

#### **DSBA** Transformer survey paper study

## A Survey of Transformers

#3: Attention 2

arXiv preprint



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#### 1. Linearized Attention

- 1. Feature map
- 2. Aggregation rule

### 2. Prototype and Memory Compression

- 1. Attention with Prototype Queries
- 2. Attention with Compressed Key-Value Memory

## 03 Overview

#### 1. Lineaerized Attention

- Transformers are RNNs: Fast Autoregressive Transformers with Linear Attention (ICML 2020, 110회 인용)
- Masked Language Modeling for Proteins via Linearly Scalable Long-Context Transformers (arXiv 2020, 17회 인용)
- Random Feature Attention (ICLR 2021, 21회 인용)
- Rethinking Attention with Performers. (ICLR 2021, 117회 인용)
- Linear Transformers Are Secretly Fast Weight Memory Systems (arXiv 2021, 5회 인용)

#### 2. Prototype and Memory Compression

- Fast Transformers with Clustered Attention (arXiv 2020, 20회 인용)
- Informer: Beyond Efficient Transformer for Long Sequence Time-Series Forecasting (AAAI 2021, 17회 인용)
- Generating Wikipedia by Summarizing Long Sequences(ICLR 2018, 379회 인용)
- Set Transformer (In Proceedings of ICML, 2019, 229회 인용), Luna (arXive 2021, 1회 인용)
- Luna: Linear Unified Nested Attention. (arXiv 2021, 1회 인용)

## Linearization을 통해 attention의 computational complexity $o(T^2) o o(T)$ 줄임

- 기존 Attention:  $Q, K, V \in \mathbb{R}^{TXD}$ 에 대한 attention matrix를 위한  $softmax(QK^T)V$  연산
  - $QK^T$ 연산은 Quadratic, computational complexity  $O(T^2)$
- Linearized Attention:  $softmax(QK^T)$  연산을 위해  $QK^T = Q'K'^T$ 로 disentangle
  - Computational complexity O(T)
  - *K'*<sup>T</sup>*V* 연산 먼저 수행 후, *Q*'와 연산
  - $Q'K'^TV \Rightarrow Q'(K'^TV)$

#### **Linearized Attention**

Un-normalized attention matrix

$$\hat{\mathbf{A}} = \exp(\mathbf{Q}\mathbf{K}^{\top})$$

- $\exp(\cdot)$  is applied element-wise
- 기존 softmax 취한 score에 따른 attention matrix에서 normalization을 위한 denominator 생략
- Regular Attention

Attention(Q, K, V) = softmax 
$$\left(\frac{QK^{\top}}{\sqrt{D_k}}\right)$$
 V = AV 
$$Z = \mathbf{D}^{-1} \hat{\mathbf{A}} \mathbf{V} \qquad \text{where} \quad \mathbf{D} = \operatorname{diag}(\hat{\mathbf{A}} \mathbf{1}_T^{\top})$$
 
$$\mathbf{1}_T^{\mathsf{T}} \text{: the all-ones column vector of length } T$$

#### **Linearized Attention**

• Approximate or replace the unnormalized attention matrix  $\exp(QK^{\mathrm{T}})$  with  $\phi(Q)\phi(K)^{\mathrm{T}}$ 

$$\hat{\mathbf{A}} = \exp(\mathbf{Q}\mathbf{K}^{\mathsf{T}}) \quad \Longrightarrow \quad \phi(\mathbf{Q})\phi(\mathbf{K})^{\mathsf{T}}$$

•  $\phi$ : is a feature map that is applied in row-wise manner

$$\mathbf{z}_i = \sum_j \frac{\sin(\mathbf{q}_i, \mathbf{k}_j)}{\sum_{j'} \sin(\mathbf{q}_i, \mathbf{k}_{j'})} \mathbf{v}_j,$$

