

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/318038620>

Fuel consumption model for heavy duty diesel trucks: Model development and testing

Article in *Transportation Research Part D Transport and Environment* · August 2017

DOI: 10.1016/j.trd.2017.06.011

CITATIONS

13

READS

6,507

2 authors:



Jinghui Wang

Flow Artificial Intelligence Inc.

14 PUBLICATIONS 83 CITATIONS

SEE PROFILE



Hesham Rakha

Virginia Polytechnic Institute and State University

404 PUBLICATIONS 6,847 CITATIONS

SEE PROFILE

Some of the authors of this publication are also working on these related projects:



INTEGRATION Software Development [View project](#)



Energy and Environmental Research [View project](#)

Fuel Consumption Model for Heavy Duty Diesel Trucks: Model Development and Testing

Jinghui Wang^a, Hesham A. Rakha^{b,*}

^a*Center for Sustainable Mobility, Virginia Tech Transportation Institute, 3500 Transportation Research Drive, Blacksburg, VA 24061, USA*

^b*Center for Sustainable Mobility, Virginia Tech Transportation Institute, 3500 Transportation Research Drive, Blacksburg, VA 24061, USA*

Abstract

A simple, efficient, and realistic fuel consumption model is essential to support the development of effective eco-freight strategies, including eco-routing and eco-driving systems. The majority of the existing heavy duty truck (HDT) fuel consumption models, however, would recommend that drivers accelerate at full throttle or brake at full braking to minimize their fuel consumption levels, which is obviously not realistic. To overcome this shortcoming, the paper applies the Virginia Tech Comprehensive Power-based Fuel consumption Model (VT-CPFM) framework to develop a new model that is calibrated and validated using field data collected using a mobile emissions research laboratory (MERL). The results demonstrate that the model accurately predicts fuel consumption levels consistent with field observations and outperforms the comprehensive modal emissions model (CMEM) and the motor vehicle emissions simulator (MOVES) model. Using the model it is demonstrated that the optimum fuel economy cruise speed ranges between 32 to 52 *km/h* with steeper roads and heavier trucks resulting in lower optimum cruise speeds. The results also demonstrate that the model generates accurate CO₂ emission estimates that are consistent with field measurements. Finally, the model can be easily calibrated using data collected using non-engine instrumentation (e.g. Global Positioning System) and readily implemented in traffic simulation software, smartphone applications and eco-freight programs.

Keywords: Heavy Duty Diesel Truck, Fuel Consumption Model, Eco-Routing, Eco-Driving, Optimum Cruise Speed

*Corresponding Author.

Email address: hrakha@vt.edu (Hesham A. Rakha)

1. Introduction

Transportation activities account for 28% of the total U.S. energy use and 33.4% of carbon dioxide (CO₂, the major component of greenhouse gas (GHG) emissions) production (Davis et al. (2015); EPA (2015)). Consequently, numerous efforts are being tested in an attempt to reduce transportation-related energy use and GHG emissions in response to global energy and environmental issues (e.g. global warming). As the largest emitter of CO₂ (42.7%) in the transportation sector, passenger cars have attracted significant attention in the past decade, and reduction in fuel consumption and emission levels have been achieved through the development of relevant regulations and technical solutions. As a counterpart, however, the investigation of heavy duty diesel truck (HDDT) fuel consumption behavior is relatively less mature compared to that of gasoline passenger cars. Although HDDTs make up only a fraction of the total vehicle population, they are major contributors to GHG emissions, accounting for 22.8% of the total CO₂ production in the transportation sector (EPA (2015)).

Currently, HDDTs are receiving increasing attention from legislators, the government and society at large. For example, in September 2011, the National Highway Traffic Safety Administration (NHTSA) and the U.S. Environmental Protection Agency (EPA) jointly promulgated the first-ever federal regulations mandating improvements in fuel economy of heavy-duty commercial vehicles (Harrington and Krupnick (2012); U.S. EPA and NHTSA (2011)). Furthermore, researchers have been committed to developing road eco-freight strategies (Pindilli (2012); Lattemann et al. (2004); Dzenisiuk (2012); Takada et al. (2007)) in order to support “green transportation” policy making.

An accurate and efficient fuel consumption model is needed to provide robust fuel estimates in support of quantifying potential reductions in fuel consumption and emission levels induced by implementing eco-friendly strategies, such as developing eco-routing (Rakha et al. (2012); Boriboonsomsin et al. (2012); Ahn and Rakha (2013)) or eco-driving systems (Schall and Mohnen (2015); Saboohi and Farzaneh (2009); Soylu (2014); Barkenbus (2010); Ahn et al. (2011)) and utilizing advanced fuel techniques (Wayne et al. (2004); Guo et al. (2015); Onat et al. (2015)) or alternative fuels (Rakopoulos et al. (2015); Balat and Balat (2009); Demirbas (2007); López et al. (2009)). Among the existing modeling efforts, most are operated at a macroscopic or microscopic level. The macroscopic models, such as MOBILE 6.2 (Arbor (2003)), were demonstrated to produce unreliable estimates due to their inability of capturing transient vehicle activities (Ahn and Rakha (2008)). Consequently, they are incapable of being utilized for the energy and environmental assessment of traffic operational projects. Microscopic models were introduced in order to better capture the variability in fuel consumption and GHG emissions associated with vehicle dynamics. A wide range of instantaneous models have been developed using in-laboratory or field data, and some of them are applicable to modeling HDDTs, such as

MOVES, VT-Micro (Rakha et al. (2004)), the Passenger Car and Heavy Duty Emission Model (PHEM) (Hausberger et al. (2010)), VERSIT (Smit et al. (2007)), and the Comprehensive Modal Emissions Model (CMEM) (Barth et al. (2000, 2004)).

The majority of the aforementioned models, however, have intrinsic limitations. For example, MOVES, which was developed as an inventory model based on a wide range of data sources, is capable of providing robust estimates. Nonetheless, it requires massive user inputs for each run, which significantly increases the time required to run multiple scenarios and large networks. CMEM generally underestimates fuel consumption levels for acceleration maneuvers; more importantly, it characterizes fuel consumption as a linear function of vehicle power (positive power section), which produces a bang-bang type of control system. A bang-bang control may arise when the partial derivative of the response with respect to the control variable is not a function of the control variable (a more detailed description of a bang-bang control system is provided in section 2). The fuel estimate module for CMEM is addressed in Eq.(1):

$$FR = \frac{K \cdot N \cdot V + P/\eta}{43.2} \cdot [1 + b_1 \cdot (N - N_0)^2] \quad (1)$$

Here FR is the fuel rate in g/s, K is the engine friction factor, N is engine speed in (revolutions per second), V is engine displacement in liters, η is the efficiency for diesel engines, b_1 equals to 1×10^{-4} , N_0 is a constant related to engine displacement, $43.2KJ/g$ is the lower heating value of a typical diesel fuel, and P is the vehicle power which is the control variable of the fuel model. Since the fuel rate is linearly related to the vehicle power, its partial derivative with respect to power is independent of the power. This may suggest that drivers accelerate at full throttle to reduce acceleration time in order to minimize their trip fuel consumption levels. Similarly, PHEM and VERSIT produce a bang-bang control as well. VT-Micro is capable of circumventing the bang-bang control; however, it requires a large amount of in-laboratory or field data to be calibrated, which is cost-prohibitive and time-consuming.

