

$$3. \quad H(A) = -0.5 \log_2(0.5) - 0.5 \log_2(0.5) = 1$$

$$H(B) = -\frac{7}{8} \log_2\left(\frac{7}{8}\right) - \frac{1}{8} \log_2\left(\frac{1}{8}\right) = 0.54$$

$$\begin{aligned} H(A|B) &= -\left(\frac{1}{2} \cdot \log_2 \frac{1}{2} - \frac{1}{2} \cdot \log_2 \frac{7}{8}\right) - (0 \log_2 0 - 0 \cdot \log_2 \frac{1}{8}) \\ &\quad - \left(\frac{3}{8} \cdot \log_2 \frac{3}{8} - \frac{3}{8} \cdot \log_2 \frac{7}{8}\right) - \left(\frac{1}{8} \log_2 \frac{1}{8} - \frac{1}{8} \cdot \log_2 \frac{1}{8}\right) \\ &= 0.86 \end{aligned}$$

$$H(A, B) = -\frac{1}{2} \cdot \log_2 \frac{1}{2} - 0 \cdot \log_2 0 - \frac{3}{8} \log_2 \frac{3}{8} - \frac{1}{8} \log_2 \frac{1}{8} = 1.41$$

$$I(A; B) = H(A) - H(A|B) = 0.14$$