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Solubility equilibria

NSOLUBLE compounds and the solubility of solid chemicals in water is critical in fields such as engineering, medicine, and dentistry. For example, the presence of acids in the saliva enables tooth decay as they enhance the solubility of tooth enamel made of Ca₅(PO₄)₃OH. On a similar note, barium sulfate BaSO₄, an insoluble compound, is opaque to x-rays and helps reveal digestive track issues. This chapter applies concepts of chemical equilibrium to the study of insoluble compounds. We will learn how to compute chemical solubilities using the equilibrium constant associated with the solubility equilibrium, and to assess the effect on the solubility of a common ion in solution.



The solubility of an insoluble solute is the concentration of a saturated solution. A solution is saturated when no more solute can dissolve on it. One can express solubility in two different ways, with respect to the solution and with respect to the solvent. If we refer solubility to the solution, we have two different solubility units: molar or mass-based solubility. Molar solubility is the molarity of a saturated solution, whereas mass-based solubility—or simply solubility—is the concentration in grams per liter of a saturated solution. Both types of solubilities—molar and mass-based—are related. If we refer to solubility with respect to the solvent, the solubility values are often expressed in g/100mL units, where mL refers to the volume of water.

Solubility Molar solubility or simply solubility s is defined as the moles of solute dissolved in 1L of a saturated solution. For example, the solubility of silver iodide (AgI) at 25° C is 9.0×10^{-9} mol/L. This means that 9.0×10^{-9} moles of silver iodide will dissolve in one liter of a saturated solution.

Mass-based solubility Mass-based solubility \overline{s} is defined as the number of grams of solute dissolved in a liter of a saturated solution. For example, the solubility of silver iodide (AgI) at 25° is 2.1×10^{-6} g/L. This means that 2.1×10^{-6} grans of silver iodide will dissolve in one liter of a saturated solution.

Relating solubility and mass-based solubility We can convert solubility values in terms of mass into solubility values in terms of moles by means of the molar mass of the insoluble solute

$$\left(\overline{s} = s \cdot MW\right) \tag{1.1}$$

where:



GOALS

- Compute solubility product constants
- Compute solubility from solubility product constants
- 3 Predict the precipitation of a ion mixture
- 4 Assess the impact of a common ion on solubility
- 5 Name complex ions

chemicals A and B. Given that the K_s of A is larger than the one for B, does this means that the solubility of A is larger than the one of a solution of B? Elaborate.

s is solubility in mol/L

 \overline{s} is solubility in g/L

MW the molar weight of the insoluble compound

Sample Problem 1

How many grams of AgCl will dissolve in 5mL of a AgCl saturated solution, given that s=1.33 \times 10⁻⁵M?

SOLUTION

As we have the molar solubility, we will convert this value into g/mol:

$$1.33 \times 10^{-5} \frac{mol}{L} \times \frac{143g}{mol} = 1.90 \times 10^{-3} \frac{g}{L}$$

In order to calculate the number of grams of solute in 5mL, we can do:

$$1.90 \times 10^{-3} \frac{g}{L} \times 0.005 L = 9.51 \times 10^{-5} g$$

STUDY CHECK

How many mL of solution contains 1ng of solute in a saturated ScF₃ solution, given $s=2.41\times10^{-12}$ M. The molar mass of is ScF₃ 101.9g/mol.

4081mL

Solubility based on water volume Often we will find solubility expressed in terms of 100mL of water. For example, the solubility of Aluminium chloride is 45.8 g/100 mL at 20°. This unit is defined with respect to the volume of water and ultimately is useful to find out the amount of solute that will dissolve in a given volume of water. For AlCl₃, we have that 45.8 grams of solute will dissolve in 100 mL of solvent.

1.2 Solubility equilibrium

When insoluble compounds dissolve in water an equilibrium between the solid and the dissolved ions establishes. Based on the stoichiometry of the compound we will obtain a different number of moles of ions in solution.

Solubility equilibrium Insoluble compounds dissolve in small amounts in water. Solubility equilibrium is the equilibrium that describes the dissolution of an insoluble compound to produced an aqueous solution of ions. For example, for the case of silver chloride, we have:

$$AgCl_{(s)} \rightleftharpoons Ag^{+}_{(aq)} + Cl^{-}_{(aq)}$$

The solubility equilibrium above represents the dissolution of the insoluble salt—a solid—to produce ions, silver and chloride in solution. In general terms, solubility equilibriums start with a solid and generate ions in solution. In order to break down the insoluble compound into ions, we just need to take into account the stoichiometry of the compound. For example, for the case of Cobalt(II) phosphate, we have:

$$Co_3(PO_4)_{2(s)} \rightleftharpoons 3 Co_{(aq)}^{2+} + 2 PO_4^{3-}_{(aq)}$$

| Name | Formula | K_{sp} | Name | Formula | K |
|-------------------------------|--|---|--|------------------------------------|--|
| | | | | | K_{sp} |
| Aluminium hydroxide | Al(OH) ₃ | 3.00×10^{-34} | Magnesium phosphate | $Mg_3(PO_4)_2$ | $1.04 \times 10^{-}$ |
| Aluminium phosphate | AlPO ₄ | 9.84×10^{-21} | Manganese(II) carbonate | MnCO ₃ | $2.24 \times 10^{-}$ |
| Barium bromate | $Ba(BrO_3)_2$ | 2.43×10^{-4} | Manganese(II) hydroxide | $Mn(OH)_2$ | $2.00 \times 10^{-}$ |
| Barium carbonate | BaCO ₃ | 2.58×10^{-9} | Manganese(II) iodate | $Mn(IO_3)_2$ | $4.37 \times 10^{-}$ |
| Barium chromate | BaCrO ₄ | 1.17×10^{-10} | Manganese(II) sulfide (green) | MnS | $3.00 \times 10^{-}$ |
| Barium fluoride | BaF ₂ | 1.84×10^{-7} | Manganese(II) sulfide (pink) | MnS | $3.00 \times 10^{-}$ |
| Barium hydroxide octahydrate | $Ba(OH)_2 \cdot 8 H_2O$ | 2.55×10^{-4} | Mercury(I) bromide | Hg_2Br_2 | $6.40 \times 10^{-}$ |
| Barium iodate | $Ba(IO_3)_2$ | 4.01×10^{-9} | Mercury(I) carbonate | Hg_2CO_3 | 3.6×10^{-1} |
| Barium iodate monohydrate | $Ba(IO_3)_2 \cdot H_2O$ | 1.67×10^{-9} | Mercury(I) chloride | Hg_2Cl_2 | $1.43 \times 10^{-}$ |
| Barium molybdate | $BaMoO_4$ | 3.54×10^{-8} | Mercury(I) fluoride | Hg_2F_2 | $3.10 \times 10^{-}$ |
| Barium nitrate | $Ba(NO_3)_2$ | 4.64×10^{-3} | Mercury(I) iodide | Hg_2I_2 | $5.20 \times 10^{-}$ |
| Barium selenate | BaSeO ₄ | 3.40×10^{-8} | Mercury(I) oxalate | $Hg_2C_2O_4$ | $1.75 \times 10^{-}$ |
| Barium sulfate | BaSO ₄ | 1.08×10^{-10} | Mercury(I) sulfate | Hg ₂ SO ₄ | $6.50 \times 10^{-}$ |
| Barium sulfite | BaSO ₃ | 5.00×10^{-10} | Mercury(I) thiocyanate | Hg ₂ (SCN) ₂ | $3.20 \times 10^{-}$ |
| Beryllium hydroxide | Be(OH) ₂ | 6.92×10^{-22} | Mercury(II) bromide | HgBr ₂ | 6.20×10^{-1} |
| Cadmium arsenate | $Cd_3(AsO_4)_2$ | 2.20×10^{-33} | Mercury(II) hydroxide | HgO | 3.60×10^{-3} |
| Cadmium carbonate | CdCO ₃ | 1.00×10^{-12} | Mercury(II) iodide | HgI_2 | 2.90×10^{-2} |
| Cadmium fluoride | CdF ₂ | 6.44×10^{-3} | Mercury(II) sulfide (black) | HgS | 2.00×10^{-2} |
| Cadmium hydroxide | Cd(OH) ₂ | 7.20×10^{-15} | Mercury(II) sulfide (red) | HgS | 2.00×10^{-3} |
| Cadmium iodate | $Cd(IO_3)_2$ | 2.50×10^{-8} | Neodymium carbonate | $Nd_2(CO_3)_3$ | 1.08×10^{-1} |
| Cadmium phosphate | $Cd_3(PO_4)_2$ | 2.53×10^{-33} | Nickel(II) carbonate | NiCO ₃ | 1.42×10^{-1} |
| Cadmium sulfide | CdS | 1.00×10^{-27} | Nickel(II) hydroxide | Ni(OH) ₂ | 5.48×10^{-1} |
| Calcium carbonate (calcite) | CaCO ₃ | 3.36×10^{-9} | Nickel(II) iodate | $Ni(IO_3)_2$ | $4.71 \times 10^{\circ}$ |
| Calcium fluoride | CaF ₂ | 3.45×10^{-11} | Nickel(II) phosphate | $Ni_3(PO_4)_2$ | $4.71 \times 10^{\circ}$ $4.74 \times 10^{\circ}$ |
| Calcium hydroxide | Ca(OH) ₂ | 5.49×10^{-6} 5.02×10^{-6} | Nickel(II) sulfide (alpha) | NiS | $4.00 \times 10^{\circ}$ |
| Calcium iodate | $Ca(O(1)_2$ $Ca(IO_3)_2$ | 6.47×10^{-6} | Nickel(II) sulfide (aipita) | NiS | $4.00 \times 10^{\circ}$ $1.30 \times 10^{\circ}$ |
| | · •/- | 0.47×10 1.46×10^{-8} | ` ' ' | | $7.48 \times 10^{\circ}$ |
| Calcium molybdate | CaMoO | | Potassium hexachloroplatinate | K ₂ PtCl ₆ | |
| Calcium phosphate | $Ca_3(PO_4)_2$ | 2.07×10^{-33} | Potassium perchlorate | KClO ₄ | $1.05 \times 10^{\circ}$ |
| Calcium sulfate | CaSO ₄ | 4.93×10^{-5} | Potassium periodate | KIO ₄ | $3.71 \times 10^{\circ}$ |
| Cobalt(II) arsenate | $Co_3(AsO_4)_2$ | 6.80×10^{-29} | Praseodymium hydroxide | Pr(OH) ₃ | $3.39 \times 10^{\circ}$ |
| Cobalt(II) carbonate | CoCO ₃ | 1.00×10^{-10} | Radium iodate | $Ra(IO_3)_2$ | $1.16 \times 10^{\circ}$ |
| Cobalt(II) phosphate | $Co_3(PO_4)_2$ | 2.05×10^{-35} | Radium sulfate | $RaSO_4$ | $3.66 \times 10^{\circ}$ |
| Copper(I) bromide | CuBr | 6.27×10^{-9} | Rubidium perchlorate | RuClO ₄ | 3.00×10^{-1} |
| Copper(I) chloride | CuCl | 1.72×10^{-7} | Scandium fluoride | ScF ₃ | $5.81 \times 10^{\circ}$ |
| Copper(I) cyanide | CuCN | 3.47×10^{-20} | Scandium hydroxide | $Sc(OH)_3$ | $2.22 \times 10^{\circ}$ |
| Copper(I) hydroxide | Cu ₂ O | 2.00×10^{-15} | Silver(I) acetate | AgCH ₃ COO | 1.94×10^{-6} |
| Copper(I) iodide | CuI | 1.27×10^{-12} | Silver(I) arsenate | Ag_3AsO_4 | 1.03×10^{-1} |
| Copper(I) thiocyanate | CuSCN | 1.77×10^{-13} | Silver(I) bromate | $AgBrO_3$ | 5.38×10^{-6} |
| Copper(II) arsenate | $Cu_3(AsO_4)_2$ | 7.95×10^{-36} | Silver(I) bromide | AgBr | 5.35×10^{-5} |
| Copper(II) hydroxide | Cu(OH) ₂ | 4.80×10^{-20} | Silver(I) carbonate | Ag_2CO_3 | 8.46×10^{-3} |
| Copper(II) iodate monohydrate | $Cu(IO_3)_2 \cdot H_2O$ | 6.94×10^{-8} | Silver(I) chloride | AgCl | 1.77×10^{-1} |
| Copper(II) oxalate | CuC_2O_4 | 4.43×10^{-10} | Silver(I) chromate | Ag ₂ CrO ₄ | 1.12×10^{-1} |
| Copper(II) phosphate | $Cu_3(PO_4)_2$ | 1.40×10^{-37} | Silver(I) cyanide | AgCN | 5.97×10^{-2} |
| Copper(II) sulfide | CuS | 8.00×10^{-37} | Silver(I) iodate | AgIO ₃ | 3.17×10^{-2} |
| Iron(II) carbonate | FeCO ₃ | 3.13×10^{-11} | Silver(I) iodide | AgI | 8.52×10^{-3} |
| Iron(II) fluoride | FeF ₂ | 2.36×10^{-6} | Silver(I) oxalate | $Ag_2C_2O_4$ | $5.40 \times 10^{\circ}$ |
| Iron(II) hydroxide | Fe(OH) ₂ | 4.87×10^{-17} | Silver(I) phosphate | Ag_3PO_4 | 8.89×10^{-3} |
| Iron(II) sulfide | FeS | 4.07×10 8.00×10^{-19} | Silver(I) phospitate Silver(I) sulfate | Ag_3IO_4 Ag_2SO_4 | $1.20 \times 10^{\circ}$ |
| Iron(III) hydroxide | Fe(OH) ₃ | 2.79×10^{-39} | Silver(I) sulfide | Ag_2SO_4 Ag_2S | 8×10^{-51} |
| Iron(III) phosphate dihydrate | FePO ₄ · 2 H ₂ O | 9.91×10^{-16} | Silver(I) sulfite | Ag_2SO_3 | 1.50×10^{-3} |

Sample Problem 2

Write down the solubility equilibrium for: Lead(II) iodate, and FeCO₃.

