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# Pixel Deconvolutional Networks

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## Abstract

Deconvolutional layers have been widely used in a variety of deep models for up-sampling, including encoder-decoder networks for semantic segmentation and deep generative models for unsupervised learning. One of the key limitations of deconvolutional operations is that they result in the so-called checkerboard problem. This is caused by the fact that no direct relationship exists among adjacent pixels on the output feature map. To address this problem, we propose the pixel deconvolutional layer (PixelDCL) to establish direct relationships among adjacent pixels on the up-sampled feature map. Our method is based on a fresh interpretation of the regular deconvolution operation. The resulting PixelDCL can be used to replace any deconvolutional layer in a plug-and-play manner without compromising the fully trainable capabilities of original models. The proposed PixelDCL may result in slight decrease in efficiency, but this can be overcome by an implementation trick. Experimental results on semantic segmentation demonstrate that PixelDCL can consider spatial features such as edges and shapes and yields more accurate segmentation outputs than deconvolutional layers. When used in image generation tasks, our PixelDCL can largely overcome the checkerboard problem suffered by regular deconvolution operations.

## 1 Introduction

Deep learning methods have shown great promise in a variety of artificial intelligence and computer vision tasks such as image classification [7, 24], semantic segmentation [14, 22, 21], and natural image generation [3, 6, 16]. Some key network layers, such as convolutional layers [9], pooling layers, fully connected layers and deconvolutional layers, have been frequently used to create deep models for different tasks. Deconvolutional layers, also known as transposed convolutional layers [26], are initially proposed in [27, 28]. They have been primarily used in deep models that require up-sampling of feature maps, such as generative models [17, 13, 20] and encoder-decoder architectures [21, 14]. Although deconvolutional layers are capable of producing larger feature maps from smaller ones, they suffer from the problem of checkerboard artifacts [15]. This greatly limits deep model’s capabilities in generating photo-realistic images and producing smooth outputs on semantic segmentation. To date, very little efforts have been devoted to improving the deconvolution operation.

In this work, we propose a simple, efficient, yet effective method, known as the pixel deconvolutional layer (PixelDCL), to address the checkerboard problem suffered by deconvolution operations. Our method is motivated from a fresh interpretation of deconvolution operations, which clearly pinpoints the root of checkerboard artifacts. That is, the up-sampled feature map generated by deconvolution can be considered as the result of periodical shuffling of multiple intermediate feature maps computed



Figure 1: Comparison of semantic segmentation results. The first and second rows are images and ground true labels, respectively. The third and fourth rows are the results of using regular deconvolution and our proposed pixel deconvolution PixelDCL, respectively.

from the input feature map by independent convolutions. As a result, adjacent pixels on the output feature map are not directly related, leading to the checkerboard artifacts. To overcome this problem, we propose the pixel deconvolutional operation to be used in PixelDCL. In this new layer, the intermediate feature maps are generated sequentially so that feature maps generated in a later stage are required to depend on previously generated ones. In this way, direct relationships among adjacent pixels on the output feature map have been established. Sequential generation of intermediate feature maps in PixelDCL may result in slight decrease in computational efficiency, but we show that this can be largely overcome by an implementation trick. Experimental results on semantic segmentation (samples in Figure 1) and image generation tasks demonstrate that the proposed PixelDCL can effectively overcome the checkerboard problem and improve predictive and generative performance.

Our work is related to the pixel recurrent neural networks (PixelRNNs) [16] and PixelCNNs [25, 19], which are generative models that consider the relationship among units on the same feature map. They belong to a more general class of autoregressive methods for probability density estimation [2, 4, 8]. By using masked convolutions in training, the training time of PixelRNNs and PixelCNNs is comparable to that of other generative models such as generative adversarial networks (GANs) [3, 18] and variational auto-encoders (VAEs) [6, 5]. However, the prediction time of PixelRNNs or PixelCNNs is very slow since it has to generate images pixel by pixel. In contrast, our PixelDCL can be used to replace any deconvolutional layer in a plug-and-play manner, and the slight decrease in efficiency can be largely overcome by an implementation trick.

