

## ▼ A simple trial

Fourier transform of  $n$  data points returns  $n + 1$  complex numbers  $z_n = a_n + b_n i$  where  $a_n$  are the  $\cos(x)$  contributions in the signal and  $b_n$  are the  $\sin(x)$  contributions in the signal.

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns

df = pd.read_csv('./sample_data/sample2_out.csv')
print(df)
```

	Re	Im
0	8.389450	0.000000
1	5.105280	-1.901240
2	5.068870	1.891270
3	8.381400	0.038920
4	5.125340	-1.912640
...	...	...
122437	-0.007879	0.009161
122438	0.008523	0.000975
122439	-0.011258	-0.007286
122440	-0.005873	0.006421
122441	0.005192	0.000000

[122442 rows x 2 columns]

## ▼ Audio specific data

```
L = 244882 # Length of data (n)
sampRate = 44100; # hz
```

## ▼ Calculating frequency spectrum

The magnitude of sound is calculated as

$$M_n = \sqrt{\operatorname{Re}(z_n)^2 + \operatorname{Im}(z_n)^2} = \sqrt{a_n^2 + b_n^2}.$$

We can calculate this for each  $n$  and store those values in a new column of the dataframe

```
df["Mag"] = np.sqrt(df["Re"]*df["Re"] + df["Im"]*df["Im"])
print(df)
```

	Re	Im	Mag
0	8.389450	0.000000	8.389450
1	5.105280	-1.901240	5.447807
2	5.068870	1.891270	5.410208
3	8.381400	0.038920	8.381490
4	5.125340	-1.912640	5.470585
...	...	...	...
122437	-0.007879	0.009161	0.012083
122438	0.008523	0.000975	0.008578
122439	-0.011258	-0.007286	0.013410
122440	-0.005873	0.006421	0.008702
122441	0.005192	0.000000	0.005192

[122442 rows x 3 columns]

To find the frequencies associated with these magnitudes, we use the following fourier specific calculation:

$$f = \operatorname{linspace}(0, \frac{1}{2T}, \operatorname{numpoints}),$$

where  $\operatorname{numpoints}$  is the number of data points in our sample and period  $T$  is the inverse of our sampling rate.

```
numpoints = int(L/2)
T = 1.0/sampRate
```

```
f = np.linspace(0, 1/(2*T), numpoints)
f = np.insert(f, 1, 0) # resize
df["Frequency"] = f.tolist()
```

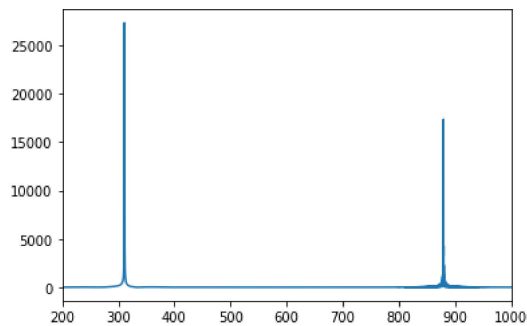
```
print(df)
```

	Re	Im	Mag	Frequency
0	8.389450	0.000000	8.389450	0.000000
1	5.105280	-1.901240	5.447807	0.000000
2	5.068870	1.891270	5.410208	0.180088
3	8.381400	0.038920	8.381490	0.360176
4	5.125340	-1.912640	5.470585	0.540265
...	...	...	...	...
122437	-0.007879	0.009161	0.012083	22049.279647
122438	0.008523	0.000975	0.008578	22049.459735
122439	-0.011258	-0.007286	0.013410	22049.639824
122440	-0.005873	0.006421	0.008702	22049.819912
122441	0.005192	0.000000	0.005192	22050.000000

```
[122442 rows x 4 columns]
```

```
# plot
fig, ax = plt.subplots()

ax.plot(df["Frequency"], df["Mag"]); # they start at the same place so maybe clip off the last bit of data?
plt.xlim(200, 1000) # x limits
plt.show();
```



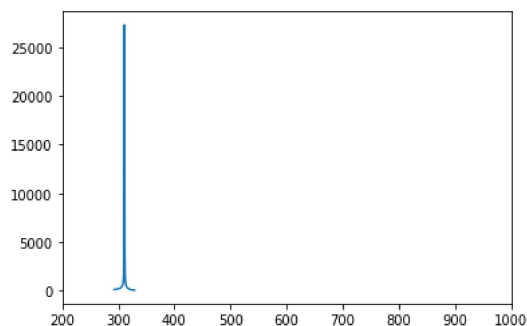
## ▼ The parsing process

We isolate the first frequency by locating a peak in the magnitude data and grabbing a window of data around the peak

```
ind = 1728 # highest index
lowerbound = ind - 100;
upperbound = ind + 100;
```

```
# plot
fig, ax = plt.subplots()
```

```
ax.plot(df["Frequency"][lowerbound:upperbound], df["Mag"][lowerbound:upperbound]); # they start at the same place so maybe clip off the last
plt.xlim(200, 1000) # x limits
plt.show();
```



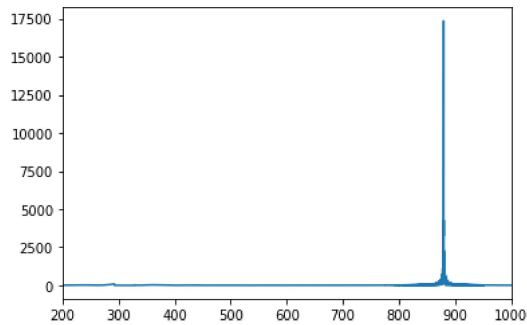
The second peak is calculated by removing the first peak -- setting the magnitude data within the selected index window to 0

```
# Kill the already isolated peak

df["Mag"][lowerbound:upperbound] = 0;

# plot
fig, ax = plt.subplots()

ax.plot(df["Frequency"], df["Mag"]);
plt.xlim(200, 1000) # x limits
plt.show();
```



## ▼ What about a more legit audio?