Regular Attention  $\supseteq sim(\cdot,\cdot)$ 

: the exponential of inner product  $\exp(\langle \cdot, \cdot \rangle)$ 

$$\mathbf{z}_{i} = \sum_{j} \frac{\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j})^{\top}}{\sum_{j'}\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j'})^{\top}} \mathbf{v}_{j}$$
$$= \frac{\phi(\mathbf{q}_{i})\sum_{j}\phi(\mathbf{k}_{j})\otimes\mathbf{v}_{j}}{\phi(\mathbf{q}_{i})\sum_{j'}\phi(\mathbf{k}_{j'})^{\top}},$$

 $sim(\cdot,\cdot)$ : a kernel function  $K(x,y) = \phi(x)\phi(y)^{T}$ 

 $\otimes$ : outer product

T: sequence length

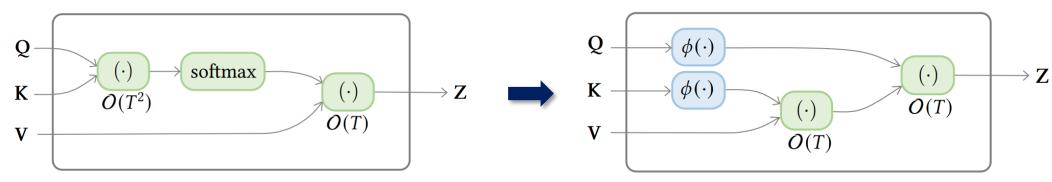
#### **Linearized Attention**

$$\mathbf{z}_i = \sum_{j} \frac{\sin(\mathbf{q}_i, \mathbf{k}_j)}{\sum_{j'} \sin(\mathbf{q}_i, \mathbf{k}_{j'})} \mathbf{v}_j, \qquad \longrightarrow$$

: the exponential of inner product  $exp(\langle \cdot, \cdot \rangle)$ 

$$\mathbf{z}_{i} = \sum_{j} \frac{\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j})^{\top}}{\sum_{j'}\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j'})^{\top}} \mathbf{v}_{j}$$
$$= \frac{\phi(\mathbf{q}_{i})\sum_{j}\phi(\mathbf{k}_{j})\otimes\mathbf{v}_{j}}{\phi(\mathbf{q}_{i})\sum_{j'}\phi(\mathbf{k}_{j'})^{\top}},$$

 $sim(\cdot,\cdot)$ : a kernel function  $K(x,y) = \phi(x)\phi(y)^{\mathrm{T}}$  $\otimes$ : outer product



(a) standard self-attention

(b) linearized self-attention

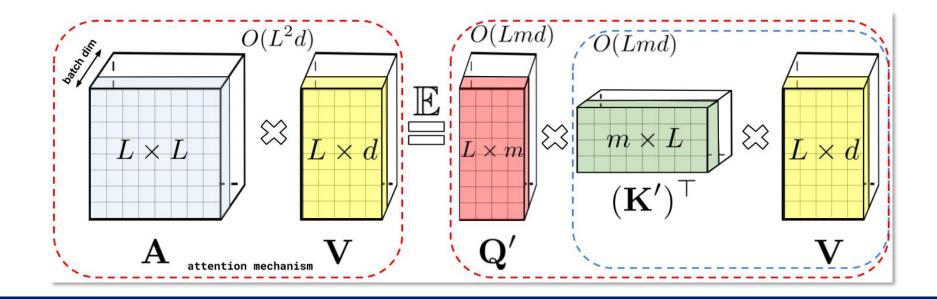
#### **Linearized Attention**

$$\mathbf{z}_i = \sum_{j} \frac{\sin(\mathbf{q}_i, \mathbf{k}_j)}{\sum_{j'} \sin(\mathbf{q}_i, \mathbf{k}_{j'})} \mathbf{v}_j,$$

$$\mathbf{z}_i = \sum_j \frac{\phi(\mathbf{q}_i)\phi(\mathbf{k}_j)^\top}{\sum_{j'}\phi(\mathbf{q}_i)\phi(\mathbf{k}_{j'})^\top} \mathbf{v}_j$$

