] ^= 1;
   if (son[o][1]) lazy[son[o][1]] ^= 1;
   lazy[o] = 0;
 }
}
// 判断 o 节点是其父节点的左孩子还是右孩子
bool Get(int o) { return son[fa[o]][1] == o; }
// 旋转节点 o
void Rotate(int o) {
 int p = fa[o], q = fa[p], ck = Get(o);
 Pull(p); Pull(o);
 son[p][ck] = son[o][ck ^ 1];
 fa[son[p][ck]] = fa[o];
 son[o][ck ^ 1] = fa[o];
 fa[p] = o;
 fa[o] = q;
 if (q) son[q][p == son[q][1]] = o;
 Push(p); Push(o);
}
// 旋转 o 节点到节点 tar
void Splay(int o, int tar = 0) {
 for (int cur = fa[o]; (cur = fa[o]) != tar; Rotate(o)) {
   Pull(fa[cur]); Pull(cur); Pull(o);
   if (fa[cur] != tar) {
     if (Get(o) == Get(cur)) Rotate(cur);
     else Rotate(o);
   }
 }
 if (!tar) rt = o;
// 获取以 r 为根节点 Splay Tree 中的第 k 大个元素在 Splay Tree 中的位置
int Kth(int r, int k) {
 Pull(r);
 int tmp = sz[son[r][0]] + 1;
 if (tmp == k) return r;
 if (tmp > k) return Kth(son[r][0], k);
 else return Kth(son[r][1], k - tmp);
```

```
}
// 获取 Splay Tree 中以 o 为根节点子树的最小值位置
int GetMin(int o) {
  Pull(o);
  while (son[o][0]) {
    o = son[o][0];
   Pull(o);
  }
  return o;
}
// 获取 Splay Tree 中以 o 为根节点子树的最大值位置
int GetMax(int o) {
  Pull(o);
  while (son[o][1]) {
    o = son[o][1];
   Pull(o);
  }
  return o;
}
// 求节点 o 的前驱节点
int GetPath(int o) {
  Splay(o, rt);
  int cur = son[rt][0];
  while (son[cur][1]) cur = son[cur][1];
  return cur;
}
// 求节点 o 的后继节点
int GetNext(int o) {
  Splay(o, rt);
  int cur = son[rt][1];
  while (son[cur][0]) cur = son[cur][0];
  return cur;
}
// 翻转 Splay Tree 中 l~r 区间
void Reverse(int 1, int r) {
  int o = Kth(rt, 1), Y = Kth(rt, r);
  Splay(o, 0); Splay(Y, o);
  lazy[son[Y][0]] ^= 1;
}
// 建立 Splay Tree
void Build(int 1, int r, int o) {
  if (1 > r) return;
  int m = (1 + r) >> 1;
```

```
Build(1, m - 1, m);
    Build(m + 1, r, m);
    fa[m] = o;
    val[m] = m - 1;
    lazy[m] = 0;
    Push(m);
    if (m < o) son[o][0] = m;
    else son[o][1] = m;
 }
  // 输出 Splay Tree
  void Print(int o) {
    Pull(o);
    if (son[o][0]) Print(son[o][0]);
    // 哨兵节点判断
    if (val[o] != -inf && val[o] != inf) printf("%d ", val[o]);
    if (val[son[o][1]]) Print(son[o][1]);
 }
};
3.11 TreeSplit
const int maxn = "Edit";
int n;
int arr[maxn];
int fa[maxn], dep[maxn];
int sz[maxn], son[maxn];
int rk[maxn], top[maxn];
int id[maxn];
int dfs_clock;
struct edge { int v, next; };
edge g[maxn << 1];</pre>
int tot;
int head[maxn];
void AddEdge(int u, int v) {
  g[tot] = (edge){v, head[u]};
 head[u] = tot++;
}
long long sum[maxn << 2];</pre>
long long lazy[maxn << 2];</pre>
void SegTreePull(int o) { sum[o] = sum[o << 1] + sum[o << 1 | 1]; }</pre>
void SegTreePush(int o, int 1, int r) {
  int m = (1 + r) >> 1;
```

```
if (lazy[o] != 0) {
    sum[o << 1] += (m - 1 + 1) * lazy[o];
    sum[o << 1 | 1] += (r - m) * lazy[o];
    lazy[o << 1] += lazy[o];</pre>
    lazy[o << 1 | 1] += lazy[o];</pre>
    lazy[o] = 0;
 }
}
void SegTreeBuild(int o, int 1, int r) {
  if (1 == r) {
    sum[o] = arr[rk[1]];
    return;
 }
  int m = (1 + r) >> 1;
 SegTreeBuild(o << 1, 1, m);</pre>
 SegTreeBuild(o \ll 1 | 1, m + 1, r);
 SegTreePull(o);
}
void SegTreeModify(int o, int l, int r, int ll, int rr, long long v) {
  if (ll <= l && rr >= r) {
    sum[o] += (r - 1 + 1) * v;
    lazy[o] += v;
    return;
 }
 SegTreePush(o, 1, r);
  int m = (1 + r) >> 1;
  if (ll <= m) SegTreeModify(o << 1, 1, m, ll, rr, v);</pre>
  if (rr > m) SegTreeModify(o << 1 | 1, m + 1, r, ll, rr, v);</pre>
 SegTreePull(o);
}
long long SegTreeQuery(int o, int l, int r, int ll, int rr) {
  if (ll <= l && rr >= r) return sum[o];
 SegTreePush(o, 1, r);
 int m = (1 + r) >> 1;
 long long ret = 0;
  if (ll <= m) ret += SegTreeQuery(o << 1, 1, m, ll, rr);</pre>
 if (rr > m) ret += SegTreeQuery(o << 1 | 1, m + 1, r, ll, rr);</pre>
 return ret;
}
void TreeSplitDfs1(int u, int p, int d) {
 fa[u] = p; dep[u] = d; sz[u] = 1;
 for (int i = head[u]; ~i; i = g[i].next) {
    int v = g[i].v;
    if (v == p) continue;
    TreeSplitDfs1(v, u, d + 1);
```

```
sz[u] += sz[v];
    if (sz[v] > sz[son[u]]) son[u] = v;
 }
}
void TreeSplitDfs2(int u, int tp) {
  top[u] = tp; id[u] = ++dfs_clock;
 rk[dfs_clock] = u;
  if (!son[u]) return;
 TreeSplitDfs2(son[u], tp);
 for (int i = head[u]; ~i; i = g[i].next) {
    int v = g[i].v;
    if (v == son[u] || v == fa[u]) continue;
    TreeSplitDfs2(v, v);
 }
}
long long TreeSplitQuery(int u, int v) {
 long long ret = 0;
 while (top[u] != top[v]) {
   if (dep[top[u]] < dep[top[v]]) std::swap(u, v);</pre>
   ret += SegTreeQuery(1, 1, n, id[top[u]], id[u]);
   u = fa[top[u]];
 }
  if (id[u] > id[v]) std::swap(u, v);
 ret += SegTreeQuery(1, 1, n, id[u], id[v]);
 return ret;
void TreeSplitModify(int u, int v, int c) {
  while (top[u] != top[v]) {
    if (dep[top[u]] < dep[top[v]]) std::swap(u, v);</pre>
   SegTreeModify(1, 1, n, id[top[u]], id[u], c);
   u = fa[top[u]];
 }
 if (id[u] > id[v]) std::swap(u, v);
 SegTreeModify(1, 1, n, id[u], id[v], c);
}
```

4 GraphTheory

4.1 AStar

```
const int inf = "Edit";
const int maxn = "Edit";
struct edge { int v, c, next; };
edge g[maxn << 1];</pre>
int head[maxn];
int tot;
edge rev_g[maxn << 1];</pre>
int rev_head[maxn];
int rev_tot;
void Init() {
 tot = 0;
 memset(head, -1, sizeof(head));
 rev_tot = 0;
 memset(rev_head, -1, sizeof(rev_head));
void AddEdge(int u, int v, int c) {
  g[tot] = edge {v, c, head[u]};
 head[u] = tot++;
 rev_g[rev_tot] = edge {u, c, rev_head[v]};
 rev_head[v] = rev_tot++;
int dis[maxn];
struct Cmp { bool operator() (const int &k1, const int &k2) { return dis[k1] >

    dis[k2]; } };

// 利用反向边图求各点到终点的最短路
void Dijkstra(int s) {
 priority_queue<int, vector<int>, Cmp> que;
 memset(dis, inf, sizeof(dis));
 dis[s] = 0;
 que.push(s);
 while (!que.empty()) {
   int u = que.top(); que.pop();
   for (int i = rev_head[u]; i != -1; i = rev_g[i].next) {
      if (dis[rev_g[i].v] > dis[u] + rev_g[i].c) {
        dis[rev_g[i].v] = dis[u] + rev_g[i].c;
        que.push(rev_g[i].v);
      }
   }
 }
```

```
}
struct node {
  int f, g, p;
 // k* 核心:f=g+H(p), 这里 H(p)=dis[p]
 bool operator < (const node &k) const {</pre>
    if (f == k.f) return g > k.g;
   return f > k.f;
 }
};
// A* 算法求起点 s 到终点 t 的第 k 短路
int AStar(int s, int t, int k) {
  int cnt = 0;
 priority_queue<node> que;
  // 注意特盘相同点是否算最短路
  if (s == t) k++;
  if (dis[s] == inf) return -1;
  que.push(node {dis[s], 0, s});
 while (!que.empty()) {
   node keep = que.top(); que.pop();
   if (keep.p == t) {
      cnt++;
      if (cnt == k) return keep.g;
   for (int i = head[keep.p]; i != -1; i = g[i].next) {
      node tmp;
      tmp.p = g[i].v;
      tmp.g = keep.g + g[i].c;
      tmp.f = tmp.g + dis[tmp.p];
      que.push(tmp);
   }
 }
 return -1;
4.2 MinimumSpanningTree
4.2.1 Kruskal
const int maxn = "Edit";
int n, pre[maxn];
struct edge { int u, v, c; };
bool operator < (edge k1 edge k2) { return k1.c < k2.c; }</pre>
std::vector<edge> g;
int Find(int x) { return pre[x] == x ? x : pre[x] = Find(pre[x]); }
void Union(int x, int y) { pre[Find(x)] = Find(y); }
```

```
int Kruskal() {
  std::sort(g.begin(), g.end());
  for (int i = 0; i <= n; ++i) pre[i] = i;
  int ret = 0;
  for (auto &e : g) {
    if (Find(e.u) != Find(e.v)) {
      Union(e.u, e.v);
      ret += e.c;
 }
 return ret;
}
4.2.2 Prim
const int inf = "Edit";
const int maxn = "Edit";
int n;
int dis[maxn];
int vis[maxn];
struct edge { int v, dis; };
std::vector<edge> g[maxn];
void AddEdge(int u, int v, int c) {
  g[u].push_back((edge){v, c});
 g[v].push_back((edge){u, c});
// Prim 算法
int Prim(int s) {
 memset(dis, inf, sizeof(dis));
 memset(vis, 0, sizeof(vis));
 dis[s] = 0;
  int ret = 0;
  for (int i = 1; i <= n; ++i) {
    int u = -1, min = inf;
    for (int j = 1; j \le n; ++j) {
      if (!vis[j] && dis[j] < min) {</pre>
        u = j;
        min = dis[j];
      }
    }
    vis[u] = 1;
    ret += min;
    for (int j = 0; j < int(g[u].size()); ++j) {</pre>
      int v = g[u][j].v;
      if (!vis[v] && g[u][j].dis < dis[v]) dis[v] = g[u][j].dis;
    }
```

