

# 1

## Solids and liquids

HERE are three different states of the matter: solid, liquid and gas. This chapter fully deals with the properties of solids and liquids. Liquids have indeed very peculiar properties and this chapter will cover—among others—the vapor pressure. Liquids are not isolated; they are normally in contact with the atmosphere. The liquid molecules which are closer to the air can escape forming a vapor; this vapor exerts certain pressure. This vapor is what you feel, for example, when the weather is very humid. Finally, this chapter covers the idea of intermolecular forces. The molecules of an ideal gas are independent of each other. This means they do not see each other at all—they do not interact with each other. Differently, the molecules of liquids and solids interact with each other through strong forces that act between molecules—these are called intermolecular forces. The properties of these forces will help you understand why some liquids boil at higher temperatures than others or why some solids have higher melting points.



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### GOALS

- 1 Identify intermolecular forces
- 2 Identify different types of solids
- 3 Identify units cells
- 4 Calculate density of solids
- 5 Calculate vapor pressure

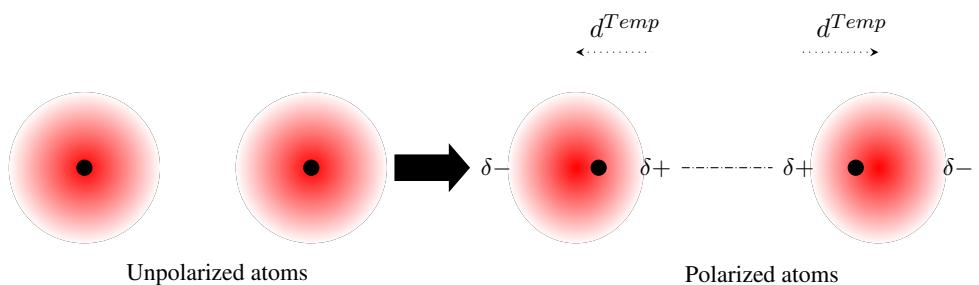
### 1.1 Intermolecular forces

Atoms in liquid or solid compound are connected by means of chemical bonds, and bonds are forces within molecules. These bonds can be ionic or covalent depending on the nature of the elements that form the molecule. At the same time, the molecules of a liquid or solid compound interact with each other by means of intermolecular forces. The word intermolecular means between molecules. This section describes the three existing types of intermolecular forces as well as its nature and intensity.

#### *Intermolecular forces and intramolecular interactions*

Molecules are made of atoms which connect by means of *intramolecular* interactions such as covalent or ionic bonds. Differently, molecules interact with each other by means of *intermolecular* interactions. The prefix *inter* means "occurring between", whereas the prefix *intra* means "occurring within". Intermolecular forces are responsible for the melting and boiling point of a chemical. On one hand, the stronger the forces the higher the melting and boiling point. On the other hand, the more intermolecular interactions the higher the melting and boiling point. This is because in order to melt or boil a chemical we need to overcome the intermolecular forces that connect molecules in order to release them into a different state of matter. In the following we will describe the three main types of intermolecular forces (some books describe four types of intermolecular forces counting the ion-molecule interaction).

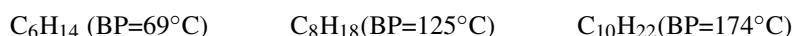
 **Discussion:** Do you know other states of the matter other than solid, liquid, or gas?



**Figure 1.1** Dispersion forces result from instantaneous dipole moments resulting from the polarization of the electron density of atoms and molecules.

*Dispersion forces* All molecules are made of atoms which contain electrons. The electron density of an atom is distributed homogeneously without uneven charge distributions. As a consequence, atoms in general have no permanent dipole moment without negatively or positively charged regions. Still, when two atoms get close together, the presence of each other affects their electron density creating temporary dipole moments. We call this effect polarizability. These temporary dipoles are responsible for London dispersion forces, also called Van der Waals forces or simply dispersion forces. Dispersion forces exist in all chemicals, as all chemicals can be polarized. The larger the atomic number, or the molar weight of the compound, the stronger these forces. This is because in general the larger the atomic weight the more polarizable atoms are, and hence, they tend to generate stronger temporary dipoles, produced from charge polarization.

The melting (or freezing) and boiling point of the noble gases are given in Table 1.1, where you can see how the larger the atomic mass of the gas the higher the melting—and boiling points. Mind that normally, the melting and freezing point of a substance are the same. Dispersion forces are common in chemicals made of hydrogen and carbon—we call these compounds hydrocarbons. The larger the size of the molecule the larger the effects of dispersion forces. For example:



**Table 1.1 Freezing and boiling point of the noble gases**

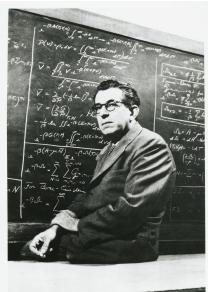
Gas	Atomic Weight (amu)	Melting Point ( $^\circ\text{C}$ )	Boiling Point ( $^\circ\text{C}$ )
He	2	—	4
Ne	10	25	27
Ar	18	84	87
Kr	36	116	121
Xe	54	162	167
Rn	6	202	211

*Dipole-Dipole forces* Atoms have different electronegativity that is, a different tendency to attract the electron density in a bond. In the periodic table, electronegativity increases going from left to right and top to bottom. Elements in the top right of the table (Cl, F) tend to be very electronegative and hence they tend to strongly attract the electrons on a chemical bond. Differently, elements on the bottom left part of the table are electropositive and they tend to give away the electrons in the bond. Dipole moments result from differences in electronegativity. When an electronegative atom is

▼ Polymer molecules interact by means of dispersion

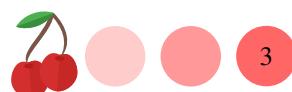


▼ Fritz London a german physicist is responsible for the name of London forces

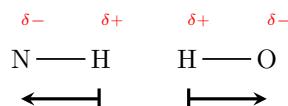


▼ geckos stick because of the van der Waals force

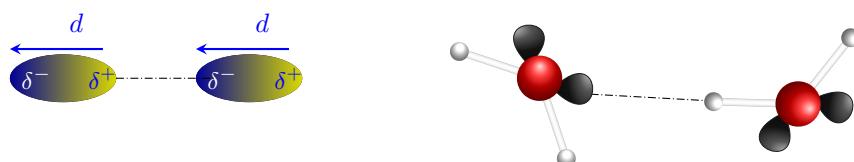




connected to a electropositive atom in a bond, the electronegativity difference creates permanent dipole moments and molecules with permanent dipole moment are called polar molecules. The dipole moment of a bond is a vector that points from the most electropositive atom to the most electronegative atom. For example for the O-H and N-H bonds,



As such, the molecule HCl would be polar as results from the combination of a electropositive atom (H) and an electronegative atom (Cl). Similarly, HF would be a polar molecule too. Dipole-dipole forces exist only in polar compounds, being the result of permanent dipole moments. This types of interactions are stronger than dispersion forces but weaker than normal interatomic covalent bonds. Molecules with dipole moment can attract each other by means of dipole forces, orienting themselves so that their positive side aligns with the negative side maximizing the electrostatic attraction. At the same type, dipole forces depend on the distance and at large distance are less effective. The dipole moment of a molecule is measured in Debye (D). For example, the dipole moment of HCl is 1.05D, whereas the dipole moment of HF is 1.82D. The stronger the dipole moment the stronger the dipole-dipole interactions. For example, when comparing C<sub>3</sub>H<sub>8</sub> and CH<sub>3</sub>OCH<sub>3</sub>, the former has a almost null dipole moment, whereas the later has a dipole moment of 1.3D. The boiling point of C<sub>3</sub>H<sub>8</sub> is -42°C whereas the boiling point of CH<sub>3</sub>OCH<sub>3</sub> is -25°C. The table below list some dipole moments and boiling points showing the trend that the larger the dipole moment the higher (more positive) the boiling point.



