



Ch. 5. The Mole and Chemical Reactions

WHEN we buy eggs in the store, we buy them by the dozen, and the word dozen actually refers to the number twelve. Similarly, when we measure substances in a chemistry lab we measure them by the mole. This chapter will introduce the idea of mole and you will learn how to relate moles of a chemical to mass using a property called the molecular mass. This chapter also introduces chemical reactions. Chemicals react with each others and a chemical reaction is written in the form an equations. In this chapter you will learn how to balance those equations in order to predict the amount of chemicals produced.

5.1 The mole

Some of the terms you use in your everyday life refer to a number. For example, you buy a pair of socks—two socks—or you buy a dozen of eggs from the grocery store—twelve eggs—and sometimes you buy a case of beer—24 cans. In a chemistry laboratory, we normally do not weigh small numbers of molecules of a chemical. In chemistry, molecules are counted by the mole, and the term mole—abbreviated as mol—refers to the 6.022×10^{23} number. For example, a mol of CO molecules contains 6.022×10^{23} molecules of CO, and a mol of water molecules contains 6.022×10^{23} molecules of water. This is because the word mole means the number 6.022×10^{23} , similarly as the word pair means the number two. The number 6.022×10^{23} is called Avogadro's number, about Amedeo Avogadro, the Italian physicist who coined the term. In chemistry labs, chemicals are often measured by weight. In this section, we will show how to convert moles into weight—into grams—by using a property called molecular weight. Finally, mind that the term mol and molecule even if they look similar they are not. Molecule refers to a combination of atoms and mole refers to a large number of molecules. As a note, the abbreviation of the mole is mol, and for example, we will say seven mol of H₂O.

From moles to molecules One mole of molecules contains 6.022×10^{23} molecules. This is because the term mole refers to Avogadro's number. Hence we can use the following unit equivalency:

$$1\text{mol of H}_2\text{O} = 6.02 \times 10^{23} \text{molecules of H}_2\text{O}$$

or a conversion factor to transform moles into molecules or molecules into moles as well:

$$\frac{1\text{mol of H}_2\text{O}}{6.02 \times 10^{23}\text{molecules of H}_2\text{O}} \text{ or } \frac{6.02 \times 10^{23}\text{molecules of H}_2\text{O}}{1\text{mol of H}_2\text{O}}$$

For example: how many molecules are there in 3 mol of H₂O? To calculate the number of molecules of H₂O in 3 moles of H₂O, (moles → molecules) you need to set up a conversion factor, starting with the given information (3 moles) and using the mol-to-molecule conversion factor with mol on the bottom:

$$\frac{3 \text{ moles of H}_2\text{O} \times 6.02 \times 10^{23} \text{ molecules of H}_2\text{O}}{1 \text{ mol of H}_2\text{O}} = 1.80 \times 10^{24} \text{ molecules of H}_2\text{O}$$

If you need to convert molecules to moles (molecules → moles), you just need to follow the same procedure, using the conversion factor between mol-to-molecule with molecules in the bottom. For example 3×10^{20} H₂O molecules equals to 4.98×10^{-4} moles of H₂O as

$$\frac{3 \times 10^{20} \text{ molecules of H}_2\text{O} \times 1 \text{ mole of H}_2\text{O}}{6.02 \times 10^{23} \text{ molecules of H}_2\text{O}} = 4.98 \times 10^{-4} \text{ moles of H}_2\text{O}$$

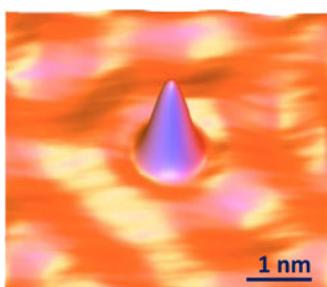
From moles to atoms Molecules are made of atoms, and for example, the CO₂ molecule contains an atom of C and two atoms of O. To convert from molecules to atoms (molecules → atoms) you need to use the coefficients in the molecular formula. For example, a H₂O molecule contains an atom of O and two atoms of H, and hence the relation between water molecules and H and O atoms is:

$\frac{1 \text{ molecule of H}_2\text{O}}{1 \text{ atom of O}}$	$\text{and } \frac{1 \text{ molecule of H}_2\text{O}}{2 \text{ atoms of H}}$
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To convert from moles into atoms (moles → atoms) you need to use a two-step process in a single line. First, you convert from moles into molecules, to then convert molecules into atoms. For example, 3 moles of H₂O contains 1.6×10^{24} H atoms, as:

$$\frac{3 \text{ moles of H}_2\text{O} \times 6.02 \times 10^{23} \text{ molecules of H}_2\text{O}}{1 \text{ mole of H}_2\text{O}} \times \frac{2 \text{ H atoms}}{1 \text{ molecule of H}_2\text{O}} = 1.6 \times 10^{24} \text{ atoms of H}$$