## 2 Pixel Deconvolutional Layers and Networks

We introduce deconvolutional layers and analyze the cause of checkerboard artifacts in this section. We then propose the pixel deconvolutional layers and the implementation trick to improve efficiency.

### 2.1 Deconvolutional Layers

Deconvolutional networks and deconvolutional layers are proposed in [27, 28]. They have been widely used in deep models for applications such as semantic segmentation [14] and generative models [6, 3, 16]. Many encoder-decoder architectures use deconvolutional layers in decoders for up-sampling. One way of understanding deconvolutional operations is that the up-sampled output feature map is obtained by periodical shuffling of multiple intermediate feature maps obtained by applying multiple convolutional operations on the input feature maps [23]. This interpretation of deconvolution is illustrated in Figure 2.

In the following, we assume the up-sampling factor is two, though deconvolution operations can be applied to more generic settings. Formally, given an input feature map  $F_{in}$ , a deconvolutional layer

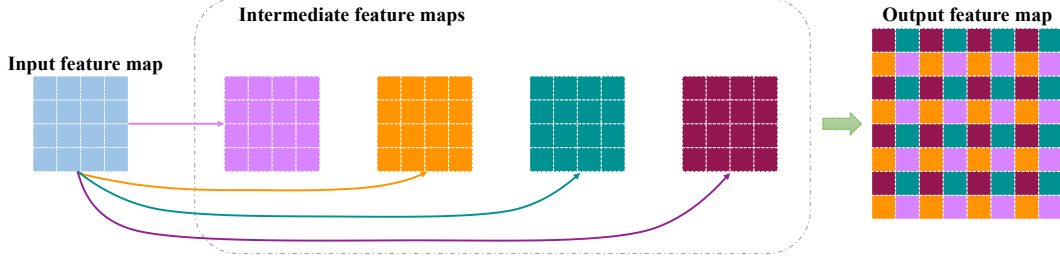


Figure 2: Illustration of the deconvolutional operation. In this deconvolutional layer, a  $4 \times 4$  feature map is up-sampled to an  $8 \times 8$  feature map. Four intermediate feature maps (purple, orange, blue, and red feature maps) are generated using four different convolutional kernels. Then these four intermediate feature maps are shuffled and combined to produce the final  $8 \times 8$  feature map. Note that the four intermediate feature maps rely on the input feature map, but there is no direct relationship among them.

can be used to generate an up-sampled output  $F_{out}$  as follows:

$$\begin{aligned} F_1 &= F_{in} \otimes k_1, & F_2 &= F_{in} \otimes k_2, & F_3 &= F_{in} \otimes k_3, & F_4 &= F_{in} \otimes k_4, \\ F_{out} &= F_1 \oplus F_2 \oplus F_3 \oplus F_4, \end{aligned} \quad (1)$$

where  $\otimes$  denotes the convolutional operation and  $\oplus$  denotes the periodical shuffling and combination operation as in Figure 2,  $F_i$  is the intermediate feature map generated by the corresponding convolutional kernel  $k_i$  for  $i = 1, \dots, 4$ .

It is clear from the above interpretation of deconvolution that there is no direct relationship among these intermediate feature maps since they are generated by independent convolutional kernels. Although pixels of the same position on intermediate feature maps depend on the same receptive field of the input feature map, they are not directly related to each other. Due to the periodical shuffling operation, adjacent pixels on the output feature map are from different intermediate feature maps. This implies that the values of adjacent pixels can be significantly different from each other, resulting in the problem of checkerboard artifacts [15]. One way to alleviate checkerboard artifacts is to apply post-processing such as smoothing [10], but this adds additional complexity to the network and makes the entire network not fully trainable. In this work, we propose the pixel deconvolutional operation to add direct dependencies among intermediate feature maps, thereby making the values of adjacent pixels close to each other and effectively solving the checkerboard artifact problem. In addition, our pixel deconvolutional layers can be easily used to replace any deconvolutional layers without compromising the fully trainable capability.

