# Algorithm Library

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# Algorithm Library by Liu Yang

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# 1 String

## 1.1 AhoCorasickAutomaton

```
#include <bits/stdc++.h>
const int maxn = "Edit";
struct AhoCorasickAutomaton {
   // 子节点记录数组
   int Son[maxn][26];
   int Val[maxn];
   // 失配指针 Fail 数组
   int Fail[maxn];
   // 节点数量
   int Tot;
   // Trie Tree 初始化
   void TrieInit() {
       Tot = 0;
       memset(Son, 0, sizeof(Son));
       memset(Val, 0, sizeof(Val));
       memset(Fail, 0, sizeof(Fail));
   }
   // 计算字母下标
   int Pos(char X) {
       return X - 'a';
   }
   // 向 Trie Tree 中插入 Str 模式字符串
   void Insert(string Str) {
       int Cur = 0, Len = int(Str.length());
       for (int i = 0; i < Len; ++i) {</pre>
           int Index = Pos(Str[i]);
           if (!Son[Cur][Index]) {
               Son[Cur][Index] = ++Tot;
           Cur = Son[Cur][Index];
       Val[Cur]++;
   }
   // Bfs 求得 Trie Tree 上失配指针
```

```
void GetFail() {
        std::queue<int> Que;
        for (int i = 0; i < 26; ++i) {
            if (Son[0][i]) {
                Fail[Son[0][1]] = 0;
                Que.push(Son[0][i]);
        }
        while (!Que.empty()) {
            int Cur = Que.front(); Que.pop();
            for (int i = 0; i < 26; ++i) {
                if (Son[Cur][i]) {
                    Fail[Son[Cur][i]] = Son[Fail[Cur]][i];
                    Que.push(Son[Cur][i]);
                }
                else {
                    Son[Cur][i] = Son[Fail[Cur]][i];
                }
            }
        }
    }
    // 询问 Str 中出现的模式串数量
    int Query(string Str) {
        int Len = int(Str.length());
        int Cur = 0, Ans = 0;
        for (int i = 0; i < Len; ++i) {</pre>
            Cur = Son[Cur][Pos(Str[i])];
            for (int j = Cur; j && ~Val[j]; j = Fail[j]) {
                Ans += Val[j];
                Val[j] = -1;
            }
        }
        return Ans;
    }
};
1.2 KMP
#include <bits/stdc++.h>
// 对模式串 Pattern 计算 Next 数组
void KMPPre(string Pattern, vector<int> &Next) {
    int i = 0, j = -1;
```

```
Next[0] = -1;
    int Len = int(Pattern.length());
    while (i != Len) {
        if (j == -1 || Pattern[i] == Pattern[j]) {
           Next[++i] = ++j;
        }
        else {
           j = Next[j];
    }
}
// 优化对模式串 Pattern 计算 Next 数组
void PreKMP(string Pattern, vector<int> &Next) {
    int i, j;
    i = 0;
    j = Next[0] = -1;
    int Len = int(Pattern.length());
    while (i < Len) {
        while (j != -1 && Pattern[i] != Pattern[j]) {
            j = Next[j];
        if (Pattern[++i] == Pattern[++j]) {
            Next[i] = Next[j];
        }
        else {
            Next[i] = j;
    }
}
// 利用预处理 Next 数组计数模式串 Pattern 在主串 Main 中出现次数
int KMPCount(string Pattern, string Main) {
    int PatternLen = int(Pattern.length()), MainLen =

    int(Main.length());

    vector<int> Next(PatternLen + 1, 0);
    //PreKMP(Pattern, Next);
    KMPPre(Pattern, Next);
    int i = 0, j = 0;
    int Ans = 0;
    while (i < MainLen) {</pre>
        while (j != -1 && Main[i] != Pattern[j]) {
            j = Next[j];
```

```
}
        i++; j++;
        if (j >= PatternLen) {
            Ans++;
            j = Next[j];
    return Ans;
}
1.3 Manacher
#include <bits/stdc++.h>
const int maxn = "Edit";
char ConvertStr[maxn << 1];</pre>
int Len[maxn << 1];</pre>
// Manacher 算法求 Str 字符串最长回文子串长度
int Manacher(char Str[]) {
    int L = 0, StrLen = int(strlen(Str));
    ConvertStr[L++] = '$'; ConvertStr[L++] = '#';
    for (int i = 0; i < StrLen; ++i) {</pre>
        ConvertStr[L++] = Str[i];
        ConvertStr[L++] = '#';
    int MX = 0, ID = 0, Ans = 0;
    for (int i = 0; i < L; ++i) {
        Len[i] = MX > i ? min(Len[2 * ID - i], MX - i) : 1;
        while (ConvertStr[i + Len[i]] == ConvertStr[i -
        → Len[i]]) {
            Len[i]++;
        if (i + Len[i] > MX) {
            MX = i + Len[i];
            ID = i;
        Ans = max(Ans, Len[i] - 1);
    }
    return Ans;
}
```

#### 1.4 PalindromicTree

```
#include <bits/stdc++.h>
const int maxn = "Edit";
struct PalindromicTree {
   // 子节点记录数组
   long long Son[maxn][26];
   // 失配指针 Fail 数组
   long long Fail[maxn];
   // Len[i]: 节点 i 表示的回文串长度 (一个节点表示一个回文串)
   long long Len[maxn];
   // Cnt[i]: 节点 i 表示的本质不同的串的个数 (最后需要运行
   → Count() 函数才可求出正确结果)
   long long Cnt[maxn];
   // Num[i]: 以节点 i 表示的最长回文串的最右端为回文串结尾的回
   → 文串个数
   long long Num[maxn];
   // 字符
   long long Str[maxn];
   // 新添加字符后最长回文串表示的节点
   long long Last;
   // 字符数量
   long long StrLen;
   // 节点数量
   long long Tot;
   // 新建节点
   long long NewNode(long long X) {
       for (long long i = 0; i < 26; ++i) {
          Son[Tot][i] = 0;
       }
       Cnt[Tot] = 0;
       Num[Tot] = 0;
      Len[Tot] = X;
       return Tot++;
   }
   // 初始化
   void Init() {
      Tot = 0;
       NewNode(0); NewNode(-1);
      Last = 0;
```

```
StrLen = 0;
       // 开头存字符集中没有的字符, 减少特判
       Str[0] = -1;
       Fail[0] = 1;
   }
    long long GetFail(long long X) {
       while (Str[StrLen - Len[X] - 1] != Str[StrLen]) {
           X = Fail[X];
       }
       return X;
   }
   void Add(long long Char) {
       Char -= 'a';
       Str[++StrLen] = Char;
       long long Cur = GetFail(Last);
       if (!Son[Cur][Char]) {
           long long New = NewNode(Len[Cur] + 2);
           Fail[New] = Son[GetFail(Fail[Cur])][Char];
           Son[Cur] [Char] = New;
           Num[New] = Num[Fail[New]] + 1;
       }
       Last = Son[Cur][Char];
       Cnt[Last]++;
   }
   void Count() {
       // 若 Fail[V]=U, 则 U 一定是 V 回文子串, 所以双亲累加孩
        → 子的 Cnt
       for (long long i = Tot - 1; i >= 0; --i) {
           Cnt[Fail[i]] += Cnt[i];
       }
   }
};
```

### 2 Math

### 2.1 Catalan

```
#include <bits/stdc++.h>
const int maxn = "Edit";
long long Catalan[maxn];
// 递推求卡特兰数
void CalalanInit() {
   memset(Catalan, 0, sizeof(Catalan));
    Catalan[0] = Catalan[1] = 1;
    for (int i = 2; i < maxn; ++i) {</pre>
        Catalan[i] = Catalan[i - 1] * (4 * i - 2) / (i + 1);
    }
}
2.2 Derangement
#include <bits/stdc++.h>
const int maxn = "Edit";
const int \mod = 1e9 + 7;
// Staggered: 错排数
long long Staggered[maxn];
// 求错排数
void StaggeredInit() {
    Staggered[1] = 0;
    Staggered[2] = 1;
    // 递推求错排数
    for (int i = 3; i < maxn; ++i) {</pre>
        Staggered[i] = (i - 1) * (Staggered[i - 1] +

    Staggered[i - 2]) % mod;

    }
}
```

#### 2.3 Euler

```
2.3.1 Euler
```

```
#include <bits/stdc++.h>
// 单独求解欧拉函数
int Phi(int X) {
    int Ans = X;
    for (int i = 2; i * i <= X; ++i) {</pre>
        if (!(X % i)) {
            Ans = Ans / i * (i - 1);
           while (!(X \% i)) {
               X /= i;
       }
    }
    if (X > 1) {
       Ans = Ans / X * (X - 1);
   return Ans;
}
2.3.2 PrimeEuler
#include <bits/stdc++.h>
const int maxn = "Edit";
// 素数标记
bool IsPrime[maxn];
// 欧拉函数
int Phi[maxn];
// 素数
int Prime[maxn];
// 素数个数
int Tot;
// 同时求得欧拉函数和素数表
void PhiPrime() {
    memset(IsPrime, false, sizeof(IsPrime));
   Phi[1] = 1;
   Tot = 0;
    for (int i = 2; i < maxn; ++i) {</pre>
       if (!IsPrime[i]) {
```

```
Prime[Tot++] = i;
            Phi[i] = i - 1;
        }
        for (int j = 0; j < Tot; ++j) {
            if (i * Prime[j] > maxn) {
                break;
            IsPrime[i * Prime[j]] = true;
            if (!(i % Prime[j])) {
                Phi[i * Prime[j]] = Phi[i] * Prime[j];
            break;
            }
            else {
                Phi[i * Prime[j]] = Phi[i] * (Prime[j] - 1);
            }
        }
   }
}
2.3.3 Sieve
#include <bits/stdc++.h>
const int maxn = "Edit";
// 欧拉函数
int Phi[maxn];
// 筛法求欧拉函数
void Euler() {
    for (int i = 1; i < maxn; ++i) {
        Phi[i] = i;
    }
    for (int i = 2; i < maxn; i += 2) {
        Phi[i] /= 2;
    for (int i = 3; i < maxn; i += 2) {
        if (Phi[i] == i) {
            for (int j = i; j < maxn; j += i) {
                Phi[j] = Phi[j] / i * (i - 1);
            }
        }
    }
}
```