Overall, the existing models either produce a bang-bang type of control (either full throttle or zero throttle input) system or cannot be easily calibrated or efficiently used. Consequently, a simple, accurate and efficient model is needed. Rakha et al. (2011) developed the Virginia Tech Comprehensive Power-based Fuel consumption Modeling (VT-CPFM) framework by characterizing fuel consumption levels as a second-order polynomial function of vehicle power to circumvent the bang-bang control problem. Furthermore, the model offers a unique ability to be calibrated using publicly available data (a more detailed description of the calibration procedure is provided in Rakha et al. (2011) without data collection. Recent efforts have validated the applicability of the model for light duty vehicles (LDVs) (Park et al. (2013)) and transit buses (Wang and Rakha (2016a,b))

under real-world driving conditions; however, it has not been expanded to HDDTs yet. Consequently, the paper is intended to develop the VT-CPFM-based model for HDDTs in order to circumvent the bang-bang problem in the family of heavy duty truck (HDT) fuel consumption modeling tools. The developed model will be applied to develop eco-routing and eco-driving systems in future studies.

2. A Bang-bang Control System

Minimizing fuel consumption levels, from the system perspective, is essentially an optimal control problem that attempts to compute the optimal solution with the control variable restricted to being between a lower and an upper bound. In optimal control problems, a bang-bang solution may occur when a control switches abruptly from one extreme to the other. To mathematically give a complete picture of the bang-bang control, the minimum-fuel problem is described in Eq.(2), which is derived from Pontryagin's Maximum Principle (Pontryagin (1987); Saelens et al. (2010)):

$$\min_{P(\cdot), t_e} \int_0^{t_e} \dot{m}_f(P(t)) dt \quad (2a)$$

$$\text{subject to : } P_{min}(t) \leq P(t) \leq P_{max}(t) \quad (2b)$$

where \dot{m}_f is the fuel mass flow rate [kg/s], P is the vehicle power [kW], P_{min} and P_{max} are the minimum and maximum of vehicle power, respectively [kW].

Vehicle power (P) is the control variable of the problem. The optimal solution is the control that minimizes the objective function. The optimal power is achieved when the total trip fuel consumption ($\int_0^{t_e} \dot{m}_f(P(t)) dt$) is at its minimum. If \dot{m}_f is independent of P , the objective function would be a linear function of vehicle power and produces a bang-bang control, implying that a driver would have to accelerate at “full throttle (P_{max})” to reduce the time spent accelerating in order to minimize the trip fuel consumption, which is not correct. Consequently, a higher-order model is needed to circumvent this bang-bang type of control.

3. Model Structure

The proposed HDDT fuel consumption model is developed using a framework that is very similar to that of other models within the VT-CPFM program. As a power-based model, the VT-CPFM framework uses a bottom-up approach. Namely, the model parameters, including the resistance forces used for power estimation are first computed using a resistance force module; and thereafter the vehicle power is estimated using an engine

103 power module that characterizes the vehicle power as a function of the resistance forces.
 104 The fuel consumption is finally predicted using a fuel rate module that models the fuel
 105 consumption as a polynomial function of the vehicle power.

106 3.1. Resistance Force Module

107 The resistance force is computed considering a combination of aerodynamic, rolling,
 108 and grade resistance forces, as expressed in Eq.(3):

$$R(t) = \frac{\rho_a}{25.92} C_d C_h A_f v(t)^2 + 9.8066m \frac{C_r}{1000} (c_1 v(t) + c_2) + 9.8066mG(t) \quad (3)$$

109 Here $R(t)$ is the vehicle resistance force (N); ρ_a is the air density at sea level at a
 110 temperature of 15 °C (59 °F) (equal to 1.2256 kg/m³); C_d is the drag coefficient (unitless)
 111 which is determined by truck type, 0.78 is used for the tested trucks (no aerodynamic
 112 aids) in this study (Rakha et al. (2001)); C_h is the correction factor for altitude (unitless),
 113 calculated by $1 - 0.085H$ (H is the altitude in km); A_f is the frontal area of trucks (m²), 10.0
 114 m² is used based on the truck type; $v(t)$ is the velocity in km/h; m is the vehicle mass in
 115 kg; C_r , c_1 and c_2 are the rolling resistance parameters (unitless), which vary as a function
 116 of road surface type and conditions as well as vehicle tire type; their typical values could
 117 be obtained from Rakha et al. (2001); Fitch (1994). $G(t)$ is the instantaneous road grade
 118 which is determined by elevation profiles.

119 3.2. Vehicle Power Module

120 The power exerted at any instant t is formulated by Wong (2001) as expressed in Eq.
 121 (4):

$$P(t) = \left(\frac{R(t) + (1 + \lambda + 0.0025\xi v(t)^2)ma(t)}{3600\eta} \right) v(t) \quad (4)$$

122 where $P(t)$ is the vehicle power in kW; λ is the mass factor accounting for rotational
 123 masses, a value of 0.1 is used for heavy duty vehicles (HDVs)(Feng (2007); Edwardes and
 124 Rakha (2014)); ξ is the gear ratio and assumed to be zero in this paper due to the lack of
 125 engine gear data. $a(t)$ is the instantaneous acceleration (m/s²); η is the driveline efficiency.