## 2.2 Pixel Deconvolutional Layers

To solve the checkerboard problem in deconvolutional layers, we propose the pixel deconvolutional layers (PixelDCL) that can add dependencies among intermediate feature maps. As adjacent pixels are from different intermediate feature maps, PixelDCL can build direct relationships among them, thus solving the checkerboard problem. In this method, intermediate feature maps are generated sequentially instead of simultaneously. The intermediate feature maps generated in a later stage are required to depend on previously generated ones. The primary purpose of sequential generation is to add dependencies among intermediate feature maps and thus adjacent pixels in final output feature maps. Finally, these intermediate feature maps are shuffled and combined to produce final output feature maps. Compared to Eqn. 1,  $F_{out}$  is obtained as follows:

$$\begin{aligned} F_1 &= F_{in} \otimes k_1, & F_2 &= [F_{in}, F_1] \otimes k_2, \\ F_3 &= [F_{in}, F_1, F_2] \otimes k_3, & F_4 &= [F_{in}, F_1, F_2, F_3] \otimes k_4, \\ F_{out} &= F_1 \oplus F_2 \oplus F_3 \oplus F_4, \end{aligned} \quad (2)$$

where  $[\cdot, \cdot]$  denotes the juxtaposition of feature maps. Note that in Eqn. 2,  $k_i$  denotes a set of kernels as it involves convolution with the juxtaposition of multiple feature maps. Since the intermediate feature maps in Eqn. 2 depend on both the input feature map and the previously generated ones, we term it input pixel deconvolutional layer (iPixelDCL). Through this process, pixels on output feature maps

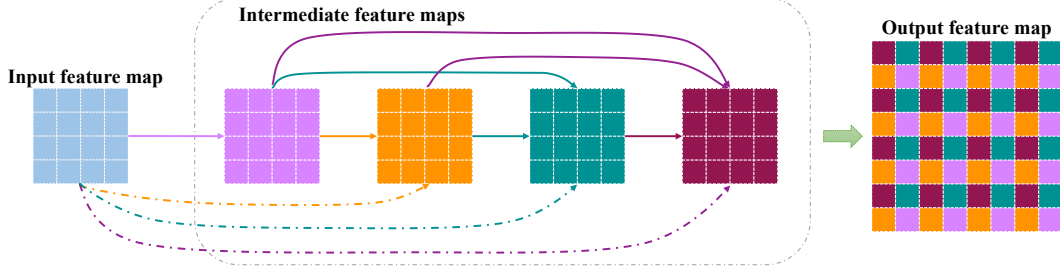


Figure 3: Illustration of iPixelDCL and PixelDCL described in section 2.2. In iPixelDCL, there are additional dependencies among intermediate feature maps. Specifically, the four intermediate feature maps are generated sequentially. The purple feature map is generated from the input feature map (blue). The orange feature map is conditioned on both the input feature map and the purple feature map that has been generated previously. In this way, the green feature map relies on the input feature map, purple and orange intermediate feature maps. The red feature map is generated based on the input feature map, purple, orange, and green intermediate feature maps. We also propose to move one step further and allow only the first intermediate feature map to depend on the input feature map. This gives rise to PixelDCL. That is, the connections indicated by dash lines are removed to avoid repeated influence of the input feature map. In this way, only the first feature map is generated from the input and other feature maps do not directly rely on the input. In PixelDCL, the orange feature map only depends on the purple feature map. The green feature map relies on the purple and orange feature maps. The red feature map is conditioned on the purple, orange, and green feature maps. The information of the input feature map is delivered to other intermediate feature maps through the first intermediate feature map (purple).

will be conditioned not only on input feature maps but also on adjacent pixels. Since there are direct relationships among intermediate feature maps and adjacent pixels, iPixelDCL is expected to solve the checkerboard problem to some extent. Note that the relationships among intermediate feature maps can be very flexible. The intermediate feature maps generated later on can rely on part or all of previously generated intermediate feature maps. This depends on the design of pixel dependencies in final output feature maps. Figure 3 illustrates a specific design of sequential dependencies among intermediate feature maps.

