# 1. Template

```
#include <bits/stdc++.h>
#define endl '\n'
#define ll long long int
#define dl double
#define ld long double
#define ff __float128
#define fore(i,a,b) for (int i = a; i < b; i++)
#define fi first
#define se second
#define pb push_back
#define all(v) v.begin(), v.end()
#define fast_io ios_base::sync_with_stdio(0);cin.tie(0);cout.tie(0);
using namespace std;
typedef vector<int> vi;
typedef vector<vi> vvi;
typedef vector<ll> vll;
typedef vector<vll> vvll;
typedef pair<int,int> pii;
typedef pair<11,11> pll;
typedef vector<pll> vpll;
const int inf = 1 << 30;
const int mod = 1e9+7;
// clear 66 g++ -std=c++17 -02 -Wall template.cpp -o template 66
\rightarrow ./template
// ifstream cin("input.txt"); ofstream cout("output.txt");
```

# 2. Data Structure

## 2.1. Segment tree with lazy

```
struct Node{
  int 1, r;
  ll sum;
  int mark;
  ll lazy;
};//0 +, 1 *, 0 gcd, 1 mcm
const int Neutro = 0;
template<typename TT> struct SegmentTree{
```

```
int n, h;
vector<Node> st;
SegmentTree (int m, vector<TT> &values) : n(m){
  h = 1 << ((int)(ceil(log2(n)) + 1));
  st.resize( h );
  build(1, 1, n, values);
TT merge(TT 1, TT r){ return 1 + r; }//for query
TT getValue(int curr){ return st[curr].sum; }//same^^
int left(int n){ return (n << 1);}</pre>
int right(int n){return (n << 1) | 1; }</pre>
void initLeaf(int curr, TT value){
  st[curr].mark = 0; st[curr].lazy = Neutro;
  st[curr].sum = value;//
void updateFromChildren(int curr){//
  st[curr].sum = st[left(curr)].sum + st[right(curr)].sum;
void updateNodeLazy(int curr, TT value){//updates lazy
  int 1 = st[curr].1, r = st[curr].r;
  st[curr].sum += (r - 1 + 1) * value;//
  st[curr].mark = 1; st[curr].lazy += value;//
void propagateToChildren(int curr){//propagate lazy
  if(st[curr].mark != 0){
    updateNodeLazy(left(curr), st[curr].lazy );
    updateNodeLazy(right(curr), st[curr].lazy);
    st[curr].mark = 0; st[curr].lazy = Neutro;
 }
void build(int curr, int 1, int r, vector<TT> &values){
  st[curr].1 = 1; st[curr].r = r;
  if(1 == r) {
    initLeaf(curr, values[1]);//
  }else{
    int m = ((r - 1) >> 1) + 1;
    build(left(curr), 1, m, values);
    build(right(curr), m + 1, r, values);
    updateFromChildren(curr);
 }
void rangeUpdate(int curr, int 1, int r, int q1, int qr, TT value){
  if( r < ql || qr < l ) return;
  else if( ql \ll l \& r \ll qr){
    updateNodeLazy(curr, value);
```

```
}else{
      propagateToChildren(curr);
      int m = ((r - 1) >> 1) + 1;
      rangeUpdate(left(curr), 1, m, q1, qr, value);
      rangeUpdate(right(curr), m + 1, r, ql, qr, value);
      updateFromChildren(curr);
 }// not lazy
 // void pointUpdate(int curr, int l, int r, int pos, TT value){
 // if(l == r){
        st[curr].sum += value:
  // }elsef
         int \ m = ((r - l) >> 1) + l:
         if(pos <= m) pointUpdate(left(curr), l, m, pos, value);</pre>
  //
         else pointUpdate(right(curr), m + 1, r, pos, value);
         updateFromChildren(curr);
 // }
 1/ 7
 TT rangeQuery(int curr, int 1, int r, int q1, int qr){
    if( r < ql || qr < l ) return Neutro;</pre>
    else if( ql \ll l \& r \ll qr){
     return getValue(curr);
    }else{
      propagateToChildren(curr);
      int m = ((r - 1) >> 1) + 1;
      return merge( rangeQuery(left(curr), 1, m, q1, qr),

→ rangeQuery(right(curr), m+1, r, ql, qr));
 }
 void update( int ql, int qr, int value){
    rangeUpdate(1, 1, n, ql, qr, value);
 }
 TT query(int ql, int qr){
    return rangeQuery(1, 1, n, ql, qr);
 }
 // void printST(){
 // cout << endl << "st = ";
 // fore(i,0,h) cout << st[i].sum << ' '; cout << endl;
 1/ }
};
// vector<ll> nums(n + 1);
// SegmentTree<ll>* st = new SegmentTree<ll>(n, nums);
// st->update(l,r,x); st->query(l, r);
```