▼Molecules are counted by the mole



▼Eggs are bought by the dozen



▼Socks are bought as pairs



▼A ream of paper contains 500 sheets



▼A six-pack contains 6 beers



▼A gross is a dozen of dozens



Figure 5.1 Collections of items and their name

Sample Problem 1

Calculate: (a) the number of CuO molecules in 3.4 moles of CuO; (b) the number of moles of CO in 5×10^{20} CO molecules

SOLUTION

(a) 3.4 moles of CuO equals to 2.05×10^{22} molecules of CuO as:

$$3.4 \text{ moles of CuO} \times \frac{6.022 \times 10^{23} \text{ molecules of CuO}}{1 \text{ mole of CuO}} = \\ = 2.05 \times 10^{24} \text{ molecules of CuO}$$

(b) 5×10^{20} CO molecules equals to 8.3×10^{-4} moles of CO, as

$$5 \times 10^{20} \text{ CO molecules} \times \frac{1 \text{ mole of CO}}{6.022 \times 10^{23} \text{ CO molecules}} = 8.3 \times 10^{-4} \text{ moles of CO}$$

◆ STUDY CHECK

Calculate the number of C, H, N and O atoms in 3.5 moles of caffeine ($C_8H_{10}N_4O_2$).

The following example shows how to relate atoms and moles.

Sample Problem 2

Calculate the number of O atoms in 4.5 moles of NO_2 .

SOLUTION

(c) 4.5 moles of NO_2 contains 5.4×10^{24} O atoms, as

$$4.5 \text{ moles of } NO_2 \times \frac{6.022 \times 10^{23} NO_2 \text{ molecules}}{1 \text{ mole of } NO_2} \times \frac{2 \text{ O atoms}}{1 NO_2 \text{ molecule}} \\ = 5.4 \times 10^{24} \text{ O atoms}$$

▼The molecular mass of cinnamic acid ($C_9H_8O_2$), used in the manufacture of flavors, is $148.16 \frac{g}{mol}$



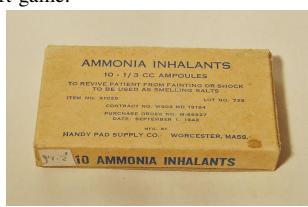
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▼Car batteries contain sulfuric acid (H_2SO_4), a corrosive chemical with a molar mass of $96.07 \frac{g}{mol}$



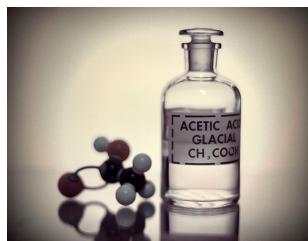
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▼Ammonia smelling salts ($(NH_4)_2CO_3$, MW=96g/mol) were historically employed to wake up injured athlete during a sport game.



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▼Acetic acid is an organic acid with molar mass $60g/mol$



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5.2 Converting moles into grams and into atoms

A standard way to measure chemicals in the lab is by weight. We can weigh different quantities and the larger the quantity the larger the weight. For a chemical, the weight of a mole is called the molar (or molecular) weight. For example, if we weigh a mole of water (H_2O) we will be weighing 18 grams of water, or if you weigh a mole of table salt ($NaCl$) the scale will show 58 grams. In this section, you will learn how to calculate the molar mass of a chemical and how to use this property to convert from weight to moles (and moles to weight).

Molar mass of a chemical Chemicals are made of atoms, and each atom has a specific atomic weight (AW) listed in the periodic table. For example, the atomic weight of Na is 23 grams whereas the atomic weight of Cl is 35 g. The weight of all the atoms of a molecule is called the molecular weight (we call this also molar weight or MW). For example, the molecular weight of $NaCl$ is 58 g, as the weight of Na and Cl is 23 and 35g. Another example would be water, H_2O with a molecular weight of 18g—as the atomic weight of H and O is 1 and 16 g, respectively, and the molecule has two

H atoms. The units for molecular weight is $\frac{g}{mol}$, also written as g/mol . To compute the molar mass of a molecule you need to break down the molecule into atoms using the coefficients in the formula. For example, the formula for vinegar is $C_2H_4O_2$ which means a vinegar molecule contains 2C, 4H and 2O atoms. If you add the atomic masses of 2C, 4H, and 2O you will get $60g/mol$. If the chemical formula has a parenthesis, you need to open up the parenthesis to calculate the total number of atoms. As an example, $Ca(NO_3)_2$ contains 1Ca, 2N, and 6O, and its molar mass is $164.09g/mol$.

Sample Problem 3

Calculate: (a) The atomic weight of Mg; (b) the molecular mass of sulfuric acid, H_2SO_4

SOLUTION

(a) According to the periodic table the atomic weight (AW) of Mg is $24.31g/mol$. (b) The molar mass of H_2SO_4 is the result of adding the atomic masses of 2H ($AW=1g/mol$) atoms, 1 S ($AW=32g/mol$) and 4O ($AW=16g/mol$) atoms, that gives $98.08g/mol$.

