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# **Sage Reference Manual: Differential Forms**

***Release 7.4***

**The Sage Development Team**

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## OPEN SUBSET OF EUCLIDIAN SPACE WITH COORDINATES

An open subset of Euclidian space with a specific set of coordinates. This is the background on which differential forms can be defined.

AUTHORS:

- Joris Vankerschaver (2010-07-25)

EXAMPLES:

```
sage: x, y, z = var('x, y, z')
sage: S = CoordinatePatch((x, y, z)); S
Open subset of R^3 with coordinates x, y, z
```

```
sage: u, v = var('u, v')
sage: S = CoordinatePatch((u, v)); S
Open subset of R^2 with coordinates u, v
```

TODO:

- Add functionality for metric tensors

**class** sage.tensor.coordinate\_patch. **CoordinatePatch** (*coordinates, metric=None*)

Bases: sage.structure.parent.Parent

Construct a coordinate patch, i.e. an open subset of Euclidian space with a given set of coordinates.

EXAMPLES:

```
sage: x, y, z = var('x, y, z')
sage: S = CoordinatePatch((x, y, z)); S
Open subset of R^3 with coordinates x, y, z

sage: u, v = var('u, v')
sage: T = CoordinatePatch((u, v)); T
Open subset of R^2 with coordinates u, v
sage: loads(T.dumps()) == T
True
```

In a future release, it will be possible to specify a metric tensor on a coordinate patch. For now, providing any kind of metric raises an exception:

```
sage: x, y, z = var('x, y, z')
sage: m = matrix(SR, 3)
sage: S = CoordinatePatch((x, y, z), metric=m)
Traceback (most recent call last):
```

```
...
NotImplementedError: Metric geometry not supported yet.
```

**coordinate** (  $i=0$  )

Return the  $i^{th}$  coordinate on self

INPUT:

- $i$  - integer (optional, default 0)

EXAMPLES:

```
sage: x, y, z = var('x, y, z')
sage: S = CoordinatePatch((x, y, z)); S
Open subset of R^3 with coordinates x, y, z
sage: S.coordinate(0)
x
sage: S.coordinate(1)
y
sage: S.coordinate(2)
z
```

**coordinates** ( )

Return coordinates on this coordinate patch.

OUTPUT:

- list - a list of coordinates on this space.

EXAMPLES:

```
sage: x, y, z = var('x, y, z')
sage: S = CoordinatePatch((x, y, z)); S
Open subset of R^3 with coordinates x, y, z
sage: S.coordinates()
(x, y, z)
```

**dim** ( )

Return the dimension of this coordinate patch, i.e. the dimension of the Euclidian space of which this coordinate patch is an open subset.

EXAMPLES:

```
sage: a, b, c, d, e = var('a, b, c, d, e')
sage: U = CoordinatePatch((a, b, c, d, e)); U
Open subset of R^5 with coordinates a, b, c, d, e
sage: U.dim()
5
```

## ALGEBRA OF DIFFERENTIAL FORMS

Algebra of differential forms defined on a `CoordinatePatch` (an open subset of Euclidian space, see `CoordinatePatch` for details).

AUTHORS:

- Joris Vankerschaver (2010-05-26)

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**Todo**

- Allow for forms with values in a vector space
  - Incorporate Kahler differentials
- 

REFERENCES:

- R. Abraham, J. E. Marsden, and T. S. Ratiu: Manifolds, tensor analysis, and applications. Springer-Verlag 1988, texts in Applied Mathematical Sciences, volume 75, 2nd edition.
- [http://en.wikipedia.org/wiki/Differential\\_form](http://en.wikipedia.org/wiki/Differential_form)

**class** `sage.tensor.differential_forms.DifferentialForms` (*coordinate\_patch=None*)  
Bases: `sage.rings.ring.Algebra`

The algebra of all differential forms on an open subset of Euclidian space of arbitrary dimension.

