CHAPTER 0

MATH SKILLS

0.1 Solve for x in the following algebraic equations:

(a)
$$3x + 1 = 5$$

(d)
$$\frac{3x+1}{2} = 2$$

(b)
$$2x - 1 = 5$$

(c) $\frac{3}{2} = \frac{1}{2x}$

(e)
$$\frac{2x-1}{3} = 2$$

(c)
$$\frac{3}{2} = \frac{1}{2x}$$

(f)
$$\frac{2}{3} = \frac{1}{3x}$$

0.2 Compute the following calculations involving scientific notation:

(a)
$$\frac{6.5 \times 10^3}{3 \times 10^2}$$

(c)
$$\frac{1.3\times10^{-3}}{2.5\times10^{-2}}$$

(e)
$$\frac{1}{3.4 \times 10^{-1}}$$

(b)
$$\frac{6.1\times10^{-3}}{3\times10^4}$$

(d)
$$\frac{2.4 \times 10^{-3}}{5.4.6 \times 10^{-6}}$$

(f)
$$\frac{1}{4.1 \times 10^{-4}}$$

UNITS OF MEASUREMENTS AND SYSTEMS OF UNITS

- **0.3** Indicate the magnitude measured in the following measurements: (a) 2 L (b) 5 cm
- **0.4** Indicate the magnitude measured in the following measurements: (a) 100 Kg (b) 10h
- **0.5** Answer the following questions: (a) Indicate the metric base unit for mass (b) Indicate the metric base unit for time (c) Indicate metric base unit for volume
- **0.6** Answer the following questions: (a) Indicate basic unit of mass in the SI (b) What magnitude measures the amount of space occupied by a substance

SIGNIFICANT FIGURES

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- **0.7** Indicate if the following statements represent measured or exact numbers: (a) The number of apples in a bag (b) The weight of an apple (c) The number of cm in a inch
- **0.8** Indicate if the following statements represent measured or exact numbers: (a) The number of students in a classroom (b) The height of a student
- **0.9** Identify the following numbers as measured or exact: (a) The number of students enrolled in a class is 25 (b) The temperature of a sample is $25^{\circ}C$ (c) The mass of an object is 10 Kg (d) 100grams is 1Kg
- **0.10** Identify the following numbers as measured or exact: (a) The length of an object is 4 cm (b) A chair has four legs (c) The density of a solution is 0.6 g/mL (d) One meter equals 100 cm
- **0.11** Identify the following numbers as measured or exact given the image below:

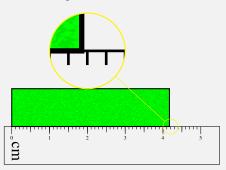


- (a) The height of the table (b) The number of table legs (c) The width of the table (d) The number of tables in the image
- **0.12** Identify the following numbers as measured or exact given the image below:

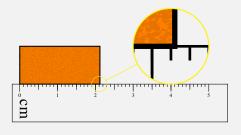


(a) The weight of the tiger (b) The number of ears of the tiger (c) The height of the tiger (d) The number of whiskers

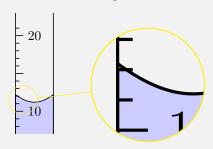
0.13 Give the following measurement with the correct number of digits, while indicating the number of significant figures of the measurement and the estimated digit.



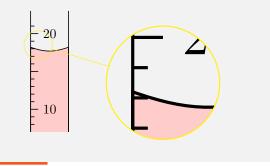
0.14 Give the following measurement with the correct number of digits, while indicating the number of significant figures of the measurement and the estimated digit.



0.15 Give the following measurement in mL with the correct number of digits, while indicating the number of significant figures of the measurement and the estimated digit.



0.16 Give the following measurement in mL with the correct number of digits, while indicating the number of significant figures of the measurement and the estimated digit.



