Sage Reference Manual

Release 7.1

The Sage Development Team

CONTENTS

| 1 | User Inter | face | 3 | | |
|---|--------------------|--------------------------------|----|--|--|
| 2 | Graphics | | | | |
| 3 | Mathemat | ics | 7 | | |
| | 3.1 Pare | nts, Elements and Categories | 7 | | |
| | 3.2 Stan | dard Rings and Fields | 7 | | |
| | 3.3 Line | ar Algebra | 7 | | |
| | 3.4 Othe | r Algebraic Structures | 7 | | |
| | 3.5 Disc | rete Mathematics | 8 | | |
| | 3.6 Calc | ulus | 8 | | |
| | 3.7 Geor | metry and Topology | 8 | | |
| | 3.8 Num | ber Theory, Algebraic Geometry | 8 | | |
| | 3.9 Logi | с | 9 | | |
| | 3.10 Prob | ability and Statistics | 9 | | |
| | 3.11 Misc | rellaneous | 9 | | |
| 4 | Programm | ing | 11 | | |
| | | faces | 11 | | |
| 5 | Conseq Information | | | | |

Welcome to Sage's Reference Manual!

This manual is a thematic index of all of Sage's features. It also contains many examples that illustrate their use, all of them systematically tested with each release.

Enjoy Sage!

CONTENTS 1

2 CONTENTS

ONE

USER INTERFACE

- Command Line Interface (REPL)
- Web Notebook

TWO

GRAPHICS

- 2D Graphics
- 3D Graphics

THREE

MATHEMATICS

3.1 Parents, Elements and Categories

- Basic Infrastructure
- Coercion
- Categories
- Base Classes for Rings and Related Objects

3.2 Standard Rings and Fields

- Integers, Rationals, etc.
- Real and Complex Numbers
- Finite Rings and Fields
- Algebraic Numbers
- Polynomials
- Formal Power Series
- Function Fields
- p-Adic Numbers
- Quaternion Algebras

3.3 Linear Algebra

- Matrices and Spaces of Matrices
- Vectors and Modules
- Tensors on free modules of finite rank

3.4 Other Algebraic Structures

• Monoids

- Groups
- Semirings
- Algebras

3.5 Discrete Mathematics

- Combinatorics
- Graph Theory
- Quivers
- Matroid Theory
- Discrete Dynamics
- Coding Theory
- Game Theory

3.6 Calculus

- Symbolic Calculus
- Mathematical Constants
- Elementary and Special Functions
- Asymptotic Expansions (experimental)

3.7 Geometry and Topology

- Combinatorial Geometry
- Cell Complexes and their Homology
- Differential Forms
- Manifolds
- Parametrized Surfaces

3.8 Number Theory, Algebraic Geometry

- Diophantine approximation
- Quadratic Forms
- L-Functions
- Schemes
- Elliptic, Plane, and Hyperelliptic Curves
- Arithmetic Subgroups of SL_2(Z)

- General Hecke Algebras and Hecke Modules
- Modular Symbols
- Modular Forms
- Modular Forms for Hecke Triangle Groups
- Modular Abelian Varieties
- Miscellaneous Modular-Form-Related Modules

3.9 Logic

- Symbolic Logic
- SAT solvers

3.10 Probability and Statistics

- Probability
- Statistics
- Quantitative Finance

3.11 Miscellaneous

- Cryptography
- Numerical Optimization
- Databases
- Games

3.9. Logic 9

FOUR

PROGRAMMING

- Data Structures
- Utilities
- Test Framework
- Parallel Computing

4.1 Interfaces

- Interpreter Interfaces
- C/C++ Library Interfaces

FIVE

GENERAL INFORMATION

- History and License
- genindex
- modindex
- search

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