Regular Attention  $\supseteq$   $sim(\cdot,\cdot)$ 

: the exponential of inner product  $exp(\langle \cdot, \cdot \rangle)$ 



### **Linearized Attention** 개념

#### **Linearized Attention**

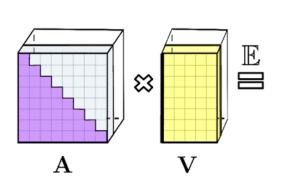
$$\mathbf{z}_i = \sum_j \frac{\sin(\mathbf{q}_i, \mathbf{k}_j)}{\sum_{j'} \sin(\mathbf{q}_i, \mathbf{k}_{j'})} \mathbf{v}_j, \qquad \longrightarrow$$

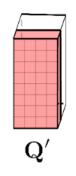
: the exponential of inner product  $exp(\langle \cdot, \cdot \rangle)$ 

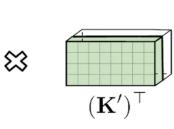
$$sim(\cdot,\cdot)$$
: a kernel function  $K(x,y) = \phi(x)\phi(y)^{T}$   
 $\otimes$ : outer product

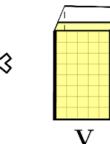
$$\mathbf{z}_{i} = \sum_{j} \frac{\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j})^{\top}}{\sum_{j'}\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j'})^{\top}} \mathbf{v}_{j}$$

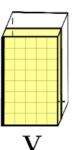
$$= \frac{\phi(\mathbf{q}_{i})\sum_{j}\phi(\mathbf{k}_{j})\otimes\mathbf{v}_{j}}{\phi(\mathbf{q}_{i})\sum_{j'}\phi(\mathbf{k}_{j'})^{\top}},$$











# 03 Linearized Attention 개념

#### **Linearized Attention**

$$\mathbf{z}_i = \sum_{j} \frac{\sin(\mathbf{q}_i, \mathbf{k}_j)}{\sum_{j'} \sin(\mathbf{q}_i, \mathbf{k}_{j'})} \mathbf{v}_j, \longrightarrow$$

: the exponential of inner product  $exp(\langle \cdot, \cdot \rangle)$ 

$$\mathbf{z}_i = \sum_{j} \frac{\phi(\mathbf{q}_i)\phi(\mathbf{k}_j)^{\top}}{\sum_{j'}\phi(\mathbf{q}_i)\phi(\mathbf{k}_{j'})^{\top}} \mathbf{v}_j$$

$$= \frac{\phi(\mathbf{q}_i)\sum_{j}\phi(\mathbf{k}_j)\otimes\mathbf{v}_j}{\phi(\mathbf{q}_i)\sum_{j'}\phi(\mathbf{k}_{j'})^{\top}},$$

 $sim(\cdot,\cdot)$ : a kernel function  $K(x,y) = \phi(x)\phi(y)^{T}$  $\otimes$ : outer product

Attention can be linearized by first computing the highlighted terms 연산량 매우 줄어듦

# O3 Linearized Attention 개념

#### **Linearized Attention**

$$\mathbf{z}_{i} = \sum_{j} \frac{\phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j})^{\top}}{\sum_{j'} \phi(\mathbf{q}_{i})\phi(\mathbf{k}_{j'})^{\top}} \mathbf{v}_{j}$$
$$= \frac{\phi(\mathbf{q}_{i})\sum_{j} \phi(\mathbf{k}_{j}) \otimes \mathbf{v}_{j}}{\phi(\mathbf{q}_{i})\sum_{j'} \phi(\mathbf{k}_{j'})^{\top}},$$

Memory matrix

$$\phi(\mathbf{q}_i)\sum_j\phi(\mathbf{k}_j)\otimes\mathbf{v}_j$$

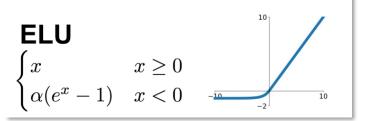
 retrieve a value by multiplying the memory matrix with feature mapped query with proper normalization.

$$\sum_j \phi(\mathbf{k}_j) \otimes \mathbf{v}_j$$

- maintains a memory matrix by aggregating associations represented by outer products of (feature mapped) keys and values
- (1) Feature map  $\phi(\cdot)$  (2) Aggregation rule