In iPixelDCL, we add dependencies among generated intermediate feature maps, thereby making adjacent pixels on final output feature maps directly related to each other. In this process, the information of the input feature map is repeatedly used when generating intermediate feature maps. When generating the intermediate feature maps, information from both the input feature map and previous intermediate feature maps is used. Since previous intermediate feature maps already contain information of the input feature map, the dependencies on the input feature map can be removed. Removing such dependencies for some intermediate feature maps can not only improve the computational efficiency but also reduce the number of trainable parameters in deep models.

In this simplified pixel deconvolutional layer, only the first intermediate feature map will depend on the input feature map. The intermediate feature maps generated afterwards will only depend on previously generated intermediate feature maps. This will simplify the dependencies among pixels on final output feature map. In this work, we use PixelDCL to denote this simplified design. Our experimental results show that PixelDCL yields better performance than iPixelDCL and regular deconvolution. Compared to Eqn. 2,  $F_{out}$  in PixelDCL is obtained as follows:

$$\begin{aligned}
 F_1 &= F_{in} \otimes k_1, & F_2 &= F_1 \otimes k_2, \\
 F_3 &= [F_1, F_2] \otimes k_3, & F_4 &= [F_1, F_2, F_3] \otimes k_4, \\
 F_{out} &= F_1 \oplus F_2 \oplus F_3 \oplus F_4.
 \end{aligned} \tag{3}$$

PixelDCL is illustrated in Figure 3 by removing the connections denoted with dash lines. When analyzing the relationships of pixels on output feature maps, it is clear that each pixel will still rely on adjacent pixels. Therefore, the checkerboard problem can be solved with even better computational efficiency. Meanwhile, our experimental results demonstrate that the performance of models with these simplified dependencies is even better than that with complete connections. This demonstrates that repeated dependencies on the input may not be necessary.

### 2.3 Pixel Deconvolutional Networks

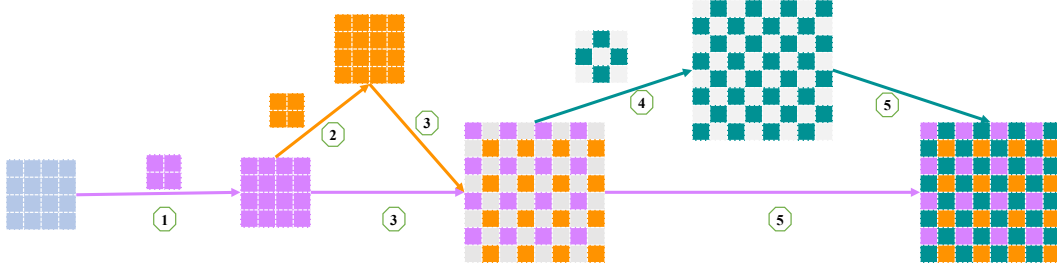


Figure 4: An efficient implementation of the pixel deconvolutional layer. In this layer, a  $4 \times 4$  feature map is up-sampled to a  $8 \times 8$  feature map. The purple feature map is generated through a  $2 \times 2$  convolutional operation from the input feature map (step 1). After that, another  $2 \times 2$  convolutional operation is applied on the purple feature map to produce the orange feature map (step 2). The purple and orange feature maps are dilated and added together to form a larger feature map (step 3). Since there is no relationship between the last two intermediate feature maps, we can apply a masked  $3 \times 3$  convolutional operation, instead of two separate  $2 \times 2$  convolutional operations (step 4). Finally, the two large feature maps are combined to generate the final output feature map (step 5).