SOLUTION

The first insoluble compound, Lead(II) iodate, with formula $Pb(IO_3)_2$, contains cation lead(II) Pb^{2+} and anion IO_3^{2-} (iodate). The solubility equilibrium will be given by:

$$Pb(IO_3)_{2(s)} \rightleftharpoons Pb_{(aq)}^{2+} + 2IO_3^{-}_{(aq)}$$

The solubility equilibrium for the second insoluble compound iron(II) carbonate will be:

$$FeCO_{3(s)} \rightleftharpoons Fe_{(aq)}^{2+} + CO_3^{2-}{}_{(aq)}$$

STUDY CHECK

Write down the solubility equilibrium for: Copper(II) phosphate, and CuCN.

$$\begin{array}{c} \text{Answer: } \operatorname{Co_3(PO_4)_{2(s)}} \Longrightarrow 3\operatorname{Co}^{2+}_{(aq)} + 2\operatorname{PO_4}^{3-}_{(aq)}; \\ \operatorname{CuCN}_{(s)} \Longrightarrow \operatorname{Cu}^+_{(aq)} + \operatorname{CN}^-_{(aq)} \end{array}$$

1.3 Solubility product

When an insoluble solid solves in liquid a solubility equilibrium establishes between the solid and the dissolved solid with an equilibrium constant associated. This equilibrium constant informs about the amount of solid that dissolves, which in general is small. Unless otherwise stated, all solutions in this chapter are water-based solutions at 298K–remember equilibrium constants are temperature and solvent-dependent.

Solubility product in terms of molarities, K_{sp} Silver chloride, AgCl is normally considered an insoluble compound in water. That means this compound will not fully dissolve in water. However, small quantities of the salt will certainly dissolve leading to a small amount of silver and chlorine ions. The dissociation equilibrium involved, indicate below, is characterized by an equilibrium constant K_{sp} called *solubility product constant* or simple *solubility product*:

$$AgCl_{(s)} \rightleftharpoons Ag^{+}_{(aq)} + Cl^{-}_{(aq)}$$

$$K_{sp} = [Ag^{+}] \cdot [Cl^{-}]$$

As pure solids are not part of any equilibrium constant, the formula above does not include silver chloride. As such, all solubility products simply result from the product of the molarities of the ions involved in the dissociation, as hence its name *product*. K_{sp} will have a different explicit expression depending on the formula of the insoluble compound. For example, K_{sp} for calcium fluoride would be:

$$\operatorname{CaF}_{2(s)} \Longleftrightarrow \operatorname{Ca}_{(aq)}^{2+} + 2\operatorname{F}_{(aq)}^{-} \qquad K_{sp} = \left[\operatorname{Ca}^{2+}\right] \cdot \left[\operatorname{F}^{-}\right]^{2}$$

The solubility product is related to the solubility of the chemical. However, the relation is not one-on-one. For example, K_{sp} for PbBr₂ is 6.6×10^{-3} M, and K_{sp} for MgCO₃ is 4.0×10^{-5} M. As such, K_{sp} is smaller for PbBr₂. Differently, the solubility of MgCO₃ is indeed smaller than the solubility of PbBr₂. This is because, the relationship between K_{sp} and solubility is not linear. Table 1.1 reports solubility product constant values.

Sample Problem 3

Write down the expression of K_{sp} in terms of the ion concentration for the following compounds: Ag_2SO_4 , $Mg(OH)_2$, and $MgCO_3$.

SOLUTION

The solubility equilibrium for first compound, silver sulfate, is

$$Ag_2SO_{4(s)} \rightleftharpoons 2Ag_{(aq)}^+ + SO_4^{2-}{}_{(aq)}$$
 $K_{sp} = [Ag^+]^2 \cdot [SO_4^{2-}]$

The solubility product depends on the square concentration of silver ions. For magnesium hydroxide:

$$Mg(OH)_{2(s)} \rightleftharpoons Mg^{2+}_{(aq)} + 2OH^{-}_{(aq)}$$
 $K_{sp} = [Mg^{2+}] \cdot [OH^{-}]^{2}$

Finally, for magnesium carbonate:

$$\operatorname{MgCO}_{3(s)} \Longrightarrow \operatorname{Mg}_{(aq)}^{2+} + \operatorname{CO}_3^{2-}_{(aq)} \qquad K_{sp} = \left[\operatorname{Mg}^{2+}\right] \cdot \left[\operatorname{CO}_3^{2-}\right]$$

STUDY CHECK

Write down the expression of K_{sp} in terms of the ion concentration for the following compounds: PbCl₂, and manganese(II) sulfide.

Answer:
$$\left[\operatorname{Pb}^{2+}\right] \cdot \left[\operatorname{Cl}^{-}\right]^{2}; \left[\operatorname{Mn}^{2+}\right] \cdot \left[\operatorname{S}^{2-}\right]$$

Relating solubility to the concentration of ions We have that insoluble compounds dissolve to produce small amounts in solutions. The concentration of these is directly related to solubility by means of the stoichiometry of the compound. For example, for silver chloride—a salt with a 1:1 stoichiometry—we have that solubility is directly related to the concentration of ions:

$$[Ag^+] = s$$
 and $[Cl^-] = s$

Similarly, for barium sulfate we have that solubility is also directly related to the concentration of ions:

$$\left[\mathrm{Ba}^{+2}\right] = s \text{ and } \left[\mathrm{SO_4}^{-2}\right] = s$$

When the stoichiometry of the compound is not 1:1 we need to include the stoichiometry coefficients in the relationship. For example, for Ag_2SO_2 -a compound with 2:1 stoichiometry, we have that

$$\left[\operatorname{Ag}^{+}\right] = 2 \cdot s \text{ and } \left[\operatorname{SO_{4}}^{-2}\right] = s$$

As for every mole of silver sulfate we produce two moles of silver and one mole of sulfate in solution. Simmilarly, for $Nd_2(CO_3)_3$ we have

$$\left[\mathrm{Nd}^{+3}\right] = 2 \cdot s \text{ and } \left[\mathrm{CO_3}^{-2}\right] = 3 \cdot s$$

1.4 Predicting precipitation

Imagine we have a clear solution with any sign of precipitate. Now we add a second solution knowing that the mixture will produce a precipitate. The question here is when would the precipitate form. Some precipitates will form after adding just a few drops.