- Linear Transformer (ICML 2020, 110회 인용)
  - Simple feature map

$$\phi_i(\mathbf{x}) = \text{elu}(x_i) + 1$$



기존의 dot product attention을 approximate하는 것을 목표로 하지 않고, 비슷한 수준의 성능을 내는 것을 목표로 하여, standard transformer에 준하는 성능 달성

Method	Validation PER	Time/epoch (s)
Bi-LSTM	10.94	1047
Softmax	5.12	2711
LSH-4	9.33	2250
Linear (ours)	8.08	824

• Speech recognition 실험 결과, linear transformer를 사용하였을 때, PER을 8까지 낮춰, 다른 모델에 비해 softmax와 가장 성능이 유사하며, 소요 시은 softmax의 3배 이상 감소했다.

## Linearized Attention (1) Feature Maps

#### **Feature Maps**

- Performer first version (arXiv 2020, 17회 인용)
   기존의 dot product attention을 approximate하는 것을 목표로 함
  - Random feature map

$$\phi(\mathbf{x}) = \frac{h(\mathbf{x})}{\sqrt{m}} [f_1(\omega_1^\top \mathbf{x}), \cdots, f_m(\omega_m^\top \mathbf{x}), \cdots, f_l(\omega_1^\top \mathbf{x}), \cdots, f_l(\omega_m^\top \mathbf{x})],$$
$$f_1, \cdots, f_l : \mathbb{R} \to \mathbb{R} \text{ and } h : \mathbb{R}^D \to \mathbb{R}.$$

where  $\omega_1, \dots, \omega_m \stackrel{\text{iid}}{\sim} \mathcal{D}$  are drawn from some distribution  $\mathcal{D} \in \mathcal{P}(\mathbb{R}^D)$ Softmax를 approximate하기 위해 아래와 같은 kernel 함수를 사용

$$h(\mathbf{x}) = \exp(\frac{\|\mathbf{x}\|^2}{2}), l = 2, f_1 = \sin, f_2 = \cos.$$

## O3 Linearized Attention (1) Feature Maps

#### **Feature Maps**

- Performer first version (arXiv 2020, 17회 인용)
   기존의 dot product attention을 approximate하는 것을 목표로 함
  - Random feature map

**Theorem 1** (Rahimi & Recht, 2007). Let  $\phi : \mathbb{R}^d \to \mathbb{R}^{2D}$  be a nonlinear transformation:

$$\phi(\mathbf{x}) = \sqrt{1/D} \left[ \sin(\mathbf{w}_1 \cdot \mathbf{x}), \dots, \sin(\mathbf{w}_D \cdot \mathbf{x}), \cos(\mathbf{w}_1 \cdot \mathbf{x}), \dots, \cos(\mathbf{w}_D \cdot \mathbf{x}) \right]^{\top}$$

When d-dimensional random vectors  $\mathbf{w}_i$  are independently sampled from  $\mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{I}_d)$ ,

$$\mathbb{E}_{\mathbf{w}_{i}}\left[\boldsymbol{\phi}\left(\mathbf{x}\right)\cdot\boldsymbol{\phi}\left(\mathbf{y}\right)\right] = \exp\left(-\left\|\mathbf{x}-\mathbf{y}\right\|^{2}/2\sigma^{2}\right).$$

## O3 Linearized Attention (1) Feature Maps

#### **Feature Maps**

• Random Feature Attention (ICLR 2021, 21회 인용)