Pixel deconvolutional layers can be applied to replace any deconvolutional layers in various models involving up-sampling operations such as U-Net [21], VAEs [6] and GANs [3]. By replacing deconvolutional layers with pixel deconvolutional layers, deconvolutional networks become pixel deconvolutional networks (PixelDCN). In U-Net for semantic segmentation, pixel deconvolutional layers can be used to up-sample from low-resolution feature maps to high-resolution ones. In VAEs, they can be applied in decoders for image reconstruction. The generator networks in GANs typically use deep model [17] and thus can employ pixel deconvolutional layers to generate large images. In our experiments, we evaluate pixel deconvolutional layers in U-Net and VAEs. The results show that the performance of pixel deconvolutional layers outperforms deconvolutional layers in these networks.

In practice, the most frequently used up-sampling operation is to increase the height and width of input feature maps by a factor of two, e.g., from  $2 \times 2$  to  $4 \times 4$ . In this case, the pixels on output feature maps can be divided into four groups as in Eqn. 1. The dependencies can be defined as in Figure 3. When implementing pixel deconvolutional layers, we design a simplified version to reduce sequential dependencies for better parallel computation and training efficiency as illustrated in Figure 4.

In this design, there are four intermediate feature maps. The first intermediate feature map depends on the input feature map. The second intermediate feature map relies on the first intermediate feature map. The third and fourth intermediate feature maps are based on both the first and the second feature maps. Such simplified relationships enable the parallel computation for the third and fourth intermediate feature maps, since there is no dependency between them. In addition, the masked convolutional operation can be used to generate the last two intermediate feature maps. As has been mentioned already, a variety of different dependencies relations can be imposed on the intermediate feature maps. Our simplified design achieves reasonable balance between efficiency and performance. Our code is publicly available<sup>1</sup>.

### 2.4 Pixel Convolutional Layers

We also propose to add dependencies among units on the same feature map through convolution. Similar to deconvolutional layers, convolutional layers can also be decomposed into two steps; namely generating intermediate feature maps, and using periodical shuffling and combination to produce final output feature maps. In this way, the intermediate feature maps are not directly related. Thus there is no direct relationship among adjacent pixels on output feature maps. The idea of adding dependencies among pixels on output feature maps can also be applied here, resulting in pixel convolutional layers. The main difference between pixel deconvolutional layers and pixel convolutional layers is the stride of each convolutional operation on the input feature map. For example, we can use a stride of two in

<sup>1</sup><https://github.com/divelab/PixelDCN>

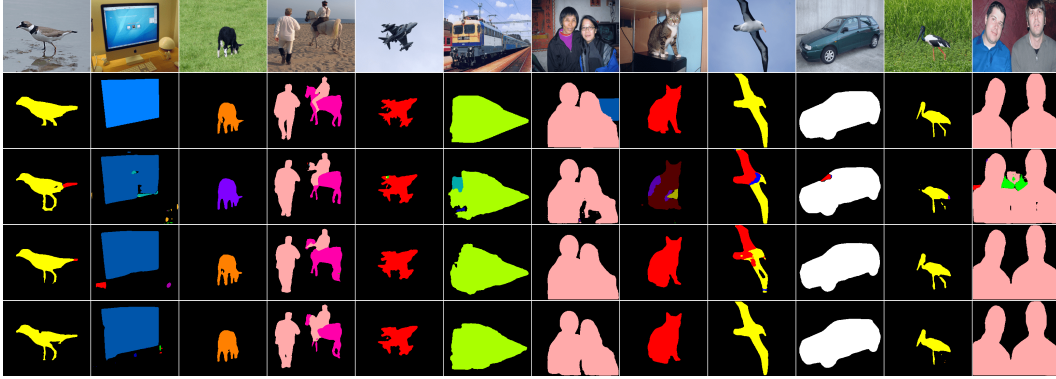


Figure 5: Sample segmentation results on the PASCAL 2012 segmentation dataset. The first and second rows are the original images and the corresponding ground truth, respectively. The third, fourth, and fifth rows are the segmentation results of models using deconvolutional layers, iPixelDCL, and PixelDCL, respectively.