### 2.2. Segment tree Geometric sum

```
/* If you have an array [0, 0, 0, 0, 0]
    update(l, r) adds x, x^2, x^3, x^4 starting from l
    Example:
                  x = 2
    update(2, 5) -> [0, 2, 4, 8, 16, 0]
    query(l, r) \rightarrow sum(arr[l], arr[l+1], \ldots, arr[r]) */
struct Node {
    int 1 = 0, r = 0;
    lli ls = 0, rs = 0;
    bool flagLazy = false;
    lli lazy_ls = 0, lazy_rs = 0;
    Node() {}
    Node(int 1, int r) : 1(1), r(r) {}
    // Combine 2 nodes
    Node operator+(const Node &b) {
        Node res(1, b.r);
        res.ls = (ls + b.ls) \% MOD;
        res.rs = (rs + b.rs) \% MOD;
        return res;
    // Update range
    void updateNode(lli sum_l, lli sum_r) {
        ls = (ls + sum_l) % MOD; rs = (rs + sum_r) % MOD;
        lazy_ls = (lazy_ls + sum_l) % MOD;
        lazy_rs = (lazy_rs + sum_r) % MOD;
        flagLazy = true;
    }
    void resetLazy() {
        flagLazy = false;
        lazv_ls = 0; lazv_rs = 0;
    }
};
struct SegmentTree {
    vector<Node> ST;
    int N;
    lli x, x_inv;
    SegmentTree(int n, lli x) : N(n), x(x) {
        x_{inv} = powerMod(x, MOD - 2);
        ST.resize(4 * N); build(1, 1, N);
    void build(int curr, int 1, int r) {
        ST[curr].1 = 1, ST[curr].r = r;
        if (1 == r) return;
        int mid = 1 + (r - 1) / 2;
        build(2 * curr, 1, mid);
        build(2 * curr + 1, mid + 1, r);
```

```
}
                                                                                    return (ans.ls - ans.rs + MOD) * powerMod(1 - x + MOD, MOD - 2) %
   void pushToChildren(int curr) {
                                                                               MOD;
       if (ST[curr].flagLazy) {
                                                                                }
           int size_child_left = (ST[2 * curr].r - ST[2 * curr].l + 1);
                                                                            };
           int size_child_right =
                (ST[2 * curr + 1].r - ST[2 * curr + 1].l + 1);
                                                                             2.3. Treap
           lli sum_r_to_left =
               ST[curr].lazy_rs * powerMod(x_inv, size_child_right) %
\hookrightarrow MOD;
                                                                            /*----*/
           lli sum_l_to_right =
                                                                            struct Node {
               ST[curr].lazy_ls * powerMod(x, size_child_left) % MOD;
                                                                                int key, priority, value;
           ST[2 * curr].updateNode(ST[curr].lazy_ls, sum_r_to_left);
                                                                                Node *left, *right;
           ST[2 * curr + 1].updateNode(sum_l_to_right,
                                                                                Node(int key, int priority)
   ST[curr].lazy_rs);
                                                                                    : key(key), priority(priority), value(key), left(NULL),
           ST[curr].resetLazy();

    right(NULL) {}
       }
                                                                            };
   }
                                                                            // modify this funciton depending on the query that you want
   // UPDATE
                                                                            void update(Node *T) {
   void update(int curr, int 1, int r, int ql, int qr, int start) {
                                                                                if (T) {
       if (1 > qr || r < ql) return;
                                                                                    T->value = T->key;
       else if (ql <= l && r <= qr) {
                                                                                    if (T->left)
           int offset_l = l - start + 1;
                                                                                        T->value += T->left->value;
           int offset_r = offset_l + (r - l + 1) - 1;
                                                                                    if (T->right)
           ST[curr].updateNode(powerMod(x, offset_1),
                                                                                        T->value += T->right->value;
                                                                                }
                                powerMod(x, offset_r + 1));
                                                                            }
           return;
                                                                            // returns the root of the union of treaps T1 and T2
       pushToChildren(curr);
                                                                            Node *merge(Node *T1, Node *T2) {
       int mid = 1 + (r - 1) / 2;
                                                                                if (T1 == NULL) return T2;
       update(2 * curr, 1, mid, q1, qr, start);
                                                                                if (T2 == NULL) return T1;
       update(2 * curr + 1, mid + 1, r, ql, qr, start);
                                                                                if (T1->priority > T2->priority) {
       ST[curr] = ST[2 * curr] + ST[2 * curr + 1];
                                                                                    T1->right = merge(T1->right, T2);
                                                                                    update(T1); return T1;
   void update(int ql, int qr, int start) { update(1, 1, N, ql, qr,
                                                                                } else {

    start); }

                                                                                    T2->left = merge(T1, T2->left);
   // QUERY
                                                                                    update(T2); return T2;
   Node query(int curr, int 1, int r, int q1, int qr) {
                                                                                }
                                                                            }
       if (1 > qr || r < ql) return Node();
       if (ql <= 1 && r <= qr) return ST[curr];
       else {
                                                                            // returns the roots the division of the treap T with parameter x
                                                                            pair<Node *, Node *> split(Node *T, int x) {
           pushToChildren(curr);
           int mid = 1 + (r - 1) / 2;
                                                                                if (T == NULL) return {NULL, NULL};
           return query(2 * curr, 1, mid, q1, qr) +
                                                                                Node *T1, *T2;
                  query(2 * curr + 1, mid + 1, r, ql, qr);
                                                                                if (T->key < x) {
       }
                                                                                    tie(T1, T2) = split(T->right, x);
   }
                                                                                    T->right = T1;
   lli query(int ql, int qr) {
                                                                                    update(T2); update(T);
       auto ans = query(1, 1, N, ql, qr);
                                                                                    return {T, T2};
```

```
} else {
       tie(T1, T2) = split(T->left, x);
       T->left = T2;
       update(T1); update(T);
       return {T1, T};
   }
}
// seed to generate random numbers
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
// generates random numbers
uniform_int_distribution<> dis(numeric_limits<int>::min(),
                               numeric_limits<int>::max());
// inserts a new node with key = x in the treap T, returns the new root
Node *insert(Node *T, int x) {
    Node *TN = new Node(x, dis(rng));
    Node *L, *R;
    tie(L, R) = split(T, x);
    TN = merge(L, TN); TN = merge(TN, R);
    return TN;
}
// returns a treap with all the elements in a
Node *create(vi &a) {
    Node *T = NULL;
    forn(i, (int)a.size()) T = insert(T, a[i]);
    return T;
}
// erases the key x from the treap T
Node *erase(Node *T, int x) {
    Node *L, *R, *AUX;
    tie(L, R) = split(T, x);
    tie(AUX, R) = split(R, x + 1);
    return merge(L, R);
}
// returns the sum of all the keys in te range [l,r]
int query(Node **T, int 1, int r) {
    Node *L, *X, *R;
    tie(L, X) = split(*T, 1);
    tie(X, R) = split(X, r + 1);
    int ans = (X) ? X->value : 0;
    X = merge(L, X); *T = merge(X, R);
    return ans;
}
// returns the k-th node of the sorted nodes in the treap
Node *findKth(Node *T, int k) {
    if (T == NULL) return NULL;
```

```
int aux = T->left ? T->left->value : 0;
if (aux >= k) return findKth(T->left, k);
else if (aux + 1 == k) return T;
else return findKth(T->right, k - aux - 1);
}
```