126 3.3. Fuel Consumption Module

127 As illustrated in Fig. 1, HDDTs present similar fuel consumption behavior compared
 128 to transit buses (as seen in Wang and Rakha (2016a)) with the fuel consumption rate a
 129 concave function of vehicle power for the positive powers, and almost constant for the

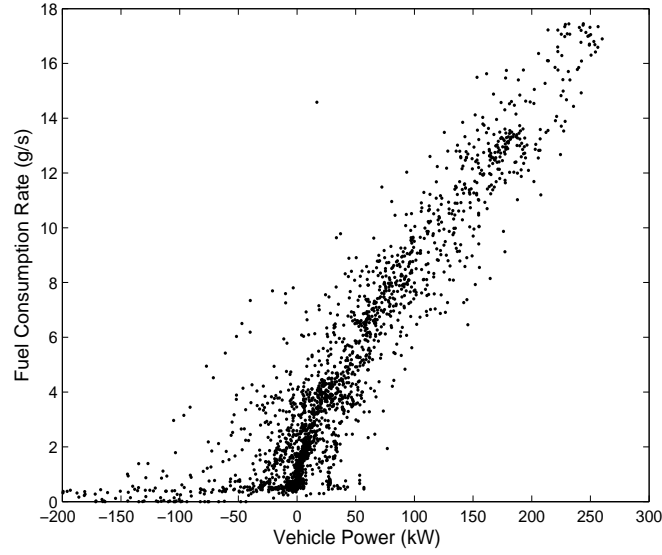


Fig. 1: Vehicle power vs. Truck fuel consumption functional form

negative conditions. Consequently, the general structure of the model is modeled as a two-regime model. Rakha et al. (2011) developed two VT-CPFM frameworks (VT-CPFM-1 and VT-CPFM-2) for LDVs each of which is a two-regime model and characterizes fuel consumption as a second-order polynomial function of vehicle power. The use of a second-order model ensures that a bang-bang control does not result from the application of the model. Furthermore, a model higher than a second-order model cannot be calibrated using standard drive cycles given the complexity of the higher order model. Consequently, a second-order model achieves a good trade-off between model accuracy and applicability. Only VT-CPFM-1 is utilized to develop the model in this study given that VT-CPFM-2 requires additional gear data which is typically not available. The VT-CPFM-1 framework is expressed in Eq.(5):

$$FC(t) = \begin{cases} \alpha_0 + \alpha_1 P(t) + \alpha_2 P(t)^2, & \forall P(t) \geq 0 \\ \alpha_0, & \forall P(t) < 0 \end{cases} \quad (5)$$

Here $FC(t)$ is the fuel consumption rate at instant t [l/s]; α_0 , α_1 and α_2 are the vehicle-specific model coefficients that remain to be calibrated.

3.4. Discussion of Model Calibration

It should be noted that the model coefficients, α_0 , α_1 , and α_2 , can be calibrated using publicly available data using Eq.(6)-(8):

$$\alpha_0 = \frac{P_{fmp}\omega_{idle}d}{22164(HV)N} \quad (6)$$

$$\alpha_2 = \frac{(F_{city} - F_{hwy} \frac{P_{city}}{P_{hwy}}) - (T_{city} - T_{hwy} \frac{P_{city}}{P_{hwy}})\alpha_0}{P_{city}^2 - P_{hwy}^2 \frac{P_{city}}{P_{hwy}}} \quad (7)$$

$$\alpha_1 = \frac{F_{hwy} - T_{hwy}\alpha_0 - P_{hwy}^2\alpha_2}{P_{hwy}} \quad (8)$$

Here P_{fmp} is the idling fuel mean pressure (400,000 Pa); d is the engine displacement (liters); HV is the fuel lower heating value (43,200,000 J/kg for conventional diesel fuel); N is the number of engine cylinders; ω_{idle} is the engine idling speed (rpm); F_{city} and F_{hwy} (liters) are the fuel consumed for the EPA city and highway drive cycles; P_{city} , P_{city}^2 , P_{hwy} , P_{hwy}^2 are the sum of the power and power squared over the EPA city- and highway-cycle respectively; T_{city} and T_{hwy} are the duration of EPA city and highway drive cycles (s). Most of the parameters typically correspond to either physical characteristics of the vehicles or fuel type, so that they are stated as specifications by the vehicle manufacturer and readily available. Nonetheless, the truck standard driving cycle and the relevant fuel economy data cannot be obtained at this time. Consequently, instead of using publicly available data, the HDDT model is calibrated using second-by-second empirical data.

4. Data Preparation

The data used for model development were collected and provided by the University of California (UC) at Riverside.

4.1. Vehicle Recruitment

The modeling effort is aimed to test the applicability of the VT-CPFM framework to modeling the HDDTs within diverse vehicle-technology categories. Consequently, the recruited trucks should differ in a wide range of vehicle-specific parameters. To this end, a total of eight trucks were randomly recruited from used vehicle fleets in Southern California within test categories by vehicle model year and engine model/displacement, and

166 a balance between horse power and manufacturers was attempted. The detailed vehicle
167 information is presented in [Table 1](#). For simplicity, the eight vehicles, from the top to the
168 bottom of [Table 1](#) are labeled as HDDT1, HDDT2, HDDT3, HDDT4, HDDT5, HDDT6,
169 HDDT7, HDDT8 in the following sections.

170 4.2. Data Set

171 Given that in-laboratory data (i.e. chassis dynamometer testing) are not always reflec-
172 tive of real-world driving conditions, on-road data were gathered instead.

173 To adequately measure real-world fuel consumption and emission levels, UC River-
174 side developed a mobile emissions research laboratory (MERL) that contains all instru-
175 mentation that is normally found in a regular vehicle emission laboratory. MERL weighs
176 approximately 45,000 lbs and could serve as a truck load, so that it is capable of capturing
177 the transient fuel consumption and emissions of a truck pulling it when the truck is being
178 tested. Further details of MERL can be found in [Barth et al. \(2004\)](#); [Cocker et al. \(2004\)](#).

179 The HDDT test was conducted by the Center for Environmental Research and Tech-
180 nology at UC Riverside on the roadways in California’s Coachella Valley involving long,
181 uninterrupted stretches of road, approximately at sea level. All trucks were tested using
182 standard fuel from the same source. The data were recorded at a frequency of 1 Hz and a
183 total of 238,893 seconds of data were gathered with a collection of 8 parameters for each
184 truck, including CO_2 , carbon monoxide (CO), hydrocarbon (HC), nitrogen oxides (NO_x),
185 velocity, fuel rate, engine speed and elevation. For more details on data collection pro-
186 cedure, the reader is encouraged to read [Barth et al. \(2004\)](#). It should be noted that the
187 primary goal of this paper is to model the fuel consumption and GHG emissions (CO_2), so
188 that modeling CO, HC and NO_x emissions is out of the scope of this research effort.

189 4.3. Data Post-processing

190 The raw fuel consumption rates were in g/s and then converted to l/s in order to use
191 the VT-CPFM framework to develop the proposed model. Simultaneously, the unit of
192 velocity was converted from mi/h to km/h for modeling purposes.