◆ STUDY CHECK

Calculate the molar mass of glucose $C_6H_{12}O_6$

From moles to grams The molar mass is used to convert moles to grams or grams to mol. For example, the molar mass of water is $18g/mol$. This means:

$$1 \text{ mole of } H_2O = 18 \text{ g of } H_2O$$

that is the same as

$$\frac{1 \text{ mole of } H_2O}{18 \text{ grams of } H_2O} \text{ or } \frac{18 \text{ grams of } H_2O}{1 \text{ mole of } H_2O}$$

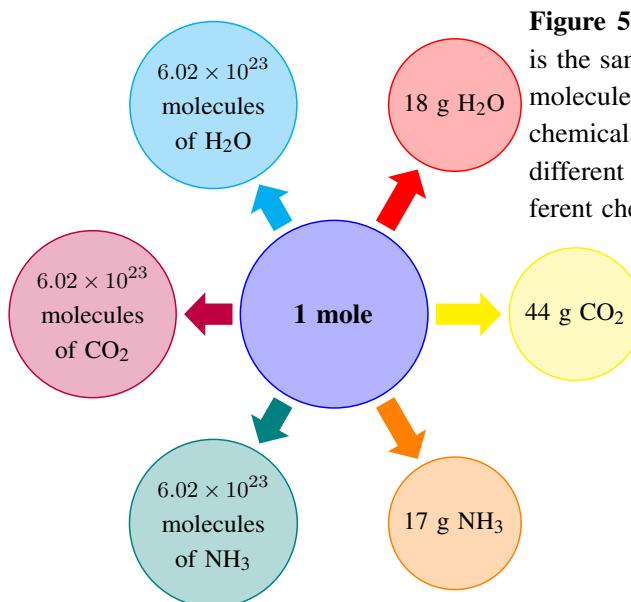


Figure 5.2 A mole is the same number of molecules for different chemicals, while being different weights for different chemicals.

Sample Problem 4

Smelling salts ($(\text{NH}_4)_2\text{CO}_3$) are chemicals used to arouse consciousness. These are used by pro athletes to get into the zone before a game. How many moles of salt do you have in 100 grams of these salts?

SOLUTION

We first need to calculate the molar mass of $(\text{NH}_4)_2\text{CO}_3$, a chemical with 2N, 8H, 1C and 3O atoms. The molar mass hence would be: $2 \times 14 + 8 \times 1 + 1 \times 12 + 3 \times 16 = 96 \text{ g/mol}$. In order to calculate the moles given the gram, you need to use the molar mass as a conversion factor:

$$\frac{100 \text{ g of } (\text{NH}_4)_2\text{CO}_3}{96 \text{ g of } (\text{NH}_4)_2\text{CO}_3} \times \frac{\text{moles of } (\text{NH}_4)_2\text{CO}_3}{\text{g of } (\text{NH}_4)_2\text{CO}_3} = 1.04 \text{ moles of } (\text{NH}_4)_2\text{CO}_3$$

◆ STUDY CHECK

Calculate the MW of table salt (NaCl) and the grams in 20 moles of this salt.

From grams to atoms In the previous sections, we covered how to convert grams to moles, moles to molecules, or molecules to atoms. You can follow the diagram below to switch from one of these properties (atoms, molecules, moles, grams) to another. For example, if you want to convert grams into moles, you will only need one step and you will only have to use a single property: the molar mass. Differently, if you need to convert grams into molecules you will have to use two different steps and use two different properties: the molar mass and Avogadro's number.

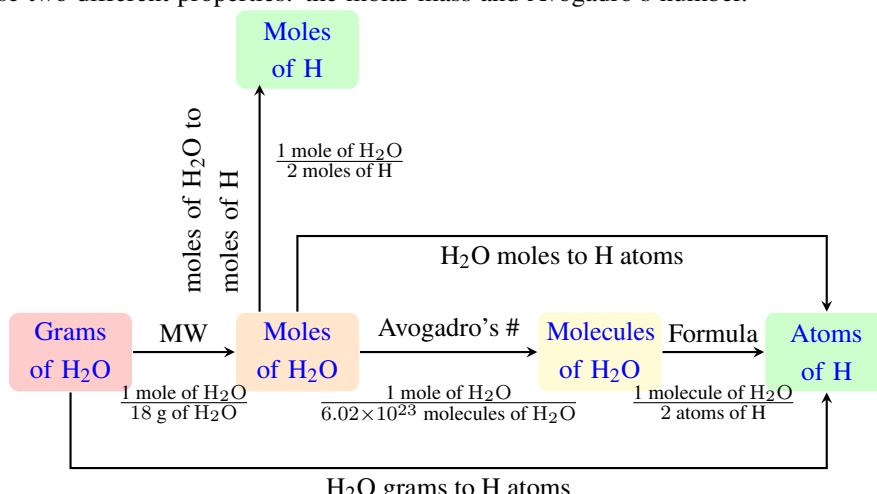


Figure 5.3 Diagrams relating grams, moles of molecules, moles of atoms, atoms and molecules.

