

# CS325 Winter 2013: Implementation 2

Daniel Reichert  
Trevor Bramwell

February 25, 2013

## pseudocode of algorithms

### Brute Force Pseudo:

```
brute_sum(n)
    size = the size of n
    max = first element in the n array
    for i = 0 .. size+1:
        sums = array of size+1 with each element initialized to n[0]
        for j = i+1 .. size+1:
            if i < j:
                sums[j] = the sum of the elements from i to j-2 plus
                if sums[j] > max_sum:
                    max = sums[j]
    return max
```

### Divide and Conquer Pseudo:

```
divide_conquer(n)
    # a miracle occurs
    return maximum contiguous subarray
```

### Dynamic Pseudo:

```

dynamic(n)
    cumulative = 0
    high_water = n[0]
    for i = 0 .. size of n
        cumulative = max of (0, cumulative+n[i])
        high_water = max of (cumulative, high_water)
    return high_water

```

## Asymptotic Analysis

1. In the brute force algorithm there are no subproblems. With the nested for loops, there is a comparison made between every element in the input, leading to an intuitive asymptotic complexity of  $O(n^2)$
2. In the divide and conquer algorithm the problem is branched into 2 subproblems for a size of  $n/2$  at each level. Those two subproblems cover the two cases where the maximal subsequence is fully contained within either half of the array. The case where the maximal subsequence is contained partially in each half of the array can be analyzed in linear time. Which leads to a complexity statement of  $T(n) = 2T(n/2) + O(n)$ . Per the master theorem, this leads to a complexity of  $O(n \log n)$ .
3. In the dynamic programming algorithm the problem is approached from the bottom up. Like all dynamic programming algorithms the complexity can be modeled by the size of the table that is created multiplied by the time it takes to fill in a cell of that table. Since the time to fill in a cell is constant and the table is 1 dimensional, the run time is  $c * n$  or  $O(n)$

## Theoretical correctness

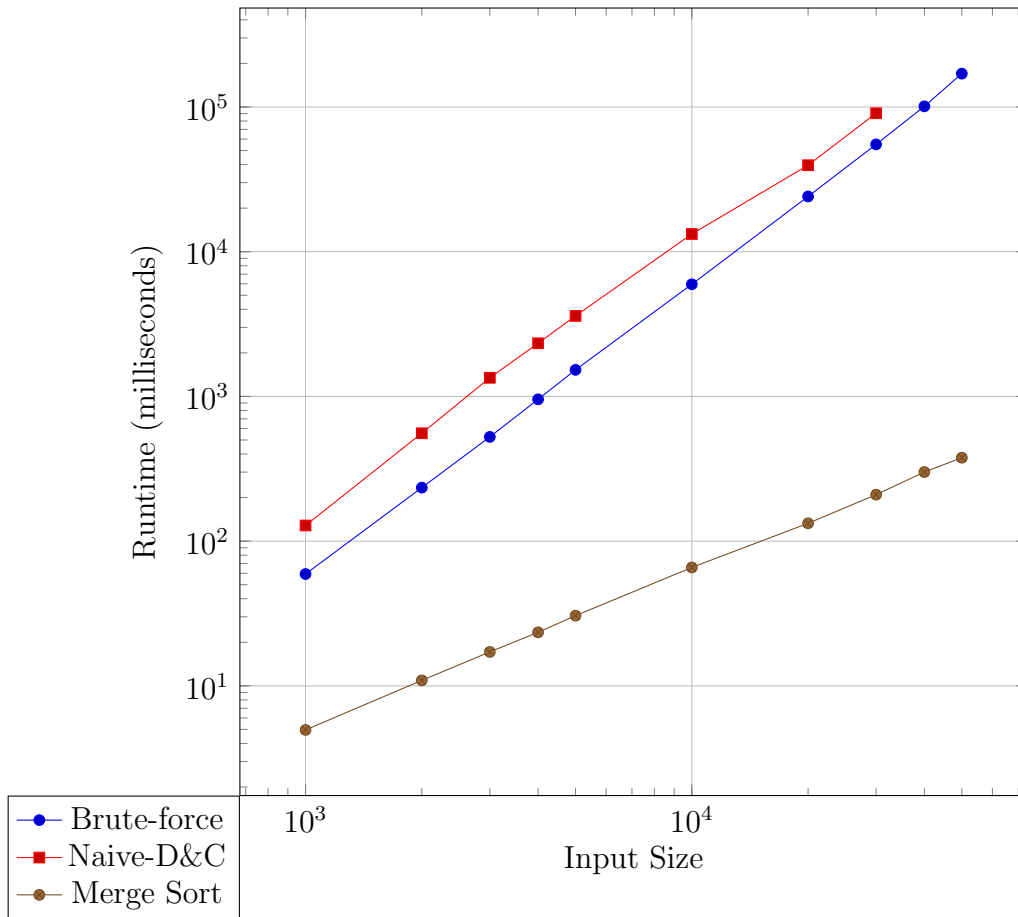
1. In the Divide and conquer algorithm the problem is divided into two halves. The maximal subsequence can be contained in one of three different cases. The first two cases are when the maximal subsequence is contained entirely in one of the two halves. The third case is when the maximal subsequence is partially in both halves of the array. Since the algorithm considers all three of these cases we know that the algorithm will calculate the correct maximum value.

2. In the Dynamic programming algorithm every possible case is considered in a linear fashion. Since the maximum value of all cases that have been considered is continually updated with each new subsequence, we know that the maximum value will be captured.

## Testing

verify.txt	test_input.txt
9670	249310
10567	252709
9282	253719
9269	249315
9675	247789
10378	254833
9911	239844
9790	257527
9580	241669
9965	255628

## Extrapolation and Interpretation



### Slope of Lines

- Brute-force: 2
- Naive-D&C: 2
- Merge Sort: 1

The largest input size the Brute-force method could solve in an hour is roughly  $10^7$ .