193 Through comparing the second-by-second CO_2 emissions with engine control unit
194 (ECU) data (i.e. velocity, fuel rate and engine speed), a time delay was found to exist.
195 Consequently, a time alignment was needed to synchronize the raw data. Since fuel rates
196 have a strong relationship with emissions, they were utilized to determine the value of
197 the required time shift. The proper time shift was determined through a cross-correlation
198 analysis by which the correlation coefficients between CO_2 and fuel data were estimated
199 by a correlation function for a range of lag times. The lag times with the highest correla-
200 tions were selected as the optimal events. It should be noted that the CO_2 emission data
201 collected for two of the trucks (HDDT 4 and HDDT 5) were invalid due to an error in

Table 1: Vehicle-specific information

Make/Model	Model Year	Engine Make/Model	Rated Power (hp)	Engine Size (l)	Vehicle Mass (kg)
International/ 9800 SBA	1997	Cummins/M11-330	330	10.8	7182
Freightliner/ D120	1997	DDC/C-60	360/400	12.7	7758
Freightliner/ D120	1997	Cummins/N14	370/435	14	7029
Freightliner/ C-120	1997	Cummins/N14	370/435	14	7623
Freightliner/ C-120	1998	DDC/C-60	370/430	12.7	8028
Freightliner/ FDL 120	1999	DDC/C-60	470	12.7	8118
Freightliner/ FDL 120	1999	DDC/C-60	360	12.7	8118
Freightliner/FLD 120	2001	CAT/C-15	475	14.6	7092

Table 2: Parameters required for model calibration

Parameter	Value	Source
Drag coefficient (C_d)	0.78	Rakha et al. (2001)
Altitude correction factor (C_h)	NA^a	Computed from field data
Vehicle frontal area (A_f)	$10.0\ m^2$	Computed from truck dimensions
Vehicle speed (v)	NA^a	Measured in field
Mass (m)	NA^a	Manufacturer website
Rolling coefficient (C_r)	1.25	Rakha et al. (2001)
c_1	0.0328	Rakha et al. (2001)
c_2	4.575	Rakha et al. (2001)
Road grade (G)	NA^a	Computed from field data
Acceleration (a)	NA^a	Computed from field data
Driveline efficiency (η)	0.94	Rakha et al. (2001)

^aThe parameter is not a single value.

the emission sensors of MERL during the collection process, and thus the model does not covered these vehicles.

The aligned data was smoothed by a moving average filter, and outliers were identified using a cook’s distance procedure.

5. Model Development

Each tested truck was individually modeled. [Table 2](#) gives a generalization of the model inputs along with their sources. Some of the variables are capable of being gathered in the field (e.g. vehicle speed), and some can be obtained from either the literature or manufacturer websites (e.g. drag coefficient, vehicle mass).

5.1. Model Calibration Challenges

The model was calibrated using general linear regression analysis, and model coefficients are summarized in [Table 3](#). Unlike LDVs, the second-order parameters (α_2) are negative, which demonstrates that fuel consumption varies as a concave polynomial function of vehicle power and exhibits a mild growth when vehicle power is increasing. This is similar to transit buses in [Wang and Rakha \(2016a,b\)](#) in which the concave model was demonstrated to accurately predict fuel consumption levels.

Nonetheless, the concave model may produce unrealistic driving recommendations as demonstrated by the sensitivity of estimated optimum fuel economy cruise speed to road grade and vehicle weight, as illustrated in [Fig. 2](#) and [Fig. 3](#), respectively. The road grade

Table 3: The concave model for each truck

Truck classification	α_0	α_1	α_2
HDDT 1	1.13E-03	1.11E-04	-1.71E-07
HDDT 2	1.88E-03	1.01E-04	-1.27E-07
HDDT 3	1.56E-03	1.09E-04	-1.24E-07
HDDT 4	1.42E-03	1.03E-04	-1.22E-07
HDDT 5	1.38E-03	1.10E-04	-1.64E-07
HDDT 6	1.02E-03	1.06E-04	-9.28E-08
HDDT 7	9.18E-04	1.06E-04	-8.75E-08
HDDT 8	2.02E-03	8.78E-05	-3.33E-08

varies from -8% to 8% with a span of 2%, and the vehicle weight varies from 17,000 *kg* to 38,000 *kg* by having a identical span of 1000 *kg*. Fig. 2 characterizes the variation of fuel consumption levels over cruise speed at different grade levels, which produces counter intuitive fuel consumption levels, especially when the road grade is high. This implies that the optimum fuel economy cruise speed may increase with the rise of road grade. Fig. 3 also gives unrealistic results that heavier vehicles have higher optimum cruise speeds, implying that, drivers of heavier vehicles, compared to those driving lighter vehicles, are recommended to achieve higher cruise speed to minimize their fuel consumption levels. This is obviously not correct in reality.

Given that the concave model generates a mild increase of fuel consumption with the growth of vehicle power, the unrealistic driving recommendations cannot be avoidable.

5.2. Model Enhancement

Given the deficiency of the concave model, an enhancement was considered to make the model more realistic. The convex model had been developed for LDVs and validated to be capable of generating reasonable driving instructions in existing eco-driving and eco-routing systems (Ahn et al. (2011); Park et al. (2011); Rakha et al. (2012)). Consequently, the model was alternatively developed by ensuring that the second-order parameter is positive (linear model has not been considered given that it produces a bang-bang control).

5.2.1. Convex Model

To develop a convex model, the order of magnitude of the second-order parameter, which impacts the degree of convexity of the function, needs to be determined. Basically, a lower order of magnitude generates estimates of the convex model less consistent with