Sample Problem 5

Convert 10 grams of ammonia (NH₃, MW=17 g/mol) into H atoms.

SOLUTION

We will have to do this conversion in three different steps. First we will go from grams to moles, then from moles to molecules to finally transform molecules

▼ A termite reaction between iron(III) oxide and Al: $\text{Fe}_2\text{O}_3 + 2\text{Al} \longrightarrow 2\text{Fe} + \text{Al}_2\text{O}_3$



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▼ An image of the combustion of Mg: $2\text{Mg(s)} + \text{O}_2\text{(g)} \longrightarrow 2\text{MgO(s)}$



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▼ Iron rust is the result of a combination reaction: $4\text{Fe} + 2\text{O}_2 \longrightarrow 2\text{Fe}_2\text{O}_3$



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▼ Wood burning is a combustion reaction



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into atoms:

$$10 \text{ g of NH}_3 \times \frac{1 \text{ mole of NH}_3}{17 \text{ g of NH}_3} \times \frac{6.022 \times 10^{23} \text{ NH}_3 \text{ molecules}}{1 \text{ mole of NH}_3} \times \frac{3 \text{ H atoms}}{1 \text{ NH}_3 \text{ molecule}} = 1.8 \times 10^{24} \text{ H atoms}$$

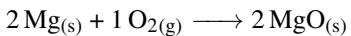
❖ STUDY CHECK

Methane is a chemical used as a fuel. Calculate how many grams of methane CH_4 contains 5×10^{25} H atoms.

5.3 Chemical reactions

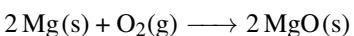
When we eat we burn food with molecular oxygen (O_2) to produce carbon dioxide and water. Similarly, when we start the engine of the car to go to work, gasoline burns to produce the same chemicals: CO_2 and H_2O . These are two examples of chemical reactions, but there are many other examples. Nitrogen from the air reacts with hydrogen to produce ammonia, a common chemical used in the production of fertilizers. This section covers the basics of chemical reactions. You will learn how to balance reactions and how to classify reactions.

Simple chemical reactions Magnesium is a metal that reacts with oxygen to produce magnesium oxide. Magnesium is solid Mg(s) whereas oxygen is gas and contains two oxygen atoms per molecule $\text{O}_2\text{(g)}$. Magnesium oxide, the result of the reaction, is solid MgO(s) . The reaction between magnesium and oxygen to produce magnesium oxide



Mg and O_2 combine—that is why we use a plus sign—to produce MgO —we use an arrow to indicate that a chemical is being produced. Also, the symbols (s) or (g) indicates solid or gas state. The reactants are located before the arrow and the products are after the arrow. The numbers in front of the reactants and products (2, 1 and 2) are called stoichiometric coefficients, and we will talk more about them in the following sections.

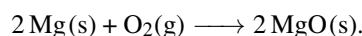
Reading a chemical reaction Chemical reactions can be read in words. To read a chemical reaction you need to connect the reactants with the word “react” and then use the words “to produce” and after that, you need to read the products. The numbers in front of the reactants and products represent the number of moles, and you need to include those numbers in the reading. For example, the following reaction



should be read as: “two moles of Mg react with one mole of O_2 to produce two moles of MgO ”.

Balanced chemical reactions Chemical reactions contain molecules, which are made of atoms. Some chemical reactions are balanced, and others need to be balanced. To identify a balanced reaction, you should use the stoichiometric coefficients and the indexes in the molecular formulas to break down the reactants and products

into atoms. In a balanced chemical reaction, the atoms of reactants should be the same as the atoms of the products. Consider the following reaction,

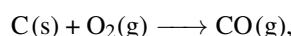


The table below shows all reactants and products in the form of atoms.

$2 \text{Mg(s)} + \text{O}_2\text{(g)} \longrightarrow 2 \text{MgO(s)}$		
Reactants	Products	
2Mg	2Mg	✓
O ₂ =2O	2O	✓

The number of Mg atoms in the reactants and products is the same and equals two. On the other hand, the number of O atoms in the reactants and products is the same, equal to two. For this reason, we say this reaction is *balanced*.

Now consider the following reaction:



The number of C atoms in the reactants and products is the same and equals one. In contrast, the number of O atoms in the reactants and products is not the same, and for this reason, we say this reaction is *not balanced*.