#### 2.4 Fibonacci

```
#include <bits/stdc++.h>
const int mod = 1e9 + 7;
// 矩阵结构体
struct Matrix {
    // 矩阵
    long long Mat[2][2];
    Matrix() {}
    // 重载矩阵乘法
    Matrix operator * (Matrix const &A) const {
        Matrix Res;
       memset(Res.Mat, 0, sizeof(Res.Mat));
        for (int i = 0; i < 2; ++i) {
            for (int j = 0; j < 2; ++j) {
               for (int k = 0; k < 2; ++k) {
                   Res.Mat[i][j] = (Res.Mat[i][j] + Mat[i][k]
                    → * A.Mat[k][j] % mod) % mod;
               }
           }
       }
        return Res;
    }
};
// 重载矩阵快速幂
Matrix operator ^ (Matrix Base, long long K) {
    Matrix Res;
   memset(Res.Mat, 0, sizeof(Res.Mat));
    Res.Mat[0][0] = Res.Mat[1][1] = 1;
    while (K) {
        if (K & 1) {
           Res = Res * Base;
       Base = Base * Base;
       K >>= 1;
    return Res;
}
// 斐波那契数列中第 X 项
long long Fib(long long X) {
```

```
Matrix Base;
    Base.Mat[0][0] = Base.Mat[1][0] = Base.Mat[0][1] = 1;
    Base.Mat[1][1] = 0;
    return (Base ^ X).Mat[0][1];
}
2.5 GeneratingFunction
#include <bits/stdc++.h>
const int maxn = "Edit";
void GeneratingFunction() {
    int n;
    int c1[maxn], c2[maxn];
    scanf("%d", &n);
    for (int i = 0; i < maxn; ++i) {</pre>
        c1[i] = 1;
        c2[i] = 0;
    }
    // c1[i] 为 x~i 的系数
    // c2 为中间变量
    for (int i = 2; i <= n; ++i) {
        for (int j = 0; j \le n; ++j) {
            for (int k = 0; k + j \le n; k += i) {
                c2[j + k] += c1[i];
            }
        for (int j = 0; j \le n; ++j) {
            c1[j] = c2[j];
            c2[j] = 0;
        }
    }
}
2.6 InverseElement
2.6.1 ExtendGcd
#include <bits/stdc++.h>
// 扩展欧几里得, A*X+B*Y=D
long long ExtendGcd(long long A, long long B, long long &X,
\hookrightarrow long long &Y) {
    // 无最大公约数
```

```
if (A == 0 && B == 0) {
        return -1;
    if (B == 0) {
        X = 1;
        Y = 0;
        return A;
    }
    long long D = ExtendGcd(B, A % B, Y, X);
    Y -= A / B * X;
    return D;
}
// 逆元, AX = 1(mod M)
long long Inv(long long A, long long N) {
    long long X, Y;
    long long D = ExtendGcd(A, N, X, Y);
    if (D == 1) {
        return (X \% N + N) \% N;
    }
    else {
        return -1;
    }
}
2.6.2 Factorial
#include <bits/stdc++.h>
const int \mod = 1e9 + 7;
const int maxn = "Edit";
// 快速乘
long long QuickMul(long long A, long long B) {
    long long Ans = 0;
    while (B) {
        if (B & 1) {
            Ans = (Ans + A) \% mod;
        }
        A = (A + A) \% mod;
        B >>= 1;
    }
    return Ans;
}
```

```
// 快速幂
long long QuickPow(long long A, long long B) {
    long long Ans = 1;
    while (B) {
        if (B & 1) {
            Ans = QuickMul(Ans, A) % mod;
        A = QuickMul(A, A) % mod;
        B >>= 1;
    }
    return Ans;
}
// Factorial: 阶乘, Factorial Inv: 阶乘逆元
long long Factorial[maxn], FactorialInv[maxn];
// 求阶乘逆元
void FactorialInvInit() {
    // 求阶乘
   Factorial[0] = 0;
    Factorial[1] = 1;
    for (int i = 2; i < maxn; ++i) {</pre>
        Factorial[i] = (Factorial[i - 1] * i) % mod;
    // 飞马小定理求最大值阶乘逆元
    FactorialInv[maxn - 1] = QuickPow(Factorial[maxn - 1], mod
    → - 2);
    // 递推求阶乘逆元
    for (int i = maxn - 2; i >= 0; --i) {
        FactorialInv[i] = (FactorialInv[i + 1] * (i + 1)) %
        \hookrightarrow mod;
    }
}
2.6.3 FermatLittleTheorem
#include <bits/stdc++.h>
const int mod = 1e9 + 7;
// 快速幂、费马小定理求逆元
long long Inv(long long X) {
    return QuickPow(X, mod - 2);
```

```
}
2.6.4 Recursive
#include <bits/stdc++.h>
const int mod = 1e9 + 7;
const int maxn = "Edit";
long long Inv[maxn];
// 递推求逆元
void InvInit() {
    Inv[1] = 1;
    for (int i = 2; i < maxn; ++i) {</pre>
        Inv[i] = (mod - mod / i) * Inv[mod % i] % mod;
    }
}
2.7 Prime
2.7.1 PrimeFactor
#include <bits/stdc++.h>
const int maxn = "Edit"
bool IsPrime[maxn];
vector<int> PrimeFactor[maxn];
void Init() {
    memset(IsPrime, true, sizeof(IsPrime));
    for (long long i = 2; i < maxn; ++i) {</pre>
        if (IsPrime[i]) {
            PrimeFactor[i].push_back(i);
            for (long long j = i + i; j < maxn; ++j) {
                IsPrime[j] = false;
                PrimeFactor[j].push_back(i);
            }
        }
    IsPrime[1] = false;
}
```

#### 2.7.2 SieveOfEratosthenes

```
#include <bits/stdc++.h>
const int maxn = "Edit";
bool IsPrime[maxn];
void Init() {
    memset(IsPrime, true, sizeof(IsPrime));
    IsPrime[0] = IsPrime[1] = false;
    for (long long i = 2; i < maxn; ++i) {</pre>
        if (IsPrime[i]) {
            for (long long j = i * i; j < maxn; j += i) {
                IsPrime[j] = false;
        }
    }
}
2.8 QuickPow
#include <bits/stdc++.h>
const int mod = 1e9 + 7;
// 快速乘求 A*B%mod
long long QuickMul(long long A, long long B) {
    long long Ans = 0;
    while (B) {
        if (B & 1) {
            Ans = (Ans + A) \% mod;
        A = (A + A) \% mod;
        B >>= 1;
    return Ans;
}
// 快速幂求 A~B%mod
long long QuickPow(long long A, long long B) {
    long long Ans = 1;
    while (B) {
        if (B & 1) {
```

```
Ans = QuickMul(Ans, A) % mod;

}
A = QuickMul(A, A) % mod;
B >>= 1;
}
return Ans;
}

2.9 Stirling

#include <bits/stdc++.h>

const double pi = acos(-1.0);
const double e = 2.718281828459;

int Stirling(int x) {
   if (x <= 1) {
      return 1;
   }
   return int(ceil(log10(2 * pi * x) / 2 + x * log10(x / → e)));
}
```

### 3 DataStructure

#### 3.1 BinaryIndexedTree

```
#include <bits/stdc++.h>
#define lowbit(x) (x\Im(-x))
const int maxn = "Edit";
// 树状数组
int C[maxn];
// 更新树状数组信息
void Update(int X, int Val) {
    while (X < maxn) {</pre>
        C[X] += Val;
        X += lowbit(X);
    }
}
// 求和
int GetSum(int X) {
    int Res = 0;
    while (X > 0) {
        Res += C[X];
        X -= lowbit(X);
    }
    return Res;
}
3.2 DfsOrder
#include <bits/stdc++.h>
const int maxn = "Edit";
// 链式前向星建图
struct Link {
    int V, Next;
};
Link edges[maxn << 1];</pre>
int Head[maxn];
int Tot = 0;
```

```
void Init() {
    Tot = 0;
    memset(Head, -1, sizeof(Head));
}
void AddEdge(int U, int V) {
    edges[++Tot] = Link {V, Head[U]};
    Head[U] = Tot;
    edges[++Tot] = Link {U, Head[V]};
    Head[V] = Tot;
}
int Cnt;
int InIndex[maxn], OutIndex[maxn];
// Dfs 序
void DfsSequence(int Node, int Pre) {
    Cnt++;
    InIndex[Node] = Cnt;
    for (int i = Head[U]; i != -1; i = edges[i].Next) {
        if (edges[i].V != Pre) {
            DfsSequence(edges[i].V, Node);
        }
    OutIndex[U] = Cnt;
}
3.3 LCA
3.3.1 DFS+ST
#include <bits/stdc++.h>
const int maxn = "Edit";
// 节点深度
int Rmq[maxn << 1];</pre>
struct ST {
    // 最小值对应下标
    int Dp[maxn << 1][20];</pre>
    // RMQ 初始化
    void init(int N) {
        for (int i = 1; i <= N; ++i) {</pre>
```

```
Dp[i][0] = i;
        for (int j = 1; (1 << j) <= N; ++j) {
            for (int i = 1; i + (1 << j) - 1 <= N; ++i) {
                Dp[i][j] = Rmq[Dp[i][j - 1]] < Rmq[Dp[i + (1)]]
                \rightarrow << (j - 1))][j - 1]] ? Dp[i][j - 1] : Dp[i
                 \rightarrow + (1 << (j - 1))][j - 1];
            }
        }
    }
    // RMQ 查询
    int Query(int A, int B) {
        if (A > B) {
            std::swap(A, B);
        int K = int(log2(B - A + 1));
        return Rmq[Dp[A][K]] \le Rmq[Dp[B - (1 << K) + 1][K]]?
        \rightarrow Dp[A][K] : Dp[B - (1 << K) + 1][K];
    }
};
// 边
struct Link {
    int V, Next;
};
// 链式前向星存树边图
Link edges[maxn << 1];</pre>
int Head[maxn];
int Tot;
// 深搜遍历顺序
int Vertex[maxn << 1];</pre>
// 节点在深搜中第一次出现的位置
int First[maxn];
// 遍历节点数量
int Cnt;
ST St;
// 链式前向星存图初始化
void Init() {
    Tot = 0;
    memset(Head, -1, sizeof(Head));
```

```
}
// 链式前向星存图添加一条由 U 至 V 的边
void AddEdge(int U, int V) {
    edges[Tot] = Link {V, Head[U]};
   Head[U] = Tot++;
}
// 深搜, U: 当前搜索节点, Pre:U 的前驱节点, Depth: 树上深度
void Dfs(int U, int Pre, int Depth) {
   Vertex[++Cnt] = U;
   Rmq[Cnt] = Depth;
   First[U] = Cnt;
   for (int i = Head[U]; i != -1; i = edges[i].Next) {
       int V = edges[i].V;
       if (V == Pre) {
           continue;
       Dfs(V, U, Depth + 1);
       Vertex[++Cnt] = U;
       Rmq[Cnt] = Depth;
   }
}
// LCA 查询前的初始化, Root: 根节点, NodeNum: 节点数量
void LCA Init(int Root, int NodeNum) {
   Cnt = 0;
   Dfs(Root, Root, 0);
   St.init(2 * NodeNum - 1);
}
// 查询节点 U 和节点 V 的 LCA
int Query_LCA(int U, int V) {
   return Vertex[St.Query(First[U], First[V])];
}
3.3.2 Tarjan
#include <bits/stdc++.h>
const int maxn = "Edit";
// 树边
struct Edge {
```

```
int V, Next;
};
// 询问
struct Query {
    int Q, Next;
    int Index;
};
// 并查集数组
int Pre[maxn << 2];</pre>
// 树边
Edge edges[maxn << 2];</pre>
int Head[maxn];
int Tot;
// 询问
Query querys[maxn << 2];
int QHead[maxn];
int QTot;
// 访问标记
int Vis[maxn];
int Ancestor[maxn];
// 结果
int Answer[maxn];
// 并查集查找
int Find(int X) {
    int R = X;
    while (Pre[R] != -1) {
        R = Pre[R];
    }
    return R;
}
// 并查集合并
void Join(int U, int V) {
    int RU = Find(U);
    int RV = Find(V);
    if (RU != RV) {
        Pre[RU] = RV;
    }
}
// 添加树边
```

```
void AddEdge(int U, int V) {
    edges[Tot] = Edge {V, Head[U]};
    Head[U] = Tot++;
}
// 添加询问
void AddQuery(int U, int V, int Index) {
    querys[QTot] = Query {V, QHead[U], Index};
    QHead[U] = QTot++;
    querys[QTot] = Query {U, QHead[V], Index};
    QHead[V] = QTot++;
}
// 初始化
void Init() {
    Tot = 0;
    memset(Head, -1, sizeof(Head));
    QTot = 0;
    memset(QHead, -1, sizeof(QHead));
    memset(Vis, false, sizeof(Vis));
    memset(Pre, -1, sizeof(Pre));
    memset(Ancestor, 0, sizeof(Ancestor));
}
// LCA 离线 Tarjan 算法
void Tarjan(int Node) {
    Ancestor[Node] = Node;
    Vis[Node] = true;
    for (int i = Head[Node]; i != -1; i = edges[i].Next) {
        if (Vis[edges[i].V]) {
            continue;
        Tarjan(edges[i].V);
        Join(Node, edges[i].V);
        Ancestor[Find(Node)] = Node;
    for (int i = QHead[Node]; i != -1; i = querys[i].Next) {
        if (Vis[querys[i].Q]) {
            Answer[querys[i].Index] =
            → Ancestor[Find(querys[i].Q)];
    }
}
```