### 2.4. Implicit Treap

```
/*----Implicit Treap 1 indexed----*/
struct Node {
    int key, priority, size, rev, value;
    Node *left, *right;
    Node(int key, int priority)
        : key(key), priority(priority), size(1), value(key), left(NULL),
};
// pushes the lazy updates
void push(Node *T) {
    if (T) {
        if (T->rev) {
            swap(T->left, T->right);
            if (T->left) T->left->rev ^= 1;
            if (T->right) T->right->rev ^= 1;
            T->rev = 0;
        }
    }
}
// modify this funciton depending on the query that you want
void update(Node *T) {//updateFromChildren
    // push(T);
    if (T) {
        T->size = 1; T->value = T->key;
        if (T->left) {
            T->size += T->left->size;
      T->value += T->left->value;
        if (T->right) {
            T->size += T->right->size;
      T->value += T->right->value;
        }
}
// returns the root of the union of treaps T1 and T2
Node *merge(Node *T1, Node *T2) {
    push(T1), push(T2);
    if (T1 == NULL) return T2;
```

```
if (T2 == NULL) return T1;
                                                                              Node *create(vi a) {
    if (T1->priority > T2->priority) {
                                                                                  Node *T = NULL;
        T1->right = merge(T1->right, T2);
                                                                                  forn(i, a.size()) T = insert(T, a[i], i + 1);
        update(T1); return T1;
                                                                                  return T;
                                                                              }
    } else {
        T2 \rightarrow left = merge(T1, T2 \rightarrow left);
                                                                              // erases the key x from the treap T
        update(T2); return T2;
                                                                              Node *erase(Node *T, int ind) {
    }
                                                                                  Node *L, *R, *AUX;
}
                                                                                  tie(L, R) = split(T, ind + 1);
// returns the roots the division of the treap T with parameter x
                                                                                  tie(L, AUX) = split(L, ind);
// T1 contains all nodes from [1,x), T2 contains all nodes from
                                                                                  return merge(L, R);
\hookrightarrow [x, T->size]
                                                                              }
pair<Node *, Node *> split(Node *T, int x) {
                                                                              //returns the sum of all the keys in te range [l,r]
                                                                               int query(Node* T, int 1, int r){
    push(T);
    if (T == NULL) return {NULL, NULL};
                                                                                Node *L,*X,*R;
    int index;
                                                                                tie(L,X) = split(T,1);
    if (T->left) index = T->left->size + 1;
                                                                                tie(X,R) = split(X,r-1+2);
    else index = 1;
                                                                                int ans = (X) ? X \rightarrow value : 0;
    if (index < x) {
                                                                                X = merge(L,X); T = merge(X,R);
        Node *T1, *T2;
                                                                                return ans;
        tie(T1, T2) = split(T->right, x - index);
        T->right = T1;
        update(T); update(T2);
        return {T, T2};
                                                                              // returns the k-th node of the treap
    } else {
                                                                              Node *findKth(Node *T, int k) {
        Node *T1, *T2;
                                                                                  if (T == NULL) return NULL;
        tie(T1, T2) = split(T->left, x);
                                                                                   int ind = T->left ? T->left->size + 1 : 1;
        T->left = T2;
                                                                                  if (ind > k) return findKth(T->left, k);
        update(T1); update(T);
                                                                                  else if (ind == k) return T;
        return {T1, T};
                                                                                   else return findKth(T->right, k - ind);
    }
                                                                              }
}
                                                                              // reverser the treap from [l,r]
// seed to generate random numbers
                                                                              Node *reverse(Node *T, int 1, int r) {
mt19937 rng(chrono::steady_clock::now().time_since_epoch().count());
                                                                                  Node *L, *R, *AUX;
// generates random numbers
                                                                                   tie(L, R) = split(T, r + 1);
uniform_int_distribution<> dis(numeric_limits<int>::min(),
                                                                                  tie(L, AUX) = split(L, 1);
                                numeric_limits<int>::max());
                                                                                  if (AUX) AUX->rev ^= 1;
// inserts a new node with key = x in the position ind of the treap T.
                                                                                  L = merge(L, AUX); T = merge(L, R);

    returns

                                                                                  return T;
                                                                              }
// the new root
                                                                              // prints the Treap inorder
Node *insert(Node *T, int x, int ind) {
    Node *TN = new Node(x, dis(rng));
                                                                              void inorder(Node *T) {
    Node *L, *R;
                                                                                  if (T) {
    tie(L, R) = split(T, ind);
                                                                                      push(T);
    TN = merge(L, TN); TN = merge(TN, R);
                                                                                       inorder(T->left);
    return TN;
                                                                                       cout << T->key << " ";
}
                                                                                       inorder(T->right);
                                                                                  }
// returns a treap with all the elements in a
```

```
2.5. Policy base
```

}

```
// 20
#include <ext/pb_ds/assoc_container.hpp> // Common file
#include <ext/pb_ds/tree_policy.hpp> // Including
→ tree_order_statistics_node_update
using namespace __gnu_pbds;
template <class T>
using ordered_set =
   tree<T, null_type, less<T>, rb_tree_tag,

→ tree_order_statistics_node_update>;
ordered_set<int> s;
*s.find_by_order(k); // To get the i-th element, O-indexed
s.order_of_key(k); // The number of items strictly smaller than n
                  // For multiset, use T = pair
                  // in second parameter a global counter
                  // s.order_of_key({k, -INF}) will return
                   // how many elements < k
```

## 2.6. SQRT and MO's

```
//SQRT decomposition
//if RTE, change limits to min(br, n)
template <typename TT>
struct SQRT{
 int n, s;
 TT neutro = 0:
 vector<TT> A, B;
 vector<TT> lazy, marks;
 SQRT(int m, vector<TT> &arr): n(m){
    s = sqrt(n) + 1; //puede variar
    A.assign(n, neutro);
    B.assign(n / s + 1, neutro);
    lazy.assign(s, neutro); marks.assign(s, neutro);
    fore(i,0,n){ A[i] = arr[i]; B[i/s] += arr[i]; }
  void pushLazy(int block){
    if(marks[block]){
      fore(i,block,(block+1) * s && i < n) A[i] += lazy[block];</pre>
      lazy[block] = neutro; marks[block] = 0;
```

```
}
  void rangeUpdate(int 1, int r, TT value){
    int bl = 1/s, br = r/s;
    if(bl == br){}
      pushLazy(bl);
      fore(i,1,r+1) A[i] += value;
      TT res = neutro;
      fore(i, bl*s, (bl+1) * s && i < n) res += A[i];
      B[bl] = res;
    }else{
      pushLazy(bl); pushLazy(br);
      fore(i,1,(bl+1) * s){ A[i] += value; B[bl] += value;}
      fore(i,bl+1, br) { B[i] += s * value; lazy[i] += value; marks[i]
\rightarrow = 1;}
      fore(i,br * s, r+1) { A[i] += value; B[br] += value;}
  void pointUpdate(int idx, TT value){//not lazy
    int block = idx / s;
    A[idx] = value:
    TT res = neutro;
    fore(i, block * s, (block + 1) * s && i < n) res += A[i];
    B[block] = res;
  TT rangeQuery(int 1, int r){
    int bl = 1/s, br = r/s;
    TT res = 0;
    if(bl == br){}
      pushLazy(bl);
      fore(i,1,r+1) res += value;
    }else{
      pushLazy(bl); pushLazy(br);
      fore(i,1,(bl+1) * s) res += A[i];
      fore(i,bl+1, br)
                            res += B[i];
      fore(i,br * s, r+1) res += A[i];
    }
 }
};
//MO's algorithm
//arr \ 1 \ or \ 0 \ indexed, \ S = sqrt(n), \ index = index \ of \ the \ query
11 answer, neutro = 0; vll arr;
struct MOquery{
  int 1, r, index, S;
  MOquery(int 1, int r, int idx, int S): 1(1), r(r), index(idx), S(S){}
  bool operator<(const MOquery & q) const{</pre>
    int bl = 1 / S, bq = q.1 / S;
    if(bl == bq && bl & 1) return r > q.r;//a little bit faster
```