$\text{C(s)} + \text{O}_2\text{(g)} \longrightarrow \text{CO(g)}$		
Reactants	Products	
1C	1C	✓
O ₂ =2O	O	✗

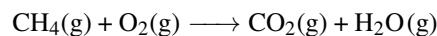
Balancing chemical reactions To balance a reaction, we need to introduce the stoichiometric coefficients that make the number of atoms of reactants and products the same. To balance the number of oxygens, we will multiply CO by two, and that will give us two oxygens and two carbons as well. If we do this, now the carbon atoms of reactants and products will not be the same. We can solve this by multiplying C(s) by two. The following table summarizes the changes we made:

$2 \text{C(s)} + \text{O}_2\text{(g)} \longrightarrow 2 \text{CO(g)}$		
Reactants	Products	
2C	2C	✓
O ₂ =2O	2O	✓

The reaction is now balanced after introducing two stoichiometric coefficients and the number of C and O atoms in the reactant molecules and products is the same.

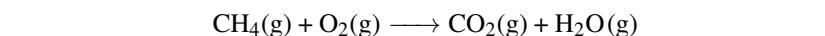
Sample Problem 6

Balance the following reaction:



SOLUTION

We will break down each molecule into atoms. In the case of O, both CO₂ and H₂O contain oxygen and hence you will have to combine both oxygen atoms:



Reactants	Products	
1C	1C	✓
4H	2H	✗
2O	3O	✗

The reaction is not balanced as the number of H and O atoms for the reactants and products is not the same. In order to balance the H, you can multiply by two H_2O , and that will balance H but also affect O.

Reactants	Products	
1C	1C	✓
4H	4H	✓
2O	4O	✗

You can balance O by multiplying O_2 by two. That will give you the final balanced reaction in which all atoms (O, H and C) are the same in the product and reactant molecules.

Reactants	Products	
1C	1C	✓
4H	4H	✓
4O	4O	✓

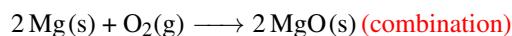
◆ STUDY CHECK

Balance the following reaction: $\text{Fe}_2\text{O}_3(\text{s}) + \text{C}(\text{s}) \longrightarrow \text{Fe}(\text{s}) + \text{CO}(\text{g})$

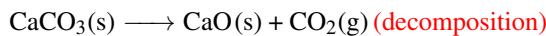
5.4 Five types of reactions

Most chemical reactions can be classified according to five types: combination, decomposition, single replacement, double replacement, and combustion.

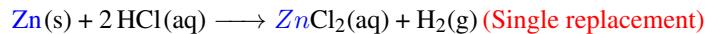
In a *combinations reaction* two reactants combine to generate a product. An example of a combination is the reaction between Mg and oxygen to produce MgO:



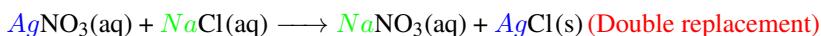
In a *decomposition reaction* a single reactant breaks down into several products. An example of a decomposition reaction is the thermal reaction of CaCO_3 to produce calcium oxide (CaO) and carbon dioxide



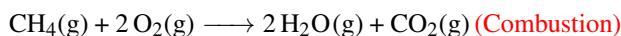
In a single replacement reaction, an element replaces another element in a chemical. An example would be the reaction of Zn with HCl, in which Zn replaces hydrogen:



In a double replacement reaction, the first element in the reacting compounds switches places. An example is the reaction between AgNO_3 and NaCl , in which Ag from AgNO_3 replaces Na in NaCl :

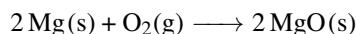


Finally, in a combustion reaction, a carbon-based chemical reacts with oxygen to produce carbon dioxide and water. An example would be the combustion of methane (CH_4):



5.5 Stoichiometry

In the previous section, you learned how to balance a chemical reaction. To do this, you had to find the stoichiometric coefficients that balance the atoms of the reactant and products. In this new section, we will learn how to use those coefficients to predict the amount of product formed. You will also learn how to predict the amount of reactant needed to react with another reactant. We will use the reaction between Mg and oxygen:



in which two moles of Mg and one mole of O_2 produce two moles of MgO. We will refer to this reaction in the following.

Mole-Mole ratio A chemical reaction can be expressed in the form of conversion factors. For example, the mole ratio between Mg (a reactant) and O_2 (another reactant) and between Mg and MgO is:

$$\frac{2 \text{ moles of Mg}}{1 \text{ moles of O}_2} \text{ or } \frac{1 \text{ moles of O}_2}{2 \text{ moles of Mg}} \text{ and } \frac{2 \text{ moles of Mg}}{2 \text{ moles of MgO}} \text{ or } \frac{2 \text{ moles of MgO}}{2 \text{ moles of Mg}}$$

Finally, the mole ratio between O_2 and MgO is:

$$\frac{1 \text{ moles of O}_2}{2 \text{ moles of MgO}} \text{ or } \frac{2 \text{ moles of MgO}}{1 \text{ moles of O}_2}$$

Mole ratios are used, for example, to transform the amount of reactant into the product.