#### 3.4 SegmentTree

#### 3.4.1 SegmentTree

```
#include <bits/stdc++.h>
const int maxn = "Edit";
// Sum: 线段树信息 (此模板为求和), Lazy: 惰性标记
int Sum[maxn << 2], Lazy[maxn << 2];</pre>
// 更新节点信息, 这里是求和
void PushUp(int Root) {
   Sum[Root] = Sum[Root << 1] + Sum[Root << 1 | 1];</pre>
}
// 下推标记函数, LeftNum, RightNum: 分别为左右子树的数字数量
void PushDown(int Root, int LeftNum, int RightNum) {
   if (Lazy[Root]) {
       // 下推标记
       Lazy[Root << 1] += Lazy[Root];</pre>
       Lazy[Root << 1 | 1] += Lazy[Root];</pre>
       // 根据惰性标修改子节点的值
       Sum[Root << 1] += Lazy[Root] * LeftNum;</pre>
       Sum[Root << 1 | 1] += Lazy[Root] * RightNum;</pre>
       // 清除本节点惰性标记
       Lazy[Root] = 0;
   }
}
// 建树, Left、Right: 当前节点区间, Root: 当前节点编号
void Build(int Left, int Right, int Root) {
   Lazy[Root] = 0;
   // 到达叶子节点
   if (Left == Right) {
       scanf("%d", &Sum[Root]);
       return;
   int Mid = (Left + Right) >> 1;
   // 左子树
   Build(Left, Mid, Root << 1);</pre>
   // 右子树
   Build(Mid + 1, Right, Root << 1 | 1);</pre>
   // 更新信息
```

```
PushUp(Root);
}
// 单点修改, Pos: 修改点位置, Value: 修改值, Left、Right: 当前区
→ 间, Root: 当前节点编号
void PointUpdate(int Pos, int Value, int Left, int Right, int
→ Root) {
   // 修改叶子节点
   if (Left == Right) {
       Sum[Root] += Value;
       return;
   int Mid = (Left + Right) >> 1;
   // 根据条件判断调用左子树还是右子树
   if (Pos <= Mid) {</pre>
       PointUpdate(Pos, Value, Left, Mid, Root << 1);</pre>
   else {
       PointUpdate(Pos, Value, Mid + 1, Right, Root << 1 |
       → 1);
   // 子节点更新后更新此节点
   PushUp(Root);
}
// 区间修改,OperateLeft、OperateRight: 操作区间,Left、Right:
→ 当前区间, Root: 当前节点编号
void IntervalUpdate(int OperateLeft, int OperateRight, int
→ Value, int Left, int Right, int Root) {
   // 若本区间完全在操作区间内
   if (OperateLeft <= Left && OperateRight >= Right) {
       Sum[Root] += Value * (Right - Left + 1);
       // 增加惰性标记,表示本区间 Sum 正确,但子区间仍需要根据
       → 惰性标记调整更新
       Lazy[Root] += Value;
       return;
   int Mid = (Left + Right) >> 1;
   // 下推标记
   PushDown(Root, Mid - Left + 1, Right - Mid);
   // 根据条件判断调用左子树还是右子树
   if (OperateLeft <= Mid) {</pre>
       IntervalUpdate(OperateLeft, OperateRight, Value, Left,

→ Mid, Root << 1);</pre>
```

```
}
    if (OperateRight > Mid) {
        IntervalUpdate(OperateLeft, OperateRight, Value, Mid +
        \rightarrow 1, Right, Root \ll 1 | 1);
    }
    // 更新当前节点信息
    PushUp(Root);
}
// 区间查询, OperateLeft、OperateRight: 操作区间, Left、Right:
    当前区间, Root: 当前节点编号
int Query(int OperateLeft, int OperateRight, int Left, int
→ Right, int Root) {
    // 区间内直接返回
    if (OperateLeft <= Left && OperateRight >= Right) {
        return Sum[Root];
    int Mid = (Left + Right) >> 1;
    // 下推标记
   PushDown(Root, Mid - Left + 1, Right - Mid);
    // 叠加结果
    int Ans = 0;
    if (OperateLeft <= Mid) {</pre>
        Ans += Query(OperateLeft, OperateRight, Left, Mid,
        \rightarrow Root \ll 1);
    if (OperateRight > Mid) {
        Ans += Query(OperateLeft, OperateRight, Mid + 1,
        \rightarrow Right, Root \ll 1 | 1);
    // 返回结果
    return Ans;
}
3.4.2 SegmentTreestruct
#include <bits/stdc++.h>
const int maxn = "Edit";
// 线段树节点
struct Node {
    int Left, Right;
    int Lazy, Tag;
```

```
int Sum;
};
Node SegmentTree[maxn << 2];</pre>
// 更新节点信息
void PushUp(int Root) {
    SegmentTree[Root].Sum = SegmentTree[Root << 1].Sum +</pre>

→ SegmentTree[Root << 1 | 1].Sum;
</pre>
}
// 建树, Left、Right: 当前节点区间, Root: 当前节点编号
void Build(int Left, int Right, int Root) {
    SegmentTree[Root].Left = Left;
    SegmentTree[Root].Right = Right;
    SegmentTree[Root].Lazy = 0;
    SegmentTree[Root].Tag = 0;
    // 叶子节点
    if (Left == Right) {
        scanf("%d", &SegmentTree[Root].Sum);
        return;
    // 左右子树
    int Mid = (Left + Right) >> 1;
    Build(Left, Mid, Root << 1);</pre>
    Build(Mid + 1, Right, Root << 1 | 1);</pre>
    // 更新
    PushUp(Root);
}
// 单点更新, Pos: 修改点位置, Value: 修改值, Root: 当前节点编号
void PointUpdate(int Pos, int Value, int Root) {
    SegmentTree[Root].Sum += Value;
    if (SegmentTree[Root].Left == Pos &&
    → SegmentTree[Root].Right == Pos) {
        return;
    int Mid = (SegmentTree[Root].Left +

    SegmentTree[Root].Right) >> 1;

    if (Pos <= Mid) {</pre>
        PointUpdate(Pos, Value, Root << 1);</pre>
    }
    else {
        PointUpdate(Pos, Value, Root << 1 | 1);</pre>
```

```
PushUp(Root);
}
// 区间修改, Left、Right: 修改区间, Value: 修改值, Root: 当前节点
→ 编号
void IntervalUpdate(int Left, int Right, int Value, int Root)
← {
    if (SegmentTree[Root].Left == Left &&
        SegmentTree[Root].Right == Right) {
        SegmentTree[Root].Lazy = 1;
        SegmentTree[Root].Tag = Value;
        SegmentTree[Root].Sum = (Right - Left + 1) * Value;
        return;
    }
    int Mid = (SegmentTree[Root].Left +
    → SegmentTree[Root].Right) >> 1;
    // 下推更新
    if (SegmentTree[Root].Lazy == 1) {
        SegmentTree[Root].Lazy = 0;
        IntervalUpdate(SegmentTree[Root].Left, Mid,

    SegmentTree[Root].Tag, Root << 1);
</pre>
        IntervalUpdate(Mid + 1, SegmentTree[Root].Right,
        → SegmentTree[Root].Tag, Root << 1 | 1);</pre>
        SegmentTree[Root].Tag = 0;
    if (Right <= Mid) {</pre>
        IntervalUpdate(Left, Right, Value, Root << 1);</pre>
    else if (Left > Mid) {
        IntervalUpdate(Left, Right, Value, Root << 1 | 1);</pre>
    else {
        IntervalUpdate(Left, Mid, Value, Root << 1);</pre>
        IntervalUpdate(Mid + 1, Right, Value, Root << 1 | 1);</pre>
    PushUp(Root);
}
// 区间查询,Left、Right: 查询区间,Root: 当前节点编号
int Query(int Left, int Right, int Root) {
    if (Left == SegmentTree[Root].Left && Right ==

    SegmentTree[Root].Right) {

        return SegmentTree[Root].Sum;
```

```
}
    int Mid = (SegmentTree[Root].Left +

    SegmentTree[Root].Right) >> 1;

    if (Right <= Mid) {</pre>
        return Query(Left, Right, Root << 1);</pre>
    }
    else if (Left > Mid) {
        return Query(Left, Right, Root << 1 | 1);</pre>
    }
    else {
       return Query(Left, Mid, Root << 1) + Query(Mid + 1,</pre>
        \rightarrow Right, Root \ll 1 | 1);
    }
}
3.5 Splay
3.5.1 SplayTree
#include <bits/stdc++.h>
const int maxn = "Edit";
struct SplayTree {
    // Root:Splay Tree 根节点
    int Root, Tot;
    // Son[i][0]:i 节点的左孩子, Son[i][0]:i 节点的右孩子
    int Son[maxn][2];
    // Pre[i]:i 节点的父节点
    int Pre[maxn];
    // Val[i]:i 节点的权值
    int Val[maxn];
    // Size[i]: 以 i 节点为根的 Splay Tree 的节点数 (包含自身)
    int Size[maxn];
    // Cnt[i]: 节点 i 的权值的出现次数
    int Cnt[maxn];
    void PushUp(int X) {
        Size[X] = Size[Son[X][0]] + Size[Son[X][1]] + Cnt[X];
    }
    // 判断 X 节点是其父节点的左孩子还是右孩子
    bool Self(int X) {
       return X == Son[Pre[X]][1];
```

```
}
void Clear(int X) {
    Son[X][0] = Son[X][1] = Pre[X] = Val[X] = Size[X] =
    \hookrightarrow Cnt[X] = 0;
}
// 旋转
void Rotate(int X) {
    int Fa = Pre[X], FaFa = Pre[Fa], XJ = Self(X);
    Son[Fa][XJ] = Son[X][XJ ^ 1];
    Pre[Son[Fa][XJ]] = Pre[X];
    Son[X][XJ ^ 1] = Pre[X];
    Pre[Fa] = X;
    Pre[X] = FaFa;
    if (FaFa) {
        Son[FaFa][Fa == Son[FaFa][1]] = X;
    PushUp(Fa);
    PushUp(X);
}