0.17 Carry the following calculations with the correct number of digits or significant figures:

- (a) 0.2301 + 0.123
- (c) 88.1 87.57
- (b) 0.2301 1.12
- (d) 24.56 + 2.4

0.18 Carry the following calculations with the correct number of digits or significant figures:

- (a) 523×5000
- (c) 27.0×0.01
- (b) 5/0.123
- (d) 345.13/100

0.19 Indicate the number of SFs. (a) 0.0032 m (b) 5100 m (c) 0.510 m (d) 0.0051 m (e) 500 m (f) 45.030

0.20 Which of the following measurents contains the designated CORRECT number of significant figures? (a) 0.05600 cm (5 SF) (b) 0.0304 cm (3 SF) (c) 456 000 cm (3 SF) (d) 1.304 cm (2 SF) (e) 3.12050 cm (4 SF)

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0.21 Round the following numbers to 3SFs: (a) 12849m (b) 5111s (c) 2.4566×10^{-3} Kg (d) 0.051376cm (e) 573456mm (f) 0.0293845 μ m

PREFIXES & CONVERSION FACTORS

0.22 Fill the gap in the following unit equalities or conversion factors: 1Km =____m

0.23 Fill the gap in the following unit equalities or conversion factors: 1cm = m

0.24 Fill the gap in the following unit equalities or conversion factors: $\frac{1nm}{m}$

0.26 Fill the gap in the following unit equalities or conversion factors:

- **0.27** Fill the gap in the following unit equalities or conversion factors:
- (d) $\frac{L}{10^{-3}L}$
- (e) $\frac{L}{10^{-2}I}$
- (f) $\frac{g}{10^{-1}g}$

USING CONVERSION FACTORS

0.28 Fill the gap in the following unit conversion:

$$70 \text{cm} \times \frac{m}{1 \text{cm}} = 0.7 m$$

0.29 The following conversion factor is used to convert $100\mu m$ into m. Fill in the gaps:

$$100\,\mu\mathrm{m} \times \frac{m}{1\,\mu\mathrm{m}} = 1 \times 10^{-4} m$$

0.30 The following conversion factor is used to convert 40m into nm. Fill in the gaps:

$$40\cancel{n} \times \frac{1nm}{\cancel{n}} = 4 \times 10^{10} nm$$

0.31 Complete the following unit conversion:

$$100Gm \times \frac{m}{Gm} = m$$

0.32 Complete the following unit conversion:

$$50 \, km \times \frac{m}{km} = m$$

0.33 Complete the following unit conversion:

$$2p\ell \times \frac{cm}{p\ell} = cm$$

0.34 Complete the following unit conversion:

$$0.3\,\mathrm{pd}\times\frac{mm}{\mathrm{pd}}=mm$$

0.35 Complete the following unit conversion:

(a)
$$0.5 \mu g \times \frac{g}{\mu g} = g$$

(b)
$$125\cancel{L} \times \frac{\text{mL}}{\cancel{L}} = \text{mI}$$

(b)
$$125\cancel{V} \times \frac{\cancel{mL}}{\cancel{V}} = \frac{mL}{\cancel{V}}$$
 (c) $100\,\cancel{pm} \times \frac{\cancel{m}}{\cancel{pm}} = \frac{m}{m}$

0.36 The following conversion factor is used to convert 30cm into km. Fill in the gaps:

$$30 \, \mathrm{cm} \times \frac{1}{1 \, \mathrm{cm}} \times \frac{1 \, \mathrm{km}}{1} = 3 \times 10^{-4} \, \mathrm{km}$$

0.37 The following conversion factor is used to convert 50dm into cm. Fill in the gaps:

$$50 \, dm \times \frac{m}{1 \, dm} \times \frac{1 cm}{m} = 500 cm$$

0.38 Fill the gap in the following conversion factors:

$$20 \text{cm} \times \frac{1 \times 10^{-2} m}{1 \text{ cm}} \times \frac{1 mm}{1 \times 10^{-3} \text{ pc}} = mm$$