```
}
 return ret;
4.3 NetFlow
4.3.1 Dinic
const int maxn = "Edit";
const int inf = "Edit";
struct edge { int v, flow, next; };
edge g[maxn << 2];</pre>
int tot;
int head[maxn];
int dep[maxn];
int cur[maxn];
void AddEdge(int u, int v, int flow, int rev = 0) {
  g[tot] = (edge){v, flow, head[u]};
 head[u] = tot++;
 g[tot] = (edge){u, rev, head[v]};
 head[v] = tot++;
}
bool Bfs(int s, int t) {
 memset(dep, -1, sizeof(dep));
 std::queue<int> que;
 dep[s] = 0;
  que.push(s);
  while (!que.empty()) {
    int u = que.front(); que.pop();
    for (int i = head[u]; ~i; i = g[i].next) {
      if (dep[g[i].v] == -1 \&\& g[i].flow > 0) {
        dep[g[i].v] = dep[u] + 1;
        que.push(g[i].v);
      }
    }
  }
 return dep[t] != -1;
}
int Dfs(int u, int t, int flow) {
  if (u == t || flow == 0) return flow;
  int max = 0, find_flow;
 for (int &i = cur[u]; ~i; i = g[i].next) {
    if (g[i].flow > 0 && dep[g[i].v] == dep[u] + 1) {
      find_flow = Dfs(g[i].v, t, std::min(flow - max, g[i].flow));
      if (find_flow > 0) {
        g[i].flow -= find_flow;
```

```
g[i ^ 1].flow += find_flow;
       max += find_flow;
       if (max == flow) return flow;
     }
   }
 }
 if (!max) dep[u] = -2;
 return max;
}
int Dinic(int s, int t) {
 int ret = 0;
 while (Bfs(s, t)) {
   for (int i = s; i <= t; ++i) cur[i] = head[i];</pre>
   ret += Dfs(s, t, inf);
 }
 return ret;
}
4.3.2 FordFulkerson
const int inf = "Edit";
const int maxn = "Edit";
int n, e;
bool vis[maxn];
int g[maxn] [maxn];
// Dfs 搜索增广路经,u: 当前搜索顶点,t: 搜索终点,now_flow: 当前最大流量
int Dfs(int u, int t, int now_flow) {
 if (u == t) return now_flow;
 vis[u] = true;
 for (int i = 1; i <= n; ++i) {
   if (!vis[i] && g[u][i]) {
     int FindFlow = Dfs(i, t, now_flow < g[u][i] ? now_flow : g[u][i]);</pre>
     if (!FindFlow) continue;
     g[u][i] -= FindFlow;
     g[i][u] += FindFlow;
     return FindFlow;
   }
 }
 return false;
// Ford-Fulkersone 算法, s: 起点, t: 终点
int FordFulkerson(int s, int t) {
 int max_flow = 0, Flow = 0;
 memset(vis, false, sizeof(vis));
 while (Flow = Dfs(s, t, inf)) {
   max_flow += Flow;
```

```
memset(vis, false, sizeof(vis));
 }
 return max_flow;
4.3.3 MaxFlow
const int inf = "Edit";
int s, t;
struct edge { int to, cap, rev; };
std::vector<std::vector<edge>> g;
std::vector<bool> vis;
void Init(int n) {
 s = 0; t = n;
 g.resize(n + 1);
}
void AddEdge(int u, int v, int cap, int rev = 0) {
  g[u].push_back((edge){v, cap, (int)g[v].size()});
 g[v].push_back((edge){u, rev, (int)g[u].size() - 1});
int Dfs(int u, int t, int flow) {
  if (u == t) return flow;
 vis[u] = true;
 for (edge &e : g[u]) {
   if (!vis[e.to] && e.cap > 0) {
      int f = Dfs(e.to, t, std::min(e.cap, flow));
      if (f > 0) {
        e.cap -= f;
        g[e.to][e.rev].cap += f;
        return f;
      }
    }
 }
 return 0;
}
int GetMaxFlow(int s, int t) {
 int ret = 0;
 while (true) {
   vis.assign(t + 1, false);
   int flow = Dfs(s, t, inf);
   if (flow == 0) return ret;
   ret += flow;
 }
}
```

4.3.4 MinCostMaxFlow

```
const int inf = "Edit";
const int maxn = "Edit";
struct edge { int v, cap, cost, flow, next; };
int n, e;
int head[maxn];
int path[maxn];
int dis[maxn];
bool vis[maxn];
int tot;
edge g[maxn];
void AddEdge(int u, int v, int cap, int cost) {
  g[tot] = (edge){v, cap, cost, 0, head[u]};
 head[u] = tot++;
 g[tot] = (edge)\{u, 0, -cost, 0, head[v]\};
 head[v] = tot++;
bool SPFA(int s, int t) {
  memset(dis, inf, sizeof(dis));
 memset(vis, false, sizeof(vis));
 memset(path, -1, sizeof(path));
 dis[s] = 0;
  vis[s] = true;
  std::queue<int> que;
  while (!que.empty()) que.pop();
 que.push(s);
  while (!que.empty()) {
    int U = que.front();
    que.pop();
    vis[U] = false;
    for (int i = head[U]; ~i; i = g[i].next) {
      int v = g[i].v;
      if (g[i].cap > g[i].flow && dis[v] > dis[U] + g[i].cost) {
        dis[v] = dis[U] + g[i].cost;
        path[v] = i;
        if (!vis[v]) {
          vis[v] = true;
          que.push(v);
        }
      }
    }
  }
  return path[t] != -1;
int MinCostMaxflow(int s, int t, int &min_cost) {
```

```
int max_flow = 0;
 min_cost = 0;
 while (SPFA(s, t)) {
   int min = inf;
   for (int i = path[t]; ~i; i = path[g[i ^ 1].v]) {
      if (g[i].cap - g[i].flow < min) min = g[i].cap - g[i].flow;
   for (int i = path[t]; ~i; i = path[g[i ^ 1].v]) {
      g[i].flow += min;
      g[i ^1].flow -= min;
     min_cost += g[i].cost * min;
   }
   max_flow += min;
 }
 return max_flow;
4.4 ShortestPath
4.4.1 BellmanFord
const int inf = "Edit";
const int maxn = "Edit";
int n;
struct edge { int u, v, dis; };
int dis[maxn];
std::vector<edge> g;
// Bellman Ford 算法判断是否存在负环回路
bool BellmanFord(int s) {
 memset(dis, inf, sizeof(dis));
 dis[s] = 0;
 // 最多做 N-1 次
 for (int i = 1; i < n; ++i) {
   bool flag = false;
   for (int j = 0; j < (int)g.size(); ++j) {</pre>
      if (dis[g[j].v] > dis[g[j].u] + g[j].dis) {
        dis[g[j].v] = dis[g[j].u] + g[j].dis;
        flag = true;
      }
   }
    if (!flag) return true;
 for (int j = 0; j < (int)g.size(); ++j) {</pre>
    if (dis[g[j].v] > dis[g[j].u] + g[j].dis) return false;
 }
 return true;
}
```

4.4.2 Dijkstra

```
const int maxn = "Edit";
const int inf = "Edit";
struct edge { int v, c, next; };
edge g[maxn << 1];</pre>
int head[maxn];
int tot;
int dis[maxn];
void AddEdge(int u, int v, int c) {
 g[tot] = (edge){v, c, head[u]};
 head[u] = tot++;
struct Cmp { bool operator() (const int &k1, const int &k2) { return dis[k1] >

    dis[k2]; };;

int n, e;
void Dijkstra(int s) {
  std::priority_queue<int, std::vector<int>, Cmp> que;
 memset(dis, inf, sizeof(dis));
 dis[s] = 0;
 que.push(s);
 while (!que.empty()) {
   int u = que.top(); que.pop();
   for (int i = head[u]; ~i; i = g[i].next) {
      if (dis[g[i].v] > dis[u] + g[i].c) {
        dis[g[i].v] = dis[u] + g[i].c;
        que.push(g[i].v);
      }
   }
 }
}
4.4.3 Floyd
const int maxn = "Edit";
int n;
int dis[maxn] [maxn];
void Floyd() {
 for (int k = 1; k \le n; ++k) {
   for (int i = 1; i <= n; ++i) {
      for (int j = 1; j \le n; ++j) {
        dis[i][j] = std::min(dis[i][j], dis[i][k] + dis[k][j]);
      }
```

```
}
  }
}
4.4.4 SPFA
const int inf = "Edit";
const int maxn = "Edit";
struct edge { int v, dis; };
int n, e;
bool vis[maxn];
int cnt[maxn];
int dis[maxn];
std::vector<edge> g[maxn];
void AddEdge (int u, int v, int c) {
  g[u].push_back((edge){v, c});
  g[v].push_back((edge){u, c});
}
bool SPFA(int s) {
  memset(vis, false, sizeof(vis));
  memset(dis, inf, sizeof(dis));
  memset(cnt, 0, sizeof(cnt));
  vis[s] = true;
  dis[s] = 0;
  cnt[s] = 1;
  std::queue<int> que;
  while (!que.empty()) que.pop();
  que.push(s);
  while (!que.empty()) {
    int U = que.front();
    que.pop();
    vis[U] = false;
    for (int i = 0; i < (int)g[U].size(); ++i) {</pre>
      int v = g[U][i].v;
      if (dis[v] > dis[U] + g[U][i].dis) {
        dis[v] = dis[U] + g[U][i].dis;
        if (!vis[v]) {
          vis[v] = true;
          que.push(v);
          if (++cnt[v] > N) return false;
        }
      }
    }
  }
  return true;
}
```

5 DynamicProgramming

5.1 Contour

```
const int maxn = "Edit";
int dp[2][1 << maxn];</pre>
void Update(int cur, int a, int b) {
  if (b & (1 << M)) dp[cur][b ^ (1 << M)] = dp[cur][b ^ (1 << M)] + dp[cur ^ 1][a];
// 轮廓线 dp(1*2 在 N*M 图上摆放数)
int Contour(int N, int M) {
 memset(dp, 0, sizeof(dp));
  int cur = 0;
 dp[cur][(1 << M) - 1] = 1;
  for (int i = 0; i < N; ++i) {
    for (int j = 0; j < M; ++j) {
      cur ^= 1;
      memset(dp[cur], 0, sizeof(dp[cur]));
      for (int k = 0; k < (1 << M); ++k) {
        Update(cur, k, k << 1);</pre>
        if (i && !(k & (1 << (M - 1)))) Update(cur, k, (k << 1) \hat{} (1 << M) \hat{} 1);
        if (j && (!(k & 1))) Update(cur, k, (k << 1) ^ 3);
      }
    }
  }
  return dp[cur][(1 << M) - 1];
5.2 Digit
const int maxn = "Edit";
int digit[25];
int dp[25] [maxn];
// site: 数位, status: 状态, pre: 前导零, limit: 数位上界
int Dfs(int site, int status, bool pre, bool limit) {
  if (site == 0) return ?;
  if (!limit && ~dp[site][status]) return dp[site][status];
  int max = limit ? digit[site] : 9;
  int ret = 0;
  for (int i = 0; i <= max; ++i) {
    int new_status = /* 状态转移 */;
    if (new_status?) ret += Dfs(site - 1, new_status, pre && i == 0, limit && i ==
    \rightarrow max);
  if (!limit) dp[site][status] = ret;
```

```
return ret;
}
int Get(int x) {
 int len = 0;
 while (x) {
   digit[++len] = x \% 10;
   x /= 10;
 }
 return Dfs(len, 0, true, true);
5.3 LCS
const int maxn = "Edit";
// dp[i][j]:str1[1]~str1[i] 和 str2[1]~str2[j] 对应的公共子序列长度
int dp[maxn] [maxn];
// 最长公共子序列 (LCS)
void GetLCS(std::string str1, std::string str2) {
 for (int i = 0; i < (int)str1.length(); ++i) {</pre>
   for (int j = 0; j < (int)str2.length(); ++j) {</pre>
      if (str1[i] == str2[j]) dp[i + 1][j + 1] = dp[i][j] + 1;
      else dp[i + 1][j + 1] = std::max(dp[i][j + 1], dp[i + 1][j]);
   }
 }
}
5.4 LIS
// 最长不下降子序列 (LIS), arr: 序列
int GetLIS(std::vector<int> &arr) {
  int ret = 1;
  // last[i]: 长度为 i 的不下降子序列末尾元素的最小值
 std::vector<int> last((int)arr.size(), 0);
 last[0] = arr[0];
 for (int i = 1; i < (int)arr.size(); ++i) {</pre>
   if (arr[i] >= last[ret]) last[++ret] = arr[i];
   else {
      int pos = std::upper_bound(last.begin(), last.end(), arr[i]) - last.begin();
      last[pos] = arr[i];
 }
 return ret;
}
5.5 Pack
const int maxn = "Edit";
```

