

SECURITY

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Exercise 1

- A. Since the modulo value n of Alice and Bob is the same Alice this means that they also have the same $p * q$ and thus the same $\phi(n)$. The value of Bob's private exponent $d_B = e_B^{-1} \bmod (p - 1)(q - 1)$ can be calculated with the public exponent e . Alice may try to find an inverse for all possible e for which holds that $0 < e < \phi$. If she found a value for d which decrypts in a logical message, she may use this value for all future messages.
- B. Usually the value of $\gcd(p, q) = 1$, so since $\gcd(e_A, e_B) = 1$ also holds Eve can use these as values for p and q . Now Eve may use these values to calculate the n for the modulo. Using the extended Euclidean algorithm she may also calculate the inverse of x and y which may be used for decrypting the messages. This method will work since x and y are used to encrypt the message.

Exercise 2

- A. We assume here that S does not have to verify the identity of Q , since they already have eachothers keys they (as a group) know who they are. S wants to know sure that he's sending a message to, Q , so, he wants to be sure that the public key is correct. He may use the certificate signed by P $Cert_P(Q)$ to verify the public key of Q since the Pk of P is known by all agents.
- B. For the signing of the message S uses his own Sk and anyone knowing the Pk_S can verify this signature. So we need to make sure that W knows the public key of S . We see that we can verify the signature with $Cert_R(S)$ if we know the Pk_R . We may verify that we have the right public key of R with $Cert_P(R)$ since we already know the public key of P . This means that we need the following certificates: $Cert_R(S)$ and $Cert_P(R)$.

Exercise 3

We completed the following basic steps to find the plaintext decryption of the 3 blocks:

1. We find the prime factors p and q of n .
2. Then we calculate ϕ using $p-1$ and $q-1$.
3. Using ϕ and e , we calculate d .
4. Then we now transform the encrypted key to a decimal one to later decrypt it using the above defined d and n .
5. Using this key and the IV, we can decrypt the first block message. I can use the key and the encrypted previous block to decrypt the last 2 blocks
6. Our final step consists of translating this message to plain text.

We wrote down the steps in more detail below:

Action	Result
Already defined data from assignment:	$P_i = D_k(C_i) \oplus C_{i-1}$
	$C_0 = IV$
	$n = 90214098372175031699994652443094898049733$
	$e = 65537$
$\phi = (p - 1) \cdot (q - 1)$	$\phi(n) = (81676168843571580071-1) \cdot (110453391300656531123-1)$ $= 9021409837217503169802522882950669938540$
$de = 1 \bmod \phi(n)$	2511078600645767929925654552860004593113
$M = c^d \bmod n$	8972163497987314734169999025202261871445
$c^d \bmod n$ (key!)	76445561849969483702366060490245165073
Hex convert with IV	B4F5556068CE8D5CE1369C6E694F2020 55BB82092A18AAA9EF680A6C2C948F00 3982E131F0021EFC1BD72FF7AC765011
$P_1 = D_k(C_1) \oplus IV$	01 D3 E7 29 67 79 CD C0 8C 48 5D 03 5E F0 FC 20 54 68 65 20 4D 61 67 69 63 20 57 6F 72 64 73 20
$P_1 = D_k(C_2) \oplus C_2$	D5 87 30 40 3B BF F8 39 80 5B F5 1D 01 6F 6F 53 61 72 65 20 53 71 75 65 61 6D 69 73 68 20 4F 73
$P_1 = D_k(C_3) \oplus C_2$	9E F7 A4 6A C6 AB 61 97 CA 29 A4 AD A7 AD BF 02 73 69 66 72 61 67 65 58 58 58 58 58 58 58 58
Translated to ASCII	The Magic Words are Squeamish Ossifrage