Performer(ver. 1)와 유사

Random feature map

$$\phi(\mathbf{x}) = \frac{h(\mathbf{x})}{\sqrt{m}} [f_1(\omega_1^\top \mathbf{x}), \cdots, f_m(\omega_m^\top \mathbf{x}), \cdots, f_l(\omega_1^\top \mathbf{x}), \cdots, f_l(\omega_m^\top \mathbf{x})],$$
$$f_1, \cdots, f_l : \mathbb{R} \to \mathbb{R} \text{ and } h : \mathbb{R}^D \to \mathbb{R}.$$

where  $\omega_1, \dots, \omega_m \stackrel{\text{iid}}{\sim} \mathcal{D}$  are drawn from some distribution  $\mathcal{D} \in \mathcal{P}(\mathbb{R}^D)$ 

query, key를 feature space에 보내기 전  $l_2$ -normalization 하기 때문에, h(x) = 1

$$h(\mathbf{x}) = \exp(\frac{\|\mathbf{x}\|^2}{2}), l = 2, f_1 = \sin, f_2 = \cos.$$

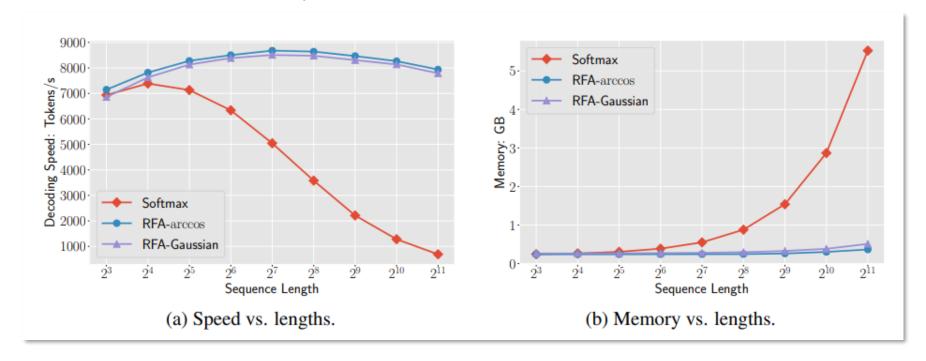
# Calculation Linearized Attention (1) Feature Maps

#### **Feature Maps**

• Random Feature Attention (ICLR 2021, 21회 인용)

Performer(ver. 1)와 유사

Random feature map



- Random Feature Attention (ICLR 2021, 21회 인용)
  - Performer(ver. 1)와 유사
  - The trigonometric random feature map leads to an unbiased approximation,

it does not guarantee non-negative attention scores

where 
$$\omega_1, \dots, \omega_m \stackrel{\text{iid}}{\sim} \mathcal{D}$$
 are drawn from some distribution  $\mathcal{D} \in \mathcal{P}(\mathbb{R}^D)$ 

query, key를 feature space에 보내기 전  $l_2$ -normalization 하기 때문에, h(x) =

$$h(\mathbf{x}) = \exp(\frac{\|\mathbf{x}\|^2}{2}), l = 2, f_1 = \sin, f_2 = \cos.$$

- Performer second version (ICLR 2021, 117회 인용)
  - Positive random feature map

$$\phi(\mathbf{x}) = \frac{h(\mathbf{x})}{\sqrt{m}} [f_1(\omega_1^\top \mathbf{x}), \cdots, f_m(\omega_m^\top \mathbf{x}), \cdots, f_l(\omega_1^\top \mathbf{x}), \cdots, f_l(\omega_m^\top \mathbf{x})],$$

$$f_1, \cdots, f_l : \mathbb{R} \to \mathbb{R} \text{ and } h : \mathbb{R}^D \to \mathbb{R}.$$

where  $\omega_1, \dots, \omega_m \stackrel{\text{iid}}{\sim} \mathcal{D}$  are drawn from some distribution  $\mathcal{D} \in \mathcal{P}(\mathbb{R}^D)$ 

$$h(\mathbf{x}) = \exp(-\frac{\|\mathbf{x}\|^2}{2}), l = 1, f_1 = \exp(-\frac{\|\mathbf{x}\|^2}{2})$$

Guarantees unbiased and non- negative approximation of dot-product attention ⇒ Performer(ver. 1) 보다 stable하고, 더 좋은 approximation 결과 보임

