

# The Magic of Nine: Mastering Multiplication and Division

Welcome to an intriguing journey into the world of the number nine! We'll uncover its unique properties, explore simple tricks for multiplication, and learn powerful rules for division. Prepare to be amazed by the hidden elegance of mathematics.



by Tony BM

- I would suggest that you watch the video "Mastering Multiplication and Division by 8" if you haven't yet. The link [🔗](#) is in the description.



# Multiplication by Nine: The Finger Trick

For multiplying any number from 1 to 10 by nine, your hands are your best tool! Simply fold down the finger that corresponds to the number you are multiplying by. Fingers to the left of the folded finger represent the tens digit, and fingers to the right represent the ones digit.

## 1 Example: $9 \times 3$

Fold the 3rd finger. You'll see 2 fingers to the left and 7 to the right.  
Result: 27.

## 2 Example: $9 \times 7$

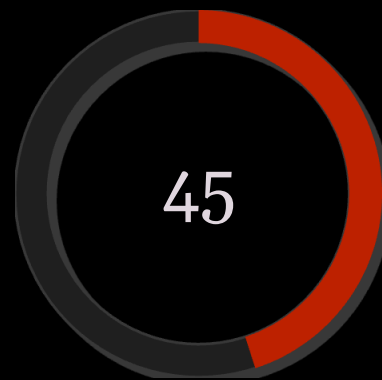
Fold the 7th finger. You'll see 6 fingers to the left and 3 to the right.  
Result: 63.





# The Sum of Digits Rule (Multiplication)

A fascinating property of the number nine is that any multiple of nine will have digits that sum to nine, or a multiple of nine (which then sums to nine). This rule provides a quick way to check if a number is indeed a multiple of 9.



$$9 \times 5 = 45$$

$$4 + 5 = 9$$



$$9 \times 7 = 63$$

$$2 + 0 + 7 = 9$$



$$9 \times 9 = 81$$

$$8 + 1 = 9$$



$$9 \times 11 = 99$$

$$9 + 9 = 18$$

$$1 + 8 = 9$$



# Verifying Large Multiples

This powerful sum-of-digits rule extends far beyond basic multiplication facts. It's an invaluable tool for quickly verifying the accuracy of calculations involving larger numbers, providing a deeper insight into the underlying patterns within our number system.

## Efficient Check

Confirm complex multiplication results quickly without re-calculating.

## Pattern Recognition

Enhance understanding of number relationships and divisibility rules.





# Introduction to Division by Nine

Division, the inverse operation of multiplication, also holds a special relationship with the number nine. If a number is a multiple of nine, it is, by definition, divisible by nine. The key lies in quickly identifying such numbers without resorting to long and tedious calculations.



## Inverse Operation

Division reverses multiplication, revealing the original factor.



## Multiples First

Numbers that are multiples of 9 are inherently divisible by 9.



## Quick Identification

Discover shortcuts to recognize numbers divisible by nine.



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# The Divisibility Rule of Nine (Division)

A number is precisely divisible by nine if, and only if, the sum of its digits is divisible by nine. This rule is a more stringent version of the divisibility rule for three, offering a powerful mental math shortcut.

● Is 72 divisible by 9?

$7 + 2 = 9$ . Since 9 is divisible by 9, yes, 72 is divisible by 9.

● Is 135 divisible by 9?

$1 + 3 + 5 = 9$ . Since 9 is divisible by 9, yes, 135 is divisible by 9.



# Applying the Divisibility Rule to Large Numbers

This divisibility rule is incredibly versatile and works just as effectively for very large numbers as it does for smaller ones. It allows for quick mental estimations and efficient checking of numbers without the need for cumbersome long division, saving time and improving accuracy.

Is 873 divisible by 9?

$8 + 7 + 3 = 18$ . Then,  $1 + 8 = 9$ . Since 9 is divisible by 9, yes, 873 is divisible by 9.

Is 5,264 divisible by 9?

$5 + 2 + 6 + 4 = 17$ . Then,  $1 + 7 = 8$ . Since 8 is not divisible by 9, no, 5,264 is not divisible by 9.





# Unlock the Power of Nine

By understanding and utilizing these simple yet profound properties of the number nine, you can significantly enhance your numerical fluency and confidence. The finger trick provides an accessible entry point to multiplication, while the sum-of-digits rule offers a powerful tool for both checking multiplication and assessing divisibility.



## Simplifying Multiplication

The finger trick makes  $9 \times$  facts easy to grasp and remember.



## Validating Calculations

Use the sum-of-digits rule for quick verification.



## Boosting Fluency

Enhance your mental math skills and number sense.





# Continuous Exploration

Mathematics is full of such elegant patterns and shortcuts. The magic of nine is just one example of the beauty embedded within numbers. We encourage you to continue exploring and discovering the hidden gems in the world of mathematics. Practice these rules and observe how they simplify complex problems, making math more intuitive and enjoyable.