```
df2 = pd.read_csv('./sample_data/jingle_out.csv')
print(df2)
```

	Re	Im
0	108.723000	0.000000
1	-13.533700	4.356070
2	6.828180	24.743000
3	-18.943900	-12.546300
4	21.483300	10.820500
...	...	...
162933	-0.006334	-0.001345
162934	0.020293	-0.002687
162935	0.010724	0.005754
162936	-0.034264	-0.006255
162937	-0.021061	0.000000

[162938 rows x 2 columns]

```
L_jingle = 325874 # Length of data (n)
sampRate_jingle = 44100; # hz
```

```
df2["Mag"] = np.sqrt(df2["Re"]*df2["Re"] + df2["Im"]*df2["Im"])
print(df2)
```

	Re	Im	Mag
0	108.723000	0.000000	108.723000
1	-13.533700	4.356070	14.217467
2	6.828180	24.743000	25.667881
3	-18.943900	-12.546300	22.721818
4	21.483300	10.820500	24.054426
...	...	...	...
162933	-0.006334	-0.001345	0.006476
162934	0.020293	-0.002687	0.020470
162935	0.010724	0.005754	0.012171
162936	-0.034264	-0.006255	0.034830
162937	-0.021061	0.000000	0.021061

[162938 rows x 3 columns]

```
numpoints_jingle = int(L_jingle/2)
T_jingle = 1.0/sampRate_jingle
f_jingle = np.linspace(0, 1/(2*T_jingle), numpoints_jingle)
```

```
f_jingle = np.insert(f_jingle, 1, 0) # resize
df2["Frequency"] = f_jingle.tolist()
```

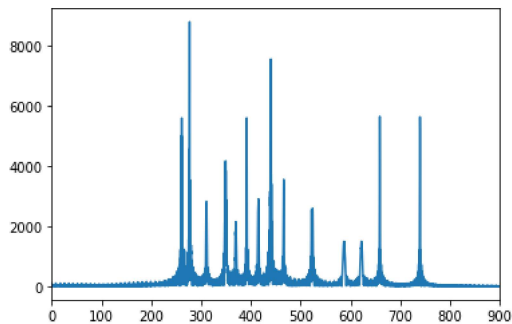
```
print(df2)
```

	Re	Im	Mag	Frequency
0	108.723000	0.000000	108.723000	0.000000
1	-13.533700	4.356070	14.217467	0.000000
2	6.828180	24.743000	25.667881	0.135329
3	-18.943900	-12.546300	22.721818	0.270658
4	21.483300	10.820500	24.054426	0.405988
...	...	...	...	...
162933	-0.006334	-0.001345	0.006476	22049.458683
162934	0.020293	-0.002687	0.020470	22049.594012
162935	0.010724	0.005754	0.012171	22049.729342
162936	-0.034264	-0.006255	0.034830	22049.864671
162937	-0.021061	0.000000	0.021061	22050.000000

```
[162938 rows x 4 columns]
```

```
# plot
fig, ax = plt.subplots()

ax.plot(df2["Frequency"], df2["Mag"]); # they start at the same place so maybe clip off the last bit of data?
plt.xlim(0, 900) # x limits
plt.show();
```

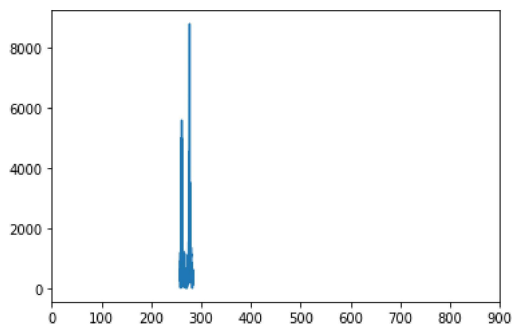


## ▼ Parsing

```
ind = 2004 # highest index
lowerbound = ind - 100;
upperbound = ind + 100;
```

```
# plot
fig, ax = plt.subplots()
```

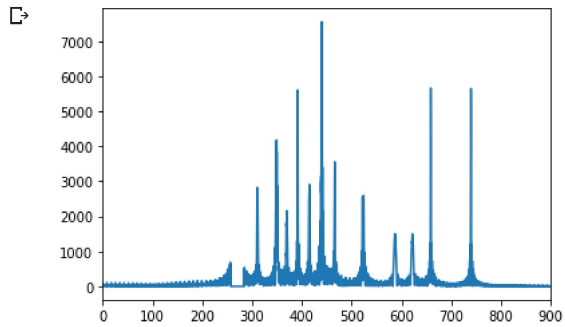
```
ax.plot(df2["Frequency"][lowerbound:upperbound], df2["Mag"][lowerbound:upperbound]);
plt.xlim(0, 900) # x limits
plt.show();
```



```
df2["Mag"][lowerbound:upperbound] = 0;
```

```
# plot
fig, ax = plt.subplots()
```

```
ax.plot(df2["Frequency"], df2["Mag"]); # they start at the same place so maybe clip off the last bit of data?  
plt.xlim(0, 900) # x limits  
plt.show();
```



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