Other would require a larger amount of reagents. Where is the limit for precipitation when we mix two reagents? As you can see is crucial to predict at what point of the addition will a precipitate form.

Predicting precipitation: an introduction The values of the solubility product constant can be used to predict the precipitation of a salt when mixing two reganets. Imagine for example that we have a $0.1 \mathrm{M~Cu^+}$ solution and you gradually add a solution containing I⁻. Given that CuI is an insoluble compound with a K_{sp} of 1.27×10^{-12} , the goal would be to compute the I⁻ concentration that would make CuI precipitate. We will answer this question by obtaining first the expression for K_{sp} :

$$\operatorname{CuI}_{(s)} \rightleftharpoons \operatorname{Cu}_{(aq)}^+ + \operatorname{I}_{(aq)}^-$$
 $K_{sp} = \left[\operatorname{Cu}^+\right] \cdot \left[\operatorname{I}^-\right] = 1.27 \times 10^{-12}$

As we know the concentration of Cu^+ , and we have that the concentration of both ions is related by means of the solubility products constant, hence we can solve for the critical $\begin{bmatrix} I^- \end{bmatrix}_c$ that would make CuI precipitate:

$$K_{sp} = [\mathrm{Cu}^+] \cdot [\mathrm{I}^-]_c = (0.1) \cdot [\mathrm{I}^-]_c = 1.27 \times 10^{-12}$$

We have that $\left[\mathrm{I}^{-}\right]_{c}=1.27\times10^{-11}\mathrm{M}$. Hence, Copper(I) iodide will precipitate with a very small iodide concentration.

Selective precipitation When we have a mixture of different ions that form insoluble precipitates (e.g. Pb²⁺ and Cu⁺) we can use the principles of selective precipitation to separate the ions. We know that PbBr₂ and CuBr are insoluble compounds. Let us say we have a mixture of both ions with 0.01M concentration, and we add a solution containing Br⁻. As two different precipitates will form (CuBr and PbBr₂) the question is: are we going to be able to separate both compounds? Or the precipitation of both will overlap? If the solubility product of both insoluble compounds is different enough, we will be able to selectively precipitate first the less soluble compound and the more soluble. We will also assume that the addition of the cation will not modify the volume of the mixture.

We will calculate the amount of the added solution needed to precipitate each solid. Let us first address the expressions for the solubility product for each solid:

$$CuBr_{(s)} \rightleftharpoons Cu_{(aq)}^{+} + Br_{(aq)}^{-} \qquad K_{sp}(CuBr) = [Cu^{+}] \cdot [Br^{-}] = 6.3 \times 10^{-9}$$

$$PbBr_{2(s)} \rightleftharpoons Pb_{(aq)}^{2+} + 2 Br_{(aq)}^{-} \qquad K_{sp}(PbBr_{2}) = [Pb^{2+}] \cdot [Br^{-}]^{2} = 6.6 \times 10^{-6}$$

We will calculate the concentration of bromide needed to precipitate each of the solids, first Copper(I) bromide:

$$K_{sp}(\text{CuBr}) = [\text{Cu}^+] \cdot [\text{Br}^-] = (0.01) \cdot [\text{Br}^-] = 6.3 \times 10^{-9}$$

Solving for $[Br^-]$ we have: $[Br^-]=6.3\times 10^{-9}/0.01=6.3\times 10^{-7} M$ for the precipitation of CuBr. Now, we calculate the concentration of bromide needed to precipitate Lead(II) bromide: $[Br^-]^2=\frac{6.6\times 10^{-6}}{0.01}$ hence $[Br^-]=(\frac{6.6\times 10^{-6}}{0.01})^{\frac{1}{2}}=2.5\times 10^{-2} M$ for PbBr₂. Comparing both concentrations we have that the values are separate enough so it would be feasible to separate both ions in solution. We will have to add $6.3\times 10^{-3} \mathrm{mL}$ of the solution to precipitate Copper(I) bromide and $2.5\times 10^2 \mathrm{mL}$ to precipitate Lead(II) bromide.

1.5 Solubility and K_{sp}

The solubility product is the equilibrium constant associated to the solubility equilibrium. At the same time, the solubility product constant is related to the solubility of the insoluble compound and the relationship is not direct. This section will cover how to express K_{sp} in terms of solubility, and at the same time, how to express solubility in terms of K_{sp} . Before that, we will start by addressing the idea of solubility.

 K_{sp} in terms of molar solubility The solubility product is directly related to molar solubility s. We will demonstrate how to obtain this relationship by means of three examples. First, the solubility product of AgCl is:

$$AgCl_{(s)} \Longrightarrow Ag^{+}_{(aq)} + Cl^{-}_{(aq)}$$

$$K_{sp} = [Ag^{+}] \cdot [Cl^{-}]$$

As the concentration of each ion, Ag⁺ and Cl⁻, is related to the molar solubility of the salt, we have

$$K_{sp} = [Ag^+] \cdot [Cl^-] = (s) \cdot (s) = s^2$$

Second, for silver sulfide, an insoluble compound with a more complex stoichiometry, we have:

$$Ag_2S_{(s)} \Longrightarrow 2 Ag_{(aq)}^+ + S_{(aq)}^{2-}$$
 $K_{sp} = [Ag^+]^2 \cdot [S^{2-}] = (2s)^2 \cdot (s) = 4s^3$

Third, the solubility equilibrium and K_{sp} expression for Nd₂(CO₃)₃ is

$$Nd_2(CO_3)_{3(s)} \rightleftharpoons 2 Nd_{(aq)}^{3+} + 3 CO_3^{2-}{}_{(aq)}$$
 $K_{sp} = [Nd^{3+}]^2 \cdot [CO_3^{2-}]^3$

As the ion concentrations are related to solubility, we have

$$K_{sp} = (2s)^2 \cdot (3s)^3 = 108s^5$$

 K_{sp} in terms of molar solubility: general formula For any insoluble salt $A_x B_y$, we have that K_{sp} is related to s by means of a general formula:

$$K_{sp} = a \cdot s^b$$
 (1.2)

where:

$$a ext{ is } x^x \cdot y^y$$
 $b ext{ is } x + y$

For example, for Ba₁F₂ the constant a would be $1^1 \cdot 2^2$, that is four, whereas the constant b will be 1+2 that equals to three. As such, the expression of K_{sp} in terms of s would be: $K_{sp} = 4s^3$. This approach is useful when the we need to compute the solubility product constant given the molar solubility.