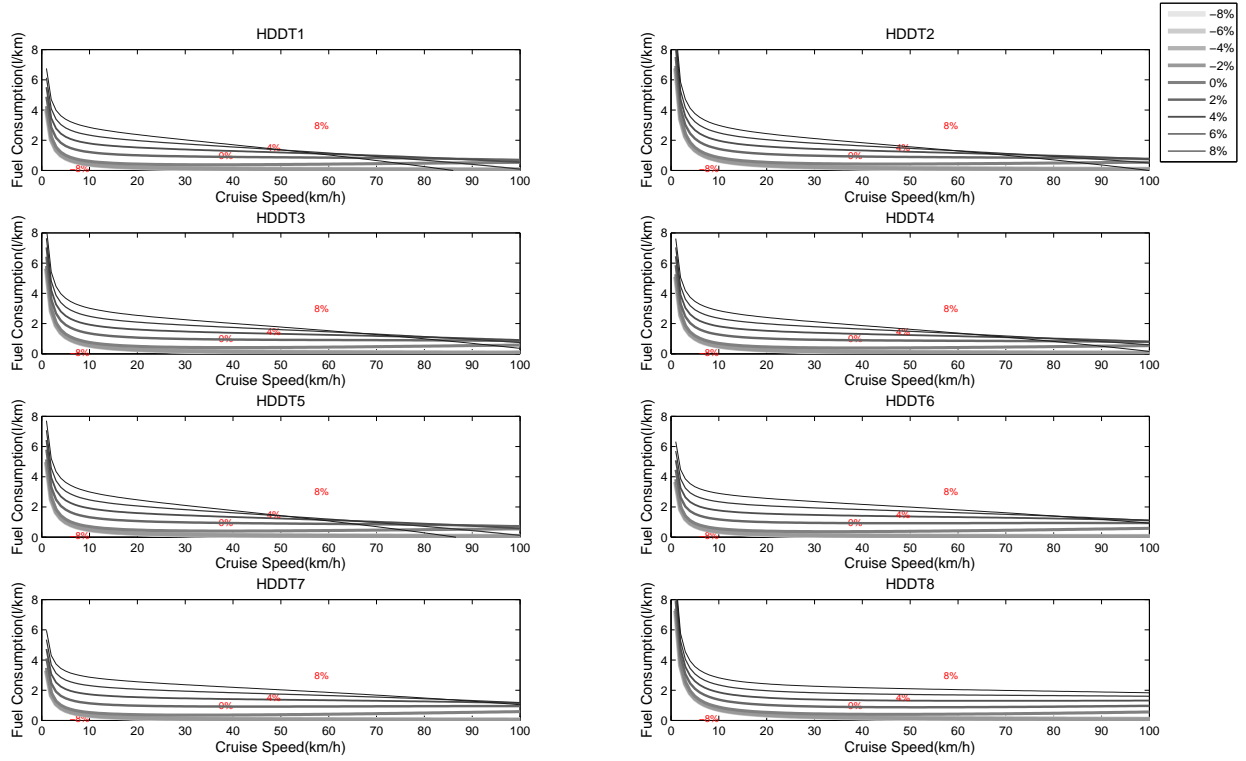


Fig. 2: Fuel consumption levels vs. cruise speed at different grade levels (concave model)

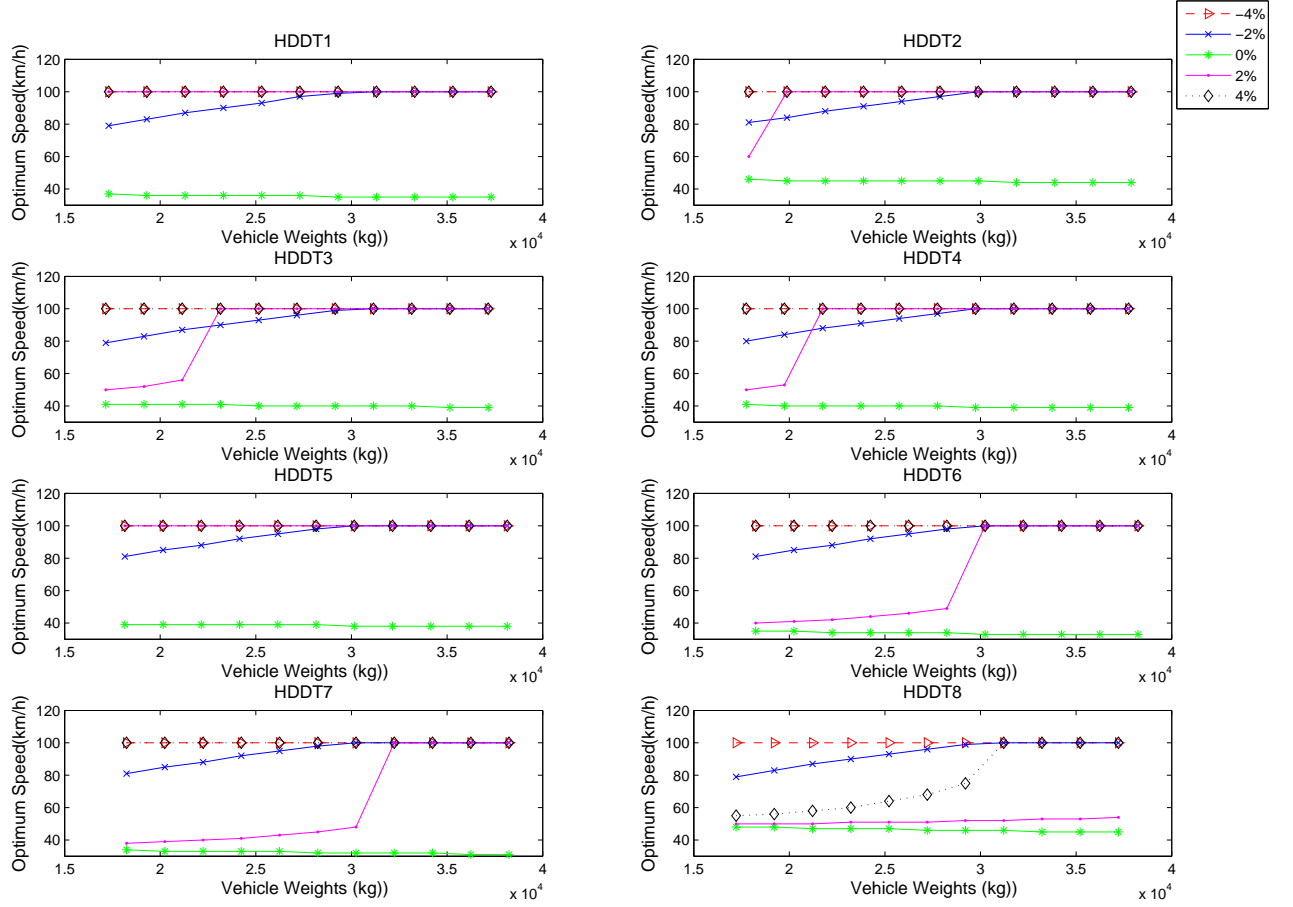


Fig. 3: Impacts of vehicle weight on the optimum fuel economy cruise speed at different grade levels (concave model)

Table 4: The convex model for each truck

Truck classification	α_0	α_1	α_2
HDDT 1	1.56E-03	8.10E-05	1.00E-08
HDDT 2	2.48E-03	7.14E-05	1.00E-08
HDDT 3	2.26E-03	7.82E-05	1.00E-08
HDDT 4	1.80E-03	7.96E-05	1.00E-08
HDDT 5	2.02E-03	7.59E-05	1.00E-08
HDDT 6	1.45E-03	8.48E-05	1.00E-08
HDDT 7	1.31E-03	8.63E-05	1.00E-08
HDDT 8	2.16E-03	7.98E-05	1.00E-08

those of the concave model. Nonetheless, a higher order of magnitude, although more accurate, is very similar to a linear model. A trade-off is thus needed between the accuracy of the model and the degree of convexity. The performance of the convex model in terms of R^2 values has been comprehensively investigated by varying the order of magnitude from $1E - 05$ to $1E - 11$, as illustrated in Fig. 4. For each model, the R^2 value increases with the growth of the order of magnitude, while the performance achieves little improvement when the coefficient is higher than $1E - 08$. Consequently, $1E - 08$ was considered as the best order of magnitude in balancing the model performance and the degree of convexity of the model. The convex model is summarized in Table 4.