Reactants to products We will calculate how much MgO will be produced from 5 moles of Mg by converting Mg into MgO using the conversion factor between both chemicals. As we want to transform the Mg into MgO we will use the conversion factor with Mg at the bottom of the fraction. This way the units will cancel out to give moles of MgO:

$$5 \cancel{\text{moles of Mg}} \times \frac{2 \text{ moles of MgO}}{2 \cancel{\text{moles of Mg}}} = 5 \text{ moles of MgO.}$$

This result means that 5 moles of Mg will produce 5 moles of MgO.

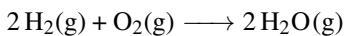
Reactant to a different reactant Sometimes we will have to calculate how much reactant will be needed to react with another reactant. In those cases, we will use the conversion factor that relates both reactants. If we have 5 moles of Mg and we want to know how much oxygen we need to react with Mg, we will proceed as:

$$5 \cancel{\text{moles of Mg}} \times \frac{1 \text{ mole of O}_2}{2 \cancel{\text{moles of Mg}}} = 2.5 \text{ moles of O}_2.$$

This result means that 2.5 moles of O_2 will react with 5 moles of Mg.

Sample Problem 7

Hydrogen reacts with oxygen to produce water according to the following reaction



Calculate: (a) the number of moles of water produced from 5 moles of H₂; (b) the number of moles of oxygen needed to react with 7 moles of H₂.

SOLUTION

(a) we will first convert 5 moles of H₂ into water:

$$\frac{5 \text{ moles of H}_2}{2 \text{ moles of H}_2} \times \frac{2 \text{ moles of H}_2\text{O}}{2 \text{ moles of H}_2} = 5 \text{ moles of H}_2\text{O},$$

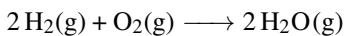
that is: 5 moles of hydrogen produce 5 moles of water. (b) We will now calculate the amount of oxygen needed to react with 7 moles of hydrogen

$$\frac{7 \text{ moles of H}_2}{2 \text{ moles of H}_2} \times \frac{1 \text{ mole of O}_2}{2 \text{ moles of H}_2} = 3.5 \text{ moles of O}_2,$$

that is: 3.5 moles of O₂ will react with 7 moles of H₂.

◆ STUDY CHECK

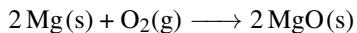
Hydrogen reacts with oxygen to produce water according to the following reaction



Calculate the number of moles of water produced by 4 moles of oxygen.

5.6 Mass calculations

In the previous sections, given the moles of reactants, we learned how to use chemical reactions to predict the amount of product formed. In this section, we will learn how to do the same, but instead of starting with the number of moles, this time, we will work our way starting with a quantity given in grams. We will base the following examples on the reaction of Mg and O₂:



Molar mass review Remember that the molar mass (also known as molecular weight, MW. Atomic weight for the atoms, AW) of a chemical is a property used to convert grams into moles. For example, the molar mass of H₂O is 18 g/mol. If we need to convert 12 grams of water into mols we should do:

$$\frac{12 \text{ g of H}_2\text{O}}{18 \text{ g of H}_2\text{O}} \times \frac{\text{moles of H}_2\text{O}}{1 \text{ g of H}_2\text{O}} = 0.66 \text{ moles of H}_2\text{O}$$

To use the stoichiometric coefficients from a chemical reaction, the starting quantity must be the moles of a reactant or products. This is because these coefficients are expressed in moles and hence to operate with them you can only use moles.

From grams to moles If we want to calculate the grams of MgO produced from 3 moles of Mg, we will start with the moles of Mg and use a conversion factor that

relates moles of Mg and moles of MgO, locating the moles of Mg on the bottom:

$$3 \cancel{\text{moles of Mg}} \times \frac{2 \text{ moles of MgO}}{2 \cancel{\text{moles of Mg}}} = 3 \text{ moles of MgO}.$$

Now we aim to calculate the number of MgO moles produced from 5 grams of Mg (AW=24g/mol). This time, we will have first to convert the grams of Mg into moles to then use the mole ratio between Mg and MgO:

$$5 \cancel{\text{g of Mg}} \times \frac{1 \cancel{\text{mole of Mg}}}{24 \cancel{\text{g of Mg}}} \times \frac{2 \text{ moles of MgO}}{2 \cancel{\text{moles of Mg}}} = 0.21 \text{ moles of MgO}.$$

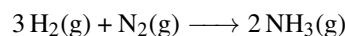
From grams to grams We want to answer the following question: we have 6 moles of Mg (AW=24g/mol) and we want to calculate the mass of MgO(MW=40g/mol) produced. The importance of this type of calculation is based on the fact that in a chemistry laboratory chemicals are normally weighted in grams. To answer this example, we will start with the grams of Mg and convert this quantity to moles of Mg using the atomic mass. After that, we will use the mole ratio between Mg and MgO to calculate the moles of MgO. At this point, we will finish the calculation by converting the moles of MgO into grams using its molecular weight:

$$5 \cancel{\text{grams of Mg}} \times \frac{1 \cancel{\text{mole of Mg}}}{24 \cancel{\text{grams of Mg}}} \times \frac{2 \cancel{\text{moles of MgO}}}{2 \cancel{\text{moles of Mg}}} \times \frac{40 \text{ grams of MgO}}{1 \cancel{\text{mole of MgO}}} \\ = 10 \text{ grams of MgO}.$$

Overall, we have that 5 grams of Mg will produce 10 grams of MgO.