pixel convolutional layers, and this produces down-sampled (by a factor of two) intermediate feature maps. We can shift the input feature map by one pixel in the horizontal and/or vertical directions and apply the same convolution of stride two to each shifted the input feature map. This yields four down-sampled intermediate feature maps, which can be combined using periodical shuffling to produce smooth output feature maps of the same size as the input one.

### 3 Experimental Studies

In this section, we evaluate the proposed pixel deconvolutional methods on semantic segmentation and image generation tasks in comparison to the regular deconvolution method. Results show that the use of the new pixel deconvolutional layers improves performance consistently in both supervised and unsupervised learning settings.

#### 3.1 Semantic Segmentation

**Experimental Setup:** We use the PASCAL 2012 segmentation dataset [1] and MSCOCO 2015 detection dataset [11] to evaluate the proposed pixel deconvolutional methods in semantic segmentation tasks. For both datasets, the images are resized to  $256 \times 256 \times 3$  for batch training. Our models directly predict the label for each pixel without any postprocessing. We use the U-Net architecture [21] as our base model as it represents the state-of-the-art in image segmentation. The network consists of four blocks in the encoder path and four corresponding blocks in the decoder path. The final output layer is adjusted based on the number of classes in the dataset. The PASCAL 2012 segmentation dataset has 21 classes while the MSCOCO 2015 detection dataset has 81 classes. As the MSCOCO 2015 detection dataset has more classes than the PASCAL 2012 segmentation dataset, the number of feature maps in each layer for this dataset is increased by a factor of two to accommodate more output channels.

The baseline U-Net model employs deconvolutional layers within the decoder path to increase the size of feature maps. We replace the deconvolutional layers with our proposed pixel deconvolutional layers (iPixelDCL) and their simplified version (PixelDCL) while keeping all other variables unchanged. This will enable us to evaluate the new pixel deconvolutional layers against the regular deconvolutional layers while controlling all other factors.

**Analysis of Results:** Some sample segmentation results of U-Net using deconvolutional layers (DCL), iPixelDCL, and PixelDCL on the PASCAL 2012 segmentation dataset and the MSCOCO 2015 detection dataset are given in Figures 5 and 6, respectively. We can see that U-Net models using iPixelDCL and PixelDCL can better capture the local information of images than the same base model using regular deconvolutional layers. By using pixel deconvolutional layers, more spacial features such as edges and shapes are considered when predicting the labels of adjacent pixels.