EXAMPLES:

To define an algebra of differential forms, first create a coordinate patch:

```
sage: p, q = var('p, q')
sage: U = CoordinatePatch((p, q)); U
Open subset of R^2 with coordinates p, q
sage: F = DifferentialForms(U); F
Algebra of differential forms in the variables p, q
```

If no coordinate patch is supplied, a default one (using the variables x, y, z) will be used:

```
sage: F = DifferentialForms(); F
Algebra of differential forms in the variables x, y, z
```

**Element**

alias of *DifferentialForm*

**base\_space** ( )

Return the coordinate patch on which this algebra is defined.

EXAMPLES:

```

sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z)); U
Open subset of R^3 with coordinates x, y, z
sage: F = DifferentialForms(U); F
Algebra of differential forms in the variables x, y, z
sage: F.base_space()
Open subset of R^3 with coordinates x, y, z

```

**gen** ( *i*=0 )

Return the  $i^{\text{th}}$  generator of `self`. This is a one-form, more precisely the exterior derivative of the *i*-th coordinate.

INPUT:

- *i* - integer (optional, default 0)

EXAMPLES:

```

sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z)); U
Open subset of R^3 with coordinates x, y, z
sage: F = DifferentialForms(U); F
Algebra of differential forms in the variables x, y, z
sage: F.gen(0)
dx
sage: F.gen(1)
dy
sage: F.gen(2)
dz

```

**gens** ( )

Return a list of the generators of `self`.

EXAMPLES:

```

sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z)); U
Open subset of R^3 with coordinates x, y, z
sage: F = DifferentialForms(U); F
Algebra of differential forms in the variables x, y, z
sage: F.gens()
(dx, dy, dz)

```

**ngens** ( )

Return the number of generators of this algebra.

EXAMPLES:

```

sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z)); U
Open subset of R^3 with coordinates x, y, z
sage: F = DifferentialForms(U); F
Algebra of differential forms in the variables x, y, z
sage: F.ngens()
3

```



## ELEMENTS OF THE ALGEBRA OF DIFFERENTIAL FORMS

AUTHORS:

- Joris Vankerschaver (2010-07-25)

```
class sage.tensor.differential_form_element.DifferentialForm ( parent,      degree,
                                                             fun=None)

Bases: sage.structure.element.AlgebraElement

Differential form class.
```

EXAMPLES:

In order to instantiate differential forms of various degree, we begin by specifying the CoordinatePatch on which they live, as well as their parent DifferentialForms algebra.

```
sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z))
sage: F = DifferentialForms(U)
sage: form1 = DifferentialForm(F, 0, sin(x*y)); form1
sin(x*y)
```

In the previous example, we created a zero-form from a given function. To create forms of higher degree, we can use the subscript operator access the various components:

```
sage: form2 = DifferentialForm(F, 1); form2
0
sage: form2[0] = 1
sage: form2[1] = exp(cos(x))
sage: form2[2] = 1/ln(y)
sage: form2
1/log(y)*dz + dx + e^cos(x)*dy
```

We may calculate the exterior derivative of a form, and observe that applying the exterior derivative twice always yields zero:

```
sage: dform = form1.diff(); dform
y*cos(x*y)*dx + x*cos(x*y)*dy
sage: dform.diff()
0
```

As can be seen from the previous example, the exterior derivative increases the degree of a form by one:

```
sage: form2.degree()
1
sage: form2.diff().degree()
2
```

The `d` function provides a convenient shorthand for applying the `diff` member function. Since `d` appears in other areas of mathematics as well, this function is not imported in the global namespace automatically:

```
sage: from sage.tensor.differential_form_element import d
sage: form2
1/log(y)*dz + dx + e^cos(x)*dy
sage: d(form2)
-1/(y*log(y)^2)*dy/\dz + -e^cos(x)*sin(x)*dx/\dy
sage: form2.diff()
-1/(y*log(y)^2)*dy/\dz + -e^cos(x)*sin(x)*dx/\dy
sage: d(form1) == form1.diff()
True
```

The wedge product of two forms can be computed by means of the `wedge` member function:

```
sage: form1 = DifferentialForm(F, 2)
sage: form1[0, 1] = exp(z); form1
e^z*dx/\dy
sage: form2 = DifferentialForm(F, 1)
sage: form2[2] = exp(-z)
sage: form1.wedge(form2)
dx/\dy/\dz
```

For this member function, there exists again a procedural function which is completely equivalent:

```
sage: from sage.tensor.differential_form_element import wedge
sage: form1.wedge(form2)
dx/\dy/\dz
sage: wedge(form1, form2)
dx/\dy/\dz
sage: form1.wedge(form2) == wedge(form1, form2)
True
```

#### NOTES:

Differential forms are stored behind the scenes as dictionaries, where the keys are the subscripts of the non-zero components, and the values are those components.