Sample Problem 8

For the reaction of hydrogen and nitrogen to produce ammonia (NH₃):



Calculate: (a) the number of moles of NH₃ produced from 10 grams of hydrogen (MW=2g/mol); (b) Calculate the number of grams of NH₃ (MW=17g/mol) produced from 10 grams of nitrogen (MW=28g/mol)

SOLUTION

(a) You will solve this problem in a single line by using two steps: first convert the grams of hydrogen to moles, to then convert the moles of hydrogen into ammonia:

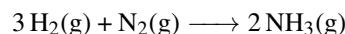
$$10 \cancel{\text{grams of H}_2} \times \frac{1 \cancel{\text{mole of H}_2}}{2 \cancel{\text{grams of H}_2}} \times \frac{2 \text{ moles of NH}_3}{3 \cancel{\text{moles of H}_2}} = 3.33 \text{ moles of NH}_3.$$

In other words, 10 grams of hydrogen produce 3.33 moles of ammonia. (b) To solve this question, we will use one additional step in order to convert the moles of ammonia into grams:

$$10 \cancel{\text{grams of N}_2} \times \frac{1 \cancel{\text{mole of N}_2}}{28 \cancel{\text{grams of N}_2}} \times \frac{2 \cancel{\text{moles of NH}_3}}{1 \cancel{\text{mole of N}_2}} \times \frac{17 \text{ grams of NH}_3}{1 \cancel{\text{mole of NH}_3}} \\ = 12.14 \text{ grams of NH}_3.$$

◆ STUDY CHECK

For the reaction of hydrogen and nitrogen to produce ammonia (NH₃):



Calculate the number of grams of nitrogen needed to react with 3 grams of hydrogen to produce ammonia.

5.7 Percent yield

Often, reactions do not fully proceed to completion. Fewer amounts of products are obtained when a specific quantity of a chemical is expected from a reaction. The percent yield tells how much of the final chemical is produced. The larger the yield the larger the amount of products generated and therefore, less waste is generated. At the same time, when mixing two reactants sometimes leftovers remain. In other words, sometimes there is a reagent that limits the reaction and an excess reagent. This section will cover the very important ideas of percent yield and limiting (or excess) reagents.

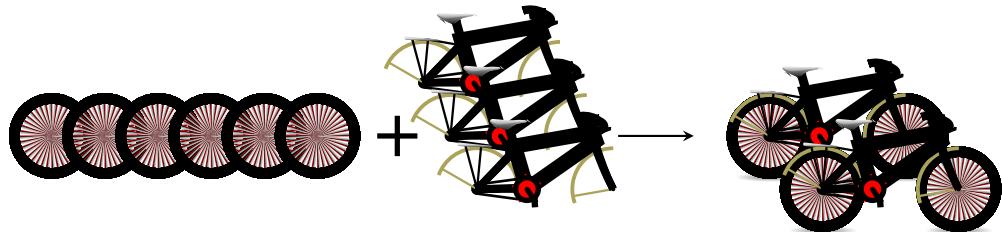
Percent yield Chemical reactions are less than perfect as the starting material does not fully convert into products. Furthermore, side reactions often occur in competition with the main reaction generating byproducts. The theoretical yield is the number of products one will expect in a hypothetically perfect chemical reaction, while the actual yield is the amount of product that is produced. Therefore, the percent yield is just the fraction between the actual yield and the theoretical yield in percent form:

$$\% \text{ Yield} = \frac{\text{actual yield}}{\text{theoretical yield}} \times 100$$

To compute the percent yield, we need the theoretical yield, which is the amount of product that will be produced following the rules of stoichiometry, and the actual yield, normally known in an experiment from lab measurements. Look at the scenario below: we need two wheels and a body to ensemble a bike. We can think about the bike production yield based on the starting materials we have.

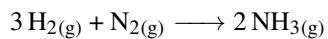


If we have three pairs of wheels and three bodies and we only produce two bikes, the yield will be 67%.



Sample Problem 9

Ammonia is produced by reacting molecular nitrogen and molecular hydrogen following the reaction:



What is the percent yield of ammonia if 4 moles of hydrogen gives 2 moles of ammonia.