0.39 Set up the conversion factor to convert 500cm into inches:

0.40 Fill the gap in the following conversion factors:

$$20\text{cm}\times = 7.87in$$

- **0.41** Compute the following power of ten calculations:
 - (a) $(10^2)^2$
- (c) $(10^{-6})^2$
- (b) $(10^2)^3$
- (d) $(10^{-2})^2$

0.42 Set up the conversion factor to convert $400cm^2$ into m^2 :

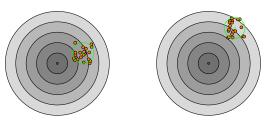


0.43 Fill the gap in the following unit equalities or conversion factors:

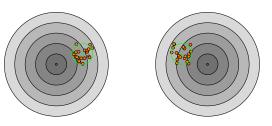
$$1 cm^2 = m^2$$
 $1 cm^3 = m^3$ $1 dm^2 = m^2$

MEASUREMENTS AND UNCERTAINTY

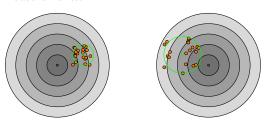
0.44 Compare the precision and accuracy of the following measurements:



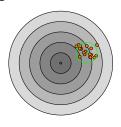
0.45 Compare the precision and accuracy of the following measurements:

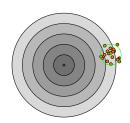


0.46 Compare the precision and accuracy of the following measurements:



0.47 Compare the precision and accuracy of the following measurements:





MATTER

- **0.48** Classify the following objects as an element, compound, and homogeneous mixture, a heterogeneous mixture or none of the others: (a) an energy drink (b) helium (a gas) (c) sulfur (a solid) (d) milk (e) milkshake (f) gelato (g) air (h) granite (i) uranium (a solid)
- **0.49** Classify the following objects as an element, compound, and homogeneous mixture, a heterogeneous mixture or none of the others: (a) a copper wire (b) a chocolate cookie (c) a chocolate-chip cookie (d) vinegar (e) ice (f) baking soda (g) aluminum foil (h) vitamin C
- **0.50** Which of the following is a property of a solid?(a) It takes the shape of the container. (b) It fills the volume of the container. (c) The particles move at a rapid rate. (d) The interactions between its particles are very weak. (e) The particles have fixed positions and are very close together.
- **0.51** Which of the following is a property of a liquid? (a) It takes the shape of the container. (b) it has no volume. (c) The particles move at a rapid rate. (d) The interactions between its particles are unesxistent. (e) The particles have fixed positions and are very close together.
- **0.52** Which of the following is a property of a gas? (a) It has no shape. (b) It fills the volume of the container. (c) The particles move slowly. (d) The interactions between its particles are strong. (e) The particles have fixed positions and are very close together.

DENSITY

- **0.53** Determine the density (g/mL) of a 0.01 L sample of a salt solution that has a mass of 50 g.
- **0.54** Which one of the following substances will float in gasoline, which has a density of 0.66 g/mL? Assume no mixing: (a) table salt (2.16 g/mL) (b) balsa wood (0.16 g/mL) (c) sugar (1.59 g/mL) (d) aluminum (2.70 g/mL) (e) mercury (13.6 g/mL)
- **0.55** You have a large water tank used as a cooler in a party and you have a bunch of cans: a coke can, a diet coke can, a water can and a schweppes can. You add all unopened cans on the tank. Describe the final vertical distribution of cans in the tank. Which can will stay on top and which will sink in more?

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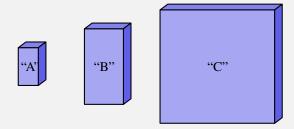
- **0.56** A nugget of gold with a mass of 521 g is added to 50.0 mL of water. The water level rises to a volume of 77.0 mL. What is the measured density of the gold?
- **0.57** A graduated cylinder contains 28.0 mL of water. What is the new water level after 35.6 g of silver metal is submerged in the water if the density of silver is 10g/mL?
- **0.58** Which of the circles is more dense: A or B.



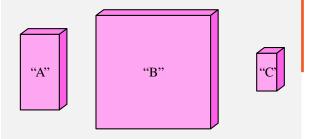
0.59 Which of the circles is more dense: A or B.