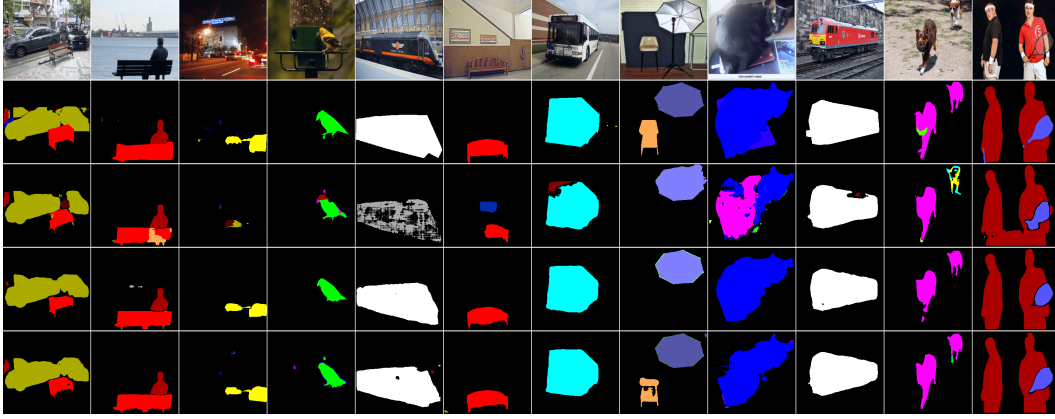


Figure 6: Sample segmentation results on the MSCOCO 2015 detection dataset. The first and second rows are the original images and the corresponding ground truth, respectively. The third, fourth, and fifth rows are the segmentation results of models using deconvolutional layers, iPixelDCL, and PixelDCL, respectively.

Table 1: Semantic segmentation results on the PASCAL 2012 segmentation dataset and MSCOCO 2015 detection dataset. We compare the same base U-Net model using three different methods for up-sampling in the decoders; namely regular deconvolution layer (DCL), the proposed input pixel deconvolutional layer (iPixelDCL) and pixel deconvolutional layer (PixelDCL). The pixel accuracy and mean IOU are used as performance measures.

Dataset	Model	Pixel Accuracy	Mean IOU
PASCAL 2012	U-Net + DCL	0.816161	0.415178
	U-Net + iPixelDCL	0.817129	0.448817
	U-Net + PixelDCL	<b>0.822591</b>	<b>0.455972</b>
MSCOCO 2015	U-Net + DCL	0.800166	0.317191
	U-Net + iPixelDCL	0.801061	<b>0.324076</b>
	U-Net + PixelDCL	<b>0.802538</b>	0.323646

Moreover, the semantic segmentation results demonstrate that the proposed models tend to produce smoother outputs than the model using deconvolution. We also observe that, when the training epoch is small (e.g., 50 epochs), the model that employs PixelDCL has better segmentation outputs than the model using iPixelDCL. When the training epoch is large enough (e.g., 100 epochs), they have similar performance, though PixelDCL still outperforms iPixelDCL in most cases. This indicates that PixelDCL is more efficient and effective, since it has much fewer parameters to learn.

Table 1 shows the evaluation results in terms of pixel accuracy and mean IOU on the two datasets. The U-Net models using iPixelDCL and PixelDCL yield better performance than the same base model using regular deconvolution. The model using PixelDCL slightly outperforms the model using iPixelDCL. In semantic segmentation, mean IOU is a more accuracy evaluation measure than pixel accuracy [1]. The two models using pixel deconvolution have much better evaluation results on mean IOU than the base model using deconvolution.

### 3.2 Image Generation

**Experimental Setup:** The dataset used for image generation is the celebFaces attributes (CelebA) dataset [12]. To avoid the influence of background, the images have been preprocessed so that only facial information is retained. The image generation task is to reconstruct the faces excluding backgrounds in training images. The size of images is  $64 \times 64 \times 3$ . We use the standard variational auto-encoder (VAE) [6] as our base model for image generation. The decoder part in standard VAE employs deconvolutional layers for up-sampling. We apply our proposed PixelDCL to replace deconvolutional layers in decoder while keeping all other components the same.