**Figure 1.2** (Left) Dipole-dipole forces result from the interaction of permanent dipole moments existing in polar molecules. (Right) two water molecules interacting by means of hydrogen bonds

**Table 1.2 Boiling (BP) point of a series of hydroacids**

Compound	Dipole moment (Debyes)	Boiling Point (°C)
C <sub>3</sub> H <sub>8</sub>	0.1	-42
CH <sub>3</sub> OCH <sub>3</sub>	1.3	-25
CH <sub>3</sub> Cl	2.0	-24
CH <sub>3</sub> COH	2.7	-21
CH <sub>3</sub> CN	3.9	-82

*Hydrogen bonds* Hydrogen bonds are the strongest of all intermolecular forces and exist only in molecules containing very specific bonds; in particular they only exist in molecules containing H–F, H–N or H–O bonds. An example of molecule with hydrogen bonds are HF or NH<sub>3</sub>. Hydrogen bonds are a specific type dipole-dipole interactions responsible, among other, for some of the high boiling point of water. Due to the existence of hydrogen bonds water



is liquid at room temperature ( $\text{H}_2\text{O}$ , BP=100°C), in comparison with similar molecules ( $\text{H}_2\text{S}$ , BP=-60°C). The anomalous character of oxygen, fluorine and nitrogen results from the fact that these are very electronegative elements with lone pairs of electrons—these are non-bonding pairs of electrons—that enable the creation of hydrogen bonds. In particular, oxygen has two lone pairs, nitrogen one and fluorine three. The combination of high electronegativity, the presence of lone pairs and the presence of hydrogen atoms, makes hydrogen bond possible.

### Sample Problem 1

Indicate what types of intermolecular forces exist in the following molecules:

	HCl	$\text{CH}_4$	$\text{H}_2\text{O}$	$\text{CH}_3\text{Cl}$
Dispersion				
Dipole				
H-bonds				

### SOLUTION

All molecules can interact by means of dispersion forces. Differently, only polar molecules can interact by means of dipole-dipole forces. Finally, only molecules with a H–F, H–N or H–O bond can interact by means of hydrogen bonds. For these reason, from the table only HCl,  $\text{H}_2\text{O}$  and  $\text{CH}_3\text{Cl}$  has dipole forces, and only  $\text{H}_2\text{O}$  has hydrogen bonds.

	HCl	$\text{CH}_4$	$\text{H}_2\text{O}$	$\text{CH}_3\text{Cl}$
Dispersion	✓	✓	✓	✓
Dipole	✓	✗	✓	✓
H-bonds	✗	✗	✓	✗

### STUDY CHECK

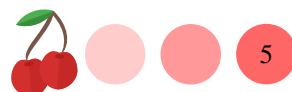
Indicate what types of intermolecular forces exist in the following molecules:  $\text{NH}_3$ , HF, and  $\text{CH}_3-\text{CH}_3$ .

*Intermolecular forces of liquids and boiling* Boiling a liquid requires energy. This energy is invested in separating the molecules from the liquid until they are spread apart. In order to separate the molecules of a liquid, we need to overcome intermolecular forces. Imagine boiling  $\text{CH}_4$ . We know the molecules of methane only interact among themselves by means of weak dispersion forces. Imagine now boiling water. Water is polar and water has O–H bonds, hence water molecules interact by means of dispersion, dipole-dipole and hydrogen bonds. The energy needed to separate the molecules of water will be larger than the energy required to separate the molecules of methane. The more intense the intermolecular forces, the higher the boiling point. Also, the more types of intermolecular forces present in a liquid the higher the boiling point. Finally, we can apply these ideas not only to liquids but also to solids.

### Sample Problem 2

Compare the boiling point of these two molecules: HCl and  $\text{H}_2\text{O}$ .

### SOLUTION



Let us build a table with the different types of intermolecular forces present in each liquid. The molecules of both liquids can interact by means of dispersion forces and also dipole-dipole forces, as both are polar molecules. Differently, only molecules with a H–F, H–N or H–O bond can interact by means of hydrogen bonds. For these reason, H<sub>2</sub>O liquid contains hydrogen bonds.

	HCl	H <sub>2</sub> O
Dispersion	✓	✓
Dipole	✓	✓
H-bonds	✗	✓

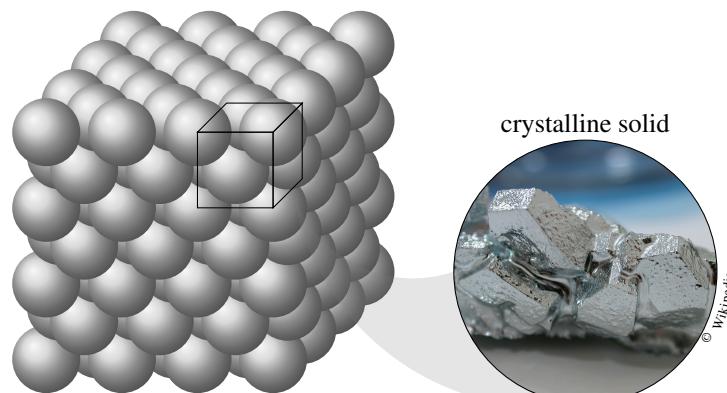
Hence, water will boil at a higher temperature.

#### ◆ STUDY CHECK

Compare the boiling point of these two molecules: CH<sub>3</sub>F and CH<sub>4</sub>.

## 1.2 The solid state

What makes solids unique in comparison to liquids and gases? They answer is their structure. There are two main different types of solids: crystalline solids and amorphous solids. Crystalline solids are made of atoms or molecules periodically, regularly, arranged in the three dimensions of the space. Examples of a crystalline solid are table salt or sugar. Amorphous solids have disordered structures. An example of an amorphous solid is window glass. This section will focus on the properties of crystalline solids as their periodicity makes their properties easier to study.



**Figure 1.3** Unit cell of a solid of a crystalline solid. The whole structure of the solid results from the replication of a unit cell and just this unit cell is necessary to characterize the structure of the solid.

**Crystalline lattice: the unit cell** The structure of crystalline solids is periodic. The term does not refer to periodic in time, but in periodic in space. Hence, the structure of crystalline solids is the result of the repetition of a small piece of the structure in the space. The overall structure is called *crystalline lattice*. Here an example of a very simple two dimensional lattice. In this lattice, the central box is repeated infinitely in two directions of the space generating a lattice. As the lattice is made of

▼ Cooking salt, NaCl is a crystalline solid



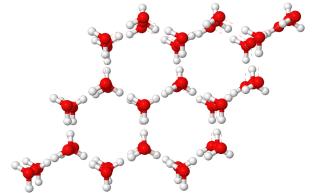
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▼ SiO<sub>2</sub> is an amorphous solid



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▼ Ice, H<sub>2</sub>O(s) is a molecular solid made of water molecules



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▼ Gold is an atomic solid made of gold atoms.



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repetition, the smallest repeating unit is called the *unit cell*. Therefore, simply with the unit cell one can generate the whole crystal lattice by repeating the unit cell in the tree dimensions. Therefore, it is unnecessary to study the crystalline whole lattice as the unit cell is enough to understand many properties of crystalline solids such as their density. In the following we will study in more detail the properties of crystalline solids and some of the most common unit cells.

*Types of crystalline solids* Examples of crystalline solids are: sugar and table salt. These two solids have very different constitutions. Table salt is made of ions:  $\text{Na}^+$  and  $\text{Cl}^-$ . Sugar is made of molecules. We say  $\text{NaCl}$  is an ionic solid, whereas sugar is a *molecular solid*. Other examples of *ionic solids*:  $\text{MgO}$ ,  $\text{CaF}_2$ . Other examples of *molecular solids*: ice which is made of water molecules. A third type of crystalline solids are called *atomic solids*, as they are made of atoms. Think of metallic iron or graphite. Both are atomic solids made of atoms, Fe and C. Overall, molecular solids are made of molecules—often times covalent molecules—whereas ionic solids are made of ions and result from ionic compounds. Finally, atomic solids are made of atoms. In the following we will study more about a specific type of atomic solids: metallic solids. Metallic solids are indeed atomic solids made of metallic elements, such as for example gold ( $\text{Au}_{(s)}$ ).