Write down the relationship between K_{sp} and s for the following salts: Co₃(PO₄)₂ and HgS.

SOLUTION

We will use Equation 1.2. For the first salt, we have:

$$K_{sp}(\text{Co}_3(\text{PO}_4)_2) = (3^3 \cdot 2^2) \cdot s^{3+2} = 108 \cdot s^5$$

For the second salt:

$$K_{sp}(HgS) = (1^1 \cdot 1^1) \cdot s^{1+1} = s^2$$

STUDY CHECK

Write down the relationship between K_{sp} and s for the following salts: ceAg2CO3 and Fe(OH)₃.

Answer: $4s^3$; $27s^4$

Molar solubility in terms of K_{sp} : general formula We previously explored the relationship between K_{sp} and molar solubility. Here we will explore the relationship between molar solubility and K_{sp} , simply solving for s in Equation 1.2. Again, for any insoluble salt A_xB_y , we have:

$$s = \left(\frac{K_{sp}}{a}\right)^{\frac{1}{b}} \tag{1.3}$$

where:

$$a ext{ is } x^x \cdot y^y$$
 $b ext{ is } x + y$

For example, for Ba_1F_2 the constant a would be $1^1 \cdot 2^2$, that is four, whereas the constant b will be 1+2 that equals to three. As such, the expression of s in terms of K_{sp} would be: $s=\left(\frac{K_{sp}}{4}\right)^{\frac{1}{3}}$. This approach is useful when the solubility product constant is given and we need to calculate the molar solubility. As the relation between molar solubility and K_{sp} is not a one-to-one relationship, K_{sp} are not directly related to solubility. For salts with a similar stoichiometry, it would be safe to compare solubilities in terms of K_{sp} . For example:

| CuS | $K_{sp} = 8 \times 10^{-37}$ | $s = 6 \times 10^{-19}$ |
|-----|------------------------------|-------------------------|
| PbS | $K_{sp} = 3 \times 10^{-28}$ | $s = 1 \times 10^{-14}$ |
| LiF | $K_{sp} = 2 \times 10^{-3}$ | $s = 3 \times 10^{-2}$ |

and we have that the lower K_{sp} the lower solubility. When the salt stoichiometry differs

| MgF_2 | $K_{sp} = 5 \times 10^{-11}$ | $s = 2 \times 10^{-4}$ |
|---------------------------------|------------------------------|------------------------|
| Li ₃ PO ₄ | $K_{sp} = 2 \times 10^{-4}$ | $s = 7 \times 10^{-2}$ |
| Li ₂ CO ₃ | $K_{sp} = 8 \times 10^{-4}$ | $s = 6 \times 10^{-2}$ |

then an increase in K_{sp} do not necessarily follows an increase in solubility.

Sample Problem 5

The solubility product of Copper(II) arsenate $Cu_3(AsO_4)_2$ is 7.95×10^{-36} . Calculate the molar solubility of the salt.

SOLUTION

In order to calculate the salt solubility, we will first break it down into ions. Copper(II) arsenate contains Cu^{2+} ions and arsenate ions AsO_4^{3+} . The solubility dissociation is given by:

$$\mathrm{Cu}_{3}(\mathrm{AsO}_{4})_{2(s)} \Longleftrightarrow 3\,\mathrm{Cu}_{(\mathrm{aq})}^{2+} + 2\,\mathrm{AsO}_{4}{}^{3+}{}_{(\mathrm{aq})} \qquad K_{sp} = \left[\mathrm{Cu}^{2+}\right]^{3} \cdot \left[\mathrm{AsO}_{4}{}^{3+}\right]^{2}$$

The molar concentration of copper and arsenate are related to solubility, taking into account the stoichiometric coefficients:

$$K_{sp} = \left[\text{Cu}^{2+} \right]^3 \cdot \left[\text{AsO}_4^{3+} \right]^2 = (3s)^3 \cdot (2s)^2 = 108s^5$$

As we know the value of the solubility product, we can solve for s:

$$7.95 \times 10^{-36} = 108s^5$$

Solving for s we have:

$$s^5 = \tfrac{7.95\times10^{-36}}{108} \text{ and } s = \sqrt[5]{\tfrac{7.95\times10^{-36}}{108}} = \big(\tfrac{7.95\times10^{36}}{108}\big)^{\frac{1}{5}} = 3.7\times10^{-8}M$$

STUDY CHECK

The solubility product of Nickel(II) phosphate $Ni_3(PO_4)_2$ is 4.74×10^{-32} . Calculate the molar solubility of the salt.

Answer: 2.13×10^{-7} M

1.6 Solubility and K_{sp}

XXXXXXXX

Solubility and PH Some insoluble salts have acid-base character. For example, Ba(OH)₂ is an insoluble salt with basic character—mind OH⁻ is a base—and FeF₂ is also a basic salt, as F⁻ is a moderately strong base resulting from the dissociation of HF, a weak acid. Therefore, for these salts, solubility is related to the PH. Only salts that result from weak acids or bases would have an acid-base character. For example, CaCO₃ or CuCN are all basic insoluble salts as carbonic acid and hydrocyanic acid are both weak acids. Let us calculate the PH of a Ba(OH)₂ solution. We have that the solubility equilibrium is given by

$$Ba(OH)_{2(s)} \rightleftharpoons Ba_{(aq)}^{2+} + 2OH_{(aq)}^{-}$$

and K_{sp} is reates to solubility s by means the following formula

$$K_{sn} = 4s^3$$

As the solubility product of Ba(OH)₂ is 2.5×10^{-4} we have that the solubility of the hydroxide is 0.04M. We have that the concentration of the ions in solution is related to solubility by

$$\left[\mathrm{Ba}^{2+}\right] = s \qquad \qquad \left[\mathrm{OH}^{-}\right] = 2s$$

Hence we have that the PH is directly related to solubility

$$POH = -log([OH^{-}]) = -log(2s) = 1.09$$

and PH will be 12.9. At the same time, solubility of insoluble compounds with acid-base properties will be affected by the PH of the solution. In the example above, as Ba(OH)₂ is a basic compound, increasing PH towards even more basic values would impede the salt dissociation and hence decrease its solubility. Differently, decreasing PH would increase solubility as the amount of hydroxils in solution would hence decrease and hence, more would need to be formed.