// 旋转 X 节点到根节点
void Splay(int X) {
    for (int i = Pre[X]; i = Pre[X]; Rotate(X)) {
        if (Pre[i]) {
            Rotate(Self(X) == Self(i) ? i : X);
        }
    Root = X;
}
// 插入数 X
void Insert(int X) {
    if (!Root) {
        Val[++Tot] = X;
        Cnt[Tot]++;
        Root = Tot;
        PushUp(Root);
        return;
    int Cur = Root, F = 0;
    while (true) {
        if (Val[Cur] == X) {
```

```
Cnt[Cur]++;
            PushUp(Cur);
            PushUp(F);
            Splay(Cur);
            break;
        }
        F = Cur;
        Cur = Son[Cur][Val[Cur] < X];</pre>
        if (!Cur) {
            Val[++Tot] = X;
            Cnt[Tot]++;
            Pre[Tot] = F;
            Son[F][Val[F] < X] = Tot;
            PushUp(Tot);
            PushUp(F);
            Splay(Tot);
            break;
        }
    }
}
// 查询 X 的排名
int Rank(int X) {
    int Ans = 0, Cur = Root;
    while (true) {
        if (X < Val[Cur]) {</pre>
            Cur = Son[Cur][0];
        }
        else {
            Ans += Size[Son[Cur][0]];
            if (X == Val[Cur]) {
                Splay(Cur);
                return Ans + 1;
            }
            Ans += Cnt[Cur];
            Cur = Son[Cur][1];
        }
    }
}
// 查询排名为 X 的数
int Kth(int X) {
    int Cur = Root;
    while (true) {
```

```
if (Son[Cur][0] && X <= Size[Son[Cur][0]]) {</pre>
           Cur = Son[Cur][0];
       }
       else {
           X -= Cnt[Cur] + Size[Son[Cur][0]];
           if (X <= 0) {
               return Val[Cur];
           }
           Cur = Son[Cur][1];
       }
   }
}
 * 在 Insert 操作时 X 已经 Splay 到根了
 * 所以 X 的前驱就是 X 的左子树的最右边的节点
 * 后继就是 X 的右子树的最左边的节点
 */
// 求前驱
int GetPath() {
   int Cur = Son[Root][0];
   while (Son[Cur][1]) {
       Cur = Son[Cur][1];
   return Cur;
}
// 求后继
int GetNext() {
   int Cur = Son[Root][1];
   while (Son[Cur][0]) {
       Cur = Son[Cur][0];
   return Cur;
}
// 删除值为 X 的节点
void Delete(int X) {
   // 将 X 旋转到根
   Rank(X);
   if (Cnt[Root] > 1) {
       Cnt[Root] --;
```

```
PushUp(Root);
            return;
        }
        if (!Son[Root][0] && !Son[Root][1]) {
            Clear(Root);
            Root = 0;
            return;
        }
        if (!Son[Root][0]) {
            int Temp = Root;
            Root = Son[Root][1];
            Pre[Root] = 0;
            Clear(Temp);
            return;
        }
        if (!Son[Root][1]) {
            int Temp = Root;
            Root = Son[Root][0];
            Pre[Root] = 0;
            Clear(Temp);
            return;
        }
        int Temp = GetPath(), Old = Root;
        Splay(Temp);
        Pre[Son[Old][1]] = Temp;
        Son[Temp][1] = Son[Old][1];
        Clear(Old);
        PushUp(Root);
    }
};
3.5.2 SplayTreeArray
#include <bits/stdc++.h>
const int maxn = "Edit";
// Root:Splay Tree 根节点
int Root, Tot;
// Son[i][0]:i 节点的左孩子, Son[i][0]:i 节点的右孩子
int Son[maxn][2];
// Pre[i]:i 节点的父节点
int Pre[maxn];
// Val[i]:i 节点的权值
```

```
int Val[maxn];
// Size[i]: 以 i 节点为根的 Splay Tree 的节点数 (包含自身)
int Size[maxn];
// 惰性标记数组
bool Lazy[maxn];
void PushUp(int X) {
   }
void PushDown(int X) {
   if (Lazy[X]) {
       std::swap(Son[X][0], Son[X][1]);
       if (Son[X][0]) {
          Lazy[Son[X][0]] ^= 1;
       }
       if (Son[X][1]) {
          Lazy[Son[X][1]] ^= 1;
       Lazy[X] = 0;
   }
}
// 判断 X 节点是其父节点的左孩子还是右孩子
bool Self(int X) {
   return Son[Pre[X]][1] == X;
}
// 旋转节点 X
void Rotate(int X) {
   int Fa = Pre[X], FaFa = Pre[Fa], XJ = Self(X);
   PushDown(Fa); PushDown(X);
   Son[Fa][XJ] = Son[X][XJ^1];
   Pre[Son[Fa][XJ]] = Pre[X];
   Son[X][XJ ^ 1] = Pre[X];
   Pre[Fa] = X;
   Pre[X] = FaFa;
   if (FaFa) {
       Son[FaFa] [Fa == Son[FaFa] [1]] = X;
   PushUp(Fa); PushUp(X);
}
// 旋转 X 节点到节点 Goal
```

```
void Splay(int X, int Goal = 0) {
    for (int Cur = Pre[X]; (Cur = Pre[X]) != Goal; Rotate(X))

→ {

       PushDown(Pre[Cur]); PushDown(Cur); PushDown(X);
       if (Pre[Cur] != Goal) {
           if (Self(X) == Self(Cur)) {
               Rotate(Cur);
           }
           else {
               Rotate(X);
           }
       }
   }
   if (!Goal) {
       Root = X;
   }
}
// 获取以 R 为根节点 Splay Tree 中的第 K 大个元素在 Splay Tree
→ 中的位置
int Kth(int R, int K) {
   PushDown(R);
    int Temp = Size[Son[R][0]] + 1;
    if (Temp == K) {
       return R;
   if (Temp > K) {
       return Kth(Son[R][0], K);
   }
    else {
       return Kth(Son[R][1], K - Temp);
}
// 获取 Splay Tree 中以 X 为根节点子树的最小值位置
int GetMin(int X) {
   PushDown(X);
   while (Son[X][0]) {
       X = Son[X][0];
       PushDown(X);
   }
   return X;
}
```

```
// 获取 Splay Tree 中以 X 为根节点子树的最大值位置
int GetMax(int X) {
   PushDown(X);
   while (Son[X][1]) {
       X = Son[X][1];
       PushDown(X);
   }
   return X;
}
// 求节点 X 的前驱节点
int GetPath(int X) {
    Splay(X, Root);
    int Cur = Son[Root][0];
   while (Son[Cur][1]) {
       Cur = Son[Cur][1];
   }
   return Cur;
}
// 求节点 Y 的后继节点
int GetNext(int X) {
   Splay(X, Root);
    int Cur = Son[Root][1];
   while (Son[Cur][0]) {
       Cur = Son[Cur][0];
   }
   return Cur;
}
// 翻转 Splay Tree 中 Left~Right 区间
void Reverse(int Left, int Right) {
    int X = Kth(Root, Left), Y = Kth(Root, Right);
    Splay(X, 0);
   Splay(Y, X);
   Lazy[Son[Y][0]] ^= 1;
}
// 建立 Splay Tree
void Build(int Left, int Right, int Cur) {
    if (Left > Right) {
       return;
```

```
}
    int Mid = (Left + Right) >> 1;
    Build(Left, Mid - 1, Mid);
   Build(Mid + 1, Right, Mid);
   Pre[Mid] = Cur;
    Val[Mid] = Mid - 1;
   Lazy[Mid] = 0;
   PushUp(Mid);
    if (Mid < Cur) {</pre>
        Son[Cur][0] = Mid;
    }
    else {
        Son[Cur][1] = Mid;
    }
}
// 输出 Splay Tree
void Print(int Cur) {
    PushDown(Cur);
    if (Son[Cur][0]) {
        Print(Son[Cur][0]);
    // 哨兵节点判断
    if (Val[Cur] !=-INF \&\& Val[Cur] != INF) {
        printf("%d ", Val[Cur]);
    }
    if (Val[Son[Cur][1]]) {
        Print(Son[Cur][1]);
    }
}
3.6 TrieTree
#include <bits/stdc++.h>
const int maxn = "Edit";
struct Trie {
    // Trie Tree 节点
    int Son[maxn][26];
    // Trie Tree 节点数量
    int Tot;
    // 字符串数量统计数组
```

```
int Cnt[maxn];
// Trie Tree 初始化
void TrieInit() {
   Tot = 0;
   memset(Cnt, 0, sizeof(Cnt));
   memset(Son, 0, sizeof(Son));
}
// 计算字母下标
int Pos(char X) {
   return X - 'a';
// 向 Trie Tree 中插入字符串 Str
void Insert(string Str) {
   int Cur = 0, Len = int(Str.length());
   for (int i = 0; i < Len; ++i) {
        int Index = Pos(Str[i]);
       if (!Son[Cur][Index]) {
           Son[Cur][Index] = ++Tot;
       Cur = Son[Cur][Index];
       Cnt[Cur]++;
   }
}
// 查找字符串 Str, 存在返回 true, 不存在返回 false
bool Find(string Str) {
   int Cur = 0, Len = int(Str.length());
   for (int i = 0; i < Len; ++i) {</pre>
       int Index = Pos(Str[i]);
       if (!Son[Cur][Index]) {
           return false;
       Cur = Son[Cur][Index];
   }
   return true;
}
// 查询字典树中以 Str 为前缀的字符串数量
int PathCnt(string Str) {
```

```
int Cur = 0, Len = int(Str.length());
for (int i = 0; i < Len; ++i) {
    int Index = Pos(Str[i]);
    if (!Son[Cur][Index]) {
        return 0;
    }
    Cur = Son[Cur][Index];
}
return Cnt[Cur];
}</pre>
```