### Sample Problem 3

Classify the following solids as ionic, molecular or atomic: diamond, dry ice ( $\text{CO}_2$ ), iron and  $\text{CaF}_2$ .

	diamond	$\text{CO}_2$	Fe	$\text{CaF}_2$
Molecular				
Ionic				
Atomic				

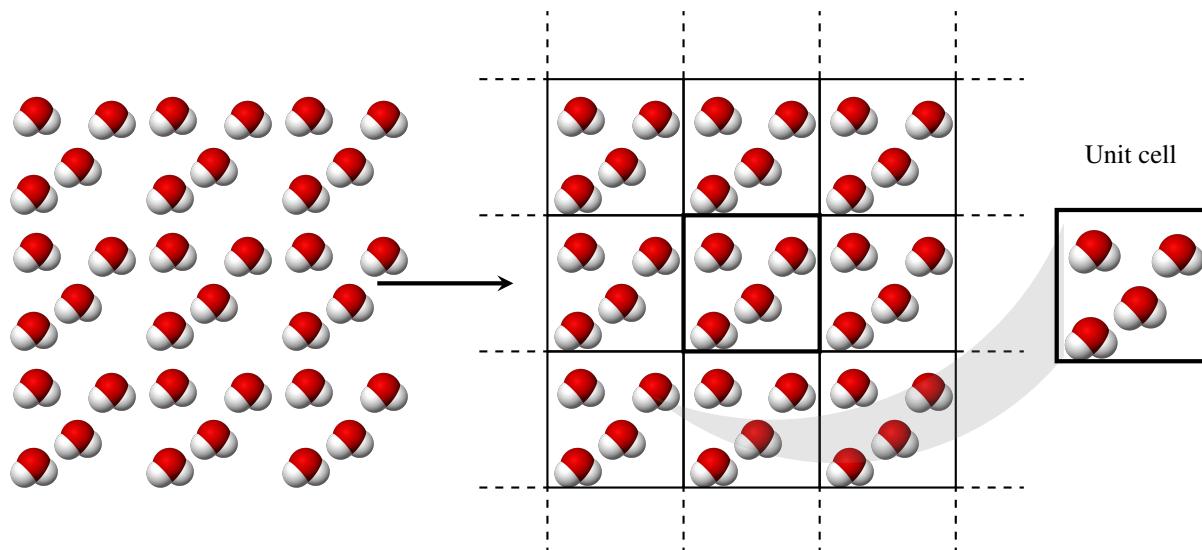
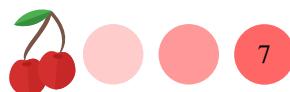
### SOLUTION

In general ionic solids correspond to ionic compounds and molecular solids correspond to covalent compounds. Therefore, dry ice should be a molecular solid and  $\text{CaF}_2$  and ionic solid. Iron and diamond are both made of atoms and hence they are atomic compounds.

	diamond	$\text{CO}_2$	Fe	$\text{CaF}_2$
Molecular	✗	✓	✗	✗
Ionic	✗	✗	✗	✓
Atomic	✓	✗	✗	✗
Metallic	✗	✗	✓	✗

### ◆ STUDY CHECK

Classify the following solids as ionic, molecular or atomic: silver, graphite,  $\text{CaCO}_3$  and  $\text{NH}_3(s)$ .



**Figure 1.4** A periodic structure made of water molecules. The unit cell on the left contains four water molecules. The repetition of the unit cell, on the right, generates a two-dimensional structure.

### 1.3 Metals and ionic solids

Among the different types of crystalline solids, metals and ionic solids are very important. This section will cover the structure of metallic solids like gold or iron and ionic solids like sodium chloride.

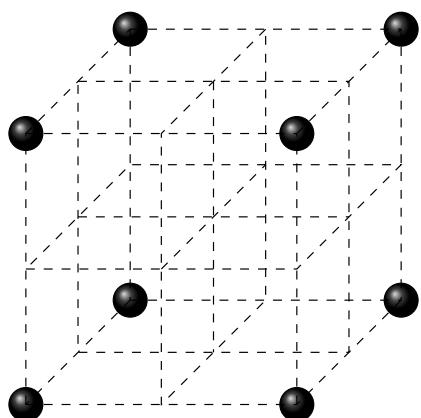
*Closed packing of metals* Metallic solids result from the packing of metal atoms in space. Picture a single layer of spheres all packed together. The most compact way to pack a layer of spheres is the situation in which one sphere is surrounded by six other spheres (layer A). This is called the closest packing. In this situation, every three spheres are connected by means of an indentation or dimple. Now let us think about how to pack a second layer on top of the first later. We can simply place the second layer just on top of the first layer (called layer A also). This would lead to a simple cubic packing arrangement (AA packing) which is not the most compact packing arrangement and the unit cell resulting from this packing is called *simple cubic*. Differently, we could pack the second layer on the indentations of the first layer, which would lead to more complex packing schemes as we try to add a third layer. There would be two possible ways to add a third layer of atoms. You can locate the third layer on top of the first layer leading to an ABA packing, with a resulting unit cell called *hexagonal close cell*, (*hcp*). Or you can locate the third layer on top of the indentations of the second layer leading to a ABC layer packing leading to a unit cell called *face centered cubic*, (*fcc*).

**Table 1.3 (Left side) atoms per cell for each unit cell; (Right side) Sharing factor for each cell location**

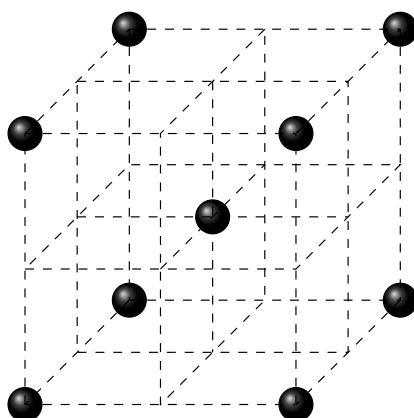
Structure	Atoms per cell	Cell location	Sharing factor, $f$
sc	1	Inside	1
bcc	2	Vertex	1/8
fcc	4	Face	1/2
		Edge	1/4



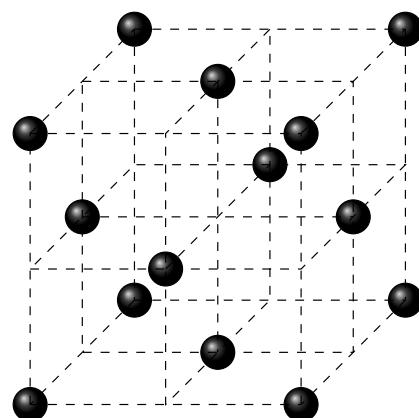
*Atom sharing in unit cells* Before we cover the different metallic units cells let us talk about atom sharing. Think about a cubit unit cell, that is a cube with one sphere (atom) in every corner of the cube. The whole lattice is produced by repeating the unit cell on the three dimensions. Hence, every corner of the cube is shared among other corders. This means, every corner-containing an atom–shares that atom with all units cells connected to that corner. Therefore, those atoms in the corner are not whole part of a single unit cell and they are shares. Every corner of a cube is shared among eight other cubes. Imagine piling numerous boxes in layers. Every corner of each box is shared by three other boxes in the same plane and by four boxes on the plane on top—that is a total of eight boxes. They way you need to think of the different atoms in a single unit cell, is that they are shared depending on their location. As we discussed, corners of a cubic unit cell are shared by a total of 8 others unit cells. Atoms that belong to a face of a unit cell are shared by two unit cells. Atoms that are inside a unit cell fully belong to a single unit cell and they are not shared. Atoms that belong to a edge of the cube—an edge is the line that connects two vertexes of a cube—are shared by four units cells.