```
int dp[maxn];
// cap: 背包容量, cnt: 总物品数
int cap, cnt;
// 01 背包, 代价为 cost, 获得的价值为 weight
void ZeroOnePack(int cost, int weight) {
 for (int i = cap; i \ge cost; --i) dp[i] = std::max(dp[i], dp[i - cost] + weight);
}
// 完全背包, 代价为 cost, 获得的价值为 weight
void CompletePack(int cost, int weight) {
 for (int i = cost; i <= cap; ++i) dp[i] = std::max(dp[i], dp[i - cost] + weight);</pre>
}
// 多重背包,代价为 cost, 获得的价值为 weight, 数量为 amount
void MultiplePack(int cost, int weight, int amount) {
  if (cost * amount >= cap) CompletePack(cost, weight);
 else {
   int k = 1;
   while (k < amount) {</pre>
     ZeroOnePack(k * cost, k * weight);
     amount -= k;
     k <<= 1;
   }
   ZeroOnePack(amount * cost, amount * weight);
 }
}
```

6 Geometry

6.1 DynamicConvexhull

```
// CodeForces 70D 动态凸包
#include <bits/stdc++.h>
typedef double db;
const int maxn = 1e5 + 5;
const db eps = 1e-9;
int Sgn(db k) { return fabs(k) < eps ? 0 : (k < 0 ? -1 : 1); }</pre>
int Cmp(db k1, db k2) { return Sgn(k1 - k2); }
struct point { db x, y; };
point operator - (point k1, point k2) { return (point){k1.x - k2.x, k1.y - k2.y}; }
point operator + (point k1, point k2) { return (point){k1.x + k2.x, k1.y + k2.y}; }
db operator * (point k1, point k2) { return k1.x * k2.x + k1.y * k2.y; }
db operator \hat{ } (point k1, point k2) { return k1.x * k2.y - k1.y * k2.x; }
db GetLen(point k) { return sqrt(k * k); }
int n;
point basic;
point p[maxn];
std::set<point> set;
bool operator < (point k1, point k2) {</pre>
  k1 = k1 - basic; k2 = k2 - basic;
  db Ang1 = atan2(k1.y, k1.x), Ang2 = atan2(k2.y, k2.x);
  db Len1 = GetLen(k1), Len2 = GetLen(k2);
  if (Cmp(Ang1, Ang2) != 0) return Cmp(Ang1, Ang2) < 0;</pre>
  return Cmp(Len1, Len2) < 0;</pre>
}
std::set<point>::iterator Prev(std::set<point>::iterator k) {
  if (k == set.begin()) k = set.end();
  return --k;
}
std::set<point>::iterator Next(std::set<point>::iterator k) {
  return k == set.end() ? set.begin() : k;
}
bool Query(point k) {
  std::set<point>::iterator it = set.lower_bound(k);
  if (it == set.end()) it = set.begin();
  return Sgn((k - *(Prev(it))) ^ (*(it) - *(Prev(it)))) <= 0;
void Insert(point k) {
  if (Query(k)) return;
```

```
set.insert(k);
 std::set<point>::iterator cur = Next(set.find(k));
 while (set.size() > 3 && Sgn((k - *(Next(cur))) ^ (*(cur) - *(Next(cur)))) <= 0)
  → {
   set.erase(cur);
   cur = Next(set.find(k));
 cur = Prev(set.find(k));
 while (set.size() > 3 && Sgn((k - *(cur)) ^{(*(cur) - *(Prev(cur))))} >= 0) {
   set.erase(cur);
    cur = Prev(set.find(k));
 }
}
int main() {
  scanf("%d", &n);
 basic.x = basic.y = 0.0;
 for (int i = 1, T; i \le 3; ++i) {
   scanf("%d%lf%lf", &T, &p[i].x, &p[i].y);
   basic.x += p[i].x; basic.y += p[i].y;
 }
 basic.x \neq 3.0; basic.y \neq 3.0;
 for (int i = 1; i <= 3; ++i) set.insert(p[i]);</pre>
 for (int i = 4, T; i <= n; ++i) {
   scanf("%d%lf%lf", &T, &p[i].x, &p[i].y);
   if (T == 1) Insert(p[i]);
   else {
      if (Query(p[i])) printf("YES\n");
      else printf("NO\n");
   }
 }
 return 0;
}
6.2 JlsGeo
#define mp make_pair
#define fi first
#define se second
#define pb push_back
typedef double db;
const db eps=1e-6;
const db pi=acos(-1);
int sign(db k){
  if (k>eps) return 1; else if (k<-eps) return -1; return 0;
int cmp(db k1,db k2){return sign(k1-k2);}
int inmid(db k1,db k2,db k3){return sign(k1-k3)*sign(k2-k3)<=0;}// k3 在 [k1,k2] 内
struct point{
```

```
db x,y;
  point operator + (const point &k1) const{return (point){k1.x+x,k1.y+y};}
  point operator - (const point &k1) const{return (point){x-k1.x,y-k1.y};}
  point operator * (db k1) const{return (point){x*k1,y*k1};}
  point operator / (db k1) const{return (point){x/k1,y/k1};}
  int operator == (const point &k1) const{return cmp(x,k1.x)==0&&cmp(y,k1.y)==0;}
  // 逆时针旋转
  point turn(db k1){return (point){x*cos(k1)-y*sin(k1),x*sin(k1)+y*cos(k1)};}
  point turn90(){return (point){-y,x};}
  bool operator < (const point k1) const{</pre>
    int a=cmp(x,k1.x);
    if (a==-1) return 1; else if (a==1) return 0; else return cmp(y,k1.y)==-1;
  }
  db abs(){return sqrt(x*x+y*y);}
  db abs2(){return x*x+y*y;}
  db dis(point k1){return ((*this)-k1).abs();}
  point unit(){db w=abs(); return (point){x/w,y/w};}
  void scan(){double k1,k2; scanf("%lf%lf",&k1,&k2); x=k1; y=k2;}
  void print(){printf("%.11lf %.11lf\n",x,y);}
  db getw(){return atan2(y,x);}
  point getdel(){if (sign(x)=-1||(sign(x)==0\&\&sign(y)==-1)) return (*this)*(-1);

    else return (*this);}

  int getP() const{return sign(y)==1||(sign(y)==0&&sign(x)==-1);}
};
int inmid(point k1,point k2,point k3){return
\rightarrow inmid(k1.x,k2.x,k3.x)&&inmid(k1.y,k2.y,k3.y);}
db cross(point k1, point k2){return k1.x*k2.y-k1.y*k2.x;}
db dot(point k1,point k2){return k1.x*k2.x+k1.y*k2.y;}
db rad(point k1, point k2) {return atan2(cross(k1, k2), dot(k1, k2));}
// -pi \rightarrow pi
int compareangle (point k1,point k2){
  return k1.getP()<k2.getP()||(k1.getP()==k2.getP()&&sign(cross(k1,k2))>0);
point proj(point k1, point k2, point q){ // q 到直线 k1, k2 的投影
  point k=k2-k1; return k1+k*(dot(q-k1,k)/k.abs2());
point reflect(point k1,point k2,point q){return proj(k1,k2,q)*2-q;}
int clockwise(point k1, point k2, point k3) {// k1 k2 k3 逆时针 1 顺时针 -1 否则 0
  return sign(cross(k2-k1,k3-k1));
int checkLL(point k1, point k2, point k3, point k4) {// 求直线 (L) 线段 (S)k1, k2 和
→ k3,k4 的交点
  return cmp(cross(k3-k1,k4-k1),cross(k3-k2,k4-k2))!=0;
point getLL(point k1,point k2,point k3,point k4){
  db w1=cross(k1-k3,k4-k3), w2=cross(k4-k3,k2-k3); return (k1*w2+k2*w1)/(w1+w2);
int intersect(db 11,db r1,db 12,db r2){
  if (11>r1) swap(11,r1); if (12>r2) swap(12,r2); return
  \rightarrow cmp(r1,12)!=-1&&cmp(r2,11)!=-1;
```

```
}
int checkSS(point k1,point k2,point k3,point k4){
  return intersect(k1.x,k2.x,k3.x,k4.x)&&intersect(k1.y,k2.y,k3.y,k4.y)&&
  sign(cross(k3-k1,k4-k1))*sign(cross(k3-k2,k4-k2)) <= 0 \& \&
  sign(cross(k1-k3,k2-k3))*sign(cross(k1-k4,k2-k4))<=0;
}
db disSP(point k1,point k2,point q){
 point k3=proj(k1,k2,q);
  if (inmid(k1,k2,k3)) return q.dis(k3); else return min(q.dis(k1),q.dis(k2));
db disSS(point k1,point k2,point k3,point k4){
  if (checkSS(k1,k2,k3,k4)) return 0;
  else return
  \rightarrow min(min(disSP(k1,k2,k3),disSP(k1,k2,k4)),min(disSP(k3,k4,k1),disSP(k3,k4,k2)));
int onS(point k1,point k2,point q){return
\rightarrow inmid(k1,k2,q)&&sign(cross(k1-q,k2-k1))==0;}
struct circle{
 point o; db r;
 void scan(){o.scan(); scanf("%lf",&r);}
 int inside(point k){return cmp(r,o.dis(k));}
};
struct line{
  // p[0]->p[1]
 point p[2];
 line(point k1,point k2){p[0]=k1; p[1]=k2;}
 point& operator [] (int k){return p[k];}
  int include(point k){return sign(cross(p[1]-p[0],k-p[0]))>0;}
 point dir(){return p[1]-p[0];}
  line push(){ // 向外 (左手边 ) 平移 eps
    const db eps = 1e-6;
   point delta=(p[1]-p[0]).turn90().unit()*eps;
    return {p[0]-delta,p[1]-delta};
  }
point getLL(line k1,line k2){return getLL(k1[0],k1[1],k2[0],k2[1]);}
int parallel(line k1,line k2){return sign(cross(k1.dir(),k2.dir()))==0;}
int sameDir(line k1,line k2){return
\rightarrow parallel(k1,k2)&&sign(dot(k1.dir(),k2.dir()))==1;}
int operator < (line k1,line k2){</pre>
  if (sameDir(k1,k2)) return k2.include(k1[0]);
  return compareangle(k1.dir(),k2.dir());
}
int checkpos(line k1,line k2,line k3){return k3.include(getLL(k1,k2));}
vector<line> getHL(vector<line> &L){ // 求半平面交 ,半平面是逆时针方向 ,输出按照逆
→ 时针
  sort(L.begin(),L.end()); deque<line> q;
  for (int i=0;i<(int)L.size();i++){</pre>
    if (i&&sameDir(L[i],L[i-1])) continue;
```

```
while (q.size()>1\&\&!checkpos(q[q.size()-2],q[q.size()-1],L[i])) q.pop_back();
   while (q.size()>1&&!checkpos(q[1],q[0],L[i])) q.pop_front();
   q.push_back(L[i]);
 }
 while (q.size()>2\&\&!checkpos(q[q.size()-2],q[q.size()-1],q[0])) q.pop_back();
 while (q.size()>2&&!checkpos(q[1],q[0],q[q.size()-1])) q.pop_front();
 vector<line>ans; for (int i=0;i<q.size();i++) ans.push_back(q[i]);</pre>
 return ans;
db closepoint(vector<point>&A,int 1,int r){ // 最近点对 , 先要按照 x 坐标排序
 if (r-1<=5){
   db ans=1e20;
   for (int i=1;i<=r;i++) for (int j=i+1;j<=r;j++) ans=min(ans,A[i].dis(A[j]));
   return ans;
 }
 int mid=l+r>>1; db ans=min(closepoint(A,1,mid),closepoint(A,mid+1,r));
 vector<point>B; for (int i=1;i<=r;i++) if (abs(A[i].x-A[mid].x)<=ans)</pre>
  → B.push_back(A[i]);
 sort(B.begin(),B.end(),[](point k1,point k2){return k1.y<k2.y;});</pre>
 for (int i=0;i<B.size();i++) for (int j=i+1;j<B.size()&&B[j].y-B[i].y<ans;j++)