6

```
if(bl == bq) return r < q.r;
    return bl < bq;
 }
};
void add(int idx){
  answer += arr[idx];
void remove(int idx){
  answer -= arr[idx];
vector<11> MO(vector<MOquery> & queries){
 vector<ll> ans(queries.size());
 sort(queries.begin(), queries.end());
 11 current = 0;
 int prevL = 0, prevR = -1;
 int i, j;
 answer = neutro;
 for(const MOquery & q : queries){
    while (prevL > q.1) { prevL--; add(prevL); }
    while (prevR < q.r) { prevR++; add(prevR); }</pre>
    while (prevL < q.1) { remove(prevL); prevL++; }</pre>
    while (prevR > q.r) { remove(prevR); prevR--;}
    ans[q.index] = answer;
 }
 return ans;
```

#### 2.7. Convex Hull Trick

```
const int MX = 200005;
const ll inf = 1e18;

bool Q = 0;
struct Line {
    mutable ll m, b, x;
    // Maximo: m < ot.m
    // Minimo: m > ot.m
    bool operator < (const Line ot) const {
      return Q ? x < ot.x : m < ot.m;
    }
};

ll ceil (ll a, ll b) {
    if (a < 0 != b < 0) return a / b;
    return (abs(a) + abs(b) - 1) / abs(b);
}</pre>
```

```
ll intersection (const Line &p, const Line &q) {
  return ceil(q.b - p.b, p.m - q.m);
struct Hull : multiset<Line> {
  bool valid (auto it) {
    if (it == begin()) {
      auto sig = it; sig++;
      if (sig != end()) sig->x = intersection(*it, *sig);
      return it->x = -inf;
    auto ant = it, sig = it;
    ant--, sig++;
    if (sig == end()) {
     it->x = intersection(*it, *ant);
     return 1;
    11 x = intersection(*it, *ant);
    11 y = intersection(*it, *sig);
    if (x > y) return 0;
    it->x = x, sig->x = y;
    return 1;
  void add (ll m, ll b) {
    auto it = lower_bound({m, b, -inf});
    if (it != end() && it->m == m) {
      //Maximo: it->b > b
      //Minimo: it->b < b
      if (it->b > b) return;
      it->b = b;
    } else { it = insert({m, b, -inf}); }
    if (!valid(it)) { erase(it); return; }
    auto ant = it;
    while (ant != begin()) {
     if (valid(--ant)) break;
      erase(ant):
      if (it == begin()) { it->x = -inf; break; }
      ant = it;
    }
    auto sig = it; sig++;
    while (sig != end() && !valid(sig)) erase(sig++);
  11 query (11 x) {
    if (empty()) return 0;
    Q = 1; auto it = upper_bound({0, 0, x});
    it--;
```

```
Q = 0; return x * it->m + it->b;
                                                                                if(tr <= r){
 }
                                                                                for(auto i = tree[v].begin(); i < tree[v].end(); i++){</pre>
};
                                                                                  if(*i <= x) vv.pb(*i);
                                                                                  else break;
                                                                                }
2.8. BIT
                                                                                return;
struct Fenwick {
                                                                              if(t1 > r) return;
    int n;
                                                                              int tm = (tl + tr) / 2;
    vector<long long> tree;
                                                                              query(v*2, tl, tm, l, r, x),
                                                                              query(v*2+1, tm+1, tr, 1, r, x);
    Fenwick(int_n): n(n), tree(n + 1, 0) {}
                                                                              return;
    void update(int idx, long long val) {
        for (; idx \le n; idx += idx & -idx) {
            tree[idx] += val;
                                                                                  Binary Search
        }
    }
                                                                            int lowerBound(vi &nums, int a) {
                                                                                int 1 = 0, r = nums.size() - 1;
    long long query(int idx) {
                                                                                while(1 <= r) {
        long long ret = 0;
                                                                                    int m = ((r - 1) >> 1) + 1;
        for (; idx > 0; idx = idx & -idx) {
                                                                              // if(nums[m] == a) return m;//binary
            ret += tree[idx];
                                                                                nums[m] < a ? 1 = m + 1 : r = m - 1; //lower & binary
                                                                              // nums[m] \le a ? l = m + 1 : r = m - 1; //upper
        return ret;
    }
                                                                                return 1;//return -1; //binary
                                                                            }
    long long query(int x, int y) { return query(y) - query(x - 1); }
};
                                                                            for(int j = 0; j < 300; j++){
                                                                              1d \ mid1 = 1 + (r - 1) / 3, \ mid2 = r - (r - 1) / 3;
2.9. merge sort tree
                                                                              ld f1 = f(p0, Friend1[i + 1], p1, Friend2[i + 1], mid1);
                                                                              ld f2 = f(p0, Friend1[i + 1], p1, Friend2[i + 1], mid2);
vi tree[400000];
                                                                              if(f1 >= f2) 1 = mid1;
vi vv;
                                                                              else r = mid2;
void build(int a[], int v, int tl, int tr) {
    if (tl == tr) {
        tree[v] = vi(1, a[t1]);
    } else {
                                                                                  Flujos
        int tm = (tl + tr) / 2;
        build(a, v*2, tl, tm);
                                                                            4.0.1. Dinic
        build(a, v*2+1, tm+1, tr);
        merge(tree[v*2].begin(), tree[v*2].end(), tree[v*2+1].begin(),

    tree[v*2+1].end(), back_inserter(tree[v]));

                                                                            typedef tuple<int, 11, 11> edge;
    }
                                                                            class max_flow{
}
                                                                              private:
void query(int v, int tl, int tr, int l, int r, int x){
                                                                                int V;
    if(1 > r) return;
                                                                                vector<edge> EL;
```

```
vvi AL;
  vi d, last;
  vpii p;
  bool BFS(int s, int t){
    d.assign(V, -1);d[s] = 0;
    queue<int> q({s});
    p.assign(V, \{-1, -1\});
    while( !q.empty()){
      int u = q.front(); q.pop();
      if( u== t) break;
      for(auto &idx: AL[u]){
        auto &[v, cap, flow] = EL[idx];
        if ( (cap - flow > 0) && d[v] == -1){
          d[v] = d[u] + 1, q.push(v), p[v] = {u, idx};
        }
     }
    }
    return d[t] != -1;
  ll send_one_flow(int s, int t, ll f = inf){
    if (s == t) return f;
    auto &[u,idx] = p[t];
    auto &cap = get<1>(EL[idx]), &flow = get<2>(EL[idx]);
    11 pushed = send_one_flow(s, u, min(f, cap-flow));
    flow += pushed;
    return pushed;
  11 DFS(int u, int t, 11 f = inf){
    if( (u == t) || (f == 0)) return f;
    for(int &i = last[u]; i < (int) AL[u].size(); ++i){</pre>
      auto &[v, cap, flow] = EL[AL[u][i]];
      if (d[v] != d[u] + 1) continue;
      if(ll pushed = DFS(v, t, min(f, cap - flow))){
        flow += pushed;
        auto &rflow = get<2> (EL[AL[u][i] ^ 1]);
        rflow -= pushed;
        return pushed;
      }
    }
    return 0;
public:
  max_flow(int initialV) : V(initialV){
    EL.clear();
    AL.assign(V, vi());
  void add_edge(int u, int v, ll w, bool directed = true){
    if( u == v) return;
```

```
EL.emplace_back(v, w, 0);
      AL[u].pb(EL.size() - 1);
      EL.emplace_back(u, directed ? 0 : w, 0);
      AL[v].pb(EL.size() - 1);
    11 edmonds_karp(int s, int t){
      11 \text{ mf} = 0;
      while( BFS(s,t)){
        11 f = send_one_flow(s, t);
        if ( f == 0)break;
        mf += f:
      return mf;
    11 dinic(int s, int t ){
      11 \text{ mf} = 0;
      while( BFS(s,t)){
        last.assign(V, 0);
        while( ll f = DFS(s,t)){
          mf += f;
        }
      }
      return mf;
    }
};
4.0.2. Ford-Fulkerson
const int sink = 37;
int C[50][50], F[50][50], visited[50];
int sendFlow(int node, int bottleneck){
  if(node == sink){
    return bottleneck;
  visited[node] = true;
  fore(i,0,sink+1){
    int f = C[node][i] - F[node][i];
    if(f>0 && !visited[i]){
      f = sendFlow(i, min(f, bottleneck));
      if(!f) continue;
      F[node][i] += f;
      F[i][node] -= f;
      return f;
    }
  }
  return 0;
```