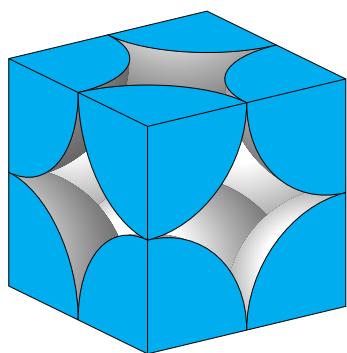
SCC (Simple cubic cell)



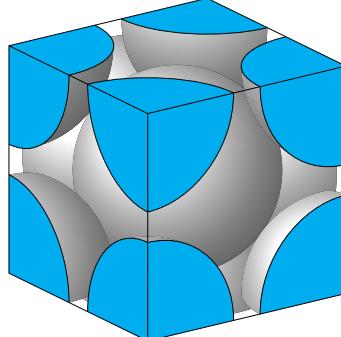
BCC (Body-centered cubic cell)



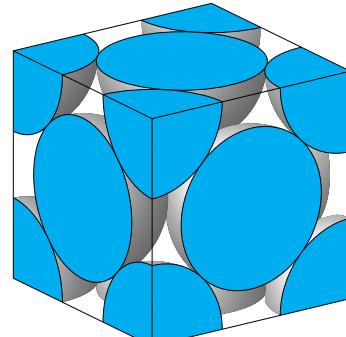
FCC (Face-centered cubic cell)



$$c = r$$

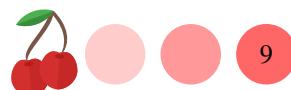


$$c = \frac{4}{\sqrt{3}}r$$

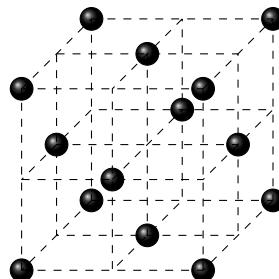


$$c = \sqrt{8}r$$

**Figure 1.5** The different unit cells. Space-fill structures are shown on the bottom. The simple cubic unit cells have atoms in the corners of the cell. The body-centered cubic unit cell have atoms in the corners and one atom in the center. The face-centered unit cell has atoms in the corners and in the faces. The relationship between the cell parameter ( $c$ ) and the atomic radius ( $r$ ) is also given for each unit cell.

**Sample Problem 4**

The following structure is called face centered unit cell. This is a cubit unit cell with one atom in each corner of the cell and atoms also in the facets of the cell. Calculate the number of atoms in the unit cell:

**SOLUTION**

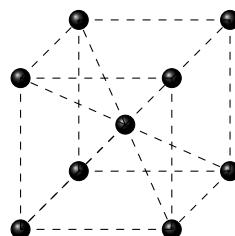
If you count the number of spheres in the drawing you might think the cell contains fourteen atoms. However, this is not true, as each sphere is shared by other unit cells. Remember each location of the unit cell counts as a fraction. If an atom is fully inside in the cell—not in the vertexes, neither in the faces or sides—the sharing factor is one. If an atom belongs to a vertex, the sharing factor is  $1/8$ . Atoms in a face has a sharing factor of  $1/2$  and atoms in the edges have a sharing factor of  $1/4$ .

Location	Sharing Factor, $f$	# atoms, $N$	$f \times N$
Corner	$1/8$	8	1
Faces	$1/2$	6	3

By multiplying the number of atoms in each location by the sharing factor and adding we obtain the total number of atoms in the cell. Overall, this unit cell has four atoms:

**◆ STUDY CHECK**

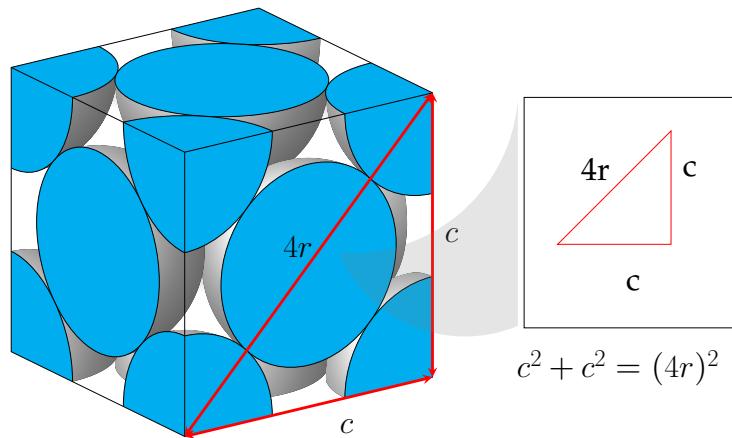
The following structure is called simple body centered unit cell. This is a cubit unit cell with one atom in each corner of the cell and an atom also in the center of cell. Calculate the number of atoms in the unit cell:



*Metal unit cells* Here we will cover three different metal unit cells, all cubic cells. First, the simple cubic unit cell, with an atom each of the vertexes of the cell. This is the less compact unit cell with one atom per unit cell. Second, the body-centered unit cell is a cubic unit cell with atoms in the vertex of the cell and a single atom in the center of the cell. This cell has two atoms per unit cell. Third, the face-centered unit cell, with atoms in the vertex of the cell and also on the faces of the cell, on the sides of the cube. This is the most compact unit cell, with four atoms per cell. In the following image you can manipulate a face-centered cubic cell.

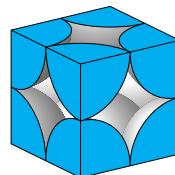


**Cell parameter** Cubic unit cells have the shape of a cube and hence all side of the cube have the same length. This length is called cell parameter  $c$ . Unit cells with large cell parameter have more spacing between atoms. The opposite is true for cells with smaller cell parameter. The cell parameter of a unit cell is related to the atomic radius. Let us analyze the case of a face-centered unit cell. In each side of the cell, in each face, we have four atoms in the vertexes and one in the center of the face. Of course these atoms do not belong only to this unit cell. However, if we symbolically cut the atoms in the face we can see the relation between the radius of the atom and the unit cell. The edges of the cell does not correspond to any cell parameter. However, the line that connect the bottom part with the opposite top part corresponds to a specific number of cell parameters, as the atoms are touching in this direction. In particular this distance is  $4r$ . Using Pythagoras theorem we have:  $c^2 + c^2 = (4r)^2$ . Therefore,  $c = \sqrt{8}r$ .



#### Sample Problem 5

For the following unit cell, calculate the relationship between the cell parameter and the atomic radius.

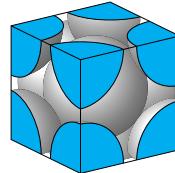


#### SOLUTION

For this unit cell, the atoms in the bottom part are touching. Hence, the cell parameter should be related to the atomic radius. In particular, two half atoms occupy the same distance as the cell parameter, so  $c = r$ .

#### ◆ STUDY CHECK

For the following unit cell, calculate the relationship between the cell parameter and the atomic radius.





*Metal density* Different metals have different density. The value for density will depend on the cell parameter but also on the compacity of the unit cell, the more compact the unit cell the more atoms per cell and hence the more density. The formula that relates density with cell parameter and atoms per cell is:

$$d = \frac{N \cdot AW}{c^3 \cdot 6.023 \times 10^{-7}}$$

Metallic density formula

where:

$d$  is the density in  $g \cdot ml^{-1}$

$N$  is the number of atoms per unit cell

$6.023 \times 10^{-7}$  is related to the conversion between atoms and grams

$AW$  is the atomic weight of the metal

$c$  is the cell parameter in pm

#### Sample Problem 6

Calculate density of iron ( $AW = 55.845 g \cdot mol^{-1}$ ) knowing this is a bcc metal with cell parameter is 286pm.

#### SOLUTION

We know that iron is a bcc metal and hence it has two atoms per unit cell. Also we know its atomic weight  $AW = 55.845 g \cdot mol^{-1}$  and the cell parameter  $c = 286\text{pm}$ . Using the metallic density formula:

$$d = \frac{2 \cdot 55.845}{286^3 \cdot 6.023 \times 10^{-7}} = \frac{111.69}{14.09} = 7.93 g \cdot ml^{-1}$$

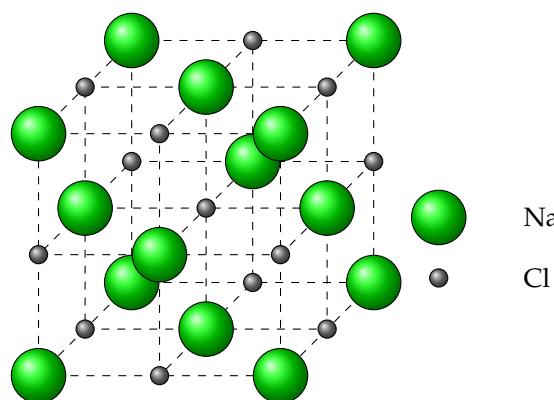
#### ◆ STUDY CHECK

Calculate density of gold ( $AW=196.96 g \cdot mol^{-1}$ ) knowing this is a fcc metal with cell parameter is 406pm.