Common ion effect Insoluble compounds dissociate to produce ions in solution. For example, a saturated AgCl solution will contain $1.3 \times 10^{-5} \text{M-Ag}^+$ and Cl⁻. By adding a chemical with a common ion (e.g. NaCl) into the solution we can decrease solubility as common ions will decrease the salt dissociation. Let us work on a problem: we want to calculate the solubility of AgCl in a 0.1M-NaCl solution given that $K_{sp}(\text{AgCl}) = 1.8 \times 10^{-10}$. In order to do this, we will first display the solubility equilibriu of the salt

$$\operatorname{AgCl}_{(s)} \Longrightarrow \operatorname{Ag}_{(aa)}^{+} + \operatorname{Cl}_{(aa)}^{-} \qquad K_{sp} = \left[\operatorname{Ag}^{+}\right] \cdot \left[\operatorname{Cl}^{-}\right] = 1.8 \times 10^{-10}$$

The concentration of the different ions in solution are related to the salt solubility. However, as we now have a common ion (Cl⁻), we should add this new concentration to the original solubility of the salt

$$\left[Ag^{+}\right] = s \qquad \left[Cl^{-}\right] = 0.1 + s$$

Solving for s we have:

$$K_{sp} = [Ag^+] \cdot [Cl^-] = (s) \cdot (0.1 + s) = 1.8 \times 10^{-10}$$

that leads to a polynomia

$$s^2 + 0.1s - 1.8 \times 10^{-10} = 0$$

1.7 Predicting precipitation from mixtures and solutions

Imagine we have a clear solution with any sign of precipitate. Now we add a second solution knowing that the mixture will produce a precipitate. The question here is when would the precipitate form. Some precipitates will form after adding just a few drops. Other would require a larger amount of reagents. Where is the limit for precipitation when we mix two reagents? As you can see is crucial to predict at what point of the addition will a precipitate form.

Mixing ion solutions can lead to precipitation. This section addresses how to predict the precipitation of an insoluble compound from mixtures containing different ions and mixtures of solutions.

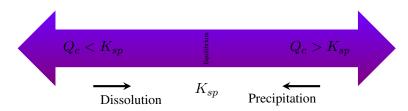
Predicting precipitation from mixtures Let us analyze a situation in which we dissolve in water an insoluble compound such as lead(II) fluoride. The solubility products constant K_{sp} is just an equilibrium constant that described the process of solubility. K_{sp} depends on the equilibrium concentration of the ions in solution. For example, K_{sp} for lead(II) fluoride is 3.3×10^{-8} and its mathematycal expression is presented below

$$PbF_2(s) \Longrightarrow Pb_{(aq)}^{2+} + 2F_{(aq)}^{-}$$
 $K_{sp} = [Pb^{2+}] \cdot [F^{-}]^2 = 3.3 \times 10^{-8}$

In the expression above, $[Pb^{2+}]$ represents the equilibrium concentration of ions Lead(II) and $[F^{-}]$ is the equilibrium concentration of fluoride. These concentrations result from dissolving the insoluble chemical in water. Let us now analyze a situation in which we have a mixture of ions containing $0.1M-Pb^{2+}$ ions and $0.1M-F^{-}$. We want to assess if a precipitate will form, given that both ions can combine to produce lead(II) fluoride. To predict precipitation, we will use the reaction concentration product Q_c , and we will compare this product with the solubility product constant K_{sp} :

$$Q_c = [Products]_{noneq} \quad concentration \text{ product}$$
 (1.4)

By comparing the calculated concentration product and the solubility product constant we can predict if a precipitate will appear or not. A precipitate will appear only for Q_c values larger than K_{sp} . In other words, mixtures of solutions more concentrated that the compound solubility will precipitate, whereas less concentrated mixtures in comparison with solubility will not precipitate.



As a side note the difference between the concentration in K_{sp} and Q_c is based on the fact that K_{sp} include *equilibrium* concentration resulting of the slow dissolution of an insoluble compound, whereas Q_c include *nonequilibrium* concentrations resulting of artificially preparing and mixing ion solutions. For the example we are considering, after mixing a 0.1M-Pb^{2+} solution and a 0.1M-F^- solution, we have that Q_c is larger than K_{sp} and therefore a precipitate will form:

$$Q_c = [\text{Pb}^{2+}]_{noneq} \cdot [\text{F}^-]_{noneq}^2 = 0.1 \cdot 0.1^2 = 1 \times 10^{-3} > K_{sp} = 3.3 \times 10^{-8}$$

hence (\downarrow)

Imaging that we mix now a 10^{-3}M-Pb^{2+} solution and a 10^{-3}M-F^- solution. For this case we have that Q_c is smaller than K_{sp} and therefore no precipitate will form:

$$Q_c = \left[\text{Pb}^{2+} \right]_{noneq} \cdot \left[\text{F}^- \right]_{noneq}^2 = 10^{-3} \cdot (10^{-3})^2 = 10^{-9} < K_{sp} = 3.3 \times 10^{-8} \\ \text{hence (} \not \text{L} \text{)}$$

Sample Problem 6

Predict if a precipitate will form in any of the following mixtures: (a) $[Cu^+]=10^{-6}M$ and $[I^-]=10^{-7}M$ given that $K_{sp}(CuI)=1.27\times 10^{-12}M$ (b) $[Cd^{2+}]=0.5M$ and $[F^-]=0.5M$ given that $K_{sp}(CdF_2)=6.44\times 10^{-3}M$ **SOLUTION**

We will calculate Q_c for each of the mixtures and we will compare the value with K_{sp} . Q_c values larger than K_{sp} will produce a precipitate, whereas Q_c values smaller than K_{sp} will not produce a precipitate. For the first mixture, we have that:

$$Q_c(\text{CuI}) = [\text{Cu}^+]_{noneq} \cdot [\text{I}^-]_{noneq} = (10^{-6}) \cdot (10^{-7}) = 10^{-13} < K_{sp}(\text{CuI})$$

Therefore in the first mixture no precipitate will form. For the second mixture:

$$Q_c(\text{CdF}_2) = \left[\text{Cd}^{2+}\right]_{noneq} \cdot \left[\text{F}^{-}\right]_{noneq}^2 = (0.5) \cdot (0.5)^2 = 3.1 \times 10^{-2} > K_{sp}(\text{CdF}_2)$$

Therefore in the second mixture a precipitate will form.