#### 4.0.3. maxflow mincost

```
template <typename T = int> struct Edge {
    int to;
    T flow, capacity, cost;
    int idx;
    bool rev;
    Edge *res;
    Edge(int to, T capacity, T cost, int idx, bool rev = false)
        : to(to), flow(0), capacity(capacity), cost(cost), idx(idx),
→ rev(rev) {}
    void addFlow(T flow) {
        this->flow += flow:
        this->res->flow -= flow;
    }
};
// MUCHO OJO CON ESTO
const lli INF_FLOW = 1e15, INF_COST = 1e9;
template <typename T = int> struct MinCostFlow {
    vector<vector<Edge<T> *>> adjList;
    int N;
    MinCostFlow(int N) : N(N) { adjList.resize(N); }
    void addEdge(int u, int v, T capacity, T cost, int idx) {
        Edge<T> *uv = new Edge<T>(v, capacity, cost, idx);
        Edge<T> *vu = new Edge<T>(u, 0, -cost, idx, true);
        uv->res = vu:
        vu->res = uv;
        adjList[u].push_back(uv);
        adjList[v].push_back(vu);
    }
    pair<T, T> getMinCostFlow(int s, int t) {
        vector<T> dist(N), cap(N);
        vector<bool> inQueue(N);
        vector<Edge<T> *> parent(N);
        T minCost = 0, maxFlow = 0;
        while (true) {
            fill(all(dist), INF_COST);
            fill(all(cap), 0);
            fill(all(parent), nullptr);
```

```
queue<int> q;
            q.push(s);
            dist[s] = 0;
            cap[s] = INF_FLOW;
            while (!q.empty()) {
                int u = q.front();
                q.pop();
                inQueue[u] = 0;
                for (auto E : adjList[u]) {
                     int v = E -> to;
                     if (E->flow < E->capacity && dist[u] + E->cost <

    dist[v]) {

                         dist[v] = dist[u] + E->cost;
                         cap[v] = min(cap[u], E->capacity - E->flow);
                         parent[v] = E;
                         if (!inQueue[v]) {
                             inQueue[v] = 1;
                             q.push(v);
                        }
                    }
                }
            }
            if (!parent[t])
                break;
            // if(dist[t] > 0) break;
            maxFlow += cap[t];
            minCost += cap[t] * dist[t];
            for (int u = t; u != s; u = parent[u]->res->to) {
                parent[u] ->addFlow(cap[t]);
            }
        }
        return {minCost, maxFlow};
};
```

# 5. Strings

#### 5.1. aho-corasik

```
//#define feach(f, q) for(auto &f: q)
const int N=1e5+10, MOD=1e9+7, SIG=26;
int id=1, dp[N];
string s;
vector<int> adj[2*N];
struct node{
 int fail,ch[SIG]={};
 vector<int> lens;
}t[2*N];
void insert(string s){
 int u=1;
 for(auto &c: s){
   c-='a';
   if(!t[u].ch[c]) t[u].ch[c]=++id;
    u=t[u].ch[c];
 t[u].lens.pb(s.size());
void dfs(int u){
 t[u].lens.insert(t[u].lens.end(), t[t[u].fail].lens.begin(),

    t[t[u].fail].lens.end());
 for(auto &v: adj) dfs(v);
}
void build(){
 queue<int> q;
 int u=1;
 t[1].fail=1;
 fore(i,0,SIG) {
   if(t[u].ch[i]) t[t[u].ch[i]].fail=u, q.push(t[u].ch[i]);
    else t[u].ch[i]=1;
 }
 while(!q.empty()){
    u=q.front(); q.pop();
    fore(i,0,SIG){
      if(t[u].ch[i]) t[t[u].ch[i]].fail=t[t[u].fail].ch[i],

    q.push(t[u].ch[i]);
      else t[u].ch[i]=t[t[u].fail].ch[i];
   }
 fore(i,2,id+1) adj[t[i].fail].pb(i);
 dfs(1);
```