5.2.2. Sensitivity Analysis of Convex Model

The effects of road grade and vehicle weight on the optimum fuel economy cruise speed were evaluated for the convex model using the same method in section 5.1. As illustrated in Fig. 5, the model produces a bowl-shaped curve as a function of cruise speed and higher road grades result in higher fuel consumption levels, which is similar to LDVs. Specifically, Fig. 6 reveals that, when moving downhill, high cruise speeds can minimize fuel consumption levels, yet not recommended for safety purposes. For uphill, steeper roads result in lower optimum cruise speeds, implying that drivers have to reduce their cruise speed to minimize their fuel consumption levels with an increase in the roadway grade.

Heavier vehicles, as demonstrated in Fig. 7, have higher optimum cruise speeds when moving downhill while lower when moving uphill. It should be noted that, in Fig. 7a, optimum cruise speeds remain constant with an increase in vehicle weight when the road grade is -8%, -6% and -4%. This is because the sensitivity analysis was performed only

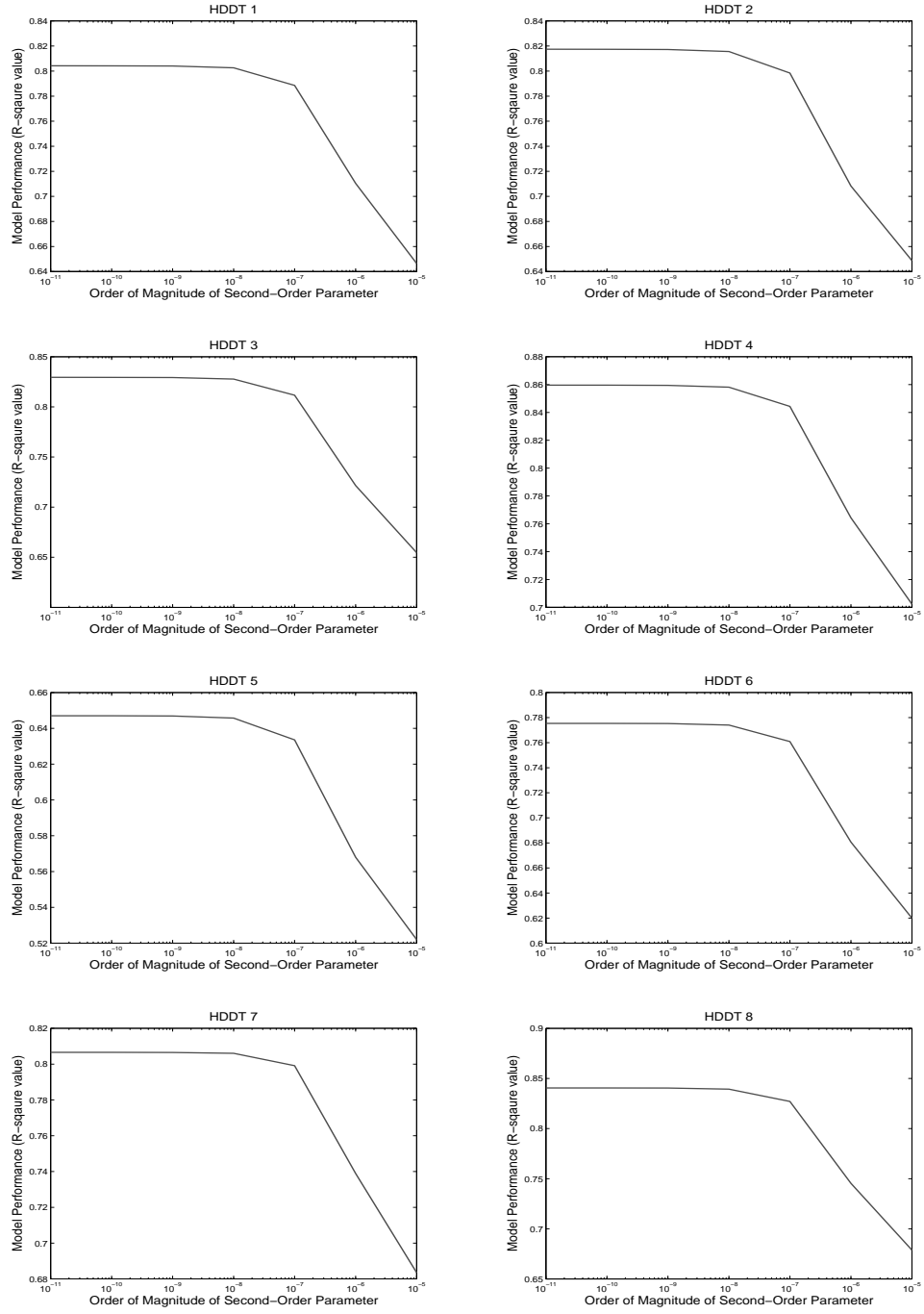


Fig. 4: Model performance vs. order of magnitude of the second-order parameter

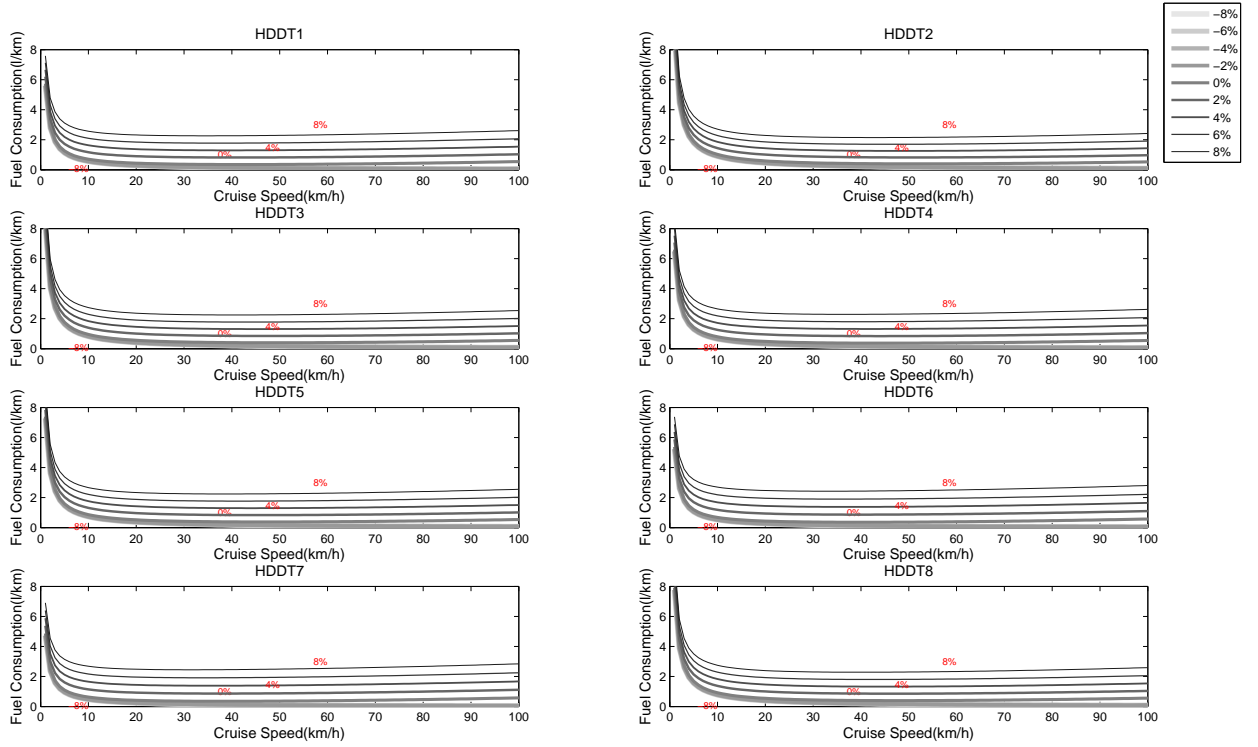


Fig. 5: Fuel consumption levels vs. cruise speed at different grade levels (convex model)

for the speed range of 0-100 km/h and the optimum cruise speeds already reached the maximum level when vehicle weights were at a low level (e.g. 17,000 kg). Furthermore, Fig. 7b clearly indicates that the optimum cruise speeds are more sensitive to vehicle weight at higher grade levels. In short, the convex model can provide reasonable driving recommendations and thus be applicable to eco-driving or eco-routing systems.

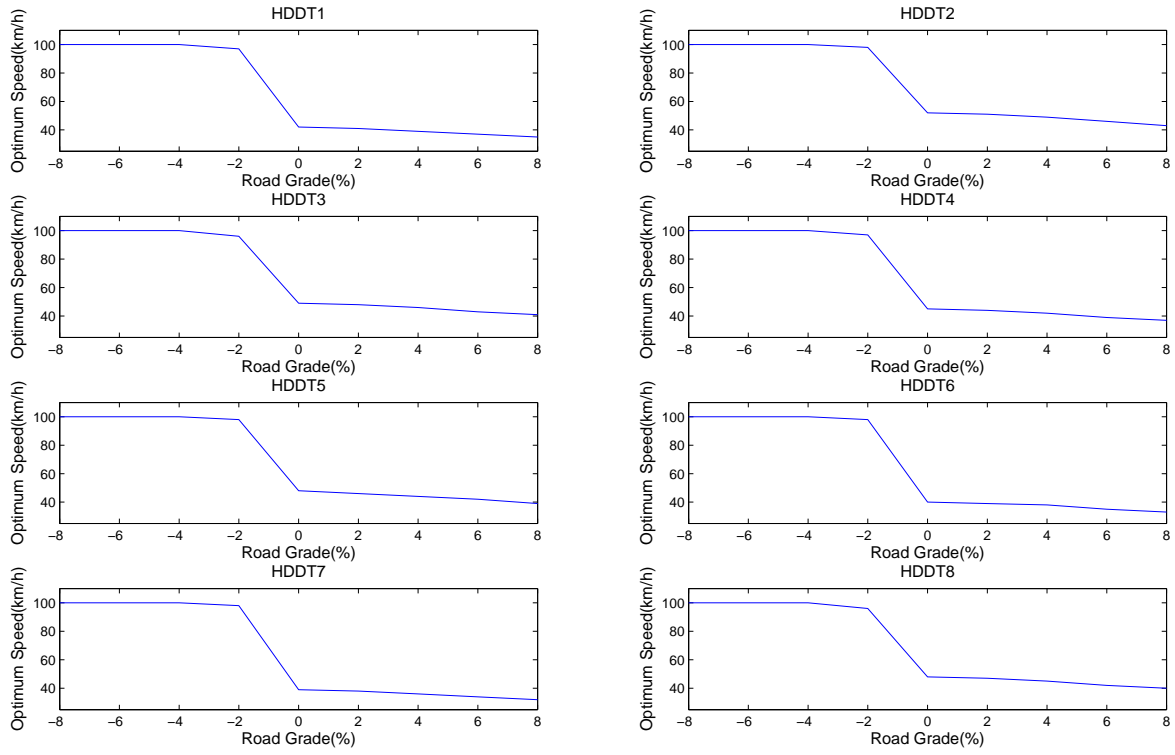
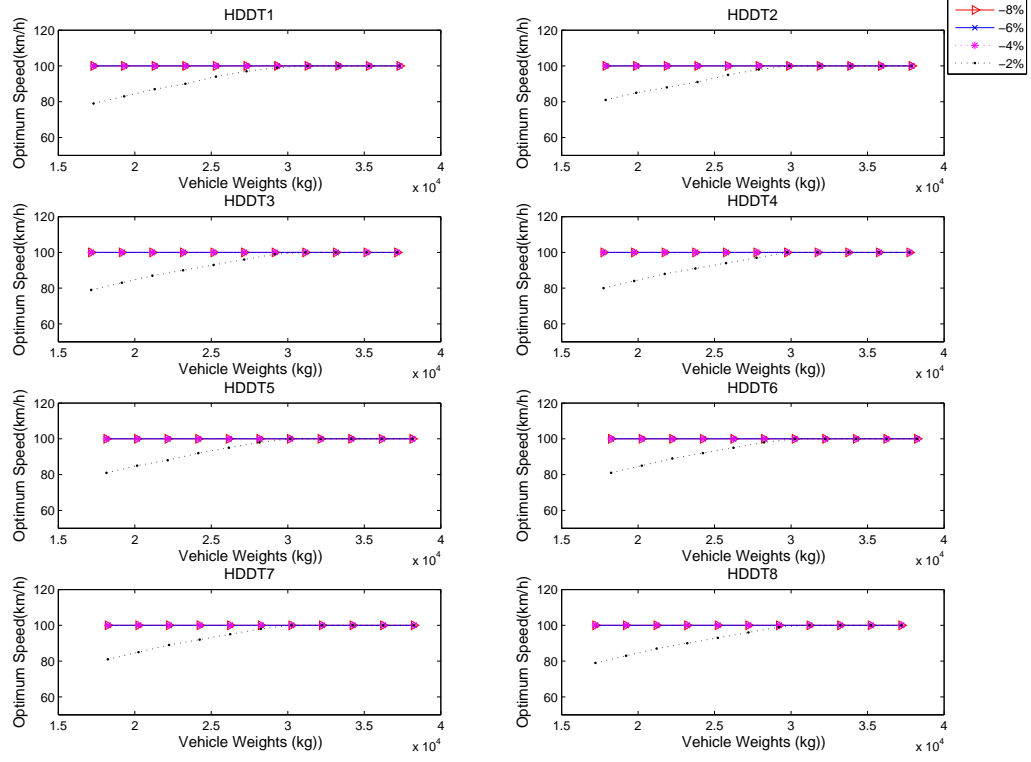
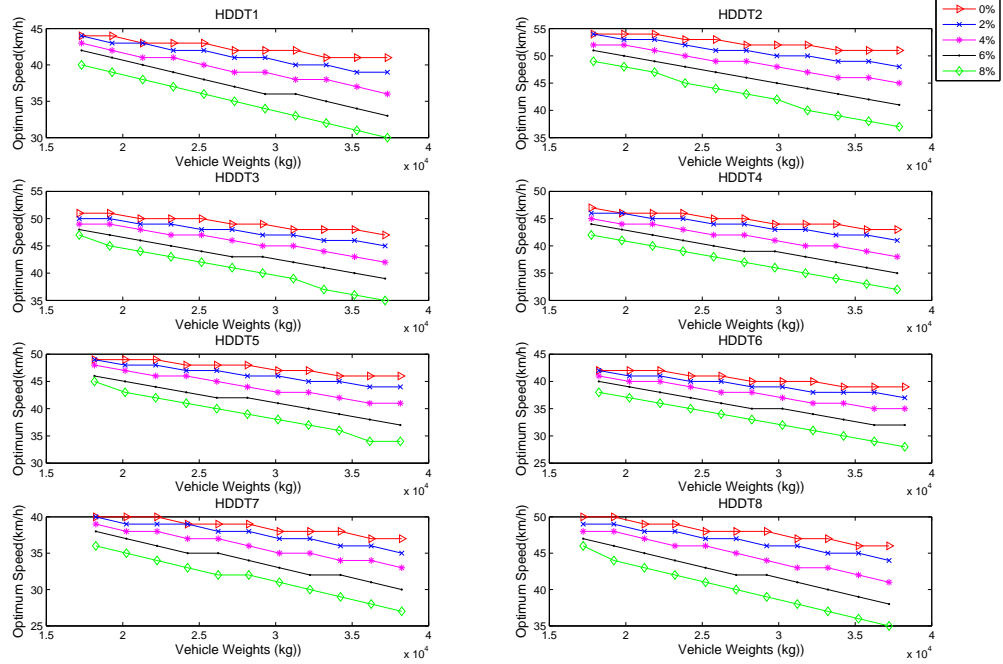