- Performer second version (ICLR 2021, 117회 인용)
  - Positive random feature map

$$\phi(\mathbf{x}) = \frac{h(\mathbf{x})}{\sqrt{m}} [f_1(\omega_1^\top \mathbf{x}), \cdots, f_m(\omega_m^\top \mathbf{x}), \cdots, f_l(\omega_1^\top \mathbf{x}), \cdots, f_l(\omega_m^\top \mathbf{x})],$$

$$f_1, \cdots, f_l : \mathbb{R} \to \mathbb{R} \text{ and } h : \mathbb{R}^D \to \mathbb{R}.$$

where  $\omega_1, \dots, \omega_m \stackrel{\text{iid}}{\sim} \mathcal{D}$  are drawn from some distribution  $\mathcal{D} \in \mathcal{P}(\mathbb{R}^D)$ 

$$h(\mathbf{x}) = 1, l = 1, f_1 = \text{ReLU}.$$

Effective in various tasks including machine translation and protein sequence modeling.

Linear Transformers Are Secretly Fast Weight Memory Systems (arXiv 2021, 5회 인용)
 feature space 상에서의 orthogonality를 이용할 수 있는 feature map 제안

$$\phi_{i+2(j-1)D}(\mathbf{x}) = \text{ReLU}([\mathbf{x}, -\mathbf{x}])_i \text{ReLU}([\mathbf{x}, -\mathbf{x}])_{i+j}$$
 for  $i = 1, \cdots, 2D, j = 1, \cdots, \nu$ . 
$$input \ x \in R^D$$
 the feature map  $\phi: R^D \to R^{2\nu D}$ 

# Usual Linearized Attention (2) Aggregation Rule

#### **Aggregation Rule**

The associations  $\{\phi(k)_j \otimes v_j\}$  are aggregated into the memory matrix by simple summation

⇒ 새로운 association을 memory network S에 추가할 때, 선택적으로 association을 drop하는 것이 효과적

#### **Aggregation Rule**

- Random Feature Attention (ICLR 2021, 21회 인용)
  - Gating mechanism

$$g_t = \operatorname{sigmoid}(\mathbf{w}_g \cdot \mathbf{x}_t + b_g),$$
  

$$\mathbf{S}_t = g_t \, \mathbf{S}_{t-1} + (1 - g_t) \, \boldsymbol{\phi}(\mathbf{k}_t) \otimes \mathbf{v}_t,$$
  

$$\mathbf{z}_t = g_t \, \mathbf{z}_{t-1} + (1 - g_t) \, \boldsymbol{\phi}(\mathbf{k}_t).$$

- $w_g$  and  $b_g$  are learned parameters, and  $x_t$  is the input representation at timestep t.
- By multiplying the learned scalar gates  $0 \langle g_t \rangle$  1 against the hidden state  $(S_t, z_t)$ , history is exponentially decayed, favoring more recent context.

## Linearized Attention (2) Aggregation Rule

#### **Aggregation Rule**

- Linear Transformers Are Secretly Fast Weight Memory Systems (arXiv 2021, 5회 인용)
  Association의 단순 합으로 memory matrix를 update하는 것은, memory matrix의 capacity를 제한하는 것,
  따라서 write-and-remove를 통해 capacity를 확장하는 방식을 제안
  - Write-and-remove update