*Ionic solids* Ionic solids have high melting point and they are typically hard. They also do not conduct the electricity in solid form. An example of an ionic solid is NaCl. The structure of NaCl and many other ionic solids results from the superposition of two different compact lattices—this is the reason these are called binary solids as they are made of two units—and each lattice is superimposed. Normally, the largest ion ( $\text{Na}^+$ ) forms a packed arrangement such as fcc or ccp, and the smallest ion ( $\text{Cl}^-$ ) resides on the holes of the lattice. Here we will care about constructing the formula of the unit cell, such as NaCl by counting the atoms in the unit cell.

#### Sample Problem 7

Calculate the formula for the following unit cell



### SOLUTION

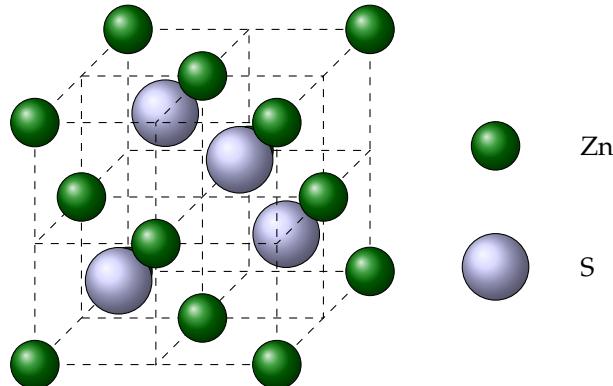
The unit cell contains  $\text{Cl}^-$  and  $\text{Na}^+$ . Remember every location in the unit cell has different sharing factor. We will compute the number of atoms in each location and multiply by the sharing factor to calculate the number of Cl and Na in the cell:

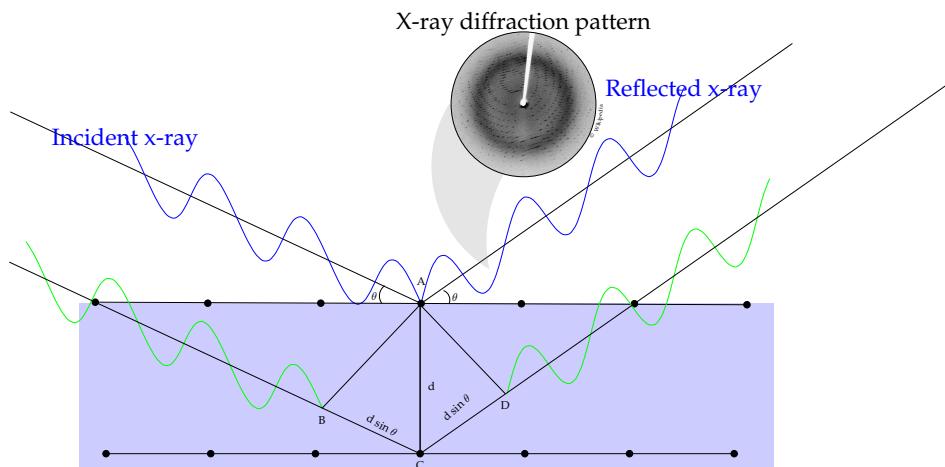
Location	Sharing Factor, $f$	# atoms, $N$	$f \times N$
Corner	$1/8$	$8\text{Na}^+$	1
Faces	$1/2$	$6\text{Na}^+$	3
sides	$1/4$	$12\text{Cl}^-$	3
Inside	1	$1\text{Cl}^-$	1

Overall, we have  $\text{Na}_4\text{Cl}_4$  which corresponds with the formula  $\text{NaCl}$ .

### ◆ STUDY CHECK

Calculate the formula for the following unit cell:





**Figure 1.6** Reflection of x-rays in two different lattice points separated by a distance. The incident waves are in phase—maximums and minimums overlap—but the reflected waves are only in phase when the difference of distances traveled by both is an integral number of wavelengths. In the image  $BC + CD = 2dsin\theta$ .

#### X-ray diffraction: a method to measure cell parameters

X-ray diffraction is an experimental technique used to study the structure of solids and specifically to obtain cell parameters—the length of the unit cell that defines the structure of a crystal. X-rays, high-frequency radiation, scatter when they encounter a regular array of atoms in which the spacing is compatible with the x-ray wavelength. Diffraction results in two different types of wave interference: constructive and destructive. Constructive interference results in bright spots and destructive interference results in dark spots. Waves impacting atoms at a different lattice positions travel different distances. If the difference in distance equals to an integral number of wavelength there both rays will interfere constructively. Bragg's equation relate the cell parameter ( $d$ ) of a solid with the angle ( $\theta$ ) of the diffracted x-rays and its wavelength ( $\lambda$ ). The number  $n$  is called the diffraction order and represents an integer values ( $n=0, 1, 2, \dots$ ).

$$n\lambda = 2dsin\theta \quad (1.1)$$

#### Sample Problem 8

We study the structure of a crystal using x-rays of 9nm, finding a first-order reflection at  $20^\circ$ . Calculate the distance between the planes responsible for this reflection.

#### SOLUTION

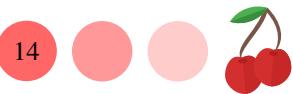
We should use Bragg's equation, using  $\theta=20^\circ$ ,  $\lambda=9\text{nm}$  and  $n=1$ . Solving for  $d$  we have:

$$1 \cdot 9 = 2dsin(20)$$

The calculated plane spacing is 26.3nm.

#### ◆ STUDY CHECK

Two lattice planes separated by a distance of 4nm produce a first-order x-ray diffraction at  $15^\circ$  using radiation of wavelength of 3.2nm. Calculate the angle for the second-order diffraction.



▼A paper clip standing on water



© wikipedia

▼Water droplets



© www.picklist.com

▼Meniscus of water and mercury



© Flickr

▼A viscous liquid



© Flickr

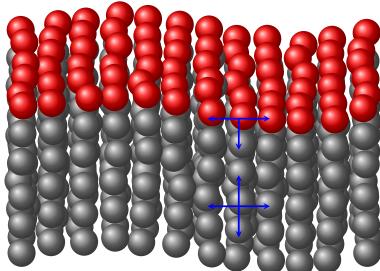
▼Capillary for tubes of different diameters



© wikipedia

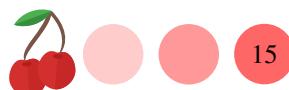
## 1.4 Liquid state

This section will cover some of the properties of the liquid state. In particular the importance of the vapor pressure, the viscosity and the surface tension. All these properties are determined by the intermolecular forces that connect the molecules of a liquid.



**Figure 1.7** A representation of surface (red spheres) and bulk (blue spheres) liquid molecules as well as two types of meniscus: a concave and a convex meniscus, typical of water and mercury respectively. Surface molecules are pulled inwards creating the surface tension whereas bulk molecules are not.