STUDY CHECK

Predict if a precipitate will form in a mixtures of $[\mathrm{Li}^+]=10^{-1}\mathrm{M}$ and $[\mathrm{CO_3}^{2-}]=10^{-1}\mathrm{M}$ given that $K_{sp}(\mathrm{Li_2CO_3})=8.15\times10^{-4}\mathrm{M}$

Answer: yes

Predicting precipitation from mixing solutions Let us now analyze a situation in which we mix two different solutions, 5mL of a solution containing $0.1M \, \text{Pb}(\text{NO}_3)_2$ and 6mL of a solution containing $0.01M \, \text{NaF}$. Assuming that liquid volume can be added, we would like to know whether lead(II) fluoride would precipitate. To answer this question, we need to calculate the concentration of lead(II) and of fluoride in the resulting mixture. With this information, we could compute the ion product and compare this value with the solubility product (3.3×10^{-8}) . We will first calculate the concentration of lead(II) produced from Pb(NO₃)₂, given that the salt dissociates giving one lead cation and two nitrate anions:

$$[Pb^{2+}] = \frac{0.1M \cdot 5mL}{11mL} = 4.5 \times 10^{-2}M$$

and then calculate the fluoride concentration produced from NaF, given that the salt dissociates giving one sodium cation and one fluoride anion:

$$[F^-] = \frac{0.01M \cdot 6mL}{11mL} = 5.4 \times 10^{-3}M$$

With these two concentrations, we can compute the ion product Q_c and compare it with K_{sp} :

$$Q_c = [Pb^{2+}]_{noneq} \cdot [F^{-}]_{noneq}^2 = (4.5 \times 10^{-2}) \cdot (5.4 \times 10^{-3})^2 =$$

$$= 1.3 \times 10^{-6} < K_{sp} = 3.3 \times 10^{-8} \text{ hence } (\downarrow)$$

Based on this comparison, we can predict that after mixing the two solutions PbF₂ will precipitate.

Sample Problem 7

Predict if a Cu₃(AsO₄)₂ precipitate will form after mixing 10mL of a 10^{-9} M Na₃AsO₄ with 10mL of a 10^{-10} M CuCl₂, given that K_{sp} (Cu₃(AsO₄)₂)=8 × 10^{-36} .

SOLUTION

We will first calculate the concentration of Cu^{2+} resulting from mixing 10mL of a $10^{-10}M$ CuCl₂ with 10mL of another solution:

$$\left[\mathrm{Cu}^{2+}\right] = \frac{10^{-10} M \cdot 10mL}{20mL} = 5 \times 10^{-11} M$$

and then calculate the concentration of ${\rm AsO_4}^{3-}$ resulting from mixing 10mL of a 10^{-9} M Na₃AsO₄ with 10mL of another solution:

$$[AsO_4^{3-}] = \frac{10^{-9}M \cdot 10mL}{20mL} = 5 \times 10^{-10}M$$

We can now calculate the ion product and compare it with the solubility product:

$$\begin{split} Q_c &= \left[\text{Cu}^{2+} \right]_{noneq}^3 \cdot \left[\text{AsO}_4{}^{3-} \right]_{noneq}^2 = (5 \times 10^{-11})^3 \cdot (5 \times 10^{-10})^2 = \\ &= 3.3 \times 10^{-50} < K_{sp} = 8 \times 10^{-36} \text{ hence } (\downarrow) \end{split}$$

The insoluble salt will precipitate. \clubsuit STUDY CHECK Predict if a FeCO₃ precipitate will form after mixing 4mL of a 10^{-6} M FeSO₄ with 5mL of a 10^{-6} M Na₂CO₃, given that K_{sp} (FeCO₃)= 3×10^{-11} .

Answer: No precipitate

Predicting the amount of precipitate formed A precipitate can form when mixing two solutions containing specific ions. For example, AgCl is an insoluble compound. A precipitate will form if you mix solutions of AgNO₃ and NaCl. In these chemicals, Ag⁺ and Cl⁻ are directly involved in the precipitate formation, whereas NO₃⁻ and Na⁺ are spectators. In this section, we will cover how to compute the amount of precipitate formed and the concentration of the leftovers. We will leave aside the spectator ions knowing that they will remain in solution. Let us consider the situation in which we mix 5mL of 0.01M-AgNO₃ with 6mL of 0.005M-AgNO₃. In order to determine the amount of precipitate formed, we will first set up the precipitation reaction:

$$Ag^{+}_{(aq)} + Cl^{-}_{(aq)} \longrightarrow AgCl_{(s)}$$

Second, we will identify the limiting reactant by comparing the moles of ions reacting. We will calculate the moles of Ag⁺ by computing the moles of silver(I) coming from AgNO₃—when multiplying volume by molarity we obtain mmol:

$$n^{\text{Ag}^+} = 5\text{mL} \cdot 0.01\text{M} = 5 \times 10^{-2}\text{mmol}$$

We will now calculate the number of moles of cloride:

$$n^{\text{Cl}^-} = 6\text{mL} \cdot 0.005\text{M} = 3 \times 10^{-2}\text{mmol}$$

We have that in order to react with the amount of Ag^+ in the mixture, we would need $n^{Cl^-} = 5 \times 10^{-2}$ mmol and we only have 3×10^{-2} mmol of cloride, hence cloride is the limiting reagent and the leftovers will be:

$$n_{left}^{\text{Ag}^+} = 5 \times 10^{-2} - 3 \times 10^{-2} = 2 \times 10^{-2} \text{mmol}$$

The number of moles of precipitate formed will be given by:

$$n^{\rm AgCl} = 3\times 10^{-2} \rm mmol~of~Cl^- \times \frac{1mol~of~AgCl}{1mol~of~Cl^-} = 3\times 10^{-2} \rm mmol~of~AgCl$$

When AgCl forms at the same time there will be silver(I) leftovers. We will finally calculate the concentration of the leftover ion simply by dividing the leftover moles by the overall volume of the mixture—mind we mix two different voluments and we asume liquid volumes can be added:

$$[Ag^{+}] = \frac{n_{left}^{Ag^{+}}}{V} = \frac{2 \times 10^{-2} \text{mmol}}{(5+6) \text{mL}} = 1.8 \times 10^{-3} \text{M}$$

Sample Problem

A mixture is prepared by adding 100mL of 0.01M-CaNO₃ with 50mL of 0.02M-NaF. Calculate the number of moles of CaF₂ that precipitate—CaF₂ is insoluble—and the concentration of the leftover ion in solution.