# 4 GraphTheory

## 4.1 MinimumSpanningTree

#### 4.1.1 Kruskal

```
#include <bits/stdc++.h>
const int maxn = "Edit";
struct Edge {
   int U, V, Dis;
};
// N: 顶点数, E: 边数, Pre 并查集
int N, E, Pre[maxn];
// edges: 边
Edge edges[maxn];
void Init() {
   // 并查集初始化
   for (int i = 0; i <= N; ++i) {
       Pre[i] = i;
}
// 并查集查询
int Find(int X) {
   int R = X;
   while (Pre[R] != R) {
       R = Pre[R];
   }
   return R;
}
// 并查集合并
void Join(int X, int Y) {
   int XX = Find(X);
   int YY = Find(Y);
   if (XX != YY) {
       Pre[XX] = YY;
    }
}
// Kruskal 算法
```

```
int Kruskal() {
   // 贪心排序
   std::sort(edges + 1, edges + E + 1);
   Init();
    int Res = 0;
   // 选边计算
   for (int i = 1; i <= E; ++i) {
       Edge Temp = edges[i];
       if (Find(Temp.U) != Find(Temp.V)) {
           Join(Temp.U, Temp.V);
           Res += Temp.Dis;
       }
   }
   return Res;
}
4.1.2 Prim
#include <bits/stdc++.h>
const int INF = "Edit";
const int maxn = "Edit";
struct Edge {
   // V: 连接点, Dis: 边权
   int V, Dis;
};
// N: 顶点数, E: 边数
int N, E;
// 松弛更新权值数组
int Dis[maxn];
// 访问标记数组
int Vis[maxn];
// 邻接表
std::vector<Edge> Adj[maxn];
// 建图加边, U. V: 顶点, Weight: 权值
void AddEdge(int U, int V, int Weight) {
   Adj[U].push_back(Edge (V, Weight));
    // 无向图反向建边
   Adj[V].push_back(Edge (U, Weight));
}
```

```
// Prim 算法
int Prim(int Start) {
    memset(Dis, INF, sizeof(Dis));
    memset(Vis, 0, sizeof(Vis));
   Dis[Start] = 0;
    int Res = 0;
    for (int i = 1; i <= N; ++i) {</pre>
        // 选择距已生成树权值最小的顶点
        int U = -1, Min = INF;
        for (int j = 1; j \le N; ++j) {
            if (!Vis[j] && Dis[j] < Min) {</pre>
                U = j;
                Min = Dis[j];
            }
        }
        // 更新、标记
        Vis[U] = 1;
        Res += Min;
        // 松弛
        for (int j = 0; j < int(Adj[U].size()); ++j) {</pre>
            int V = Adj[U][j].V;
            if (!Vis[V] && Adj[U][j].Dis < Dis[V]) {</pre>
                Dis[V] = Adj[U][j].Dis;
        }
    // 返回结果
   return Res;
}
4.2 NetworkFlow
4.2.1 Dinic
#include <bits/stdc++.h>
const int INF = "Edit";
const int maxn = "Edit";
// 边
struct Edge {
    // V: 连接点, Weight: 权值, Next: 上一条边的编号
    int V, Weight, Next;
};
```

```
// 边, 一定要开到足够大
Edge edges[maxn << 1];</pre>
// Head[i] 为点 i 上最后一条边的编号
int Head[maxn];
// 增加边时更新编号
int Tot;
// N: 顶点数, E: 边数
int N, E;
// Bfs 分层深度
int Depth[maxn];
// 当前弧优化
int Current[maxn];
// 链式向前星初始化
void Init() {
   Tot = 0;
   memset(Head, -1, sizeof(Head));
}
// 添加一条由 U 至 V 权值为 Weight 的边
void AddEdge(int U, int V, int Weight, int ReverseWeight = 0)
edges[Tot] = Edge (V, Weight, Head[U]);
   Head[U] = Tot++;
   // 反向建边
   edges[Tot] = Edge (U, ReverseWeight, Head[V]);
   Head[V] = Tot++;
}
// Bfs 搜索分层图, Start: 起点, End: 终点
bool Bfs(int Start, int End) {
   memset(Depth, -1, sizeof(Depth));
   std::queue<int> Que;
   Depth[Start] = 0;
   Que.push(Start);
   while (!Que.empty()) {
       int Cur = Que.front();
       Que.pop();
       for (int i = Head[Cur]; ~i; i = edges[i].Next) {
           if (Depth[edges[i].V] == -1 && edges[i].Weight >
           → 0) {
               Depth[edges[i].V] = Depth[Cur] + 1;
               Que.push(edges[i].V);
```

```
}
       }
   }
   return Depth[End] != -1;
}
// Dfs 搜索增广路径, Cur: 当前搜索顶点, End: 终点, NowFlow: 当前
→ 最大流
int Dfs(int Cur, int End, int NowFlow) {
   // 搜索到终点或者可用当前最大流为 o 返回
   if (Cur == End || NowFlow == 0) {
       return NowFlow;
   }
   // UsableFlow: 可用流量, 当达到 NowFlow 时不可再增加,
    → FindFlow: 递归深搜到的最大流
   int UsableFlow = 0, FindFlow;
   // &i=Current[Cur] 为当前弧优化,每次更新 Current[Cur]
   for (int &i = Current[Cur]; ~i; i = edges[i].Next) {
       if (edges[i].Weight > 0 && Depth[edges[i].V] ==
        → Depth[Cur] + 1) {
           FindFlow = Dfs(edges[i].V, End, std::min(NowFlow -

    UsableFlow, edges[i].Weight));

           if (FindFlow > 0) {
               edges[i].Weight -= FindFlow;
               // 反边
               edges[i ^ 1].Weight += FindFlow;
               UsableFlow += FindFlow;
               if (UsableFlow == NowFlow) {
                  return NowFlow;
               }
           }
       }
   }
   // 炸点优化
   if (!UsableFlow) {
       Depth[Cur] = -2;
   return UsableFlow;
}
// Dinic 算法, Start: 起点, End: 终点
int Dinic(int Start, int End) {
   int MaxFlow = 0;
```

```
while (Bfs(Start, End)) {
       // 当前弧优化
       for (int i = 1; i <= N; ++i) {
           Current[i] = Head[i];
       MaxFlow += Dfs(Start, End, INF);
   // 返回结果
   return MaxFlow;
}
4.2.2 FordFulkerson
#include <bits/stdc++.h>
// 正无穷
const int INF = "Edit";
const int maxn = "Edit";
// N: 顶点数, E: 边数
int N, E;
// 访问标记数组
bool Vis[maxn];
// 邻接矩阵
int Adj[maxn] [maxn];
// Dfs 搜索增广路经, Vertex: 当前搜索顶点, End: 搜索终点,
→ NowFlow: 当前最大流量
int Dfs(int Vertex, int End, int NowFlow) {
   // 搜索到终点结束
   if (Vertex == End) {
       return NowFlow;
   // 标记访问过的顶点
   Vis[Vertex] = true;
   // 枚举寻找顶点
   for (int i = 1; i <= N; ++i) {</pre>
       if (!Vis[i] && Adj[Vertex][i]) {
           int FindFlow = Dfs(i, End, NowFlow <</pre>
           → Adj[Vertex][i] ? NowFlow : Adj[Vertex][i]);
           if (!FindFlow) {
               continue;
           // 找到增广路径后更新邻接矩阵残留网
           Adj[Vertex][i] -= FindFlow;
```

```
Adj[i][Vertex] += FindFlow;
           // 返回搜索结果
           return FindFlow;
       }
   }
   // 未找到增广路径, 搜索失败
   return false;
}
// Ford-Fulkersone 算法, Start: 起点, End: 终点
int FordFulkerson(int Start, int End) {
   // MaxFlow: 最大流, Flow: 搜索到的增广路径最大流
   int MaxFlow = 0, Flow = 0;
   memset(Vis, false, sizeof(Vis));
   // 搜索增广路径
   while (Flow = Dfs(Start, End, INF)) {
       MaxFlow += Flow;
       memset(Vis, false, sizeof(Vis));
   }
   // 返回结果
   return MaxFlow;
}
4.2.3 MinCostMaxFlow
#include <bits/stdc++.h>
const int INF = "Edit";
const int maxn = "Edit";
// 边
struct Edge {
   // V: 连接点, Flow: 流量, Cost: 费用
   int V, Cap, Cost, Flow, Next;
};
// N: 顶点数, E: 边数
int N, E;
int Head[maxn];
// 前驱记录数组
int Path[maxn];
int Dis[maxn];
// 访问标记数组
bool Vis[maxn];
```

```
int Tot;
// 链式前向星
Edge edges[maxn];
// 链式前向星初始化
void Init() {
   Tot = 0;
   memset(Head, -1, sizeof(Head));
}
// 建图加边, U、V 之间建立一条费用为 Cost 的边
void AddEdge(int U, int V, int Cap, int Cost) {
    edges[Tot] = Edge {V, Cap, Cost, 0, Head[U]};
   Head[U] = Tot++;
    edges[Tot] = Edge {U, 0, -Cost, 0, Head[V]};
   Head[V] = Tot++;
}
// SPFA 算法, Start: 起点, End: 终点
bool SPFA(int Start, int End) {
   memset(Dis, INF, sizeof(Dis));
   memset(Vis, false, sizeof(Vis));
   memset(Path, -1, sizeof(Path));
   Dis[Start] = 0;
   Vis[Start] = true;
    std::queue<int> Que;
    while (!Que.empty()) {
        Que.pop();
    }
    Que.push(Start);
    while (!Que.empty()) {
        int U = Que.front();
        Que.pop();
        Vis[U] = false;
        for (int i = Head[U]; ~i; i = edges[i].Next) {
            int V = edges[i].V;
            if (edges[i].Cap > edges[i].Flow && Dis[V] >
            \rightarrow Dis[U] + edges[i].Cost) {
                Dis[V] = Dis[U] + edges[i].Cost;
                Path[V] = i;
                if (!Vis[V]) {
                    Vis[V] = true;
                    Que.push(V);
                }
```

```
}
        }
    }
    return Path[End] != -1;
}
// 最小费用最大流, Start: 起点, End: 终点, Cost: 最小费用
int MinCostMaxFlow(int Start, int End, int &MinCost) {
    int MaxFlow = 0;
    MinCost = 0;
    while (SPFA(Start, End)) {
        int Min = INF;
        for (int i = Path[End]; ~i; i = Path[edges[i ^ 1].V])
            if (edges[i].Cap - edges[i].Flow < Min) {</pre>
                Min = edges[i].Cap - edges[i].Flow;
        }
        for (int i = Path[End]; ~i; i = Path[edges[i ^ 1].V])
            edges[i].Flow += Min;
            edges[i ^ 1].Flow -= Min;
            MinCost += edges[i].Cost * Min;
       MaxFlow += Min;
    // 返回最大流
    return MaxFlow;
}
4.3 ShortestPath
4.3.1 BellmanFord
#include <bits/stdc++.h>
const int INF = "Edit";
const int maxn = "Edit";
struct Edge {
    // U、V: 顶点, Dis: 边权
    int U, V;
    int Dis;
};
```

```
// 松弛更新数组
int Dis[maxn];
// 边
std::vector<Edge> edges;
// Bellman Ford 算法判断是否存在负环回路
bool BellmanFord(int Start, int N) {
    memset(Dis, INF, sizeof(Dis));
    Dis[Start] = 0;
    // 最多做 N-1 次
    for (int i = 1; i < N; ++i) {
        bool flag = false;
        for (int j = 0; j < int(edges.size()); ++j) {</pre>
            if (Dis[edges[j].V] > Dis[edges[j].U] +
            → edges[j].Dis) {
               Dis[edges[j].V] = Dis[edges[j].U] +
                → edges[j].Dis;
               flag = true;
            }
        }
        // 没有负环回路
        if (!flag) {
           return true;
    }
    // 有负环回路
    for (int j = 0; j < int(edges.size()); ++j) {</pre>
        if (Dis[edges[j].V] > Dis[edges[j].U] + edges[j].Dis)
           {
           return false;
        }
    // 没有负环回路
    return true;
}
4.3.2 Dijkstra
#include <bits/stdc++.h>
const int maxn = "Edit";
const int INF = "Edit";
// 边
```

```
struct Edge {
   // V: 连接点, Weight: 权值, Next: 上一条边的编号
   int V, Weight, Next;
};
// 边,一定要开到足够大
Edge edges[maxn << 1];</pre>
// Head[i] 为点 i 上最后一条边的编号
int Head[maxn];
// 增加边时更新编号
int Tot;
// 松弛更新数组, 最短路
int Dis[maxn];
// 链式前向星初始化
void Init() {
   Tot = 0;
   memset(Head, -1, sizeof(Head));
}
// 添加一条 U 至 V 权值为 Weight 的边
void AddEdge(int U, int V, int Weight) {
   edges[Tot] = Edge (V, Weight, Head[U]);
   Head[U] = Tot++;
}
// 最短路优化堆排序规则
struct Cmp {
   bool operator() (const int &A, const int &B) {
       return Dis[A] > Dis[B];
   }
};
// N: 顶点数, E: 边数
int N, E;
// Dijkstra 算法, Start: 起点
void Dijkstra(int Start) {
   std::priority_queue<int, std::vector<int>, Cmp> Que;
   memset(Dis, INF, sizeof(Dis));
   Dis[Start] = 0;
   Que.push(Start);
   while (!Que.empty()) {
```

```
int U = Que.top(); Que.pop();
        for (int i = Head[U]; ~i; i = edges[i].Next) {
            if (Dis[edges[i].V] > Dis[U] + edges[i].Weight) {
               Dis[edges[i].V] = Dis[U] + edges[i].Weight;
                Que.push(edges[i].V);
            }
       }
   }
}
4.3.3 Floyd
#include <bits/stdc++.h>
const int maxn = "Edit";
// N: 顶点数
int N;
// Dis[i][j] 为 i 点到 j 点的最短路
int Dis[maxn] [maxn];
// Floyd 算法
void Floyd() {
    for (int k = 1; k \le N; ++k) {
        for (int i = 1; i <= N; ++i) {
            for (int j = 1; j <= N; ++j) {
                Dis[i][j] = std::min(Dis[i][j], Dis[i][k] +
                → Dis[k][j]);
            }
       }
    }
}
4.3.4 SPFA
#include <bits/stdc++.h>
const int INF = "Edit";
const int maxn = "Edit";
// 边
struct Edge {
    // V: 连接点, Dis: 边权
    int V, Dis;
```

```
};
// N: 顶点数, E: 边数
int N, E;
// 访问标记数组
bool Vis[maxn];
// 每个点的入队列次数
int Cnt[maxn];
// 最短路数组
int Dis[maxn];
// 邻接表
std::vector<Edge> Adj[maxn];
// 建图加边, U V 之间权值为 Weight 的边
void AddEdge (int U, int V, int Weight) {
   Adj[U].push_back(Edge (V, Weight));
   // 无向图建立反向边
   Adj[V].push_back(Edge (U, Weight));
}
// SPFA 算法, Start: 起点
bool SPFA(int Start) {
   memset(Vis, false, sizeof(Vis));
   memset(Dis, INF, sizeof(Dis));
   memset(Cnt, 0, sizeof(Cnt));
   Vis[Start] = true;
   Dis[Start] = 0;
   Cnt[Start] = 1;
   std::queue<int> Que;
   while (!Que.empty()) {
       Que.pop();
   Que.push(Start);
   while (!Que.empty()) {
       int U = Que.front();
       Que.pop();
       Vis[U] = false;
       for (int i = 0; i < int(Adj[U].size()); ++i) {</pre>
           int V = Adj[U][i].V;
           if (Dis[V] > Dis[U] + Adj[U][i].Dis) {
               Dis[V] = Dis[U] + Adj[U][i].Dis;
               if (!Vis[V]) {
                   Vis[V] = true;
```

```
Que.push(V);
// Cnt[i] 为 i 顶点入队列次数, 用来判定是否
→ 存在负环回路
if (++Cnt[V] > N) {
    return false;
}

}

return true;
}
```