For example, on a space with coordinates  $x, y, z$ , the form

$$f = \sin(x*y) \, dx \wedge dy + \exp(z) \, dy \wedge dz$$

would be represented as the dictionary

$$\{(0, 1): \sin(x*y), (1, 2): \exp(z)\}.$$

Most differential forms are “sparse” in the sense that most of their components are zero, so that this representation is more efficient than storing all of the components in a vector.

#### **abs** ( )

Method not defined for differential forms.

#### EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.abs()
Traceback (most recent call last):
...
NotImplementedError: Absolute value not defined for differential forms.
```

**degree ( )**

Return the degree of self.

EXAMPLES:

```
sage: F = DifferentialForms(); F
Algebra of differential forms in the variables x, y, z
sage: f = DifferentialForm(F, 2)
sage: f[1, 2] = x; f
x*dy/\dz
sage: f.degree()
2
```

The exterior differential increases the degree of forms by one:

```
sage: g = f.diff(); g
dx/\dy/\dz
sage: g.degree()
3
```

**derivative ( \*args, \*\*kwargs)**

Compute the exterior derivative of self. This is the same as calling the `diff` member function.

EXAMPLES:

```
sage: x, y = var('x, y')
sage: U = CoordinatePatch((x, y))
sage: F = DifferentialForms(U)
sage: q = DifferentialForm(F, 1)
sage: q[0] = -y/2
sage: q[1] = x/2
sage: q.diff()
dx/\dy
sage: q.derivative()
dx/\dy
```

Invoking `diff` on a differential form has the same effect as calling this member function:

```
sage: diff(q)
dx/\dy
sage: diff(q) == q.derivative()
True
```

When additional arguments are supplied to `diff`, an error is raised, since only the exterior derivative has intrinsic meaning while derivatives with respect to the coordinate variables (in whichever way) are coordinate dependent, and hence not intrinsic.

```
sage: diff(q, x)
Traceback (most recent call last):
...
ValueError: Differentiation of a form does not take any arguments.
```

**diff ( )**

Compute the exterior differential of self.

EXAMPLES:

```
sage: x, y, z = var('x, y, z')
sage: F = DifferentialForms()
```

```

sage: f = DifferentialForm(F, 0, sin(x*y)); f
sin(x*y)
sage: f.diff()
y*cos(x*y)*dx + x*cos(x*y)*dy
sage: g = DifferentialForm(F, 1)
sage: g[0] = y/2
sage: g[1] = -x/2
sage: g
1/2*y*dx + -1/2*x*dy
sage: g.diff()
-1*dx/\dy
sage: h = DifferentialForm(F, 2)
sage: h[0, 1] = exp(z)
sage: h.diff()
e^z*dx/\dy/\dz

```

The square of the exterior differential operator is identically zero:

```

sage: f
sin(x*y)
sage: f.diff()
y*cos(x*y)*dx + x*cos(x*y)*dy
sage: f.diff().diff()
0

sage: g.diff().diff()
0

```

The exterior differential operator is a derivation of degree one on the space of differential forms. In this example we import the operator `d()` as a short-hand for having to call the `diff()` member function.