**Surface tension** In a liquid there are two types of molecules, based on their location. Some molecules are located in the interior part of the liquid, far away from its surface. We call this the bulk of the liquid. Others are located at the surface of the liquid. The molecules at the bulk are surrounded by other molecules in all directions, being pushed and pulled in all directions by intermolecular forces. For these molecules, overall there is no net pull in any direction. Differently, surface molecules because of their location are surrounded by fewer molecules located on the bottom part of the surface. As such, they are pushed and pulled down and to the side by the surrounding molecules, but not upwards. As a result of this imbalance, surface molecules experience elastic forces that cause the surface of the liquid to tighten up so that the surface minimizes its surface area. The surface tension of a liquid ( $\gamma_t$ ) is a measure of these elastic forces in the surface of the liquid. It is defined as the amount of energy needed to modify the surface of a liquid by the unit of area, with units of milli Newton per meter, mN/m. Surface tension values depend on the temperature and the phases in contact. For example, let us consider three different phases: water (a liquid), air (a gas), and mercury (a liquid). The surface tension of water in the water-air interface is different than the value for the water-mercury interface as the chemicals in contact with water are different. The stronger the intermolecular forces connecting the molecules of a given phase, the higher the surface energy—it would take more energy to modify, expand or contract, the surface of the liquid. For example, the surface tension of the H<sub>2</sub>O-air interface (73mN/m) is stronger than the one for the C<sub>6</sub>H<sub>6</sub>-air interface (29mN/m), as water molecules interact by means of strong hydrogen bonds whereas the only intermolecular forces existing among the C<sub>6</sub>H<sub>6</sub> are weak dispersion forces. The surface tension is responsible for phenomena such as capillary, the beading of water on the plant's leaves—water form beads or drops on the top of leaves—or the formation of the meniscus, a curved surface of a liquid in a narrow tube. In particular, capillary results from the competitive effect of cohesive and adhesive forces. In the case of mercury, the cohesive forces are stronger than the adhesive. Hence, the meniscus created is convex. In the case of water, the adhesive forces are stronger, and therefore this liquid forms a concave meniscus.

**Table 1.4 Surface tension ( $\gamma_t$ ) values for several interfaces at different temperatures.**

Interface	$\gamma_t$ (mN/m)	T	Interface	$\gamma_t$ (mN/m)	T
H <sub>2</sub> O-Air	73	20°C	H <sub>2</sub> O-Hg	415	20°C
CH <sub>3</sub> I-Air	67	20°C	H <sub>2</sub> O-Air	73	22°C
C <sub>6</sub> H <sub>6</sub> -Air	30	20°C	H <sub>2</sub> O-Air	72	25°C
CH <sub>3</sub> OH-Air	22	20°C	Hg-Air	486	20°C

**Viscosity** Viscosity ( $\eta$ ) is the measure of a fluid's resistance to flow. High viscosity liquids flow slowly and this effect results from the intermolecular forces. Liquids with strong intermolecular forces tends to present high viscosities. Viscosity, as well as surface tension, depends on temperature and high temperature reduce the viscosity. Molecular complexity also affect viscosity and long molecules made of carbon and hydrogen have higher viscosities than small molecules due to the fact that because of their size they present more intermolecular interactions. The units of viscosity are milli Pascal-second, mPa·s.

**Table 1.5 Viscosities ( $\eta$ ) for several substances at different temperatures.**

Substance	$\eta$ (mPa·s)	T	Substance	$\eta$ (mPa·s)	T
Benzene	0.604	25°C	Honey	5000-20000	20°C
Water	1.0016	20°C	Pitch	$2.3 \times 10^{11}$	10-30°C
Mercury	1.526	25°C			
Whole milk	2.12	20°C			
Olive oil	56.2	26°C			

**Vapor pressure of a liquid** The molecules of a liquid in contact with the atmosphere are more likely to escape into the gas phase forming what we call the vapor pressure of the liquid. When we put a liquid in a closed container, some of the liquid molecules would go into the gas. This process is called vaporization. Whereas molecules of the gas would also go back to the liquid phase. This process is called condensation. Therefore, vaporization and condensation compete until both processes occur at the same speed and the system reaches what we call as equilibrium. The vapor pressure at this state is called the equilibrium vapor pressure or simply the vapor pressure of the liquid. This effect is responsible for the humidity the air and the smell of liquid chemicals. Chemicals with high vapor pressure vaporize readily and if they have a smell, one would be able to smell them. Solids also have vapor pressure—solids also have a smell—as their molecules are also able to escape into a gas phase.

▼ Rubbing alcohol has low heat of vaporization



© wikipedia

▼ Acetone has low heat of vaporization



© Flickr

▼ Perfumes have low vaporization heat



© Wikipedia

▼ Metals have high vaporization heat



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**Table 1.6 Vapor pressure (P<sup>vap</sup>) for several substances at different temperatures.**

Substance	P <sup>vap</sup> (mmHg)	T	Substance	P <sup>vap</sup> (mmHg)	T
Tungsten	0.75	3203°C	Carbon dioxide	42753	20°C
Ethylene glycol	3.75	20°C	Nitrous oxide	42453	25°C
Water	17.5	20°C	Carbonyl sulfide	9412	25°C
Propanol	18.0	20°C	Propane	7584	27°C
Ethanol	43.7	20°C	Formaldehyde	3268	20°C
Acetaldehyde	740	20°C	Butane	1650	20°C



**Enthalpy of vaporization** The enthalpy of vaporization of a liquid ( $\Delta H_{vap}$ ) is the energy needed to vaporize a liquid. This energy is often called heat of vaporization or molar heat of vaporization. Mind that  $\Delta H_{vap}$  values are normally positive. This corresponds to the fact that we have to give energy to the liquid in order to create a vapor, and hence the process is endothermic. In general compounds with small heat of vaporization can vaporize easily. Think about the smell of a perfume you like. Now, think about the smell of water. Why a perfume smells and water does not. The enthalpy of vaporization of a perfume is small whereas  $\Delta H_{vap}$  for water is larger (41kJ/mol). This means it is easier for the perfume molecules to escape into the gas phase and hence produce a smell. Another example is acetone–nail polish remover. This chemical has a very distinctive smell.  $\Delta H_{vap}$  for acetone is 31kJ/mol. If you compare this value with the value of water you can see acetone is more likely to have a smell.

**Table 1.7 Enthalpy of vaporization ( $\Delta H_{vap}$ ) for several substances and boiling points.**

Substance	T	$\Delta H_{vap}$ (J/mol)	Substance	T	$\Delta H_{vap}$ (J/mol)
Acetone	56°C	31300	Water	100°C	40660
Aluminium	2519°C	294000	Phosphine	-88°C	14600
Ammonia	-33°C	23350	Propane	-42°C	15700
Butane	-1°C	21000	Methanol	64.7°C	35200
Ethanol	78 °C	38600	Isopropyl alcohol	83°C	44000
Hydrogen	-253°C	899.2	Iron	2862°C	340000

### Sample Problem 9

Order the following compounds from high to low vapor pressure: C<sub>6</sub>H<sub>6</sub> ( $\Delta H_{vap}=31\text{kJ/mol}$ ), C<sub>6</sub>H<sub>5</sub>OH ( $\Delta H_{vap}=39\text{kJ/mol}$ ), H<sub>2</sub>O ( $\Delta H_{vap}=41\text{kJ/mol}$ )

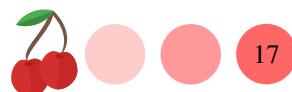
#### SOLUTION

The larger  $\Delta H_{vap}$  the harder it is to vaporize a liquid and hence the lower the vapor pressure of the liquid. If we compare the liquids in this example, water has the lowest vapor pressure, whereas cyclohexane (C<sub>6</sub>H<sub>6</sub>) has the highest vapor pressure.

#### ❖ STUDY CHECK

Order the following compounds from high to low vapor pressure ( $P^{vap}$ ): NH<sub>3</sub> ( $\Delta H_{vap}=23\text{kJ/mol}$ ), CH<sub>4</sub> ( $\Delta H_{vap}=8\text{kJ/mol}$ ), C<sub>4</sub>H<sub>10</sub> ( $\Delta H_{vap}=15\text{kJ/mol}$ )

**Vapor pressure change with temperature** This vapor pressure strongly depends on temperature. That is the reason why summer days can also be humid days if you live near the seaside. In particular, this change depends on the value of the heat of vaporization. The reason for this, is because at higher temperature more molecules have enough kinetic energy to escape from the liquid into the gas phase. For chemicals with low heat of vaporization we can expect a more sharp change of the vapor pressure with temperature. The following formula gives the relation between vapor pressure and temperature. Mind that for every temperature we will have a



vapor pressure value. In the formula you will need two pairs of temperatures and hence two pairs of vapor pressures:

$$\ln\left(\frac{P_{T_1}^{vap}}{P_{T_2}^{vap}}\right) = \frac{\Delta H_{vap}}{R}\left(\frac{1}{T_2} - \frac{1}{T_1}\right)$$