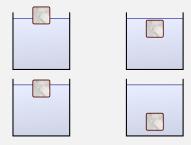
0.60 The objects below have all the same mass but represent different metals cobalt, gold, and palladium. Given that the density of cobalt is 8g/mL, whereas the density of gold is 19g/mL and the density of palladium is 12g/mL, identify each object as cobalt, gold, and palladium.



0.61 The objects below have all the same mass but represent different metals iron, nickel, and tungsten. Given that the density of iron is 7g/mL, whereas the density of nickel is 9g/mL and the density of tungsten is 20g/mL, identify each object as cobalt, gold, and palladium.



0.62 The diagrams below represent a solid immersed in a liquid, with some of the solids floating and others sinking. Match the diagrams with the description: (a) The density of the solid is 1.1 times the density of the liquid (b) The density of the solid is the same the density of the liquid (c) The density of the solid is 0.8 times the density of the liquid (d) The density of the solid is 0.5 times the density of the liquid



- **0.63** Answer the following questions involving specific gravity: (a) A sample has a density of 0.9g/mL. How much is its specific gravity? (b) A sample has a specific gravity of 1.20. How much is its density? (c) True or false: an orange juice sample should have a specific gravity larger than one.
- **0.64** Answer the following questions involving specific gravity: (a) True or false: an olive oil sample should have a specific gravity larger than one. (b) A sample has a mass of 5mg and a specific gravity of 0.87. Calculate its volume in mL.