### 6. Math

#### 6.1. FFT

```
using cd = complex<double>;
const double PI = acos(-1);
void fft(vector<cd> & a, int inv) {
    int n = a.size():
   for(int i = 1, j = 0; i < n - 1; ++i){
    for(int k = n >> 1; (j \hat{} = k) < k; k >>= 1);
    if(i < j) swap(a[i], a[j]);
  }
  vector < cd > w(n >> 1);
    for (int k = 2: k \le n: k \le 1) {
        // cd w1 = polar(1.0, 2 * PI / k * inv);
        w[0] = 1;
        for (int j = 1; j < k >> 1; j++) // best precision but slower
            w[j] = polar(1.0, 2 * j * PI / k * inv);
          // w[j] = w[j-1]*w1;
        for (int i = 0; i < n; i += k) {
            for (int j = 0; j < k >> 1; j++) {
                cd u = a[i + j], v = a[i + j + (k >> 1)] * w[j];
                a[i + j] = u + v;
                a[i + j + (k >> 1)] = u - v;
            }
        }
    if (inv == -1) for (cd & x : a) x \neq n;
}
vector<11> multiply(vector<11> const& a, vector<11> const& b) {
    vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
    int n = 1;
    while (n < a.size() + b.size() - 1) n <<= 1;
  fa.resize(n); fb.resize(n);
  fft(fa, 1); fft(fb, 1);
  fore(i,0,n) fa[i] *= fb[i];
    fft(fa, -1);
    vector<ll> result(n);
    for (int i = 0; i < n; i++) result[i] = round(fa[i].real());</pre>
    return result;
```

```
}
/* if it's numbers and not polynomials, we have to normalise */
void normalise(vll &ans) {
 int carry = 0;
 for (ll i = 0; i < ans.size(); ++i) {
    ans[i] += carry;
   carry = ans[i] / 10;
    ans[i] \%= 10;
 if(carry > 0) ans.pb(carry);
 int t = ans.size();
 while(t > 0 && ans[t-1] == 0){
    ans.pop_back();
   t--;
 }
 if(ans.size() == 0) ans.push_back(0);
6.2. NTT
const int mod = 998244353, g = 3;
lli powMod(lli a, lli b, lli mod){
 lli ans = 1;
 b \% = mod - 1;
 if(b < 0) b+= mod-1;
 while(b){
    if (b&1) ans = ans * a \% mod;
   a = a*a \%mod;
   b>>=1;
 }
 return ans;
lli inverse(lli a, lli mod){return powMod(a,mod-2, mod);}
template<int mod, int g>
void ntt(vector<int> & X, int inv){
 int n = X.size();
 for(int i = 1, j = 0; i < n - 1; ++i){
   for(int k = n >> 1; (j \hat{} = k) < k; k >>= 1);
    if(i < j) swap(X[i], X[j]);</pre>
 }
 vector<lli> wp(n>>1, 1);
 for(int k = 1; k < n; k <<= 1){
    lli wk = powMod(g, inv * (mod - 1) / (k<<1), mod);
    for(int j = 1; j < k; ++j)
      wp[j] = wp[j - 1] * wk % mod;
```

```
for(int i = 0; i < n; i += k << 1){
      for(int j = 0; j < k; ++j){
        int u = X[i + j], v = X[i + j + k] * wp[j] % mod;
       X[i + j] = u + v < mod ? u + v : u + v - mod;
        X[i + j + k] = u - v < 0 ? u - v + mod : u - v;
   }
  }
  if(inv == -1){
   lli nrev = inverse(n, mod);
    for(int i = 0; i < n; ++i)
      X[i] = X[i] * nrev % mod;
 }
}
template<int mod, int g>
vector<int> multiply(vector<int> const& a, vector<int> const& b) {
    vector<int> fa(a.begin(), a.end()), fb(b.begin(), b.end());
    int n = 1:
    while (n < a.size() + b.size() - 1) n <<= 1;
  fa.resize(n); fb.resize(n);
  ntt<mod, g>(fa, 1); ntt<mod, g>(fb, 1);
  fore(i,0,n) fa[i] = (1LL * fa[i] * fb[i]) % mod;
    ntt < mod, g > (fa, -1);
    return fa;
}
6.3. Field extension
```

```
int sq = 5;
// const lli sqrt5 = 383008016;//mod1e9+9
const ll mod = 10000000007;//is important to be CONST
struct EX {
    ll re, im;
    EX (ll re = 0, ll im = 0) : re(re), im(im){}

    EX& operator = (EX oth) {
        return re = oth.re, im = oth.im, *this;
    }
    int norm () const {
        return trim((1ll * re * re - 1ll * sq * im % mod * im) % mod);
    }

    EX conj () const {
        return {re, trim(-im)};
    }
}
```

```
EX operator * (EX ot) const {
  return {
    int((111 * re * ot.re + 111 * sq * im % mod * ot.im) % mod),
    int((111 * re * ot.im + 111 * im * ot.re) % mod)
  };
};
EX& operator *= (const EX& ot) {
  *this = *this * ot; return *this;
}
EX operator * (ll k) const {
  k = ((k \% mod) + mod) \% mod;
  return { (re * k) % mod, (im * k) % mod };
};
EX operator / (ll n) const {
  return { re * inv(n) % mod, im * inv(n) % mod };
}
EX operator / (EX ot) const {
  return *this * ot.conj() / ot.norm();
}
EX& operator /= (const EX& ot) {
  *this = *this / ot; return *this;
}
EX operator + (EX ot) const {
  return { trim(re + ot.re), trim(im + ot.im) };
}
EX% operator += (const EX% ot) {
  *this = *this + ot; return *this;
}
EX operator - (EX ot) const {
  return { trim(re - ot.re), trim(im - ot.im) };
}
EX& operator -= (const EX& ot) {
  *this = *this - ot; return *this;
}
EX pow (ll p) const {
  EX res(1), b = *this;
  while (p) {
    if (p \& 1) res *= b; b *= b; p /= 2;
  return res;
bool operator == (EX ot) const {
  return re == ot.re && im == ot.im;
bool operator != (EX ot) const {
  return !(*this == ot);
}
```

```
static ll trim(ll a) {
    if (a >= mod) a -= mod;
    if (a < 0) a += mod;
    return a;
  static ll inv (ll b) {
    11 \text{ res} = 1, p = \text{mod} - 2;
    while (p) {
      if (p & 1) res = 111 * res * b % mod;
      b = 111 * b * b \% mod;
      p /= 2;
    }
    return res;
 };
};
6.4. nCr
vll fact(200007,0), inv(200007,0), invfact(200007,0);
void factorial(){
  fact[0] = 1; inv[0] = inv[1] = 1; invfact[0] = 1;
  fore(i,1,200005) fact[i] = (fact[i-1] * i) % MOD;
  fore(i,2,200005) inv[i] = inv[MOD % i] * (MOD - MOD / i) % MOD;
  fore(i,1,200005) invfact[i] = invfact[i-1] * inv[i] % MOD;
11 ncr(11 n, 11 r){
  return fact[n] * invfact[n - r] % MOD * invfact[r] % MOD ;
6.5. Discrete Root
int generator(int p) {
    vector<int> fact;
    int phi = p-1, n = phi;
    for (int i = 2; i * i <= n; ++i)
        if (n \% i == 0)
            fact.push_back(i); while (n \% i == 0) n /= i;
    if (n > 1) fact.push_back(n);
    for (int res = 2; res <= p; ++res) {
        bool ok = true;
        for (int factor : fact)
            if (powmod(res, phi / factor, p) == 1)
                ok = false; break;
        if (ok) return res;
```