→ ans=min(ans,B[i].dis(B[j]));
 return ans;
}
int checkposCC(circle k1, circle k2) {// 返回两个圆的公切线数量
 if (cmp(k1.r,k2.r)=-1) swap(k1,k2);
 db dis=k1.o.dis(k2.o); int w1=cmp(dis,k1.r+k2.r),w2=cmp(dis,k1.r-k2.r);
 if (w1>0) return 4; else if (w1==0) return 3; else if (w2>0) return 2;
 else if (w2==0) return 1; else return 0;
vector<point> getCL(circle k1,point k2,point k3){ // 沿着 k2->k3 方向给出 , 相切给出
→ 两个
 point k=proj(k2,k3,k1.o); db d=k1.r*k1.r-(k-k1.o).abs2();
 if (sign(d)==-1) return {};
 point del=(k3-k2).unit()*sqrt(max((db)0.0,d)); return {k-del,k+del};
vector<point> getCC(circle k1, circle k2){// 沿圆 k1 逆时针给出 , 相切给出两个
 int pd=checkposCC(k1,k2); if (pd==0||pd==4) return {};
  \Rightarrow a=(k2.o-k1.o).abs2(),cosA=(k1.r*k1.r+a-k2.r*k2.r)/(2*k1.r*sqrt(max(a,(db)0.0)));
 db b=k1.r*cosA, c=sqrt(max((db)0.0, k1.r*k1.r-b*b));
 point k=(k2.o-k1.o).unit(),m=k1.o+k*b,del=k.turn90()*c;
 return {m-del,m+del};
}
vector<point> TangentCP(circle k1,point k2){// 沿圆 k1 逆时针给出
 db a=(k2-k1.o).abs(),b=k1.r*k1.r/a,c=sqrt(max((db)0.0,k1.r*k1.r-b*b));
 point k=(k2-k1.o).unit(),m=k1.o+k*b,del=k.turn90()*c;
 return {m-del,m+del};
vector<line> TangentoutCC(circle k1,circle k2){
```

```
int pd=checkposCC(k1,k2); if (pd==0) return {};
  if (pd==1){point k=getCC(k1,k2)[0]; return {(line){k,k}};}
  if (cmp(k1.r,k2.r)==0){
   point del=(k2.o-k1.o).unit().turn90().getdel();
   return
    \rightarrow \{(line)\{k1.o-del*k1.r,k2.o-del*k2.r\},(line)\{k1.o+del*k1.r,k2.o+del*k2.r\}\};
 } else {
   point p=(k2.0*k1.r-k1.0*k2.r)/(k1.r-k2.r);
   vector<point>A=TangentCP(k1,p),B=TangentCP(k2,p);
   vector<line>ans; for (int i=0;i<A.size();i++) ans.push_back((line){A[i],B[i]});</pre>
   return ans;
 }
}
vector<line> TangentinCC(circle k1,circle k2){
  int pd=checkposCC(k1,k2); if (pd<=2) return {};</pre>
  if (pd==3){point k=getCC(k1,k2)[0]; return {(line){k,k}};}
 point p=(k2.0*k1.r+k1.0*k2.r)/(k1.r+k2.r);
  vector<point>A=TangentCP(k1,p),B=TangentCP(k2,p);
 vector<line>ans; for (int i=0;i<A.size();i++) ans.push_back((line){A[i],B[i]});</pre>
 return ans;
}
vector<line> TangentCC(circle k1,circle k2){
  int flag=0; if (k1.r<k2.r) swap(k1,k2),flag=1;</pre>
  vector<line>A=TangentoutCC(k1,k2),B=TangentinCC(k1,k2);
  for (line k:B) A.push_back(k);
  if (flag) for (line \&k:A) swap(k[0],k[1]);
 return A;
}
db getarea(circle k1,point k2,point k3){
  // 圆 k1 与三角形 k2 k3 k1.o 的有向面积交
 point k=k1.o; k1.o=k1.o-k; k2=k2-k; k3=k3-k;
  int pd1=k1.inside(k2),pd2=k1.inside(k3);
 vector<point>A=getCL(k1,k2,k3);
  if (pd1>=0){
   if (pd2>=0) return cross(k2,k3)/2;
   return k1.r*k1.r*rad(A[1],k3)/2+cross(k2,A[1])/2;
  } else if (pd2>=0){
   return k1.r*k1.r*rad(k2,A[0])/2+cross(A[0],k3)/2;
 }else {
    int pd=cmp(k1.r,disSP(k2,k3,k1.o));
    if (pd<=0) return k1.r*k1.r*rad(k2,k3)/2;</pre>
    return cross(A[0],A[1])/2+k1.r*k1.r*(rad(k2,A[0])+rad(A[1],k3))/2;
 }
}
circle getcircle(point k1,point k2,point k3){
 db a1=k2.x-k1.x, b1=k2.y-k1.y, c1=(a1*a1+b1*b1)/2;
 db a2=k3.x-k1.x, b2=k3.y-k1.y, c2=(a2*a2+b2*b2)/2;
 db d=a1*b2-a2*b1;
 point o=(point)\{k1.x+(c1*b2-c2*b1)/d,k1.y+(a1*c2-a2*c1)/d\};
```

```
return (circle){o,k1.dis(o)};
}
circle getScircle(vector<point> A){
  random_shuffle(A.begin(), A.end());
  circle ans=(circle){A[0],0};
 for (int i=1;i<A.size();i++)</pre>
    if (ans.inside(A[i])==-1){
      ans=(circle){A[i],0};
      for (int j=0; j<i; j++)</pre>
        if (ans.inside(A[j])==-1){
          ans.o=(A[i]+A[j])/2; ans.r=ans.o.dis(A[i]);
          for (int k=0;k<j;k++)</pre>
            if (ans.inside(A[k])==-1)
              ans=getcircle(A[i],A[j],A[k]);
        }
    }
 return ans;
}
db area(vector<point> A){ // 多边形用 vector<point> 表示 , 逆时针
 db ans=0;
 for (int i=0;i<A.size();i++) ans+=cross(A[i],A[(i+1)%A.size()]);</pre>
 return ans/2;
int checkconvex(vector<point>A){
  int n=A.size(); A.push_back(A[0]); A.push_back(A[1]);
 for (int i=0; i<n; i++) if (sign(cross(A[i+1]-A[i],A[i+2]-A[i]))==-1) return 0;
 return 1;
}
int contain(vector<point>A, point q){ // 2 内部 1 边界 0 外部
  int pd=0; A.push_back(A[0]);
  for (int i=1;i<A.size();i++){</pre>
    point u=A[i-1], v=A[i];
    if (onS(u,v,q)) return 1; if (cmp(u.y,v.y)>0) swap(u,v);
    if (cmp(u.y,q.y) \ge 0 \mid |cmp(v.y,q.y) \le 0) continue;
    if (sign(cross(u-v,q-v))<0) pd<sup>=1</sup>;
 }
 return pd<<1;
}
vector<point> ConvexHull(vector<point>A, int flag=1){ // flag=0 不严格 flag=1 严格
  int n=A.size(); vector<point>ans(n*2);
  sort(A.begin(), A.end()); int now=-1;
 for (int i=0;i<A.size();i++){</pre>
    while (now>0&&sign(cross(ans[now]-ans[now-1],A[i]-ans[now-1]))<flag) now--;
    ans [++now] = A[i];
  } int pre=now;
 for (int i=n-2;i>=0;i--){
    while (now>pre&&sign(cross(ans[now]-ans[now-1],A[i]-ans[now-1]))<flag) now--;
    ans [++now] = A[i];
 } ans.resize(now); return ans;
```

```
}
db convexDiameter(vector<point>A){
  int now=0,n=A.size(); db ans=0;
 for (int i=0;i<A.size();i++){</pre>
   now=max(now,i);
   while (1){
      db k1=A[i].dis(A[now%n]), k2=A[i].dis(A[(now+1)%n]);
      ans=max(ans,max(k1,k2)); if (k2>k1) now++; else break;
   }
 return ans;
}
vector<point> convexcut(vector<point>A,point k1,point k2){
  // 保留 k1,k2,p 逆时针的所有点
  int n=A.size(); A.push_back(A[0]); vector<point>ans;
 for (int i=0;i<n;i++){</pre>
    int w1=clockwise(k1,k2,A[i]),w2=clockwise(k1,k2,A[i+1]);
   if (w1>=0) ans.push_back(A[i]);
    if (w1*w2<0) ans.push_back(getLL(k1,k2,A[i],A[i+1]));</pre>
 }
 return ans;
int checkPoS(vector<point>A,point k1,point k2){
  // 多边形 A 和直线 ( 线段 )k1->k2 严格相交 , 注释部分为线段
 struct ins{
   point m,u,v;
    int operator < (const ins& k) const {return m<k.m;}</pre>
  }; vector<ins>B;
  //if (contain(A, k1)==2//contain(A, k2)==2) return 1;
 vector<point>poly=A; A.push_back(A[0]);
 for (int i=1;i<A.size();i++) if (checkLL(A[i-1],A[i],k1,k2)){
   point m=getLL(A[i-1],A[i],k1,k2);
   if (inmid(A[i-1],A[i],m)/*@inmid(k1,k2,m)*/)
    \rightarrow B.push_back((ins){m,A[i-1],A[i]});
 }
  if (B.size()==0) return 0; sort(B.begin(),B.end());
  int now=1; while (now<B.size()&&B[now].m==B[0].m) now++;</pre>
  if (now==B.size()) return 0;
  int flag=contain(poly,(B[0].m+B[now].m)/2);
  if (flag==2) return 1;
 point d=B[now].m-B[0].m;
 for (int i=now;i<B.size();i++){</pre>
    if (!(B[i].m==B[i-1].m)&&flag==2) return 1;
    int tag=sign(cross(B[i].v-B[i].u,B[i].m+d-B[i].u));
    if (B[i].m==B[i].u||B[i].m==B[i].v) flag+=tag; else flag+=tag*2;
  }
  //return 0;
  return flag==2;
```

