```
In [243]: import numpy as np
          data = np.load('mnist.npz')
          import matplotlib.pyplot as plt
          import pandas as pd
          import gzip
          import os
          import sys
          import struct
          %matplotlib inline
In [244]: def relu(x):
              return (x > 0) * x
          def softmax(x, axis=1):
              e_x = np.exp(x - np.max(x, axis=axis, keepdims=True))
              return e_x / e_x.sum(axis=axis, keepdims=True)
          def onehot(y, n classes):
              o = np.zeros(shape=(y.shape[0], n_classes))
              for i in range(y.shape[0]):
                  o[i, int(y[i])] = 1
              return o
```

Data Preparation

reading data and preparing the test, train and validation sets

```
In [245]: def read image(fi):
               magic, n, rows, columns = struct.unpack(">IIII", fi.read(16))
               assert magic == 0x00000803
               assert rows == 28
               assert columns == 28
               rawbuffer = fi.read()
               assert len(rawbuffer) == n * rows * columns
               rawdata = np.frombuffer(rawbuffer, dtype='>u1', count=n*rows*columns)
               return rawdata.reshape(n, rows, columns).astype(np.float32) / 255.0
           def read label(fi):
               magic, n = struct.unpack(">II", fi.read(8))
               assert magic == 0 \times 000000801
               rawbuffer = fi.read()
               assert len(rawbuffer) == n
               return np.frombuffer(rawbuffer, dtype='>u1', count=n)
           os.system('wget -N http://yann.lecun.com/exdb/mnist/train-images-idx3-ubyte.gz')
           os.system('wget -N http://yann.lecun.com/exdb/mnist/train-labels-idx1-ubyte.gz')
           os.system('wget -N http://yann.lecun.com/exdb/mnist/t10k-images-idx3-ubyte.gz')
           os.system('wget -N http://yann.lecun.com/exdb/mnist/t10k-labels-idx1-ubyte.gz')
           train_x=read_image(gzip.open('train-images-idx3-ubyte.gz', 'rb')),
           train y=read label(gzip.open('train-labels-idx1-ubyte.gz', 'rb')),
           test_x=read_image(gzip.open('t10k-images-idx3-ubyte.gz', 'rb')),
           test y=read label(gzip.open('t10k-labels-idx1-ubyte.gz', 'rb'))
In [246]:
          data = np.load('mnist.npz')
           X_train = data['train_x'][:55000].reshape(55000, 784)
           y_train = data["train_y"][:55000]
          X_valid = data['train_x'][55000:].reshape(5000, 784)
           y_valid = data["train_y"][55000:]
           X \text{ test} = \text{data}['\text{test } x'].\text{reshape}(10000, 784)
           y_test = data['test_y']
```

y_train_onehot = onehot(y_train, 10)
y_valid_onehot = onehot(y_valid, 10)
y test onehot = onehot(y test, 10)

```
In [255]: class MLP:
              def init (self, init method, input size = 784, hidden size = 512, output !
                           hidden dims=(512,512), n hidden=2, mode='train', datapath=None,
                  self.W1 = np.random.normal(0, 1, (hidden_dims[0], input_size))
                  self.b1 = np.zeros(hidden size)
                  self.W2 = np.random.normal(0, 1, (hidden dims[0], hidden dims[1]))
                  self.b2 = np.zeros(hidden size)
                  self.W3 = np.random.normal(0, 1, (output size, hidden dims[1]))
                  self.b3 = np.zeros(output_size)
                  self.parameters = [self.b1, self.W1, self.b2, self.W2, self.b3, self.W3]
              def forward(self, x):
                  y_1 = np.dot(x, self.W1.T) + self.b1
                  r_1 = relu(y_1)
                  y = np.dot(r 1, self.W2.T) + self.b2
                  r 2 = relu(y 2)
                  y_3 = np.dot(r_2, self.W3.T) + self.b3
                  os = softmax(y_3, axis=1)
                  return y_1, r_1, y_2, r_2, y_3, os
              def backward(self, y, x, y_1, r_1, y_2, r_2, y_3, os, weight_decay=0):
                  bs = x.shape[0]
                  d_y_3 = os - y
                  d_r_2 = np.dot(d_y_3, self.W3)
                  d_y_2 = (y_2 > 0) * d_r_2
                  d_r_1 = np.dot(d_y_2, self.W2)
                  d_y_1 = (y_1 > 0) * d_r_1
                  d_W3 = np.dot(d_y_3.T, r_2) / bs + weight_decay * self.W3
                  d_b3 = d_y_3.mean(axis=0)
                  d_W2 = np.dot(d_y_2.T, r_1) / bs + weight_decay * self.W2
                  d b2 = d y 2.mean(axis=0)
                  d_W1 = np.dot(d_y_1.T, x) / bs + weight_decay * self.W1
                  d b1 = d y 1.mean(axis=0)
                  return d_b1, d_W1, d_b2, d_W2, d_b3, d_W3
              def loss(self, os, y):
                  return (y * (-np.log(os))).sum(axis=1).mean(axis=0)
              def train(self, data, target, mb size=100, learning rate=1e-1, weight decay=
                  for i in range(data.shape[0] // mb_size):
                      xi = data[i*mb size:(i+1)*mb size]
                      yi = target[i*mb_size:(i+1)*mb_size]
                      y_1, r_1, y_2, r_2, y_3, os = self.forward(xi)
                      average_grads = self.backward(yi, xi, y_1, r_1, y_2, r_2, y_3, os
                      average loss = self.loss(os, yi)
                      for p, grad in zip(self.parameters, average_grads):
                          p -= learning_rate * grad
                  return average loss
```

```
def mat_predict(self, x):
    _, _, _, _, os = self.forward(x)
    return os.argmax(axis=1)

def test(self, x, y):
    _, _, _, os = self.forward(x)
    return self.loss(os, y), os.argmax(axis=1)
```

```
In [251]: | def run(init method, num epoche = 10):
              mlp = MLP(init method = init method)
              train accuracies, train losses = [], []
              valid_accuracies, valid_losses = [], []
              test_accuracies, test_losses = [], []
              for e in range(num epoche):
                  loss = mlp.train(X_train, y_train_onehot, mb_size=100, learning_rate=1e-1
                  loss_train, pred_train = mlp.test(X_train, y_train_onehot)
                  loss_valid, pred_valid = mlp.test(X_valid, y_valid_onehot)
                  loss_test, pred_test = mlp.test(X_test, y_test_onehot)
                  valid losses.append(loss valid)
                  test_losses.append(loss_test)
                  valid accuracies.append((pred valid == y valid).mean())
                  test_accuracies.append((pred_test == y_test).mean())
                  train_losses.append(loss_train)
                  train accuracies.append((pred train == y train).mean())
              ### Plotting the loss and accuracy
              plt.figure(figsize=(12, 4))
              axis = plt.subplot(1, 2, 1)
              axis.plot(range(1, len(train_losses)+1), train_losses, label='train')
              axis.plot(range(1, len(valid losses)+1), valid losses, label='valid')
              axis.plot(range(1, len(test losses)+1), test losses, label='test')
              axis.legend()
              axis.set_ylabel('Loss')
              axis.set_xlabel('Epochs')
              axis = plt.subplot(1, 2, 2)
              axis.plot(range(1, len(train_accuracies)+1), train_accuracies, label='train'
              axis.plot(range(1, len(valid accuracies)+1), valid accuracies, label='valid'
              axis.plot(range(1, len(test_accuracies)+1), test_accuracies, label='test')
              axis.legend()
              axis.set ylabel('Accuracy')
              axis.set_xlabel('Epochs')
```