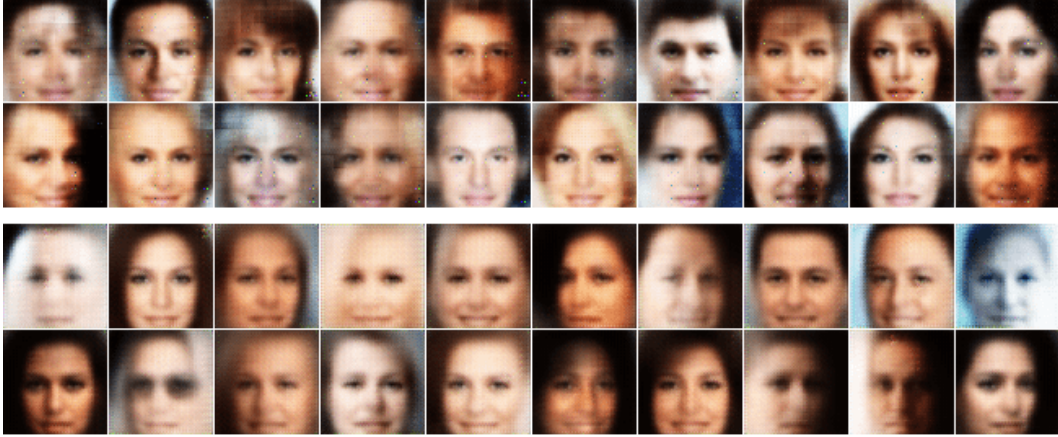


Figure 7: Sample face images generated by VAEs when trained on the CelebA dataset. The first two rows are images generated by a standard VAE with deconvolutional layers for up-sampling. The last two rows are images generated by the same VAE model, but using PixelDCL for up-sampling in the generator network.

Table 2: Training and prediction time on semantic segmentation using the PASCAL 2012 segmentation dataset on a Tesla K40 GPU. We compare the training time of 10,000 iterations and prediction time of 2109 images for the same base U-Net model using three different methods for up-sampling in the decoders; namely DCL, iPixelDCL, and PixelDCL.

Model	Training time	Prediction time
U-Net + DCL	365m26s	2m42s
U-Net + iPixelDCL	511m19s	4m13s
U-Net + PixelDCL	464m31s	3m27s

**Analysis of Results:** Figure 7 provides the generated faces using VAEs with regular deconvolution (baseline) and PixelDCL in decoders. Some images generated by the baseline model suffer from apparent checkerboard artifacts, while none is found on the images generated by the model with PixelDCL. This demonstrates that the proposed pixel deconvolutional layers are able to establish direct relationships among adjacent pixels on generated feature maps and images, thereby effectively overcoming the checkerboard problem. Our results demonstrate that PixelDCL is very useful for generative models since it can consider local spatial information and produce photo-realistic images without the checkerboard problem.

### 3.3 Timing Comparison

Table 2 shows the comparison of the training and prediction time of the U-Net models using DCL, iPixelDCL, and PixelDCL for up-sampling. We can see that the U-Net models using iPixelDCL and PixelDCL take slightly more time during training and prediction than the model using DCL, since the intermediate feature maps are generated sequentially. The model using PixelDCL is more efficient due to reduced dependencies and efficient implementation discussed in Section 2.3. Overall, the increase in training and prediction time is not dramatic, and thus we do not expect this to be a major bottleneck of the proposed methods.

## 4 Conclusion and Future Work

In this work, we propose pixel deconvolutional layers that can solve the checkerboard problem in deconvolutional layers. The checkerboard problem is caused by the fact that there is no direct relationship among intermediate feature maps generated in deconvolutional layers. PixelDCL proposed here try to add direct dependencies among these generated intermediate feature maps. PixelDCL generates intermediate feature maps sequentially so that the intermediate feature maps generated in a later stage are required to depend on previously generated ones. The establishment of dependencies in PixelDCL can ensure adjacent pixels on output feature maps are directly related. Experimental



results on semantic segmentation and image generation tasks show that PixelDCL is effective in overcoming the checkerboard artifacts. Results on semantic segmentation also show that PixelDCL is able to consider local spatial features such as edges and shapes, leading to better segmentation results.

With the widespread use of deep learning methods, deconvolutions are been used in an increasing number of models. In this work, we evaluate the PixelDCL in encoder-decoder architectures and VAEs. We plan to employ our PixelDCL in a broader class of models, such as the generative adversarial networks (GANs). As has been mentioned briefly in this work, the idea of PixelDCL can be extended to improving the convolution operations as well. We plan to explore pixel convolution and its applications in the future.

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