}

```
bool MillerRabin(lli n){
    return -1;
}
                                                                                  if(n < 2) return false;
vi\ rootK()\ \{//\ finds\ all\ numbers\ x\ such\ that\ x^k=a\ (mod\ n)
                                                                                  if(n <= 3) return true;
    int n, k, a;
                                                                                  if( ~n & 1) return false;
    scanf("%d %d %d", &n, &k, &a);
                                                                                  for(lli a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}){
    if (a == 0) return vi(1,1);
                                                                                      if(n == a) return true;
    int g = generator(n);
                                                                                  if(!singleTest(a, n)) return false;
    // Baby-step giant-step discrete logarithm algorithm
    int sq = (int) sqrt (n + .0) + 1;
                                                                                  return true; //Probability = 1 - (1/4) ^size_of(vector_a)
    vector<pair<int, int>> dec(sq);
                                                                              }
    for (int i = 1; i \le sq; ++i)
        dec[i-1] = \{powmod(g, i * sq * k % (n - 1), n), i\};
                                                                              bool MillerRabinOther(lli n){
    sort(dec.begin(), dec.end());
                                                                                  if(n < 2) return false;
    int any_ans = -1;
                                                                                  if(n <= 3) return true:
    for (int i = 0; i < sq; ++i) {
                                                                                  if( "n & 1) return false;
        int my = powmod(g, i * k \% (n - 1), n) * a \% n;
                                                                                  lli d = n-1, s = 0; //n-1 = 2^s*k
        auto it = lower_bound(dec.begin(), dec.end(), make_pair(my, 0));
                                                                                  for(;(^d\&1); d >>= 1, s++); //d = k
                                                                                  for(lli a: {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}){
        if (it != dec.end() && it->first == my) {
            any_ans = it->second * sq - i;break;
                                                                                      if(n == a) return true;
        }
                                                                                      i128 residuo = powerMod(a, d, n);
    }
                                                                                      if(residuo == 1 or residuo == n-1) continue;
    if (any_ans == -1) return vi(1,-1);
                                                                                      lli x = s;
                                                                                      while (--x) {
    // Print all possible answers
    int delta = (n-1) / gcd(k, n-1);
                                                                                          residuo = (residuo * residuo) % n;
    vi ans;
                                                                                          if(residuo == n-1) break;
    for (int cur = any_ans % delta; cur < n-1; cur += delta)
                                                                                      }
        ans.push_back(powmod(g, cur, n));
                                                                                      if(x==0) return false;
    sort(ans.begin(), ans.end());
    return ans;
                                                                                  return true; //Probability = 1 - (1/4)^size_of(vector_a)
}
                                                                              }
```

#### 6.6. Miller Rabin

# 7. Graphs

#### 7.1. bfs-dfs

```
void bfs(vector<vector<int>> &graph, int start){
  int n = graph.size();
  queue<int> q; q.push(start);
  vector<int> visited(n,0);
  while(!q.empty()){
    int current = q.front(); q.pop();
    for(auto next: graph[current])
      if(!visited[next])
        q.push(next);
  }
  return;
```

```
}
                                                                            int n = graph.size();
                                                                            queue<pair<int, int>> q; //node, color
void dfs(int current, vector<vector<int>> &graph, vector<int> visited){
 visited[current] = 1;
                                                                            q.push({start, 1});
 for(auto next: graph[current])
                                                                            color[start] = 1;
   if(!visited[next]) dfs(next, graph, visited);
                                                                            while(!q.empty()){
 return:
                                                                              auto current = q.front(); q.pop();
                                                                              for (int child :graph[current.first]){
                                                                                if(color[child] == current.second) return false;
                                                                                if(color[child] == 0){
7.2. cicles
                                                                                  color[child] = current.second == 1 ? 2 : 1;
                                                                                  q.push({child, color[child]});
int hasCycleDirected(int current, vector<vector<int>> &graph, vector<int>
                                                                              }
}
 if(color[current] == 1) return 1;
 if(color[current] == 2) return 0;
                                                                            return true;
  color[current] = 1;
 int ans = 0;
 for(int child: graph[current]){
                                                                          7.3. Dijkstra
   ans = ans | hasCycleDirected(child, graph, color);
  color[current] = 2;
                                                                          vi dijkstra(int start, int n, vvpii graph){
 return ans;
                                                                            priority_queue<pii, vpii, greater<pii>>> pq;
                                                                            vi pesos(n, INT_MAX);
int hasCycleUndirected(int current, int father, vector<vector<int>>
                                                                            pq.push({0, start});
pesos[start] = 0;
 if(color[current] == 1) return 1;
                                                                            while(!pq.empty()){
  color[current] = 1;
                                                                              int v = pq.top().second;pq.pop();
 int ans = 0;
                                                                              for (auto next : graph[v]){
 for(int child: graph[current]) if(child != father)
                                                                                int u = next.first, w = next.second;
   ans = ans | hasCycleUndirected(child, current, graph, color);
                                                                                if(pesos[u] > pesos[v] + w){
                                                                                  pesos[u] = pesos[v] + w;
 return ans:
                                                                                  pq.push({pesos[u], u });
int isBipartiteDFS(int current, vector<vector<int>> &graph, vector<int>
}
 bool is = 1;
 for(int child : graph[current]){
                                                                            return pesos;
   if(color[child] == 0){//no esta coloreado
      color[child] = color[current] == 1 ? 2 : 1;// coloreo con el color
→ opuesto a mi nodo current
                                                                          7.4. DSU
     is = is & isBipartiteDFS(child, graph, color);
   else if(color[child] == color[current]) return 0;//si son iquales no
                                                                          struct DSU {
\hookrightarrow es bipartito
                                                                            vector<int> parent;
 }
                                                                            vector<int> rank;
                                                                            DSU(int n) : parent(n), rank(n) {
 return is;
                                                                              fore(i,0,n) parent[i] = i;
bool isBipartiteBFS(int start, vector<vector<int>> &graph, vector<int>
int find(int u) {
```

```
return parent[u] = (u == parent[u]? u : find(parent[u]));
}
void setUnion(int u, int v) {
   int pv = find(v);
   int pu = find(u);
   if(pv != pu) {
      if(rank[pu] < rank[pv]) swap(pu, pv);
      if(rank[pu] == rank[pv]) rank[pu]++;
      parent[pv] = pu;
   }
}
bool isSame(int u, int v) {
   return find(u) == find(v);
}
};</pre>
```

# 7.5. FloydWarshall

```
void floydWarshall(vvi &mtx){
  int n = mtx.size();
  fore(k,0,n) fore(i,0,n) fore(j,0,n)
    mtx[i][j] = min(mtx[i][j], mtx[i][k] + mtx[k][j]);
}
```

## 7.6. Kruskal

```
vector<int> parent, rank;
void make_set(int v) {
    parent[v] = v; rank[v] = 0;
}
int find_set(int v) {
    if (v == parent[v]) return v;
    return parent[v] = find_set(parent[v]);
}
void union_sets(int a, int b) {
    a = find_set(a);
    b = find_set(b);
    if (a != b) {
        if (rank[a] < rank[b]) swap(a, b);</pre>
        parent[b] = a;
        if (rank[a] == rank[b]) rank[a]++;
    }
}
struct Edge {
    int u, v, weight;
    bool operator<(Edge const& other) {</pre>
```

```
return weight < other.weight;
};
void Kruskal(){
  vector<Edge> edges, result;
  int n, cost = 0;
  parent.resize(n); rank.resize(n);
  for (int i = 0; i < n; i++) make_set(i);
  sort(edges.begin(), edges.end());
  for (Edge e : edges) {
    if (find_set(e.u) != find_set(e.v)) {
      cost += e.weight;
      result.push_back(e);
      union_sets(e.u, e.v);
    }
}</pre>
```