$$\begin{aligned} \boldsymbol{k}^{(i)}, \boldsymbol{v}^{(i)}, \boldsymbol{q}^{(i)} &= \boldsymbol{W}_k \boldsymbol{x}^{(i)}, \boldsymbol{W}_v \boldsymbol{x}^{(i)}, \boldsymbol{W}_q \boldsymbol{x}^{(i)} \\ \bar{\boldsymbol{v}}^{(i)} &= \boldsymbol{W}^{(i-1)} \phi(\boldsymbol{k}^{(i)}) \\ \beta^{(i)} &= \sigma(\boldsymbol{W}_\beta \boldsymbol{x}^{(i)}) \\ \boldsymbol{v}^{(i)}_{\text{new}} &= \beta^{(i)} \boldsymbol{v}^{(i)} + (1 - \beta^{(i)}) \bar{\boldsymbol{v}}^{(i)} \end{aligned} \qquad \begin{aligned} \boldsymbol{W}^{(i)} &= \boldsymbol{W}^{(i-1)} \underbrace{+ \boldsymbol{v}^{(i)}_{\text{new}} \otimes \phi(\boldsymbol{k}^{(i)})}_{\text{write}} \underbrace{- \bar{\boldsymbol{v}}^{(i)} \otimes \phi(\boldsymbol{k}^{(i)})}_{\text{remove}} \\ &= \boldsymbol{W}^{(i-1)} + \beta^{(i)} (\boldsymbol{v}^{(i)} - \bar{\boldsymbol{v}}^{(i)}) \otimes \phi(\boldsymbol{k}^{(i)}) \\ \boldsymbol{v}^{(i)}_{\text{new}} &= \beta^{(i)} \boldsymbol{v}^{(i)} + (1 - \beta^{(i)}) \bar{\boldsymbol{v}}^{(i)} \end{aligned}$$

 $\beta(i)$  is the "write-strength. only depends on input x(i)

새로운 input key-value pair가 들어오면,

- 1)  $k^i$ 와 직전 memory matrix  $W^{i-1}$ 의 association  $\bar{v}^i$  을 구하고
- 2) 현재  $v^i$ 의 convex combination을 memory matrix에 update함

#### 목적

Reduce the complexity of attention by

- (1) Query prototyping: reducing the number of queries
- (2) Memory compression: reducing the number of key-value pairs

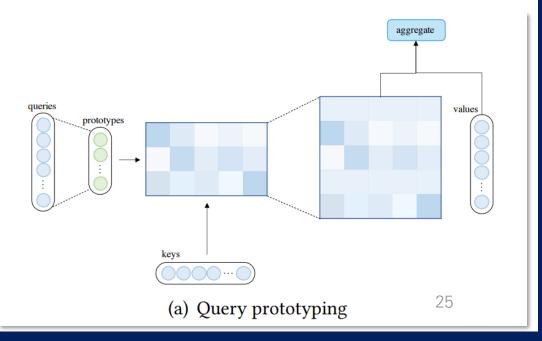
The key-value pairs are often referred to as a **key-value memory** 

(1) Attention with Prototype Queries

#### **Attention with Prototype Queries**

Several prototypes of queries serve as the main source to compute attention distributions query representation 중,

- 특정 position의 query distribution을 copy
- discrete uniform distribution으로 채움



(1) Attention with Prototype Queries

#### **Attention with Prototype Queries**

- Clustered Attention (arXiv 2020, 20회 인용)
  - groups queries into several clusters and then computes attention distributions for cluster centroids.
  - ① Centroid 구하기

$$Q_j^c = \frac{\sum_{i=1}^{N} S_{ij} Q_i}{\sum_{i=1}^{N} S_{ij}}$$

 $S_{ij} = 1$ , if the *i*-th query  $Q_i$  belongs to the *j*-th cluster and 0 otherwise.

② Centroid에 대한 attention score 계산③ Centroid에 의한 새로운 value 계산

$$A^c = \operatorname{softmax}\left(\frac{Q^c K^T}{\sqrt{D_k}}\right)$$

 $Q^c \in \mathbb{R}^{C \times D_k}$  as the centroid matrix

$$\hat{V}^c = A^c V.$$

④ 가장 가까운 centroid에 대한 attention value 도출

$$\hat{V}_i = \sum_{j=1}^C S_{ij} \hat{V}_j^c.$$

(1) Attention with Prototype Queries

#### **Attention with Prototype Queries**

- Clustered Attention (arXiv 2020, 20회 인용)
  - groups queries into several clusters and then computes attention distributions for cluster centroids.

	full	clustered-100	i-clustered-100
WER (%)	15.0	18.5	15.5
Time/Epoch (h)	3.84	1.91	2.57
Time/Epoch (h) Convergence Time (h)	228.05	132.13	127.44