SOLUTION

We will first compute the theoretical yield, that is the moles of ammonia pro-

duced from 4 moles of hydrogen:

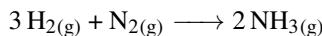
$$\frac{4 \text{ moles of H}_2}{3 \text{ moles of H}_2} \times \frac{2 \text{ moles of NH}_3}{3 \text{ moles of H}_2} = 2.66 \text{ moles of NH}_3.$$

Hence the theoretical yield is 2.66 moles of NH₃, and the actual yield given in the problem is 2 moles of NH₃. The actual yield is smaller than the theoretical yield. That is reasonable as the moles of ammonia produced in the real experiment should always be smaller than the amount of ammonia produced in theory. To calculate the percent yield we use the formula:

$$\text{Percent Yield} = \frac{\text{actual yield}}{\text{theoretical yield}} \times 100 = \frac{2}{2.66} \times 100 = 75.18\%$$

STUDY CHECK

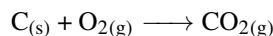
Ammonia is produced by reacting molecular nitrogen and molecular hydrogen following the reaction:



Calculate the percent yield of ammonia if 1 moles of nitrogen gives 1.5 moles of ammonia

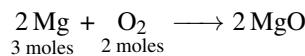
5.8 Limiting reagent

Let us consider the reaction between solid carbon and molecular oxygen to produce CO₂:



This reaction should be read as “one mole of carbon reacts with one mole of molecular oxygen to produce one mole of carbon dioxide”. Mind that to produce one mole of CO₂ you need one mole of C and one mole of molecular oxygen. Now, what would happen if you mix one mole of carbon with 0.5 moles of oxygen? In this scenario, when the 0.5 moles of oxygen are consumed the reaction will stop; half a mole of carbon dioxide will be formed and half a mole of C will remain. Differently, no oxygen will remain and the whole 0.5 moles will consume. We say that C is the excess reactant and oxygen is the limiting reactant. Often a reaction will be accompanied by the reagent quantities and you will have to identify the limiting reagent. This reagent will limit the amount of product formed, and hence, any stoichiometric calculation aimed to predict the amount of product formed should be based on the limiting reagent and never on the excess reagent. Next, we will explain how to systematically identify the limiting reagent.

Identify the limiting reagent Consider the following reaction, in which 3 moles of Mg react with 2 moles of oxygen to produce magnesium oxide:



To identify the limiting reagent, we will choose one of the given reagent quantities and calculate the moles of the other reagent needed (we will call this n_{needed}). For example, if we choose to start with 3 moles of Mg, the amount of oxygen needed to react with

this quantity will be:

$$n_{\text{needed}}^{\text{O}_2} = 3 \frac{\text{moles of Mg}}{\text{mole of O}_2} \times \frac{1 \text{ moles of O}_2}{2 \frac{\text{moles of Mg}}{\text{mole of O}_2}} = 1.5 \text{ moles of O}_2.$$

This means that to react with 3 moles of Mg you need $n_{\text{needed}}^{\text{O}_2} = 1.5$ moles of oxygen. On the other hand, you have two moles of oxygen ($n_{\text{given}}^{\text{O}_2} = 2$), and that is more than what you need to react with the 3 moles of Mg. Hence,

$$n_{\text{needed}}^{\text{O}_2} < n_{\text{given}}^{\text{O}_2}$$

oxygen is the excess reagent and Mg is the limiting reagent. The leftovers will be:

$$n_{\text{left}}^{\text{O}_2} = |n_{\text{needed}}^{\text{O}_2} - n_{\text{given}}^{\text{O}_2}| = 0.5 \text{ moles of O}_2$$

Let us reinforce the idea of limiting reagents with the scenario below. If we have three wheels and two bodies, the number of wheels limits bike production.

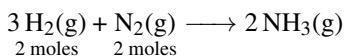


Differently, if we have three wheels and one body, then the body of the bikes limit production.



Sample Problem 10

In the synthesis of ammonia (NH_3):



you mix 2 moles of hydrogen with 2 moles of nitrogen. Identify the limiting and excess reagents and indicate the moles of leftover remaining.

SOLUTION

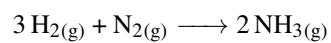
We will choose one of the reagents, for example the two moles of hydrogen, and calculate the amount of nitrogen needed to react with this amount of oxygen:

$$2 \frac{\text{moles of H}_2}{\text{mole of N}_2} \times \frac{1 \text{ moles of N}_2}{3 \frac{\text{moles of H}_2}{\text{mole of N}_2}} = 0.66 \text{ moles of N}_2.$$

Therefore, to react with 2 moles of hydrogen we need 0.66 moles of nitrogen, and we have 2 moles of nitrogen. This means we have more nitrogen than what we need and hence, nitrogen is the excess reagent and hydrogen the limiting reagent. As we need 0.66 moles of nitrogen and we have 2 moles, 1.33 moles of nitrogen will remain.

❖ STUDY CHECK

In the synthesis of ammonia (NH_3):



you mix 3 moles of hydrogen with 0.5 moles of nitrogen. Identify the limiting and excess reagents and indicate the moles of leftover remaining.