# 5 DynamicProgramming

#### 5.1 Contour

```
#include <bits/stdc++.h>
const int maxn = "Edit";
int Dp[2][1 << maxn];</pre>
void Update(int Cur, int A, int B) {
    if (B & (1 << M)) {
        Dp[Cur][B ^ (1 << M)] = Dp[Cur][B ^ (1 << M)] + Dp[Cur]
        \rightarrow 1][A];
    }
}
// 轮廓线 Dp(1*2 在 N*M 图上摆放数)
int Contour(int N, int M) {
    memset(Dp, 0, sizeof(Dp));
    int Cur = 0;
    Dp[Cur][(1 << M) - 1] = 1;
    for (int i = 0; i < N; ++i) {
        for (int j = 0; j < M; ++j) {
            Cur ^= 1;
            memset(Dp[Cur], 0, sizeof(Dp[Cur]));
            for (int k = 0; k < (1 << M); ++k) {
                Update(Cur, k, k << 1);</pre>
                if (i && !(k & (1 << (M - 1)))) {
                     Update(Cur, k, (k << 1) ^ (1 << M) ^ 1);</pre>
                }
                if (j && (!(k & 1))) {
                     Update(Cur, k, (k \ll 1)^3);
                }
            }
        }
    }
    return Dp[Cur][(1 << M) - 1];</pre>
}
5.2 Digit
#include <bits/stdc++.h>
const int maxn = "Edit";
```

```
long long Digit[25];
long long Dp[25][maxn];
// Site: 数位, Statu: 状态, Pre: 前导零, Limit: 数位上界
long long Dfs(long long Site, long long Statu, bool Pre, bool
→ Limit) {
    if (Site == 0) {
       return ?;
    if (!Limit && ~Dp[Site][Statu]) {
       return Dp[Site][Statu];
    }
   long long Max = Limie ? Digit[Site] : 9;
   long long Ans = 0;
   for (int i = 0; i <= Max; ++i) {</pre>
       long long NowStatu = /* 状态转移 */;
       if (NowStatu?) {
           Ans += Dfs(Site - 1, NowStatu, Pre && i == 0,
            }
    }
   if (!Limit) {
       Dp[Site][Statu] = Ans;
   return Ans;
}
long long Cal(long long X) {
   // 数位分解
   long long Len = 0;
   while (X) {
       Digit[++Len] = X \% 10;
       X /= 10;
   return Dfs(Len, 0, true, true);
}
5.3 LCS
#include <bits/stdc++.h>
const int maxn = "Edit";
```

```
// Dp[i][j]:Str1[1]~Str1[i] 和 Str2[1]~Str2[j] 对应的公共子序列
→ 长度
int Dp[maxn] [maxn];
// 最长公共子序列 (LCS)
void LCS(std::string Str1, std::string Str2) {
    for (int i = 0; i < int(Str1.length()); ++i) {</pre>
        for (int j = 0; j < int(Str2.length()); ++j) {</pre>
            if (Str1[i] == Str2[j]) {
                Dp[i + 1][j + 1] = Dp[i][j] + 1;
            }
            else {
                Dp[i + 1][j + 1] = std::max(Dp[i][j + 1], Dp[i]
                \rightarrow + 1][j]);
            }
       }
    }
}
5.4 LIS
#include <bits/stdc++.h>
// 最长不下降子序列 (LIS), Num: 序列
int LIS(std::vector<int> &Num) {
    int Ans = 1;
    // Last[i] 为长度为 i 的不下降子序列末尾元素的最小值
    std::vector<int> Last(int(Num.size()) + 1, 0);
    Last[1] = Num[1];
    for (int i = 2; i <= int(Num.size()); ++i) {</pre>
        if (Num[i] >= Last[Ans]) {
           Last[++Ans] = Num[i];
        }
        else {
            int Index = std::upper_bound(Last.begin() + 1,
            → Last.end(), Num[i]) - Last.begin();
            Last[Index] = Num[i];
    }
    // 返回结果
    return Ans;
}
```