```
int checkinp(point r,point l,point m){
  if (compareangle(1,r)){return compareangle(1,m)&&compareangle(m,r);}
 return compareangle(1,m)||compareangle(m,r);
}
int checkPosFast(vector<point>A,point k1,point k2){ // 快速检查线段是否和多边形严格
→ 相交
 if (contain(A,k1)=2||contain(A,k2)=2) return 1; if (k1=-k2) return 0;
 A.push_back(A[0]); A.push_back(A[1]);
 for (int i=1;i+1<A.size();i++)</pre>
   if (checkLL(A[i-1],A[i],k1,k2)){
     point now=getLL(A[i-1],A[i],k1,k2);
     if (inmid(A[i-1],A[i],now)==0||inmid(k1,k2,now)==0) continue;
     if (now==A[i]){
       if (A[i] == k2) continue;
       point pre=A[i-1],ne=A[i+1];
       if (checkinp(pre-now,ne-now,k2-now)) return 1;
     } else if (now==k1){
       if (k1==A[i-1]|k1==A[i]) continue;
       if (checkinp(A[i-1]-k1,A[i]-k1,k2-k1)) return 1;
     } else if (now==k2||now==A[i-1]) continue;
     else return 1;
   }
 return 0;
}
// 拆分凸包成上下凸壳 凸包尽量都随机旋转一个角度来避免出现相同横坐标
// 尽量特判只有一个点的情况 凸包逆时针
void getUDP(vector<point>A,vector<point>&U,vector<point>&D){
 db l=1e100,r=-1e100;
 for (int i=0;i<A.size();i++) l=min(1,A[i].x),r=max(r,A[i].x);</pre>
 int wherel, wherer;
 for (int i=0; i<A.size(); i++) if (cmp(A[i].x,1)==0) where l=i;
 for (int i=A.size();i;i--) if (cmp(A[i-1].x,r)==0) wherer=i-1;
 U.clear(); D.clear(); int now=wherel;
 while (1){D.push_back(A[now]); if (now==wherer) break; now++; if (now>=A.size())
  \rightarrow now=0;}
 now=wherel;
 while (1){U.push_back(A[now]); if (now==wherer) break; now--; if (now<0)</pre>
  \rightarrow now=A.size()-1;}
// 需要保证凸包点数大于等于 3,2 内部 ,1 边界 ,0 外部
int containCoP(const vector<point>&U,const vector<point>&D,point k){
 db lx=U[0].x,rx=U[U.size()-1].x;
 if (k==U[0]||k==U[U.size()-1]) return 1;
 if (cmp(k.x,lx)=-1||cmp(k.x,rx)==1) return 0;
 int where1=lower_bound(U.begin(),U.end(),(point){k.x,-1e100})-U.begin();
 int where2=lower_bound(D.begin(),D.end(),(point){k.x,-1e100})-D.begin();
 int w1=clockwise(U[where1-1],U[where1],k),w2=clockwise(D[where2-1],D[where2],k);
 if (w1==1||w2==-1) return 0; else if (w1==0||w2==0) return 1; return 2;
```

```
// a 是方向 , 输出上方切点和下方切点
pair<point, point> getTangentCow(const vector<point> &U,const vector<point> &D,point
\rightarrow d){
  if (sign(d.x)<0||(sign(d.x)==0\&\&sign(d.y)<0)) d=d*(-1);
  point whereU, whereD;
  if (sign(d.x)==0) return mp(U[0],U[U.size()-1]);
  int l=0,r=U.size()-1,ans=0;
  while (1<r){int mid=1+r>>1; if (sign(cross(U[mid+1]-U[mid],d))<=0)
  → l=mid+1,ans=mid+1; else r=mid;}
  where U=U[ans]; l=0, r=D. size()-1, ans=0;
  while (1<r){int mid=1+r>>1; if (sign(cross(D[mid+1]-D[mid],d))>=0)
  → l=mid+1,ans=mid+1; else r=mid;}
  whereD=D[ans]; return mp(whereU, whereD);
}
// 先检查 contain, 逆时针给出
pair<point,point> getTangentCoP(const vector<point>&U,const vector<point>&D,point
\rightarrow k){
 db lx=U[0].x,rx=U[U.size()-1].x;
  if (k.x<lx){
    int l=0,r=U.size()-1,ans=U.size()-1;
    while (1<r){int mid=1+r>>1; if (clockwise(k,U[mid],U[mid+1])=1) 1=mid+1; else

    ans=mid,r=mid;
}
    point w1=U[ans]; l=0,r=D.size()-1,ans=D.size()-1;
    while (1<r){int mid=1+r>>1; if (clockwise(k,D[mid],D[mid+1])=-1) 1=mid+1; else

→ ans=mid,r=mid;}
    point w2=D[ans]; return mp(w1,w2);
  } else if (k.x>rx){
    int l=1,r=U.size(),ans=0;
    while (1<r){int mid=1+r>>1; if (clockwise(k,U[mid],U[mid-1])==-1) r=mid; else
    \rightarrow ans=mid, l=mid+1;}
    point w1=U[ans]; l=1,r=D.size(),ans=0;
    while (1<r)\{int mid=1+r>>1; if (clockwise(k,D[mid],D[mid-1])==1) r=mid; else

    ans=mid,l=mid+1;}

    point w2=D[ans]; return mp(w2,w1);
  } else {
    int where1=lower_bound(U.begin(),U.end(),(point){k.x,-1e100})-U.begin();
    int where2=lower_bound(D.begin(),D.end(),(point){k.x,-1e100})-D.begin();
    if ((k.x==lx\&\&k.y>U[0].y)||(where1\&\&clockwise(U[where1-1],U[where1],k)==1)){
      int l=1,r=where1+1,ans=0;
      while (1<r){int mid=1+r>>1; if (clockwise(k,U[mid],U[mid-1])==1)
         ans=mid,l=mid+1; else r=mid;}
      point w1=U[ans]; l=where1,r=U.size()-1,ans=U.size()-1;
      while (1<r){int mid=1+r>>1; if (clockwise(k,U[mid],U[mid+1])==1) 1=mid+1;
      → else ans=mid,r=mid;}
      point w2=U[ans]; return mp(w2,w1);
    } else {
      int l=1,r=where2+1,ans=0;
      while (1<r){int mid=1+r>>1; if (clockwise(k,D[mid],D[mid-1])==-1)
      → ans=mid,l=mid+1; else r=mid;}
```

```
point w1=D[ans]; l=where2,r=D.size()-1,ans=D.size()-1;
      while (1<r){int mid=1+r>>1; if (clockwise(k,D[mid],D[mid+1])==-1) 1=mid+1;
      \rightarrow else ans=mid,r=mid;}
      point w2=D[ans]; return mp(w1,w2);
 }
}
struct P3{
  db x,y,z;
 P3 operator + (P3 k1){return (P3){x+k1.x,y+k1.y,z+k1.z};}
  P3 operator - (P3 k1){return (P3){x-k1.x,y-k1.y,z-k1.z};}
  P3 operator * (db k1){return (P3){x*k1,y*k1,z*k1};}
  P3 operator / (db k1){return (P3){x/k1,y/k1,z/k1};}
  db abs2(){return x*x+y*y+z*z;}
  db abs(){return sqrt(x*x+y*y+z*z);}
  P3 unit(){return (*this)/abs();}
  int operator < (const P3 k1) const{</pre>
    if (cmp(x,k1.x)!=0) return x<k1.x;
    if (cmp(y,k1.y)!=0) return y<k1.y;
    return cmp(z,k1.z) == -1;
  }
  int operator == (const P3 k1){
    return cmp(x,k1.x) == 0 \&\&cmp(y,k1.y) == 0 \&\&cmp(z,k1.z) == 0;
  }
  void scan(){
    double k1,k2,k3; scanf("%lf%lf",&k1,&k2,&k3);
    x=k1; y=k2; z=k3;
 }
};
P3 cross(P3 k1,P3 k2){return
\rightarrow (P3) \{k1.y*k2.z-k1.z*k2.y,k1.z*k2.x-k1.x*k2.z,k1.x*k2.y-k1.y*k2.x\};\}
db dot(P3 k1,P3 k2){return k1.x*k2.x+k1.y*k2.y+k1.z*k2.z;}
//p=(3,4,5), l=(13,19,21), theta=85 ans=(2.83,4.62,1.77)
P3 turn3D(db k1,P3 1,P3 p){
  l=1.unit(); P3 ans; db c=cos(k1), s=sin(k1);
  ans.x=p.x*(1.x*1.x*(1-c)+c)+p.y*(1.x*1.y*(1-c)-1.z*s)+p.z*(1.x*1.z*(1-c)+1.y*s);
  ans.y=p.x*(1.x*1.y*(1-c)+1.z*s)+p.y*(1.y*1.y*(1-c)+c)+p.z*(1.y*1.z*(1-c)-1.x*s);
  ans.z=p.x*(1.x*1.z*(1-c)-1.y*s)+p.y*(1.y*1.z*(1-c)+1.x*s)+p.z*(1.x*1.x*(1-c)+c);
  return ans;
typedef vector<P3> VP;
typedef vector<VP> VVP;
db Acos(db x){return acos(max(-(db)1,min(x,(db)1)));}
// 球面距离 , 圆心原点 , 半径 1
db Odist(P3 a,P3 b){db r=Acos(dot(a,b)); return r;}
db r; P3 rnd;
vector<db> solve(db a,db b,db c){
  db r=sqrt(a*a+b*b),th=atan2(b,a);
  if (cmp(c,-r)==-1) return \{0\};
```

```
else if (cmp(r,c) \le 0) return \{1\};
  else {
    db tr=pi-Acos(c/r); return {th+pi-tr,th+pi+tr};
  }
vector<db> jiao(P3 a,P3 b){
  // dot(rd+x*cos(t)+y*sin(t),b) >= cos(r)
  if (cmp(Odist(a,b),2*r)>0) return \{0\};
 P3 rd=a*cos(r),z=a.unit(),y=cross(z,rnd).unit(),x=cross(y,z).unit();
  vector<db> ret =
  \Rightarrow solve(-(dot(x,b)*sin(r)),-(dot(y,b)*sin(r)),-(cos(r)-dot(rd,b)));
 return ret;
}
db norm(db x,db l=0,db r=2*pi){ // change x into [l,r)
  while (cmp(x,1)==-1) x+=(r-1); while (cmp(x,r)>=0) x-=(r-1);
  return x;
db disLP(P3 k1,P3 k2,P3 q){
  return (cross(k2-k1,q-k1)).abs()/(k2-k1).abs();
db disLL(P3 k1,P3 k2,P3 k3,P3 k4){
 P3 dir=cross(k2-k1,k4-k3); if (sign(dir.abs())==0) return disLP(k1,k2,k3);
  return fabs(dot(dir.unit(),k1-k2));
VP getFL(P3 p,P3 dir,P3 k1,P3 k2){
  db a=dot(k2-p,dir),b=dot(k1-p,dir),d=a-b;
  if (sign(fabs(d))==0) return {};
  return \{(k1*a-k2*b)/d\};
VP getFF(P3 p1,P3 dir1,P3 p2,P3 dir2){// 返回一条线
  P3 e=cross(dir1,dir2),v=cross(dir1,e);
  db d=dot(dir2,v); if (sign(abs(d))==0) return {};
  P3 q=p1+v*dot(dir2,p2-p1)/d; return \{q,q+e\};
// 3D Covex Hull Template
db getV(P3 k1,P3 k2,P3 k3,P3 k4){ // get the Volume
  return dot(cross(k2-k1,k3-k1),k4-k1);
}
db rand_db(){return 1.0*rand()/RAND_MAX;}
VP convexHull2D(VP A,P3 dir){
  P3 x={(db)rand(),(db)rand()}; x=x.unit();
  x=cross(x,dir).unit(); P3 y=cross(x,dir).unit();
 P3 vec=dir.unit()*dot(A[0],dir);
  vector<point>B;
  for (int i=0;i<A.size();i++) B.push_back((point){dot(A[i],x),dot(A[i],y)});</pre>
  B=ConvexHull(B); A.clear();
  for (int i=0;i<B.size();i++) A.push_back(x*B[i].x+y*B[i].y+vec);</pre>
  return A;
```