(1) Attention with Prototype Queries

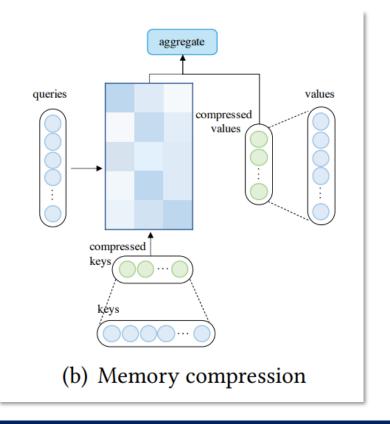
#### **Attention with Prototype Queries**

- Informer (AAAI 2021, 17회 인용)
  - Query sparsity measurement를 제안하여, 상위 u개의 query만을 가지고 attention distribution 계산
    - 나머지 query에는 discrete uniform distribution 부여
  - Query sparsity measurement
    - Query의 attention distribution과 the discrete uniform distribution 사이의 Kullback-Leibler divergence 값을 기반으로 정의
    - Attention distribution이 the discrete uniform distribution과의 차이가 클수록 몇몇 key에 dominant한 attention을 주는 query라고 할 수 있기 때문에, KLD가 클수록 중요한 query로 봄

(2) Attention with Compressed Key-Value Memory

#### Attention with Compressed Key-Value Memory

reduce the complexity by reducing the number of the key-value pairs before applying the attention mechanism



(2) Attention with Compressed Key-Value Memory

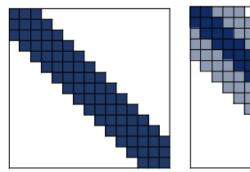
#### Attention with Compressed Key-Value Memory

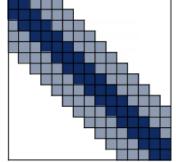
- Memory Compressed Attention(ICLR 2018, 379회 인용)
  - Strided convolution을 사용하여 key와 value의 개수를 줄임
  - Kernel size k에 따라 줄이고자 하는 key, value 개수를 조절하며, attention 연산량이 줄어들기 때문에, 같은 시간 안에 vanilla transformer보다 훨씬 긴 sequence를 처리할 수 있다.
- Set Transformer (In Proceedings of ICML 2019, 229회 인용),
- Luna (arXive 2021, 1회 인용)
  - Trainable global node를 정의하여, input으로부터의 정보를 취합하게 하며, 취합된 정보는 input이 attend할 memory로 사용된다.

(2) Attention with Compressed Key-Value Memory

#### Attention with Compressed Key-Value Memory

- Linformer(arXiv 2020, 132회 인용)
  - Key, value에 대해 linear projection을 적용하여 length n에서 더 짧은  $n_k$ 의 sequence로 사영
  - 단점: autoregressive attention에 사용할 수 없음
- Poolingformer (ICML 2021, 1회 인용)
  - 여러 개의 pooling operation을 사용하여, key와 value를 줄이면서도 receptive field를 키우고자 함





(a) Single-level local attention (b) Two-level pooling attention

## 03 Summary

#### 1. Lineaerized Attention

- Transformers are RNNs: Fast Autoregressive Transformers with Linear Attention (ICML 2020, 110회 인용)
- Masked Language Modeling for Proteins via Linearly Scalable Long-Context Transformers (arXiv 2020, 17회 인용)
- Random Feature Attention (ICLR 2021, 21회 인용)
- Rethinking Attention with Performers. (ICLR 2021, 117회 인용)
- Linear Transformers Are Secretly Fast Weight Memory Systems (arXiv 2021, 5회 인용)

#### 2. Prototype and Memory Compression

- Fast Transformers with Clustered Attention (arXiv 2020, 20회 인용)
- Informer: Beyond Efficient Transformer for Long Sequence Time-Series Forecasting (AAAI 2021, 17회 인용)
- Generating Wikipedia by Summarizing Long Sequences(ICLR 2018, 379회 인용)
- Set Transformer (In Proceedings of ICML, 2019, 229회 인용), Luna (arXive 2021, 1회 인용)
- Luna: Linear Unified Nested Attention. (arXiv 2021, 1회 인용)

## 감사합니다