### 5.5 Pack

```
#include <bits/stdc++.h>
const int maxn = "Edit";
int Dp[maxn];
// NValue: 背包容量, NKind: 总物品数
int NValue, NKind;
// 01 背包, 代价为 Cost, 获得的价值为 Weight
void ZeroOnePack(int Cost, int Weight) {
   for (int i = NValue; i >= Cost; --i) {
       Dp[i] = std::max(Dp[i], Dp[i - Cost] + Weight);
}
// 完全背包, 代价为 Cost, 获得的价值为 Weight
void CompletePack(int Cost, int Weight) {
    for (int i = Cost; i <= NValue; ++i) {</pre>
       Dp[i] = std::max(Dp[i], Dp[i - Cost] + Weight);
    }
}
// 多重背包, 代价为 Cost, 获得的价值为 Weight, 数量为 Amount
void MultiplePack(int Cost, int Weight, int Amount) {
    if (Cost * Amount >= NValue) {
       CompletePack(Cost, Weight);
    else {
       int k = 1;
       while (k < Amount) {</pre>
           ZeroOnePack(k * Cost, k * Weight);
           Amount -= k;
           k <<= 1;
       ZeroOnePack(Amount * Cost, Amount * Weight);
   }
}
```

# 6 ComputationalGeometry

### 6.1 Plane

```
#include <bits/stdc++.h>
const double eps = "Edit";
int Sgn(double X) {
    if (fabs(X) < eps) {</pre>
        return 0;
   return X < 0 ? -1 : 1;
}
// 点
struct Point {
    // X: 横坐标, Y: 纵坐标
    double X, Y;
   Point() {}
    Point(double _X, double _Y) {
        X = X;
        Y = Y;
    }
    void input() {
        scanf("%lf%lf", &X, &Y);
    }
    // 减法
   Point operator - (const Point &B) const {
        return Point (X - B.X, Y - B.Y);
    }
        // 点积
        double operator * (const Point &B) const {
                return X * B.X + Y * B.Y;
doub
        // 叉积
    double operator ^ (const Point &B) const {
        return X * B.Y - Y * B.X;
```

```
}
};
// 两点间距离
double Distance(Point A, Point B) {
        return sqrt((B - A) * (B - A));
}
// 线
struct Line {
    Point S, T;
    Line() {}
    Line(Point _S, Point _T) {
        S = _S;
        T = _T;
    }
    void Input() {
        S.Input();
        T.Input();
    }
        // 向量叉积
    double operator ^ (const Line &B) const {
        return (T - S) ^ (B.T - B.S);
    }
    // 判断是否平行
    bool IsParallel(const Line &B) const {
        return Sgn((S - T) ^ (B.S - B.T)) == 0;
    }
    // 求交点
    Point operator & (const Line &B) const {
        double Temp = ((S - B.S) \hat{ } (B.S - B.T)) / ((S - T) \hat{ }
        \hookrightarrow (B.S - B.T));
        return Point(S.X + (T.X - S.X) * Temp, S.Y + (T.Y -
        \rightarrow S.Y) * Temp);
    }
};
// 判断线段 A、B 是否相交
```

```
bool IsIntersect(Line A, Line B) {
    return
        max(A.S.X, A.T.X) >= min(B.S.X, B.T.X) &&
        max(B.S.X, B.T.X) >= min(A.S.X, A.T.X) &&
        max(A.S.Y, A.T.Y) >= min(B.S.Y, B.T.Y) &&
        max(B.S.Y, B.T.Y) >= min(A.S.Y, A.T.Y) &&
        Sgn((B.S - A.T) ^ (A.S - A.T)) * Sgn((B.T - A.T) ^
        \leftrightarrow (A.S - A.T)) <= 0 &&
        Sgn((A.S - B.T) ^ (B.S - B.T)) * Sgn((A.T - B.T) ^
        \rightarrow (B.S - B.T)) <= 0;
}
// 判断线段 A 所在直线与线段 B 是否相交
bool IsIntersect(Line A, Line B) {
    return Sgn((B.S - A.T) ^ (A.S - A.T)) * Sgn((B.T - A.T) ^
    \hookrightarrow (A.S - A.T)) <= 0;
}
// 判断直线 A、B 是否相交
bool IsIntersect(Line A, Line B) {
    return !Parallel(A, B) || (Parallel(A, B) && !(Sgn((A.S -
    \rightarrow B.S) \hat{} (B.T - B.S)) == 0));
}
// 判断 N 个点 (下标 1~N-1) 能否组成凸包
bool IsConvexHull(Point points[], int N) {
    for (int i = 0; i < N; ++i) {
        if (Sgn((points[(i + 1) % N] - points[i]) ^ (points[(i
        \rightarrow + 2) % N] - points[(i + 1) % N])) < 0) {
            return false;
    }
    return true;
}
// 凸包, points: 所有点, 返回凸包总长度
double ConvexHull(std::vector<Point> points) {
    int N = int(points.size());
    // 特判点数小于等于 2 的情况
    if (N == 1) {
        return 0;
    else if (N == 2) {
```

```
return Distance(points[0], points[1]);
    // 查找最左下角的基准点
    int Basic = 0;
   for (int i = 0; i < N; ++i) {
        if (points[i].Y > points[Basic].Y ||
            (points[i].Y == points[Basic].Y && points[i].X <</pre>
            → points[Basic].X)) {
                Basic = i;
        }
    }
    std::swap(points[0], points[Basic]);
    // 对其它点进行极角排序
    std::sort(points.begin() + 1, points.end(), [&] (const
    → Point &A, const Point &B) {
        double Temp = (A - points[0]) ^ (B - points[0]);
        if (Temp > 0) {
            return true;
        else if (!Temp && Distance(A, points[0]) < Distance(B,
        → points[0])) {
            return true;
        return false;
   });
    // 凸包选点
    std::vector<Point> Stack;
   Stack.push_back(points[0]);
    for (int i = 2; i < N; ++i) {
        while (Stack.size() >= 2 && ((Stack.back() -

    Stack[int(Stack.size()) - 2]) ^ (points[i] -

    Stack[int(Stack.size()) - 2])) <= 0) {
</pre>
            Stack.pop_back();
        }
   Stack.push_back(points[0]);
    // 计算总长
    double Ans = 0;
   for (int i = 1; i < int(Stack.size()); ++i) {</pre>
        Ans += Distance(Stack[i], Stack[i - 1]);
    // 返回结果
   return Ans;
}
```

```
// 半平面,表示 S->T 逆时针 (左侧) 的半平面
struct HalfPlane:public Line {
    double Angle;
   HalfPlane() {}
   HalfPlane(Point _S, Point _T) {
       S = _S;
       T = _T;
    }
   HalfPlane(Line ST) {
       S = ST.S;
       T = ST.T;
   }
   void CalAngle() {
       Angle = atan2(T.Y - S.Y, T.X - S.X);
   }
   bool operator < (const HalfPlane &B) const {</pre>
       if (fabs(Angle - B.Angle) > eps) {
           return Angle < B.Angle;</pre>
       return ((S - B.S) ^ (B.T - B.S)) < 0;
   }
};
// 半平面交
struct HPI {
   // 半平面数量
   int Tot;
   // 半平面
   HalfPlane halfplanes[maxn];
   // 半平面交双向队列
   HalfPlane Deque[maxn];
   // 点队列
   Point points[maxn];
   // 半平面交内核
   Point Res[maxn];
   // 双向队列首尾指针
    int Front, Tail;
   // 添加半平面
   void Push(HalfPlane X) {
```

```
halfplanes[Tot++] = X;
}
// 半平面去重
void Unique() {
    int Cnt = 1;
    for (int i = 1; i < Tot; ++i) {</pre>
        if (fabs(halfplanes[i].Angle - halfplanes[i -
           1].Angle) > eps) {
            halfplanes[Cnt++] = halfplanes[i];
        }
    Tot = Cnt;
}
// 判断半平面交是否有内核
bool HalfPlaneInsert() {
    for (int i = 0; i < Tot; ++i) {</pre>
        halfplanes[i].CalAngle();
    sort(halfplanes, halfplanes + Tot);
    Unique();
    Deque[Front = 0] = halfplanes[0];
    Deque[Tail = 1] = halfplanes[1];
    for (int i = 2; i < Tot; ++i) {
        if (fabs((Deque[Tail].T - Deque[Tail].S) ^
        \rightarrow (Deque[Tail - 1].T - Deque[Tail - 1].S)) < eps
        → || fabs((Deque[Front].T - Deque[Front].S) ^
           (Deque[Front + 1].T - Deque[Front + 1].S)) <
        → eps) {
            return false;
        while (Front < Tail && (((Deque[Tail] & Deque[Tail</pre>
        → - 1]) - halfplanes[i].S) ^ (halfplanes[i].T -
        → halfplanes[i].S)) > eps) {
            Tail--;
        while (Front < Tail && (((Deque[Front] &
        → Deque[Front + 1]) - halfplanes[i].S) ^
        \rightarrow (halfplanes[i].T - halfplanes[i].S)) > eps) {
            Front++;
        Deque[++Tail] = halfplanes[i];
    }
```

```
while (Front < Tail && (((Deque[Tail] & Deque[Tail -</pre>
         → 1]) - Deque[Front].S) ^ (Deque[Front].T -
         → Deque[Front].S)) > eps) {
            Tail--;
        }
        while (Front < Tail && (((Deque[Front] & Deque[Front -</pre>
         _{\hookrightarrow} 1]) - Deque[Tail].S) ^ (Deque[Tail].T -
         → Deque[Tail].T)) > eps) {
            Front++;
        if (Tail <= Front + 1) {</pre>
            return false;
        }
        return true;
    }
    // 获取半平面交内核点集 Res
    void GetHalfPlaneInsertConvex() {
        int Cnt = 0;
        for (int i = Front; i < Tail; ++i) {</pre>
            Res[Cnt++] = Deque[i] & Deque[i + 1];
        if (Front < Tail - 1) {</pre>
            Res[Cnt++] = Deque[Front] & Deque[Tail];
        }
    }
};
     Stereoscopic
#include <bits/stdc++.h>
const double INF = 1e20;
const int maxn = "Edit";
const double eps = 1e-8;
const double delta = 0.98;
// 点
struct Point {
        double X, Y, Z;
    void Input() {
        scanf("%lf%lf", &X, &Y, &Z);
    }
```

```
};
// 求点 A、B 间距离
double Distance(Poinn A, Point B) {
    return sqrt((A.X - B.X) * (A.X - B.X) + (A.Y - B.Y) * (A.Y
    \rightarrow - B.Y) + (A.Z - B.Z) * (A.Z - B.Z));
}
int N;
Point points[maxn];
// 模拟退火求 N 个点的最小球覆盖
double MinimimSphereCoverage() {
    Point Cur = points[0];
    double Probability = 10000, Ans = INF;
    while (Probability > eps) {
        int Book = 0;
        for (int i = 0; i < N; ++i) {</pre>
            if (Distance(Cur, points[i] > Distance(Cur,
            → points[Book]))) {
                Book = i;
        }
        double Redius = Distance(Cur, points[Book]);
        Ans = min(Ans, Redius);
        Cur.X += (points[Book].X - Cur.X) / Redius *
        → Probability;
        Cur.Y += (points[Book].Y - Cur.Y) / Redius *
        → Probability;
        Cur.Z += (points[Book].Z - Cur.Z) / Redius *
        → Probability;
        Probability *= delta;
    }
    // 返回覆盖最小球半径
    return Ans;
}
```