```

sage: from sage.tensor.differential_form_element import d
sage: d(f)
y*cos(x*y)*dx + x*cos(x*y)*dy

sage: d(f).wedge(g) + f.wedge(d(g))
(-x*y*cos(x*y) - sin(x*y))*dx/\dy
sage: d(f.wedge(g))
(-x*y*cos(x*y) - sin(x*y))*dx/\dy

sage: d(f.wedge(g)) == d(f).wedge(g) + f.wedge(d(g))
True

```

**is\_zero()**

Return True if `self` is the zero form.

EXAMPLES:

```

sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1); f
0
sage: f.is_zero()
True
sage: f[1] = 1
sage: f.is_zero()
False
sage: f.diff()
0

```

```
sage: f.diff().is_zero()
True
```

**leading\_coefficient** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.leading_coefficient()
Traceback (most recent call last):
...
NotImplementedError: leading_coefficient not defined for differential forms.
```

**leading\_item** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.leading_item()
Traceback (most recent call last):
...
NotImplementedError: leading_item not defined for differential forms.
```

**leading\_monomial** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.leading_monomial()
Traceback (most recent call last):
...
NotImplementedError: leading_monomial not defined for differential forms.
```

**leading\_support** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.leading_support()
Traceback (most recent call last):
...
NotImplementedError: leading_support not defined for differential forms.
```

**leading\_term** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.leading_term()
```

```
Traceback (most recent call last):
...
NotImplementedError: leading_term not defined for differential forms.
```

**map\_coefficients** (*f*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.map_coefficients(lambda x: x)
Traceback (most recent call last):
...
NotImplementedError: map_coefficients not defined for differential forms.
```

**map\_item** (*f*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.map_item(lambda x: x)
Traceback (most recent call last):
...
NotImplementedError: map_item not defined for differential forms.
```

**map\_support** (*f*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.map_support(lambda x: x)
Traceback (most recent call last):
...
NotImplementedError: map_support not defined for differential forms.
```

**trailing\_coefficient** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.trailing_coefficient()
Traceback (most recent call last):
...
NotImplementedError: trailing_coefficient not defined for differential forms.
```

**trailing\_item** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
```

```
sage: f.trailing_item()
Traceback (most recent call last):
...
NotImplementedError: leading_coefficient not defined for differential forms.
```

**trailing\_monomial** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.trailing_monomial()
Traceback (most recent call last):
...
NotImplementedError: trailing_monomial not defined for differential forms.
```

**trailing\_support** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.trailing_support()
Traceback (most recent call last):
...
NotImplementedError: trailing_support not defined for differential forms.
```

**trailing\_term** (*key=None*)

Method not defined for differential forms.

EXAMPLES:

```
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f.trailing_term()
Traceback (most recent call last):
...
NotImplementedError: trailing_term not defined for differential forms.
```

**wedge** (*other*)

Returns the wedge product of *self* and *other*.

EXAMPLES:

```
sage: x, y, z = var('x, y, z')
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f[0] = x^2
sage: f[1] = y
sage: f
x^2*dx + y*dy
sage: g = DifferentialForm(F, 1)
sage: g[2] = z^3
sage: g
z^3*dz
sage: f.wedge(g)
y*z^3*dy/\dz + x^2*z^3*dx/\dz
```

The wedge product is graded commutative:

```
sage: f.wedge(g)
y*z^3*dy/\dz + x^2*z^3*dx/\dz
sage: g.wedge(f)
-y*z^3*dy/\dz + -x^2*z^3*dx/\dz
sage: f.wedge(f)
0
```

When the wedge product of forms belonging to different algebras is computed, an error is raised:

```
sage: x, y, p, q = var('x, y, p, q')
sage: F = DifferentialForms(CoordinatePatch((x, y)))
sage: G = DifferentialForms(CoordinatePatch((p, q)))
sage: f = DifferentialForm(F, 0, 1); f
1
sage: g = DifferentialForm(G, 0, x); g
x
sage: f.parent()
Algebra of differential forms in the variables x, y
sage: g.parent()
Algebra of differential forms in the variables p, q
sage: f.wedge(g)
Traceback (most recent call last):
...
TypeError: unsupported operand parents for wedge: 'Algebra of differential
forms in the variables x, y' and 'Algebra of differential forms in the
variables p, q'
```

**class** `sage.tensor.differential_form_element.DifferentialFormFormatter (space)`

This class contains all the functionality to print a differential form in a graphically pleasing way. This class is called by the `_latex_` and `_repr_` methods of the `DifferentialForm` class.

In a nutshell (see the documentation of `DifferentialForm` for more details), differential forms are represented internally as a dictionary, where the keys are tuples representing the non-zero components of the form and the values are the component functions. The methods of this class create string and latex representations out of the specification of a subscript and a component function.

EXAMPLES:

```
sage: from sage.tensor.differential_form_element import DifferentialFormFormatter
sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z))
sage: D = DifferentialFormFormatter(U)
sage: D.repr((0, 2), sin(x*y))
'sin(x*y)*dx/\dz'
sage: D.latex((0, 2), sin(x*y))
'\\sin\\left(x y\\right) d x \\wedge d z'
sage: D.latex((1, 2), exp(z))
'e^{z} d y \\wedge d z'
```

**latex** (comp, fun)

Latex representation of a primitive differential form, i.e. a function times a wedge product of d's of the coordinate functions.

INPUT:

- `comp` – a subscript of a differential form.
- `fun` – the component function of this form.



EXAMPLES:

```
sage: from sage.tensor.differential_form_element import _
      ↪DifferentialFormFormatter
sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z))
sage: D = DifferentialFormFormatter(U)
sage: D.latex((0, 1), z^3)
'z^{3} d x \wedge d y'
sage: D.latex((), 1)
'1'
sage: D.latex((), z^3)
'z^{3}'
sage: D.latex((0,), 1)
'd x'
```

**repr** ( *comp, fun* )

String representation of a primitive differential form, i.e. a function times a wedge product of d's of the coordinate functions.

INPUT:

- *comp* – a subscript of a differential form.
- *fun* – the component function of this form.

EXAMPLES:

```
sage: from sage.tensor.differential_form_element import _
      ↪DifferentialFormFormatter
sage: x, y, z = var('x, y, z')
sage: U = CoordinatePatch((x, y, z))
sage: D = DifferentialFormFormatter(U)
sage: D.repr((0, 1), z^3)
'z^3*dx/\dy'
```

`sage.tensor.differential_form_element.d ( form )`

Returns the exterior derivative of a given form, i.e. calls the `diff()` member function.

EXAMPLES:

```
sage: from sage.tensor.differential_form_element import d
sage: x, y, z = var('x, y, z')
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f[2] = cos(x); f
cos(x)*dz
sage: d(f)
-sin(x)*dx/\dz
sage: f.diff()
-sin(x)*dx/\dz
sage: d(f) == f.diff()
True
```

`sage.tensor.differential_form_element.sort_subscript ( subscript )`

A subscript is a range of integers. This function sorts a subscript in the sense of arranging it in ascending order. The return values are the sign of the subscript and the sorted subscript, where the sign is defined as follows:

1. `sign == 0` if two or more entries in the subscript were equal.
2. `sign == +1, -1` if a positive (resp. negative) permutation was used to sort the subscript.

INPUT:

- subscript – a subscript, i.e. a range of not necessarily distinct integers

OUTPUT:

- Sign of the permutation used to arrange the subscript, where 0** means that the original subscript had two or more entries that were the same
- Sorted subscript.

EXAMPLES:

```
sage: from sage.tensor.differential_form_element import sort_subscript
sage: sort_subscript((1, 3, 2))
(-1, (1, 2, 3))
sage: sort_subscript((1, 3))
(1, (1, 3))
sage: sort_subscript((4, 2, 7, 9, 8))
(1, (2, 4, 7, 8, 9))
```

`sage.tensor.differential_form_element.wedge ( left, right)`

Computes the wedge product of two forms, i.e. calls the `wedge()` member function.

EXAMPLES:

```
sage: from sage.tensor.differential_form_element import wedge
sage: x, y, z = var('x, y, z')
sage: F = DifferentialForms()
sage: f = DifferentialForm(F, 1)
sage: f[2] = cos(x); f
cos(x)*dz
sage: g = DifferentialForm(F, 1)
sage: g[1] = sin(y); g
sin(y)*dy
sage: wedge(f, g)
-cos(x)*sin(y)*dy/\dz
sage: f.wedge(g)
-cos(x)*sin(y)*dy/\dz
sage: wedge(f, g) == f.wedge(g)
True
```

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