Clausius-Clapeyron relation

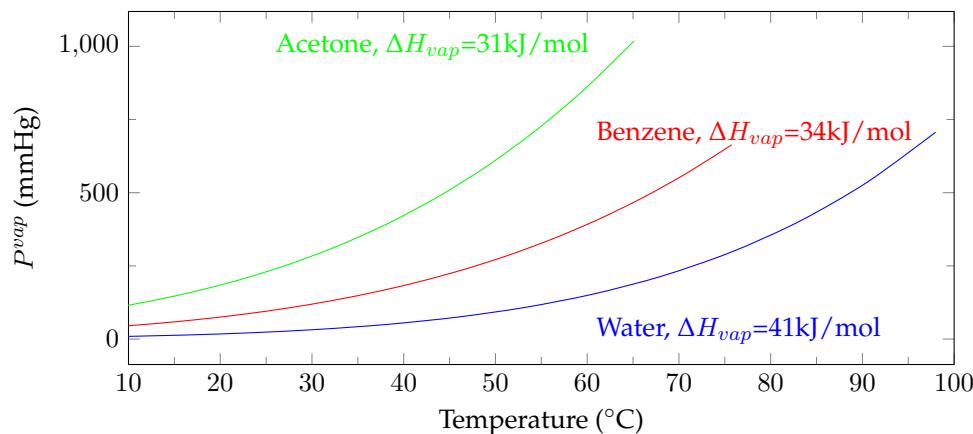
where:

$P_{T_1}^{vap}$  is the vapor pressure at temperature  $T_1$  in Kelvin

$P_{T_2}^{vap}$  is the vapor pressure at temperature  $T_2$  in Kelvin

$\Delta H_{vap}$  is the enthalpy of vaporization in  $J \cdot mol^{-1}$

$R=8.314 J \cdot K^{-1} mol^{-1}$  is the constant of the gases in energy units



**Figure 1.8** Vapor pressure change with temperature for three chemicals with different heat of vaporization.

#### Sample Problem 10

The vapor pressure of water at 298K is 0.03 atm. Calculate the vapor pressure of water at 323K given  $\Delta H_{vap} = 43.9 KJ \cdot mol^{-1}$ .

#### SOLUTION

In order to use the Clausius-Clapeyron relation we need two pairs of ( $T$ ,  $P^{vap}$ ) values. In this problem, we have the value of the vapor pressure at 298K, hence we have (298K, 0.03 atm) and they ask the pressure at 323K. Therefore the second pair is (298K, x atm), where X is the vapor pressure at 298—what they are asking in the problem. We can call (298K, 0.03 atm) as  $(T_1, P_{T_1}^{vap})$  and (298K, X atm) as  $(T_2, P_{T_2}^{vap})$ . At this point we have  $T_1 = 298K$  and  $P_{T_1}^{vap} = 0.03 \text{ atm}$  and  $T_2 = 323K$  and  $P_{T_2}^{vap} = x$ . We also have the enthalpy of vaporization. Note that this value has to be given in  $J \cdot mol^{-1}$  and hence, we will use  $\Delta H_{vap} = 43.9 \times 10^3 J \cdot mol^{-1}$ . Now we can plug these values into the formula:

$$\ln\left(\frac{0.03}{x}\right) = \frac{43.9 \times 10^3}{8.314} \left(\frac{1}{323} - \frac{1}{298}\right)$$



Let us solve this step by step. First we solve the part on the right:

$$\ln\left(\frac{0.03}{x}\right) = -1.37$$

Now, in order to eliminate the logarithm we should use the exponential function in both sides:

$$\frac{0.03}{x} = e^{-1.37}$$

Calculating the exponential of -1.37 we have:

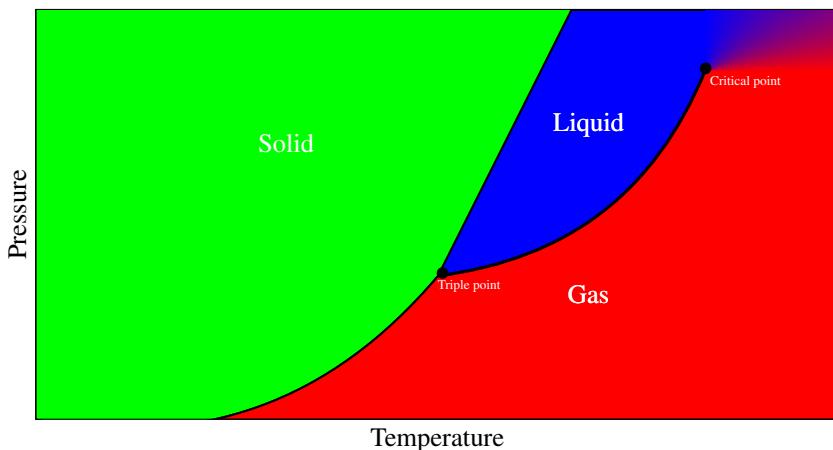
$$\frac{0.03}{x} = 0.25$$

That leads to a  $x$  value of 0.12 atm.

#### ❖ STUDY CHECK

Using the data below, calculate  $\Delta H_{vap}$  for  $\text{HNO}_3$ .

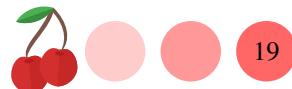
T (K)	$P^{vap}$ (mmHg)
10	26.6
20	47.9
30	81.3



**Figure 1.9** A typical phase diagram showing the different phases, the critical and the triple point. As the slope of the line that separates liquid and gas has an angle lower than  $90^\circ$  the solid phase has higher density than the liquid.

## 1.5 Phase diagrams

Water can be found at different states: liquid, solid and gas. We know at room temperature—and atmospheric pressure—water is a liquid. However, what if we warm up a sample of water? When does it become vapor? And more importantly, what if the working pressure is not one atmosphere? Would water boil the same near the sea or on top of a mountain? The answer to all these questions can be found in the phase diagram of water. This section



will cover phase diagrams. You will learn how to read phase diagrams in order to predict the state of matter at any temperature and pressure conditions. You will also learn how to identify critical and triple points.

*Description of a phase diagram: important points* A phase diagram is a representation of the different temperature and pressure conditions in which we can find the different states of matter of a substance. Normally, temperature is listed in the horizontal axis and pressure in the vertical axis. The different phase, liquid, solid and gas, are listed. At low temperature we tend to find solids and gases are common at high temperature. Similarly, at low pressures we tend to find gases and solids at high pressure. With pressure we refer to compressive pressure. The lines in a phase diagram represent equilibrium and the line separating solid and gas represents all the pressure and temperature conditions in which we can find a gas in equilibrium with a liquid. Similarly, the line separating liquid and solid represents all the pressure and temperature conditions in which we can find a liquid in equilibrium with a solid. With equilibrium, we mean that both phase are present and the process of phase transition proceeds at the same speed in both directions. There are two important points in a phase diagram: the critical point and the triple point. The triple point is the pressure and temperature conditions in which the three phases—solid, liquid and gas—coexist. Another important point is the critical point. Beyond this point one cannot liquefy (go from gas into a liquid) or condense (go from liquid into a gas) the substance. There is one more important feature one can extract from a phase diagram. Normally, but not always, solids are more dense than liquids. We can compare the density of the solid and the liquid by analyzing the slope of the line connecting both phase. If the slope is lower than  $90^\circ$  then the solid will be more dense than the liquid. If it is larger than  $90^\circ$  then the solid is less dense than the liquid. If the slope is  $90^\circ$  then both liquid and solid have the same density.

*What are normal conditions?* When we speak about normal conditions we refer to a pressure of 1atm, which is the common atmospheric pressure. But remember that the atmospheric pressure depends on the height of the location where measured. And locations near the sea—at low height—tend to have higher pressure than locations near the mountains—at a larger height.