```
namespace CH3{
 VVP ret; set<pair<int,int> >e;
  int n; VP p,q;
 void wrap(int a,int b){
    if (e.find({a,b})==e.end()){
      int c=-1;
      for (int i=0;i<n;i++) if (i!=a&&i!=b){
        if (c==-1||sign(getV(q[c],q[a],q[b],q[i]))>0) c=i;
      }
      if (c!=-1){
        ret.push_back({p[a],p[b],p[c]});
        e.insert({a,b}); e.insert({b,c}); e.insert({c,a});
        wrap(c,b); wrap(a,c);
      }
   }
 }
 VVP ConvexHull3D(VP _p){
   p=q=_p; n=p.size();
   ret.clear(); e.clear();
   for (auto &i:q) i=i+(P3){rand_db()*1e-4,rand_db()*1e-4,rand_db()*1e-4};
   for (int i=1; i < n; i++) if (q[i].x<q[0].x) swap(p[0],p[i]),swap(q[0],q[i]);
   for (int i=2;i<n;i++) if
    ((q[i].x-q[0].x)*(q[1].y-q[0].y)>(q[i].y-q[0].y)*(q[1].x-q[0].x))
    \rightarrow swap(q[1],q[i]),swap(p[1],p[i]);
   wrap(0,1);
   return ret;
 }
}
VVP reduceCH(VVP A){
 VVP ret; map<P3,VP> M;
 for (VP nowF:A){
   P3 dir=cross(nowF[1]-nowF[0],nowF[2]-nowF[0]).unit();
   for (P3 k1:nowF) M[dir].pb(k1);
 for (pair<P3,VP> nowF:M) ret.pb(convexHull2D(nowF.se,nowF.fi));
 return ret;
}
// 把一个面变成 (点, 法向量)的形式
pair<P3,P3> getF(VP F){
 return mp(F[0],cross(F[1]-F[0],F[2]-F[0]).unit());
// 3D Cut 保留 dot(dir,x-p)>=0 的部分
VVP ConvexCut3D(VVP A,P3 p,P3 dir){
 VVP ret; VP sec;
 for (VP nowF: A){
    int n=nowF.size(); VP ans; int dif=0;
   for (int i=0;i<n;i++){</pre>
      int d1=sign(dot(dir,nowF[i]-p));
      int d2=sign(dot(dir,nowF[(i+1)%n]-p));
```

```
if (d1>=0) ans.pb(nowF[i]);
      if (d1*d2<0){
        P3 q=getFL(p,dir,nowF[i],nowF[(i+1)%n])[0];
        ans.push_back(q); sec.push_back(q);
      if (d1==0) sec.push_back(nowF[i]); else dif=1;
      dif = (sign(dot(dir, cross(nowF[(i+1)\%n] - nowF[i], nowF[(i+1)\%n] - nowF[i]))) = -1);
    }
    if (ans.size()>0&&dif) ret.push_back(ans);
  if (sec.size()>0) ret.push_back(convexHull2D(sec,dir));
  return ret;
}
db vol(VVP A){
  if (A.size()==0) return 0; P3 p=A[0][0]; db ans=0;
  for (VP nowF:A)
    for (int i=2;i<nowF.size();i++)</pre>
      ans+=abs(getV(p,nowF[0],nowF[i-1],nowF[i]));
  return ans/6;
VVP init(db INF) {
 VVP pss(6, VP(4));
 pss[0][0] = pss[1][0] = pss[2][0] = {-INF, -INF, -INF};
  pss[0][3] = pss[1][1] = pss[5][2] = {-INF, -INF, INF};
  pss[0][1] = pss[2][3] = pss[4][2] = {-INF, INF, -INF};
 pss[0][2] = pss[5][3] = pss[4][1] = {-INF, INF, INF};
 pss[1][3] = pss[2][1] = pss[3][2] = {INF, -INF, -INF};
 pss[1][2] = pss[5][1] = pss[3][3] = {INF, -INF, INF};
  pss[2][2] = pss[4][3] = pss[3][1] = {INF, INF, -INF};
 pss[5][0] = pss[4][0] = pss[3][0] = {INF, INF};
 return pss;
}
6.3 Pick
/*
  polygon:
    S = in + (on / 2) - 1
6.4 Plane
namespace Geometry {
 typedef double db;
  const db inf = "Edit";
  const int maxn = "Edit";
  const db eps = "Edit";
  const db delta = 0.98;
  int Sgn(db k) { return fabs(k) < eps ? 0 : (k < 0 ? -1 : 1); }</pre>
```

```
int Cmp(db k1, db k2) { return Sgn(k1 - k2); }
db Max(db k1, db k2) \{ return Cmp(k1, k2) > 0 ? k1 : k2; \}
db Min(db k1, db k2) \{ return Cmp(k1, k2) < 0 ? k1 : k2; \}
struct point { db x, y; };
bool operator == (point k1, point k2) { return Cmp(k1.x, k2.x) == 0 && Cmp(k1.y,
\rightarrow k2.y) == 0; }
point operator + (point k1, point k2) { return (point){k1.x + k2.x, k1.y + k2.y};
point operator - (point k1, point k2) { return (point){k1.x - k2.x, k1.y - k2.y};
db operator * (point k1, point k2) { return k1.x * k2.x + k1.y * k2.y; }
db operator ^ (point k1, point k2) { return k1.x * k2.y - k1.y * k2.x; }
point operator * (point k1, db k2) { return (point){k1.x * k2, k1.y * k2}; }
point operator / (point k1, db k2) { return (point){k1.x / k2, k1.y / k2}; }
db GetLen(point k) { return sqrt(k * k); }
db GetDisP2P(point k1, point k2) { return sqrt((k1 - k2) * (k1 - k2)); }
db GetDisP2P2(point k1, point k2) { return (k1 - k2) * (k1 - k2); }
db GetAng(point k1, point k2) { return fabs(atan2(fabs(k1 ^ k2), k1 * k2)); }
point Rotate(point k, db ang) { return (point){k.x * cos(ang) - k.y * sin(ang),
\rightarrow k.x * sin(ang) + k.y * cos(ang)}; }
point Rotate90(point k) { return (point){-k.y, k.x}; }
bool IsConvexhull(std::vector<point> &p) {
  int n = (int)p.size();
  for (int i = 0; i < n; ++i)
    if (Sgn((p[(i + 1) % n] - p[i]) ^ (p[(i + 2) % n] - p[(i + 1) % n])) < 0)
      return false;
  return true;
}
db ClosestP2P(point p[], int l, int r) {
  if (1 + 1 == r) return GetDisP2P(p[1], p[r]);
  if (1 + 2 == r) return Min(GetDisP2P(p[1 + 1], p[r]), Min(GetDisP2P(p[1], p[1 +
  → 1]), GetDisP2P(p[1], p[r])));
  int mid = (1 + r) >> 1;
  db ret = Min(ClosestP2P(1, mid), ClosestP2P(mid + 1, r));
  std::vector<point> mid_p;
  for (int i = 1; i <= r; ++i) {
    if (Cmp(fabs(p[i].x - p[mid].x), ret) \le 0) mid_p.push_back(p[i]);
  std::sort(mid_p.begin(), mid_p.end(), [&](point k1, point k2) {return Cmp(k1.y,
  \rightarrow k2.y) < 0;});
  for (int i = 0; i < (int)mid_p.size(); ++i) {</pre>
    for (int j = i + 1; j < (int)mid_p.size(); ++j) {</pre>
      if (Cmp(mid_p[j].y - mid_p[i].y, ret) >= 0) break;
      ret = Min(ret, GetDisP2P(mid_p[i], mid_p[j]));
    }
  return ret;
```

```
}
typedef std::vector<point> poly;
void RotateCaliper() {
  db ret = -1e20;
  if (ConvexHull.size() == 3) {
    if (Cmp(GetDisP2P(ConvexHull[0], ConvexHull[1]), ret) > 0) ret =

→ GetDisP2P(ConvexHull[0], ConvexHull[1]);
    if (Cmp(GetDisP2P(ConvexHull[0], ConvexHull[2]), ret) > 0) ret =

→ GetDisP2P(ConvexHull[0], ConvexHull[2]);
    if (Cmp(GetDisP2P(ConvexHull[1], ConvexHull[2]), ret) > 0) ret =
    → GetDisP2P(ConvexHull[1], ConvexHull[2]);
    return;
  }
  int cur = 2, size = ConvexHull.size();
  for (int i = 0; i < size; ++i) {
    while (Cmp(fabs((ConvexHull[i] - ConvexHull[(i + 1) % size]) ^
    \hookrightarrow ConvexHull[(i + 1) % size]))) < 0) cur = (cur + 1) % size;
    if (Cmp(GetDisP2P(ConvexHull[i], ConvexHull[cur]), ret) > 0) ret =

→ GetDisP2P(ConvexHull[i], ConvexHull[cur]);
  }
}
poly Grahamscan(std::vector<point> p) {
  poly ret;
  if ((int)p.size() < 3) {
    for (int i = 0; i < (int)p.size(); ++i) ret.push_back(p[i]);</pre>
    return ret;
  }
  int low = 0;
  for (int i = 0; i < (int)p.size(); ++i)</pre>
    if (Cmp(p[i].x, p[low].x) < 0 \mid | (Cmp(p[i].x, p[low].x) == 0 && Cmp(p[i].y,
    \rightarrow p[low].y) < 0))
     low = i;
    std::swap(p[0], p[low]);
    std::sort(p.begin() + 1, p.end(), [&](point k1, point k2) {
    double tmp = (k1 - p[0]) \hat{k2} - p[0]);
    if (Sgn(tmp) > 0) return true;
    else if (Sgn(tmp) == 0 \&\& Cmp(GetDisP2P(k2, p[0]), GetDisP2P(k1, p[0])) > 0)

    return true;

    return false;
  });
  ret.push_back(p[0]);
  for (int i = 1; i < (int)p.size(); ++i) {</pre>
    while ((int)ret.size() >= 2 && Sgn((ret.back() - ret[(ret.size()) - 2]) ^
    \rightarrow (p[i] - ret[(int)ret.size() - 2])) <= 0) {
     ret.pop_back();
```

```
}
    ret.push_back(p[i]);
 }
 return ret;
db GetMinCircle(std::vector<point> p) {
 point cur = p[0];
 db pro = 10000, ret = inf;
 while (pro > eps) {
    int book = 0;
    for (int i = 0; i < (int)p.size(); ++i)</pre>
      if (GetDisP2P(cur, p[i]) > GetDisP2P(cur, p[book]))
        book = i;
    db r = GetDisP2P(cur, p[book]);
    if (Cmp(r, ret) < 0) ret = r;
    cur = cur + (p[book] - cur) / r * pro;
   pro *= delta;
 }
 return ret;
}
struct line { point s, t; };
typedef line seg;
db GetLen(seg k) { return GetDisP2P(k.s, k.t); }
db GetDisP2Line(point k1, line k2) { return fabs((k1 - k2.s) ^ (k2.t - k2.s)) /

   GetLen(k2); }

db GetDisP2Seg(point k1, seg k2) {
  if (Sgn((k1 - k2.s) * (k2.t - k2.s)) < 0 \mid | Sgn((k1 - k2.t) * (k2.s - k2.t)) <
    return Min(GetDisP2P(k1, k2.s), GetDisP2P(k1, k2.t));
 }
 return GetDisP2Line(k1, k2);
bool IsParallel(line k1, line k2) { return Sgn((k1.s - k1.t) ^ (k2.s - k2.t)) ==
→ 0; }
bool IsSegInterSeg(seg k1, seg k2) {
 return
    Max(k1.s.x, k1.t.x) >= Min(k2.s.x, k2.t.x) &&
    Max(k2.s.x, k2.t.x) >= Min(k1.s.x, k1.t.x) &&
    Max(k1.s.y, k1.t.y) >= Min(k2.s.y, k2.t.y) &&
    Max(k2.s.y, k2.t.y) >= Min(k1.s.y, k1.t.y) &&
    Sgn((k2.s - k1.t) ^ (k1.s - k1.t)) * Sgn((k2.t - k1.t) ^ (k1.s - k1.t)) <= 0
    → &&
    Sgn((k1.s - k2.t) ^ (k2.s - k2.t)) * Sgn((k1.t - k2.t) ^ (k2.s - k2.t)) <= 0;
bool IsLineInterSeg(line k1, seg k2) {
 return Sgn((k2.s - k1.t) ^ (k1.s - k1.t)) * Sgn((k2.t - k1.t) ^ (k1.s - k1.t))
```