Answers 0.1 (a) 0.33 (b) 3 (c) 0.33 (d) 1 (e) 3.5 (f) 0.5 **0.2** (a) 21.66 (b) 2.03×10^{-7} (c) 0.052 (d) 104.35(e) 8.3×10^{-1} (f) 650 **0.3** (a) 2 L (volume) (b) 5 cm (length) **0.4** (a) 100 Kg (mass) (b) 10h (time) **0.5** (a) g (b) s (c) L **0.6** (a) kg (b) the volume **0.7** (a) The number of apples in a bad (exact) (b) The weight of an apples (measured) (c) The number of cm in a inch (exact) **0.8** (a) The number of students in a classroom (exact) (b) The height of a student (measured) **0.9** (a) exact (b) measured (c) measured (d) exact **0.10** (a) measured (b) exact (c) measured (d) exact **0.11** (a) measured (b) exact (c) measured (d) exact **0.12** (a) measured (b) exact (c) measured (d) exact **0.13** 4.25cm, 3SF **0.14** 2.10cm, 3SF **0.15** 10.10cm, 4SF **0.16** 10.75cm, 4SF **0.17** (a) 0.2301 + 0.123 = 0.353 (b) 0.2301 - 1.12 = -0.89 (c) 88.1 - 87.57 = 0.5 (d) 24.56 + 2.4 = 27.0 **0.18** (a) $523 \times 5000 = 3000000$ (b) 5/0.123 $=40 \text{ (c) } 27.0 \times 0.01 = 0.3 \text{ (d) } 345.13/100 = 3$ **0.19** (a) 0.0032 m (2SF) (b) 5100 m (2SF) (c) 0.510 m (3SF) (d) 0.0051 m (2SF) (e) 500 m (1SF) (f) 45.030 m (6SF) **0.20** 456 000 (3 SF) **0.21** (a) 12900m (b) 5110s (c) 2.45×10^{-3} Kg (d) $0.0514 \mathrm{cm}$ (e) (f) $0.0294 \mu\mathrm{m}$ **0.22** 1×10^3 **0.23** 1×10^{-2} **0.24** 1×10^{-9} **0.25** 1×10^{-15} **0.26** $1 \mathrm{Tm} = 10^{12} \mathrm{m}$ $1 \text{dm} = 10^{-1} \text{m} \ 1 \text{cg} = 10^{-2} \text{g} \ 1 \text{ms} = 10^{-3} \text{s} \ 1 \text{qt} = 1 \text{mL} \ 1 \text{L} = 1 dm^3 \ 1 \text{lb} = 454 \text{g} \ 1 \text{in} = 2.54 \text{cm} \ \textbf{0.27} \ (a) \ \frac{1 \text{km}}{10^3 \text{m}}$ (b) $\frac{1 \text{cm}}{10^{-2} \text{m}}$ (c) $\frac{1 \text{ms}}{10^{-3} \text{s}}$ (d) $\frac{\text{mL}}{10^{-3} \text{L}}$ (e) $\frac{\text{cL}}{10^{-2} \text{L}}$ (f) $\frac{\text{dg}}{10^{-1} \text{g}}$ **0.28** 1×10^{-2} **0.29** $1 \cdot 10^{-6}$ **0.30** $1 \cdot 10^{-9}$ **0.31** $1 \cdot 10^{12} m$ $1.25 \times 10^{5} mL \text{ (c) } 100 \text{ pm} \times \frac{1 \times 10^{-9} m}{\text{pm}} = 1 \times 10^{-7} m \text{ 0.36 } 1 \cdot 10^{-2}; 10 \cdot 10^{3} \text{ 0.37 } 1 \cdot 10^{-1}; 1 \cdot 10^{-2} \text{ 0.38 } 200$ $0.39 \ 19.68 in \ 0.40 \ \frac{1 in}{2.54 \text{ cm}} \ 0.41 \text{ (a) } (10^{2})^{2} = 10^{4} \text{ (b) } (10^{2})^{3} = 10^{6} \text{ (c) } (10^{-6})^{2} = 10^{-12} \text{ (d) } (10^{-2})^{2} = 10^{-4}$ $0.42 \ 0.04 m^{2} \ 0.43 \ 1 \text{cm}^{2} = 1 \times 10^{-4} \text{m}^{2} \ 1 \text{dm}^{3} = 1 \times 10^{-3} \text{m}^{3} \ 1 \text{cm}^{3} = 1 \times 10^{-6} \text{m}^{3} \ 1 \text{dm}^{2} = 1 \times 10^{-2} \text{dm}^{2} \ 0.44 \text{ more}$ accurate same precision (left), less accurate same precision (right) **0.45** same accuracy and precision **0.46** same precision, more accurate (left), less accurate (right) **0.47** same accuracy, more precise (left), less precise (right) **0.48** (a) a energy drink (Homogeneous mixture) (b) helium gas (element) (c) sulfur (element) (d) milk (homogeneous mixture) (e) milkshake (Homogeneous mixture) (f) gelato (Homogeneous mixture) (g) air (Homogeneous mixture) (h) granite (Heterogeneous mixture) (i) uranium (element) **0.49** (a) a copper wire (Element) (b) a chocolate cookie (Homogeneous mixture) (c) a chocolate-chip cookie (Heterogeneous mixture) (d) vinegar (Homogeneous mixture) (e) ice (Compound) (f) baking soda(Compound) (g) aluminum foil(element) (h) vitamin C(compound) 0.50 The particles have fixed positions and are very close together. **0.51** It takes the shape of the container. **0.52** It fills the volume of the container. **0.53** $5g \cdot ml^{-1}$ **0.54** balsa wood (0.16 g/mL) **0.55** from top to bottom: coke, diet, schweppes, water **0.56** 19.3 g/mL **0.57** 31.56mL**0.58** A **0.59** A **0.60** A is gold, B is palladium and C is cobalt. **0.61** A is cickel, B is iron and C is tungsten. **0.62** ssss **0.63** (a) A sample has a density of 0.9g/mL. How much is its specific gravity? (b) A sample has a specific gravity of 1.20. How much is its density? (c) True or false: an orange juice sample should have a specific gravity larger than one. **0.64** (a) True or false: an olive oil sample should have a specific gravity larger than one. (b) A sample has a mass of 5mg and a specific gravity of 0.87. Calculate its volume in mL.