## 7 Others

### 7.1 Factorial

```
#include <bits/stdc++.h>
void Factorial() {
    int res[10010];
    int Book = 1;
    int BaoFour = 0;
    res[Book] = 1;
    int n;
    scanf("%d", &n);
    // 乘法计算
    for (int i = 1;i <= n;++i) {
        BaoFour = 0;
        for (int j = 1; j \le Book; ++j) {
            res[j] = res[j] * i + BaoFour;
            BaoFour = res[j] / 10000;
            res[j] = res[j] % 10000;
        }
        if (BaoFour > 0) {
            res[++Book] += BaoFour;
        }
    }
    printf("%d", res[Book]);
    // 补零输出
    for (int i = Book - 1; i > 0; --i) {
        if (res[i] >= 1000) {
            printf("%d", res[i]);
        else if (res[i] >= 100) {
            printf("0%d",res[i]);
        else if (res[i] >= 10) {
            printf("00%d",res[i]);
        else {
            printf("000%d",res[i]);
    putchar('\n');
}
```

### 7.2 FastIO

```
#include <bits/stdc++.h>
// 普通读入挂
template <class T>
inline bool read(T &ret) {
    char c;
    int sgn;
    if (c = getchar(), c == EOF) {
        return false;
    }
    while (c != '-' \&\& (c < '0' || c > '9')) {
        c = getchar();
    sgn = (c == '-') ? -1 : 1;
    ret = (c == '-') ? 0 : (c - '0');
    while (c = getchar(), c >= ^{0}' && c <= ^{9}') {
        ret = ret * 10 + (c - '0');
    }
   ret *= sgn;
    return true;
}
// 普通输出挂
template <class T>
inline void out(T x) {
    if (x < 0) {
        putchar('-');
        x = -x;
    }
    if (x > 9) {
        out(x / 10);
   putchar(x \% 10 + 0);
}
// 牛逼读入挂
namespace fastIO {
    const int MX = 4e7;
    char buf[MX];
    int c, sz;
    void begin() {
        c = 0;
```

```
sz = fread(buf, 1, MX, stdin);
    template <class T>
    inline bool read(T &t) {
        while (c < sz && buf[c] != '-' && (buf[c] < '0' ||
        → buf[c] > '9')) {
           c++;
        }
        if (c >= sz) {
           return false;
        }
        bool flag = 0;
        if (buf[c] == '-') {
           flag = 1;
           c++;
        }
        for (t = 0; c < sz && '0' <= buf[c] && buf[c] <= '9';

→ ++c) {
           t = t * 10 + buf[c] - '0';
        }
        if (flag) {
           t = -t;
       return true;
   }
}
// 超级读写挂
namespace IO{
    #define BUF_SIZE 100000
    #define OUT_SIZE 100000
    #define ll long long
    //fread->read
    bool IOerror=0;
    inline char nc(){
        static char
        → buf[BUF_SIZE],*p1=buf+BUF_SIZE,*pend=buf+BUF_SIZE;
        if (p1==pend){
           p1=buf; pend=buf+fread(buf,1,BUF_SIZE,stdin);
           if (pend==p1){IOerror=1;return -1;}
            //{printf("IO error!\n");system("pause");for
```

```
}
    return *p1++;
inline bool blank(char ch){return ch=='

    ' | | ch=='\n' | | ch=='\r' | | ch=='\t';}
inline void read(int &x){
    bool sign=0; char ch=nc(); x=0;
    for (;blank(ch);ch=nc());
    if (IOerror)return;
    if (ch=='-')sign=1,ch=nc();
    for (;ch>='0'\&\&ch<='9';ch=nc())x=x*10+ch-'0';
    if (sign)x=-x;
}
inline void read(ll &x){
    bool sign=0; char ch=nc(); x=0;
    for (;blank(ch);ch=nc());
    if (IOerror)return;
    if (ch=='-')sign=1,ch=nc();
    for (;ch>='0'&&ch<='9';ch=nc())x=x*10+ch-'0';
    if (sign)x=-x;
}
inline void read(double &x){
    bool sign=0; char ch=nc(); x=0;
    for (;blank(ch);ch=nc());
    if (IOerror)return;
    if (ch=='-')sign=1,ch=nc();
    for (;ch>='0'\&\&ch<='9';ch=nc())x=x*10+ch-'0';
    if (ch=='.'){
        double tmp=1; ch=nc();
        \rightarrow (; ch>='0'&&ch<='9'; ch=nc())tmp/=10.0, x+=tmp*(ch-'0');
    if (sign)x=-x;
inline void read(char *s){
    char ch=nc();
    for (;blank(ch);ch=nc());
    if (IOerror)return;
    for (;!blank(ch)&&!IOerror;ch=nc())*s++=ch;
    *s=0;
inline void read(char &c){
    for (c=nc();blank(c);c=nc());
    if (IOerror){c=-1;return;}
```

```
//fwrite->write
struct Ostream_fwrite{
   char *buf,*p1,*pend;
   Ostream_fwrite(){buf=new
   void out(char ch){
      if (p1==pend){
         fwrite(buf,1,BUF_SIZE,stdout);p1=buf;
      *p1++=ch;
   void print(int x){
      static char s[15],*s1;s1=s;
      if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
      while(x)*s1++=x\%10+'0', x/=10;
      while (s1--!=s) out (*s1);
   }
   void println(int x){
      static char s[15],*s1;s1=s;
      if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
      while(x)*s1++=x\%10+'0', x/=10;
      while(s1--!=s)out(*s1); out('\n');
   void print(ll x){
      static char s[25],*s1;s1=s;
      if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
      while(x)*s1++=x\%10+'0', x/=10;
      while (s1--!=s) out (*s1);
   void println(ll x){
      static char s[25],*s1;s1=s;
      if (!x)*s1++='0'; if (x<0)out('-'), x=-x;
      while(x)*s1++=x\%10+'0',x/=10;
      while(s1--!=s)out(*s1); out('\setminus n');
   void print(double x,int y){
      static 11
      if (x<-1e-12) out('-'), x=-x; x*=mul[y];
```

```
11 x1=(11)floor(x); if (x-floor(x)>=0.5)++x1;
           11 x2=x1/mul[y],x3=x1-x2*mul[y]; print(x2);
           if (y>0){out('.'); for (size_t
            \rightarrow i=1;i<y&&x3*mul[i]<mul[y];out('0'),++i);
            \rightarrow print(x3);}
       void println(double x,int y){print(x,y);out('\n');}
       void print(char *s){while (*s)out(*s++);}
       void println(char *s){while (*s)out(*s++);out('\n');}
       void flush(){if
        ~Ostream_fwrite(){flush();}
    }Ostream;
    inline void print(int x){Ostream.print(x);}
    inline void println(int x){Ostream.println(x);}
    inline void print(char x){Ostream.out(x);}
    inline void println(char

    x){Ostream.out(x);Ostream.out('\n');}
    inline void print(ll x){Ostream.print(x);}
    inline void println(ll x){Ostream.println(x);}
    inline void print(double x,int y){Ostream.print(x,y);}
    inline void println(double x,int y){Ostream.println(x,y);}
    inline void print(char *s){Ostream.print(s);}
    inline void println(char *s){Ostream.println(s);}
    inline void println(){Ostream.out('\n');}
    inline void flush(){Ostream.flush();}
    #undef ll
    #undef OUT_SIZE
    #undef BUF_SIZE
};
using namespace IO;
7.3 LeepYear
#include <bits/stdc++.h>
inline bool Leep(int Year) {
   return (!(Year % 4) && (Year % 100)) || !(Year % 400);
}
7.4 NimGame
#include <bits/stdc++.h>
```

### // 尼姆博弈

```
bool Nim(std::vector<int> Num) {
    int Ans = 0;
    for (int i = 0; i < int(Num.size()); ++i) {</pre>
       Ans ^= Num[i];
    // ans 不为零则先手赢, 否则为后手赢
   return Ans != 0 ? true : false;
}
7.5 vim
syntax on
set nu
set tabstop=4
set shiftwidth=4
set cindent
set mouse=a
map <F9> :call Run()<CR>
func! Run()
       exec "w"
       exec "!g++ -Wall % -o %<"
       exec "!./%<"
endfunc
```