```
}
bool IsLineInterLine(line k1, line k2) {
  return !IsParallel(k1, k2) || (IsParallel(k1, k2) && !(Sgn((k1.s - k2.s) ^
  \rightarrow (k2.t - k2.s)) == 0));
bool IsPointOnSeg(point k1, seg k2) {
  point Cross(line k1, line k2) {
  db temp = ((k1.s - k2.s) \hat{ }(k2.s - k2.t)) / ((k1.s - k1.t) \hat{ }(k2.s - k2.t));
  return (point) \{k1.s.x + (k1.t.x - k1.s.x) * temp, k1.s.y + (k1.t.y - k1.s.y) *
}
// 表示 s->t 逆时针 (左侧) 的半平面
struct hulfplane:public line { db ang; };
void GetAng(halfplane k) { k.ang = atan2(k.t.y - k.s.y, k.t.x - k.s.x); }
bool operator < (halfplane k1, halfplane k2) {</pre>
  if (Sgn(k1.ang - k2.ang) > 0) return k1.ang < k2.ang;</pre>
  return Sgn((k1.s - k2.s) ^ (k2.t - k2.s)) < 0;
struct HalfPlaneInsert {
  int tot;
  halfplane hp[maxn];
  halfplane deq[maxn];
  point points[maxn];
  point res[maxn];
  int front, tail;
  void Push(halfplane k) { hp[tot++] = k; }
  void Unique() {
    int cnt = 1;
    for (int i = 1; i < tot; ++i)
      if (fabs(hp[i].ang - hp[i - 1].ang) > eps)
       hp[cnt++] = hp[i];
    tot = cnt;
  }
  bool IsHalfPlaneInsert() {
    for (int i = 0; i < tot; ++i) GetAng(hp[i]);</pre>
    sort(hp, hp + tot);
    Unique();
    deq[front = 0] = hp[0];
    deq[tail = 1] = hp[1];
    for (int i = 2; i < tot; ++i) {
      if (fabs((deq[tail].t - deq[tail].s) ^ (deq[tail - 1].t - deq[tail - 1].s))
      \rightarrow < eps || fabs((deq[front].t - deq[front].s) ^ (deq[front + 1].t -
      → deq[front + 1].s)) < eps) return false;</pre>
```

```
while (front < tail && ((Cross(deq[tail], deq[tail - 1]) - hp[i].s) ^
       \rightarrow (hp[i].t - hp[i].s)) > eps) tail--;
      while (front < tail && ((Cross(deq[front], deq[front + 1]) - hp[i].s) ^
       \rightarrow (hp[i].t - hp[i].s)) > eps) front++;
      deq[++tail] = hp[i];
    }
    while (front < tail && ((Cross(deq[tail], deq[tail - 1]) - deq[front].s) ^

    deq[front].t - deq[front].s)) > eps) tail--;

    while (front < tail && ((Cross(deq[front], deq[front - 1]) - deq[tail].s) ^
    \  \, \hookrightarrow \  \, (\texttt{deq[tail].t} \,\, - \,\, \texttt{deq[tail].t)}) \,\, > \,\, \texttt{eps)} \,\,\, \texttt{front++};
    if (tail <= front + 1) return false;</pre>
    return true;
  }
  void GetHalfPlaneInsertConvex() {
    int cnt = 0;
    for (int i = front; i < tail; ++i) res[cnt++] = Cross(deq[i], deq[i + 1]);</pre>
    if (front < tail - 1) res[cnt++] = Cross(deq[front], deq[tail]);</pre>
  }
};
struct circle {point o; db r;};
circle GetCircle(point k1, point k2, point k3) {
  db a1 = k2.x - k1.x, b1 = k2.y - k1.y, c1 = (a1 * a1 + b1 * b1) / 2;
  db a2 = k3.x - k1.x, b2 = k3.y - k1.y, c2 = (a2 * a2 + b2 * b2) / 2;
  db d = a1 * b2 - a2 * b1;
  point o = (point)\{k1.x + (c1 * b2 - c2 * b1) / d, k1.y + (a1 * c2 - a2 * c1) / d\}
  return (circle){o, GetDisP2P(k1, o)};
}
circle GetMinCircle(std::vector<point> p) {
  std::random_shuffle(p.begin(), p.end());
  int n = (int)p.size();
  circle ret = (circle)\{p[0], 0.0\};
  for (int i = 1; i < n; ++i) {
    if (Cmp(GetDisP2P(ret.o, p[i]), ret.r) <= 0) continue;</pre>
    ret = (circle){p[i], 0.0};
    for (int j = 0; j < i; ++j) {
      if (Cmp(GetDisP2P(ret.o, p[j]), ret.r) <= 0) continue;</pre>
      ret.o = (p[i] + p[j]) / 2; ret.r = GetDisP2P(ret.o, p[i]);
      for (int k = 0; k < j; ++k) {
         if (Cmp(GetDisP2P(ret.o, p[k]), ret.r) <= 0) continue;</pre>
         ret = GetCircle(p[i], p[j], p[k]);
      }
    }
  }
  return ret;
}
```

```
};
using namespace Geometry;
6.5 Simpson
typedef double db;
struct Simpson {
  /* 系数 */
  db F(db x) {
    return /* 表达式 */;
  db Simpson(db 1, db r) {
    db m = (1 + r) / 2.0;
    return (F(1) + 4 * F(m) + F(r)) * (r - 1) / 6.0;
  }
  db Asr(db 1, db r, db ans, db eps) {
    db m = (1 + r) / 2.0;
    db l_ans = Simpson(l, m), r_ans = Simpson(m, r);
    if (fabs(l_ans + r_ans - ans) \le 15.0 * eps) return l_ans + r_ans + (l_ans + ans)
    \rightarrow r_ans - ans) / 15.0;
    return Asr(1, m, 1_ans, eps / 2.0) + Asr(m, r, r_ans, eps / 2.0);
};
6.6 Stereoscopic
namespace Geometry3D {
  typedef double db;
  const db inf = "Edit";
  const int maxn = "Edit";
  const db eps = "Edit";
  const db delta = 0.98;
  int Sgn(db k) { return fabs(k) < eps ? 0 : (k < 0 ? -1 : 1); }</pre>
  int Cmp(db k1, db k2) { return Sgn(k1 - k2); }
  struct point { db x, y, z; };
  bool operator == (point k1, point k2) { return Sgn(k1.x - k2.x) == 0 && Sgn(k1.y
  \rightarrow - k2.y) == 0 && Sgn(k1.z - k1.z) == 0; }
  point operator + (point k1, point k2) { return (point){k1.x + k2.x, k1.y + k2.y,
  \rightarrow k1.z + k2.z}; }
 point operator - (point k1, point k2) { return (point){k1.x - k2.x, k1.y - k2.y,
  \rightarrow k1.z - k2.z}; }
  db operator * (point k1, point k2) { return k1.x * k2.x + k1.y * k2.y + k1.z *
  \rightarrow k2.z; }
  db GetLen(point k) { return sqrt(k * k); }
```

```
db GetLen2(point k) { return k * k; }
db operator ^ (point k1, point k2) { return GetLen((point){k1.y * k2.z - k1.z *
\rightarrow k2.y, k1.z * k2.x - k1.x * k2.z, k1.x * k2.y - k1.y * k2.x}); }
point operator * (point k1, db k2) { return (point){k1.x * k2, k1.y * k2, k1.z *
\rightarrow k2}; }
point operator / (point k1, db k2) { return (point){k1.x / k2, k1.y / k2, k1.z /
\rightarrow k2}; }
db GetDisP2P(point k1, point k2) { return GetLen(k2 - k1); }
db GetDisP2P2(point k1, point k2) { return GetLen2(k2 - k1); }
db GetAngle(point k1, point k2) { return fabs(atan2(fabs(k1 ^ k2), k1 * k2)); }
db GetMinSphere(std::vector<point> p) {
  point cur = p[0];
  db pro = 10000, ret = inf;
  while (pro > eps) {
    int mark = 0;
    for (int i = 0; i < (int)p.size(); ++i) {</pre>
      if (Cmp(GetDisP2P(cur, p[i]), GetDisP2P(cur, p[mark])) > 0) mark = i;
    db r = GetDisP2P(cur, p[mark]);
    ret = min(ret, r);
    cur = cur + (p[mark] - cur) / r * pro;
    pro *= delta;
  }
  return ret;
}
struct line { point s, t; };
typedef line seg;
db GetLen(seg k) { return GetDisP2P(k.s, k.t); }
db GetLe2(seg k) { return GetDisP2P2(k.s, k.t); }
db GetDisP2Line(point k1, line k2) { return fabs((k1 - k2.s) ^ (k2.t - k2.s)) /

   GetLen(k2); }

db GetDisP2Seg(point k1, seg k2) {
  if (Sgn((k1 - k2.s) * (k2.T - k2.s)) < 0 \mid | Sgn((k1 - k2.t) * (k2.s - k2.t)) <
    return min(GetDisP2P(k1, k2.s), GetDisP2P(k1, k2.t));
  }
  return GetDisP2Line(k1, k2);
}
struct sphere { point o;db r; };
db GetV(sphere k) { return 4.0 / 3.0 * pi * k.r * k.r * k.r; }
db GetSphereInterV(sphere k1, sphere k2) {
  db ret = 0.0;
  db dis = GetDisP2P(k1.o, k2.o);
  if (Sgn(dis - k1.r - k2.r) >= 0) return ret;
  if (Sgn(k2.r - (dis + k1.r)) >= 0) return GetV(k1);
  else if (Sgn(k1.r - (dis + k2.r)) >= 0) return GetV(k2);
```

```
db len1 = ((k1.r * k1.r - k2.r * k2.r) / dis + dis) / 2;
    db len2 = dis - len1;
    db x1 = k1.r - len1, x2 = k2.r - len2;
    db v1 = pi * x1 * x1 * (k1.r - x1 / 3.0);
    db v2 = pi * x2 * x2 * (k2.r - x2 / 3.0);
    return v1 + v2;
  }
  struct ray { point o, dir; };
  bool IsRayInterSphere(ray k1, sphere k2, db &dis) {
    db a = k1.dir * k1.dir;
    db b = (k1.o - k2.o) * k1.dir * 2.0;
    db c = ((k1.0 - k2.0) * (k1.0 - k2.0)) - (k2.r * k2.r);
    db \ dlt = b * b - 4.0 * a * c;
    if (Sgn(dlt) < 0) return false;</pre>
    db x1 = (-b - sqrt(dlt)) / (2.0 * a), x2 = (-b + sqrt(dlt)) / (2.0 * a);
    if (Cmp(x1, x2) > 0) swap(x1, x2);
    if (Sgn(x1) <= 0) return false;</pre>
    dis = x1;
    return true;
  }
  void Reflect(ray &k1, sphere k2, db dis) {
    point pos = k1.o + (k1.dir * dis);
    Vector temp = k2.0 + (((pos - k2.0) * ((pos - k2.0) * (k1.0 - k2.0))) /

   GetLen2(pos - k2.o));
    k1.dir = temp * 2.0 - k1.o - pos; k1.o = pos;
  }
};
using namespace Geometry3D;
```

7 Others

7.1 BeetMatch

```
/*
  // windows
  :loop
 data.exe > in.txt
 main.exe < in.txt > out.txt
 std.exe < in.txt > std.txt
  fc out.txt std.txt
 if not errorlevel 1 goto loop
 pause
 :end
*/
7.2 FastIO
// 普通读入挂
template <typename t>
inline bool Read(t &ret) {
  char c; int sgn;
 if (c = getchar(), c == EOF) return false;
 while (c != '-' \&\& (c < '0' || c > '9')) c = getchar();
 sgn = (c == '-') ? -1 : 1;
 ret = (c == '-') ? 0 : (c - '0');
 while (c = getchar(), c >= '0' && c <= '9') ret = ret * 10 + (c - '0');
 ret *= sgn;
 return true;
// 普通输出挂
template <typename t>
inline void Out(t x) {
 if (x < 0) {
   putchar('-');
   x = -x;
 }
 if (x > 9) Out(x / 10);
 putchar(x % 10 + '0');
}
// 牛逼读入挂
namespace FastIO {
 const int MX = 4e7;
 char buf[MX];
 int c, sz;
 void Begin() {
   c = 0;
   sz = fread(buf, 1, MX, stdin);
```