SOLUTION

Given that CaF₂ precipitates, we will have the following ions in the solution:

$$Ca_{(aq)}^{2+} + 2NO_3^{-}{}_{(aq)} + Na_{(aq)}^{+} + F_{(aq)}^{-} \longrightarrow CaF_{2(s)} \downarrow + 2NO_3^{-}{}_{(aq)} + Na_{(aq)}^{+}$$

The spectators will be NO_3^- and Na^+ , whereas Ca^{2+} and F^- are involved in the precipitation reaction. We will first calculate the number of moles the ions involved in the precipitation

$$n^{\mathrm{Ca}^{2+}} = 100 \mathrm{mL} \cdot 0.01 \mathrm{M} = 1 \mathrm{mmol}$$
 and $n^{\mathrm{F}^{-}} = 50 \mathrm{mL} \cdot 0.02 \mathrm{M} = 1 \mathrm{mmol}$

to then identify the limiting reagent, calculating the number of moles needed to react with 1mmol of Ca^{2+}

$$n_{needed}^{\rm F^-} = 1$$
mmol of Ca²⁺ $\times \frac{2$ mol of F⁻ $}{1$ mol of Ca²⁺ $} = 2$ mmol of F⁻

As we will need 2-mmol of F^- but we only have 1-mmol, F^- will limit the precipitation whereas Ca^{2+} will be in excess. We will based our calculations on F^- to predict the moles of precipitate formed

$$n^{\mathrm{CaF_2}} = 1$$
mmol of F $^- imes \frac{1$ mol of CaF $_2$ $}{2$ mol of F $^ } = 0.5$ mmol of CaF $_2$

and the leftover moles of Ca²⁺, given that the we have 1mmol of Ca²⁺ and we need

$$n_{needed}^{\rm Ca^{2+}} = 1 \rm mmol~of~F^- \times \frac{1 mol~of~Ca^{2+}}{2 mol~of~F^-} = 0.5 \rm mmol~of~Ca^{2+}$$

the leftovers will be 0.5mmol. Finally, we can calculate the concentration of leftover ions by doing

$$\left[\text{Ca}^{2+}\right] = \frac{n_{left}^{\text{Ag}^+}}{V} = \frac{0.5 \text{mmol}}{(50 + 100) \text{mL}} = 3.3 \times 10^{-3} \text{M}$$

STUDY CHECK

A mixture is prepared by adding 50mL of 0.03M-GaCl₃ with 75mL of 0.05M-NaOH. Calculate the number of moles of Ga(OH)₃ that precipitate and the concentration of the leftover ion in solution.

Answer: 1.25mmol; 2×10^{-3} M

CHAPTER 1

SOLUBILITY

- **1.1** The solubility of AlNO₃ is 82 g/100mL at 30°C expressed with respect to the solvent. Calculate the grams of solute that can be dissolved in 5mL of water.
- **1.2** The solubility of ammonium chlorate NH₄ClO₄ is 96 g/100mL at 50°C expressed with respect to the solvent. Calculate the liters of water needed to dissolve 1 gram of ammonium chlorate.
- **1.3** The solubility of an insoluble solute is 25 g/L at 25°C expressed with respect to the solution. Calculate the milliliters of solution needed to dissolve 5 grams of solute.
- **1.4** The solubility of an insoluble solute is 100 g/L at 20°C expressed with respect to the solution. Calculate the milliliters of solution needed to dissolve 10 grams of solute.
- **1.5** The solubility of an insoluble solute is 4mol/L at a given temperature expressed with respect to the solution. Calculate the moles of solute dissolved in 100mL of solution.
- **1.6** The molar solubility of silver carbonate is $1.3 \times$ 10⁻⁴mol/L at 20°C. Calculate the moles of solute dissolved in 25mL of solution.
- The molar solubility of zinc hydroxide 1.7 (MW=99.4g/mol) is 4.6×10^{-6} mol/L at 20° C. Express this value in grams per liter.
- **1.8** The molar solubility of lead(II) fluoride (MW=254.2g/mol) is 0.56g/L at 20°C. Express this value in moles per liter.

SOLUBILITY EQUILIBRIUM

- **1.9** Write down the solubility equilibrium for the following chemicals: (a) CuCl (b) Iron(II) sulfide (c) CuS
- **1.10** Write down the solubility equilibrium for the following chemicals: (a) Mercury(II) sulfide (b) AlPO₄

- (c) Manganese(II) sulfide
- 1.11 Write down the solubility equilibrium for the following chemicals: (a) Beryllium hydroxide (b) Ba(BrO₃)₂ (c) Lead(II) iodide
- **1.12** Write down the solubility equilibrium for the following chemicals: (a) SrSO₄ (b) Silver(I) chromate (c) $Sr(IO_3)_2$
- **1.13** Write down the relationship between solubility sand the ionic concentration for the following insoluble compounds: (a) NiCO₃ (b) Ra(IO₃)₂ (c) FeF₂
- **1.14** Write down the relationship between solubility sand the ionic concentration for the following insoluble compounds: (a) Al(OH)₃ (b) Mn(IO₃)₂ (c) BaMoO₄

SOLUBILITY PRODUCT

- **1.15** Write down the solubility product in terms of the molarities of the ions in solution for the following chemicals: (a) CuCl (b) FeS (c) MnS
- **1.16** Write down the solubility product in terms of the molarities of the ions in solution for the following chemicals: (a) MgCO₃ (b) PbCrO₄ (c) TlBr
- **1.17** Write down the solubility product in terms of the molarities of the ions in solution for the following chemicals: (a) ScF₃ (b) NiS (c) HgI₂
- **1.18** Write down the solubility product in terms of the molarities of the ions in solution for the following chemicals: (a) Cu₂O (b) Co₃(PO₄)₂ (c) Fe(OH)₃

PREDICTING PRECIPITATION

- **1.19** A solution has a 0.1M concentration of Na₂CO₃. Calculate the concentration of a Ba(NO₃)₂ solution needed to precipitate BaCO₃. $K_{sp}(BaCO_3) = 2.6 \times$ 10^{-9} .
- **1.20** A solution has a 0.001M concentration of Mn(NO₃)₂. Calculate the concentration of a Na₂CO₃

solution needed to precipitate MnCO₃. $K_{sp}(\text{MnCO}_3) = 2.2 \times 10^{-11}$.

- **1.21** We have a mixture of $Cd(NO_3)_2$ and $Ca(NO_3)_2$ containing a 0.01M concentration of both compounds. We gradually add a Na_3PO_4 solution. Indicate if we would be able to separate both cations using fractional precipitation. $K_{sp}(Cd_3(PO_4)_3) = 2.5 \times 10^{-33}$ and $K_{sp}(Ca_3(PO_4)_3) = 2.1 \times 10^{-33}$.
- **1.22** We have a mixture of Ba(NO₃)₂ and Ca(NO₃)₂ containing a 0.001M concentration of both compounds. We gradually add a Na₂SO₄ solution. Indicate if we would be able to separate both cations using fractional precipitation. $K_{sp}(\mathrm{Ba_3(SO_4)_3}) = 1.1 \times 10^{-10}$ and $K_{sp}(\mathrm{Ca_3(SO_4)_3}) = 2.1 \times 10^{-33}$.

Answers