## 7.7. topoSort

```
vi toposortBFS(vvi &graph){
    int n = graph.size();
    vi incoming_edges(n);
  fore(i,0,n) for(auto v: graph[i]) incoming_edges[v]++;
    queue<int> q;
    fore(i,0,n) if(incoming_edges[i] == 0) q.push(i);
    int cnt = 0;
    vi ans;
    while(!q.empty()){
        int u = q.front(); q.pop();
        ans.push_back(u);
        cnt++;
        for(auto v: graph[u]){
            incoming_edges[v]--;
            if(incoming_edges[v] == 0) q.push(v);
        }
    if(cnt != n) return \{-1\};
    return ans;
}
void dfs(int curr, vector<bool> &visited, vector<vector<int>> &graph,

    vector<int> &ans){
    if(visited[curr]) return;
    visited[curr] = true;
    for(auto nextNode: graph[curr]) dfs(nextNode, visited, graph, ans);
    ans.push_back(curr);
    return;
```

```
}
                                                                                int LCA(int u, int v) {
vector<int> toposort_dfs(vector<vector<int>> &graph){
                                                                                   if(level[u] < level[v]) swap(u,v);</pre>
    int n = graph.size();
                                                                                   int k = level[u] - level[v];
    vector<bool> visited(n);
                                                                                   u = kAncestorOfx(k, u);
                                                                                   if(u == v) return u;
    vector<int> ans;
    fore(i,0,n) if(!visited[i]) dfs(i, visited, graph, ans);
                                                                                   forr(i, 20, -1){
    reverse(ans.begin(), ans.end());//dfs => reverse
                                                                                     if(ancestros[i][u] != ancestros[i][v]){
    return ans;
                                                                                       u = ancestros[i][u];
}
                                                                                       v = ancestros[i][v];
                                                                                    }
                                                                                  }
                                                                                   return ancestros[0][u];
      Tree
8.
                                                                                // int LCA(int u, int v) {
struct Tree {
                                                                                // if (isAncestor(u, v)) return u;
  int n, root, idx;
                                                                                // if (isAncestor(v, u)) return v;
 vvi ancestros;
                                                                                // forr(k, 20, -1) if (!isAncestor(ancestros[k][u], v)) u =
 vi level, tin, tout, aplanado, sz;
                                                                               \rightarrow ancestros[k][u];
                                                                                     return ancestros[0][u]:
 Tree(int n, int root, vvi& adj) :root(root),n(n), ancestros(21, vi(n+1,
                                                                                 1/ }
\rightarrow 0)),
                                                                                int centroid(vvi& adj){
            level(n+1), tin(n+1), tout(n+1), aplanado(n+1), sz(n+1, 1){
                                                                                   int vf = 1;
    idx = 1; dfs(root, root, adj);
                                                                                   while(vf){
    fore(k, 1, 21) fore(x, 1, n + 1) ancestros[k][x] = ancestros[k - 1]
                                                                                     vf = 0;
\rightarrow 1] [ancestros[k - 1][x]];
                                                                                     for(auto next: adj[root]){
 }
                                                                                       if(sz[next] > n/2){
  void dfs(int curr, int father, vvi &adj) {
                                                                                         int aux = sz[root];
    tin[curr] = idx;
                                                                                         sz[root] -= sz[next];
    aplanado[idx] = curr;
                                                                                         sz[next] = aux;
    for (auto& next : adj[curr]) {
                                                                                         root = next;
      if (next == father) continue;
                                                                                         vf = 1;
                                                                                       }
      idx++; dfs(next, curr, adj);
                                                                                    }
                                                                                   }
      ancestros[0][next] = curr;
                                                                                   return root;
      level[next] = level[curr] + 1;
      sz[curr] += sz[next];
                                                                                 void printAncestros(){
                                                                                   fore(i,0,4) {fore(j,0,n+1) cout << ancestros[i][j] <<' '; cout <<
    tout[curr] = idx;

    endl;}

 }
                                                                                }
                                                                              };
  int kAncestorOfx(int k, int x) {
    fore(j,0,21) if (k & (1 << j)) x = ancestros[j][x];
    return x;
  int isAncestor(int u, int v) {
    return tin[u] <= tin[v] && tout[v] <= tout[u];</pre>
 }
```

#### 8.1. HLD

```
struct HeavyLightDecomp {
 int n, root, idx;
 vi level, size, head, pos, newVals;
 vvi ancestros;
 HeavyLightDecomp(int n, int root, vvi & adj, vi& vals):n(n),
\rightarrow root(root), ancestros(21, vi(n+1,0)),level(n+1), size(n+1, 1),
\rightarrow head(n+1), pos(n+1), newVals(1){
    dfs(root, root, adj);
   idx = 1; hld(root, root, adj, vals);
 }
 void dfs(int curr, int father, vvi & adj) {
    for (auto& next : adj[curr]) {
      if (next == father) continue;
      ancestros[0][next] = curr;
      level[next] = level[curr] + 1;
      dfs(next, curr, adj);
      size[curr] += size[next];
    }
 }
  void hld(int curr, int nodeHead, vvi &adj, vi &vals){
    head[curr] = nodeHead;
    pos[curr] = idx++;
    newVals.pb(vals[curr]);
    int sz_heavy = 0, heavy = -1;
    for(auto next: adj[curr]){
      if(next == ancestros[0][curr]) continue;
      if(size[next] > sz_heavy)
        sz_heavy = size[next], heavy = next;
    if(heavy != -1) hld(heavy, nodeHead, adj, vals);
    for(auto next: adj[curr])
      if(next != heavy && next != ancestros[0][curr])
        hld(next, next, adj, vals);
 }
 template <class BinaryOperation>
  void traversePath(int u, int v, BinaryOperation op){
    for(; head[u] != head[v]; u = ancestros[0][head[u]]){
      if(level[head[u]] < level[head[v]]) swap(u,v);</pre>
      op(pos[head[u]], pos[u]);
    if(pos[u] > pos[v]) swap(u,v);
    op(pos[u], pos[v]);
  template <class DSType> 11 query(int u, int v, DSType *st){
```

```
int ans = -1;
  traversePath(u, v, [this, &ans, st](int 1, int r){ans = max(ans,
  st->query(1,r));});
  return ans;
}

template <class DSType> void update(int u, ll val, DSType *st){
  traversePath(u, u, [this, &val, st](int 1, int r){st->update(1,
  val);});
};
};
```

## 9. Memorización

# 9.1. Knapsack