*Phase transition terminology* Each phase transition has a specific name. You may be familiar with some of the terms like freezing that involves the change from liquid to solid. Other names are listed below:

Liquid  $\longrightarrow$  Solid

Freezing

Liquid  $\longrightarrow$  Gas

Evaporation or vaporization

Solid  $\longrightarrow$  Liquid

Melting

Gas  $\longrightarrow$  Liquid

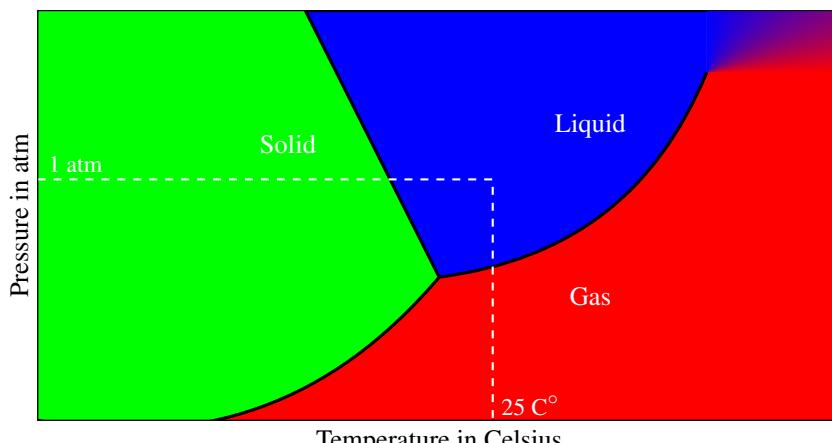
Condensation

Solid  $\longrightarrow$  Gas

Sublimation

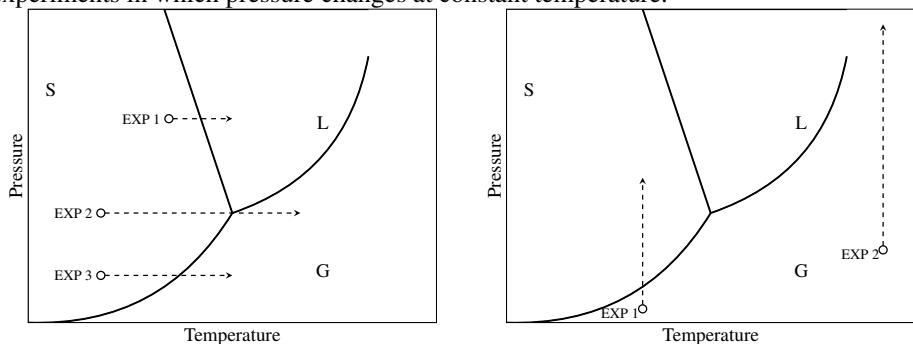
Gas or Solid  $\longrightarrow$  Liquid

Liquefy



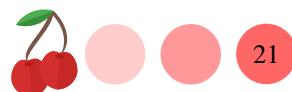
**Figure 1.10** The phase diagram of water with pressure in the Y axis and temperature in the X axis. This diagram displays the different states of matter of water for different pressure and temperature conditions. The coordinates of the triple point are ( $0.0098\text{ C}^\circ, 0.0060\text{ atm}$ ). This means that at this low pressure and temperature conditions we have three phases in contact: water, ice and steam. The coordinates of the critical point are ( $374\text{ C}^\circ, 218\text{ atm}$ ). This means that for temperature beyond  $374\text{ C}^\circ$  it is not possible to liquefy steam.

*Phase diagram of water* A phase diagram is just a diagram with temperature in the X axis and pressure in the Y axis. It tells you whether you have gas, liquid or gas at a large range of pressure and temperature conditions. For example, the figure on the side of the page presents the phase diagram of water and the line indicates the phase present at (Temperature, Pressure) conditions of ( $25\text{ C}^\circ, 1\text{ atm}$ ). Obviously, this phase is liquid water. *Normal conditions* refer to pressure conditions of 1 atm. Hence, we say that the normal boiling point of water—this means at 1 atm—is  $100\text{ C}^\circ$ . In the following we will analyze a set of experiments represented as vertical and horizontal lines in the diagram. Horizontal lines are cooling/heating experiments in which pressure is kept fixed and temperature changes. Vertical lines represent compression/decompression experiments in which pressure changes at constant temperature.



**Figure 1.11** Heating experiments (left) and compression experiments (right).

*Heating and compression experiments* We will analyze now some cooling/heating experiments. In the first experiment, we start by having a solid that we heat up to obtain first a mixture between liquid and solid and then a pure liquid. In this experiment we just transitioned between solid into a liquid. Experiment 2 is different. We also start by having a solid. The difference is that this time we reach a point called *triple point* in this point the three phase coexist at a single pressure and temperature. Therefore, in this experiment, we go from a solid into a mixture of solid, liquid and gas.



After that we transition directly into a gas. Experiment number three is called sublimation. In this experiment we start by having a solid that transitions into a gas by means of a mixture of solid and gas. We can also discuss some compression/decompression experiments. The first experiment is a compression experiment in which we start from a gas and we end up having a liquid by means of a mixture of both. The second experiment starts beyond the *critical point* and hence even if you compress the gas you will never reach a liquid state. The critical point is the point beyond which one cannot liquefy a gas or gasify a liquid.

*Energy calculations involving phase transitions* The enthalpy of vaporization of a substance gives you the amount of energy needed to vaporize an amount of substance. Similarly, the enthalpy of fusion tells you about the energy involved in the fusion process. Each phase—gas, liquid and vapor—has different specific heat. Using water as an example, imagine we need to calculate the energy involved in the heating of  $m=18\text{ grams}$  ( $n=1\text{ mole}$ ) of water from  $20^\circ\text{C}$  to a  $150^\circ\text{C}$ . This energy results from three contributions: the energy needed to warm up liquid from  $20^\circ\text{C}$  to a  $100^\circ\text{C}$  (we can call this  $\Delta T_1$ ), the energy to boil 1 mole of water, and the energy to warm up 1 mole of gas water from  $100^\circ\text{C}$  to a  $150^\circ\text{C}$  (we can call this  $\Delta T_2$ ). The final calculation will be:

$$Q = m \cdot c_e^{\text{H}_2\text{O}(\ell)} \cdot \Delta T_1 + n \cdot \Delta H_{\text{vap}}^{\text{H}_2\text{O}} + m \cdot c_e^{\text{H}_2\text{O(g)}} \cdot \Delta T_2$$

**Table 1.8 Properties of the different states of matter of water.**

Property	Ice	Water	Steam
Density (g/mL)	0.93	1	0.6
$c_e$ ( $\text{J}\cdot\text{g}^{-1}\cdot{}^\circ\text{C}^{-1}$ )	2.18	4.184	1.99
$\Delta H_{\text{fusion}}$ (kJ/mol)	6.01		
$\Delta H_{\text{vap}}$ (kJ/mol)	44		

**Funny facts!**

Water is weird. Everyone knows the chemical symbol for water is  $H_2O$ , and that all living things need water to survive. Here are eight facts about weird water that you might not know!



1. Water is alien. All water on earth arrived as ice on asteroids and comets from space.
2. All water on earth has been recycled through animals, plants, rocks, oceans, and clouds. In other words, you're drinking dinosaur pee.
3. Water doesn't follow the normal rules of chemistry. Water is made of two elements: oxygen and hydrogen, both of which are very light. The rules of chemistry say that on earth, liquid water should not exist. Instead, if water followed the rules, it would exist on earth only as water vapor.
4. Water is the only chemical that expands when it goes from a liquid to a solid. Because solid water, aka ice, is less dense than liquid water, ice floats. This allows ice to insulate the liquid water underneath it. Without this unique property, life would not have survived earth's many ice ages.
5. Hot water freezes faster than cold water, and no one knows why. This is known as the Mpemba effect, named after the Tanzanian student who discovered this phenomenon.
6. Water molecules are so good at sticking to each other that they can overcome the force of gravity. In biology, this is called capillary action and is the mechanism that allows plants to move water from their roots to their leaves. This unique property of water also allows oxygen and nutrients to reach the outermost edges of your brain.
7. Water is the second most common molecule in the universe, after molecular hydrogen. There's water on Mars, the moon, and almost every other object in our solar system, including Pluto.
8. Water is a universal solvent. Water is able to break most chemical bonds and dissolve most chemicals. It is very difficult to create pure water even in a laboratory setting, as nearly all chemical compounds will dissolve in water. This makes water one of the most reactive compounds known to man.