# A Tour Of Sage Release 7.0

**The Sage Development Team** 

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This is a tour of Sage that closely follows the tour of Mathematica that is at the beginning of the Mathematica Book.

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**CHAPTER** 

ONE

#### SAGE AS A CALCULATOR

The Sage command line has a sage: prompt; you do not have to add it. If you use the Sage notebook, then put everything after the sage: prompt in an input cell, and press shift-enter to compute the corresponding output.

```
sage: 3 + 5
```

The caret symbol means "raise to a power".

```
sage: 57.1 ^ 100
4.60904368661396e175
```

We compute the inverse of a  $2 \times 2$  matrix in Sage.

```
sage: matrix([[1,2], [3,4]])^(-1)
[ -2     1]
[ 3/2 -1/2]
```

Here we integrate a simple function.

```
sage: x = var('x') # create a symbolic variable sage: integrate(sqrt(x)*sqrt(1+x), x) 1/4*((x + 1)^3/2)/x^3/2) + sqrt(x + 1)/sqrt(x))/((x + 1)^2/x^2 - 2*(x + 1)/x + 1) - 1/8*log(<math>sqrt(x))
```

This asks Sage to solve a quadratic equation. The symbol == represents equality in Sage.

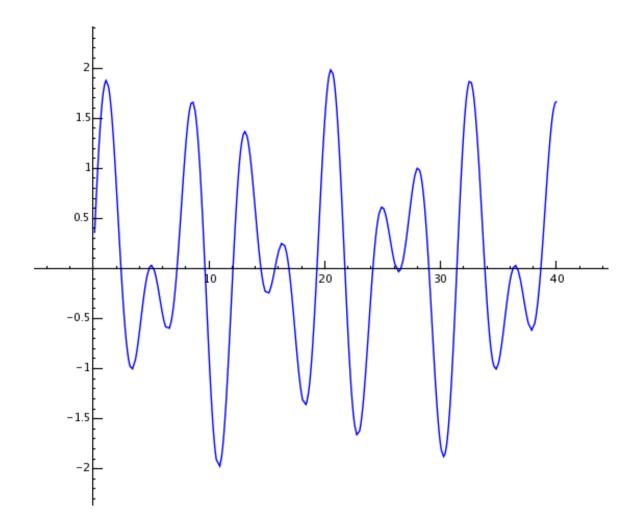
```
sage: a = var('a')
sage: S = solve(x^2 + x == a, x); S
[x == -1/2*sqrt(4*a + 1) - 1/2, x == 1/2*sqrt(4*a + 1) - 1/2]
```

The result is a list of equalities.

```
sage: S[0].rhs()
-1/2*sqrt(4*a + 1) - 1/2
```

Naturally, Sage can plot various useful functions.

```
sage: show(plot(sin(x) + sin(1.6*x), 0, 40))
```



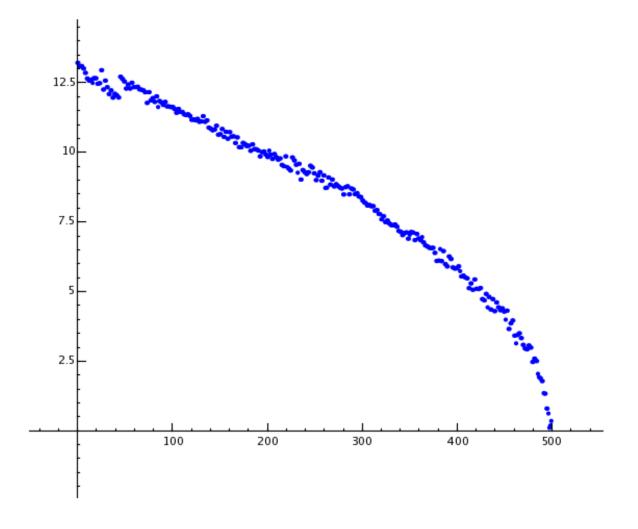
## **POWER COMPUTING WITH SAGE**

First we create a  $500 \times 500$  matrix of random numbers.

```
sage: m = random_matrix(RDF,500)
```

It takes Sage a few seconds to compute the eigenvalues of the matrix and plot them.

```
sage: e = m.eigenvalues() #about 2 seconds
sage: w = [(i, abs(e[i])) for i in range(len(e))]
sage: show(points(w))
```



Thanks to the GNU Multiprecision Library (GMP), Sage can handle very large numbers, even numbers with millions or billions of digits.

```
sage: factorial(100)
9332621544394415268169923885626670049071596826438162146859296389521759999322991560894146397615651828
sage: n = factorial(1000000) #about 2.5 seconds
```

This computes at least 100 digits of  $\pi$ .

```
sage: N(pi, digits=100)
3.141592653589793238462643383279502884197169399375105820974944592307816406286208998628034825342117068
```

This asks Sage to factor a polynomial in two variables.

Sage takes just under 5 seconds to compute the numbers of ways to partition one hundred million as a sum of positive integers.

```
sage: z = Partitions(10^8).cardinality() #about 4.5 seconds
sage: str(z)[:40]
'1760517045946249141360373894679135204009'
```

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# **THREE**

# **ACCESSING ALGORITHMS IN SAGE**

Whenever you use Sage you are accessing one of the world's largest collections of open source computational algorithms.