```
}
 template <class T>
  inline bool Read(T &t) {
   while (c < sz && buf[c] != '-' && (buf[c] < '0' || buf[c] > '9')) c++;
   if (c >= sz) return false;
   bool flag = 0;
   if (buf[c] == '-') {
     flag = 1;
      C++;
   }
   for (t = 0; c < sz && '0' <= buf[c] && buf[c] <= '9'; ++c) t = t * 10 + buf[c]
    → - '0';
   if (flag) t = -t;
   return true;
 }
};
// 超级读写挂
namespace IO{
  #define BUF_SIZE 100000
 #define OUT_SIZE 100000
 #define ll long long
  //fread->read
 bool IOerror=0;
  inline char nc(){
    static char buf[BUF_SIZE],*p1=buf+BUF_SIZE,*pend=buf+BUF_SIZE;
   if (p1==pend){
      p1=buf; pend=buf+fread(buf,1,BUF_SIZE,stdin);
      if (pend==p1){IOerror=1;return -1;}
      //{printf("IO error!\n");system("pause");for (;;);exit(0);}
   }
   return *p1++;
  }
  inline bool blank(char ch){return ch==' '||ch=='\n'||ch=='\r'||ch=='\t';}
  inline void read(int &x){
   bool sign=0; char ch=nc(); x=0;
   for (;blank(ch);ch=nc());
   if (IOerror)return;
    if (ch=='-')sign=1,ch=nc();
   for (;ch>='0'&&ch<='9';ch=nc())x=x*10+ch-'0';
    if (sign)x=-x;
  inline void read(ll &x){
   bool sign=0; char ch=nc(); x=0;
   for (;blank(ch);ch=nc());
   if (IOerror)return;
   if (ch=='-')sign=1,ch=nc();
   for (;ch>='0'&&ch<='9';ch=nc())x=x*10+ch-'0';
```

```
if (sign)x=-x;
}
inline void read(double &x){
  bool sign=0; char ch=nc(); x=0;
  for (;blank(ch);ch=nc());
  if (IOerror)return;
  if (ch=='-')sign=1,ch=nc();
  for (;ch>='0'\&\&ch<='9';ch=nc())x=x*10+ch-'0';
  if (ch=='.'){
    double tmp=1; ch=nc();
    for (;ch>='0'\&\&ch<='9';ch=nc())tmp/=10.0,x+=tmp*(ch-'0');
  }
  if (sign)x=-x;
}
inline void read(char *s){
  char ch=nc();
  for (;blank(ch);ch=nc());
  if (IOerror)return;
  for (;!blank(ch)&&!IOerror;ch=nc())*s++=ch;
  *s=0;
}
inline void read(char &c){
  for (c=nc();blank(c);c=nc());
  if (IOerror){c=-1;return;}
}
//fwrite->write
struct Ostream_fwrite{
  char *buf,*p1,*pend;
  Ostream fwrite() {buf=new char[BUF_SIZE]; p1=buf; pend=buf+BUF_SIZE;}
  void out(char ch){
    if (p1==pend) fwrite(buf,1,BUF_SIZE,stdout);p1=buf;
    *p1++=ch;
  }
  void print(int x){
    static char s[15],*s1;s1=s;
    if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
    while(x)*s1++=x\%10+'0', x/=10;
    while (s1--!=s) out (*s1);
  }
  void println(int x){
    static char s[15],*s1;s1=s;
    if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
    while (x)*s1++=x\%10+'0', x/=10;
    while(s1--!=s)out(*s1); out('\n');
  }
  void print(ll x){
    static char s[25],*s1;s1=s;
    if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
    while(x)*s1++=x\%10+'0',x/=10;
```

```
while (s1--!=s) out (*s1);
   }
   void println(ll x){
     static char s[25],*s1;s1=s;
     if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
     while(x)*s1++=x%10+'0',x/=10;
     while(s1--!=s)out(*s1); out('\n');
   }
   void print(double x,int y){
     if (x<-1e-12) out('-'), x=-x; x*=mul[y];
     11 x1=(11)floor(x); if (x-floor(x)>=0.5)++x1;
     11 x2=x1/mul[y],x3=x1-x2*mul[y]; print(x2);
     if (y>0){out('.'); for (size_t i=1;i<y&&x3*mul[i]<mul[y];out('0'),++i);
     \rightarrow print(x3);}
   }
   void println(double x,int y){print(x,y);out('\n');}
   void print(char *s){while (*s)out(*s++);}
   void println(char *s){while (*s)out(*s++);out('\n');}
   void flush(){if (p1!=buf){fwrite(buf,1,p1-buf,stdout);p1=buf;}}
   ~Ostream_fwrite(){flush();}
 }Ostream;
 inline void print(int x){Ostream.print(x);}
 inline void println(int x){Ostream.println(x);}
 inline void print(char x){Ostream.out(x);}
 inline void println(char x){Ostream.out(x);Ostream.out('\n');}
 inline void print(ll x){Ostream.print(x);}
 inline void println(ll x){Ostream.println(x);}
 inline void print(double x,int y){Ostream.print(x,y);}
 inline void println(double x,int y){Ostream.println(x,y);}
 inline void print(char *s){Ostream.print(s);}
 inline void println(char *s){Ostream.println(s);}
 inline void println(){Ostream.out('\n');}
 inline void flush(){Ostream.flush();}
 #undef ll
 #undef OUT_SIZE
 #undef BUF_SIZE
using namespace IO;
7.3 LeepYear
bool IsLeep(int x) { return (!(x % 4) && (x % 100)) || !(x % 400); }
```

7.4 MoAlgorithm

7.4.1 Dynamic

```
const int maxn = "Edit";
// 动态莫队算法求区间不同数字数量(支持单点修改)
struct MoCap {
 int n, m;
 int block;
 int arr[maxn];
 struct query { int 1, r, pre, id; };
 int q_tot;
 query q[maxn];
 struct change { int pos, val; };
 int c_tot;
 change c[maxn];
 int cnt[maxn << 7];</pre>
 int cur;
 int ans[maxn];
 void Add(int x) { cur += (++cnt[arr[x]] == 1); }
 void Del(int x) { cur -= (--cnt[arr[x]] == 0); }
 void Modify(int x, int i) {
   if (c[x].pos >= q[i].l \&\& c[x].pos <= q[i].r) {
     cur -= (--cnt[arr[c[x].pos]] == 0);
     cur += (++cnt[c[x].val] == 1);
   std::swap(c[x].val, arr[c[x].pos]);
 void Solve() {
   scanf("%d%d", &n, &m);
   block = (int)sqrt(n);
   for (int i = 1; i <= n; ++i) scanf("%d", &arr[i]);
   for (int i = 1; i <= m; ++i) {
     char op; getchar();
     scanf("%c", &op);
     if (op == 'Q') {
       int 1, r; scanf("%d%d", &1, &r);
       q[++q_tot] = (query){1, r, c_tot, q_tot};
     }
     else {
       int p, v; scanf("%d%d", &p, &v);
        c[++c_{tot}] = (change)\{p, v\};
     }
   std::sort(q + 1, q + q_tot + 1, [\&](query k1, query k2) {
```

```
if ((k1.1 / block) == k2.1 / block) {
        if ((k1.r / block) == (k2.r / block)) return k1.pre < k2.pre;</pre>
        return k1.r < k2.r;</pre>
      return k1.1 < k2.1;
   });
   int 1 = 1, r = 0, t = 0;
   for (int i = 1; i <= q_tot; ++i) {</pre>
      while (1 < q[i].1) Del(1++);
      while (1 > q[i].1) Add(--1);
      while (r < q[i].r) Add(++r);
      while (r > q[i].r) Del(r--);
      while (t < q[i].pre) Modify(++t, i);</pre>
      while (t > q[i].pre) Modify(t--, i);
      ans[q[i].id] = cur;
   }
   for (int i = 1; i \le q_{tot}; ++i) printf("%d\n", ans[i]);
}mo;
7.4.2 Static
const int maxn = "Edit";
// 静态莫队算法求区间不同数字数量
struct MoCap {
 int n, m;
 int block;
 int arr[maxn];
 struct query { int 1, r, id; };
 query q[maxn];
 int cnt[maxn << 1];</pre>
 int cur;
 int ans[maxn];
 void Add(int x) { cur += (++cnt[arr[x]] == 1); }
 void Del(int x) { cur -= (--cnt[arr[x]] == 0); }
 void Solve() {
   scanf("%d%d", &n, &m);
   block = (int)sqrt(n);
   for (int i = 1; i <= n; ++i) scanf("%d%d", &arr[i]);</pre>
   for (int i = 1; i <= m; ++i) {
      scanf("%d%d", &q[i].1, &q[i].r);
      q[i].id = i;
   }
```

```
std::sort(q + 1, q + m + 1, [\&](query k1, query k2) { return (k1.1 / block) == }
    \rightarrow (k2.1 / block) ? k1.r < k2.r : k1.1 < k2.1; });
   int 1 = 0, r = 0;
   for (int i = 1; i <= m; ++i) {
      while (1 < q[i].1) Del(1++);
      while (1 > q[i].1) Add(--1);
      while (r < q[i].r) Add(++r);
      while (r > q[i].r) Del(r--);
      ans[q[i].id] = cur;
   }
   for (int i = 1; i \le m; ++i) printf("%d\n", ans[i]);
  }
}mo;
7.5 STL
// pbds
#include <bits/extc++.h>
// --- tree ---
template < typename Key,
          typename Mapped,
          typename Cmp_Fn = std::less<Key>,
          typename Tag = rb_tree_tag,
          template<typename Node_Cltr,
                   typename Node_Itr,
                   typename Cmp_Fn_,
                   typename _Alloc_> class Node_Update = null_node_update,
          typename _Alloc = std::allocator<char> >
__gnu_pbds::tree< Key, Mapped, Cmp_Fn, Tag, Node_Update, _Alloc >
/*
Member types:
 Key:
   Key type.
  Mapped:
   Map type.
  Cmp\_Fn:
    Comparison function.
  Taq:
    Instantiating data structure type
   __gnu_pbds::ov_tree_tag: Ordered-vector tree.
   __gnu_pbds::rb_tree_tag: Red-black tree;
    __gnu_pbds::splay_tree_tag: Splay tree.
 Node_Update:
    Updates nodes, restores invariants when invalidated.
   \it XXX\ See\ design::tree-based-containers::node\ invariants.
  _Alloc:
```

Allocator type.

```
Member functions:
  insert({key, mapped}):
   Insert element.
  erase({key, mapped}):
   Delete element.
  order_of_key({key, mapped}):
    Get the rank of {key, mapped}.
  find_by_order(int x):
    Find the k-th element. Return iterator.
  join(tree t):
    Insert the tree t into the tree if the origin tree type is the same ans there
\rightarrow are no duplicate elements.
  split(value, t):
   Split the tree, the origin tree contains elements that are less than or equal
→ to value, the tree t contains elements that are greater to value.
  lower_bound(value):
   Reture the iterator of the first element greater or equal to value.
  upper bound(value):
   Reture the iterator of the first element greater to value.
  Examples:
    typedef __qnu_pbds::tree<int, int, std::less<int>, __qnu_pbds::splay_tree_tag,
   __gnu_pbds::tree_order_statistics_node_update> splay_tree;
7.6 vim
syntax on
set nu ts=2 sw=2 et mouse=a cindent
"map <F9> :call Run()<CR>
"func! Run()
    exec "w"
    exec "!g++ % -o %<"
    exec "! %<"
"endfunc
"map <F2> :call SetTitle()<CR>
"func SetTitle()
    let 1 = 0
    let l = l + 1 | call setline(l, "#include <bits/stdc++.h>")
    let 1 = 1 + 1 | call setline(1, "")
    let 1 = 1 + 1 | call setline(1, "int main() {")
    let 1 = 1 + 1 | call setline(1, " return 0;")
    let 1 = 1 + 1 | call setline(1, "}")
    let 1 = 1 + 1 | call setline(1, "")
"endfunc
```