Fig. 6: Impacts of road grade on the optimum fuel economy cruise speed



(a) downhill



(b) uphill

Fig. 7: Impacts of vehicle weight on the optimum fuel economy cruise speed at different grade levels (convex model)

6. Model Validation

A rigorous validation procedure was designed using an independent dataset. The validation process was firstly initiated by comparing the model estimates with field measurements along with CMEM and MOVES estimates at an instantaneous fuel consumption level. Furthermore, the variation of fuel estimates over cruise speed was compared between the proposed model and CMEM. Finally, CO₂ emissions were computed using fuel estimates and validated against in-field measurements.

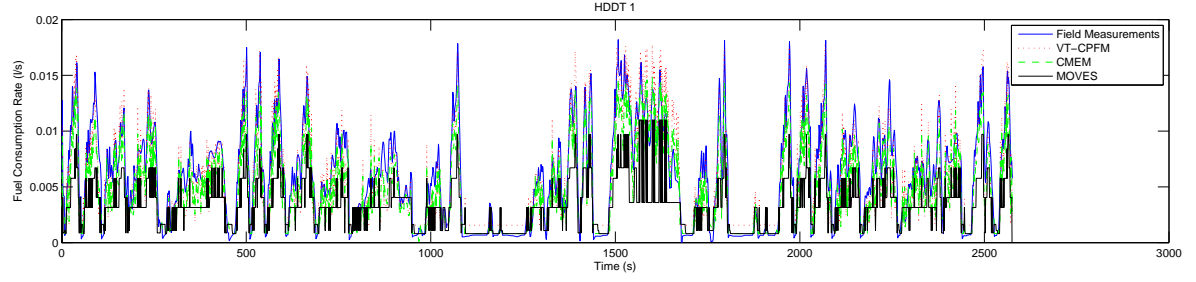
6.1. Instantaneous Fuel Consumption Validation

Fig. 8 provides two example illustrations of the instantaneous model validation, demonstrating that the model estimates in general provide a good agreement with in-field measurements as well as CMEM and MOVES predictions by following the peaks and valleys of the fuel rates. Specifically, Table 5 statistically summarizes the performance of different models. Basically, CMEM performs the best in terms of R^2 values, whereas it produces a bang-bang type of control. Although convex models have a slightly lower R^2 value compared to concave models, they can provide realistic driving recommendations. MOVES performs the worst among the models given that it is designed for conformity use instead of instantaneous analysis; however, it can reflect a large proportion of transient fuel consumption behavior by producing relatively high R^2 values.

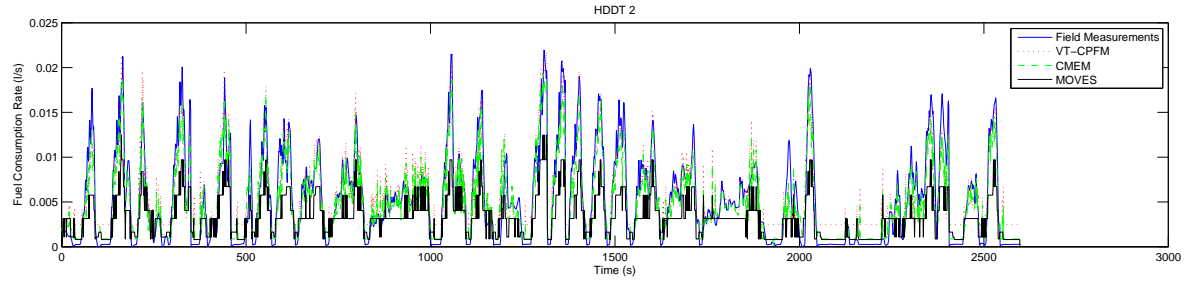
Based on the slopes of the regression lines between model estimates and field measurements, all of the models tend to underestimate the fuel consumption levels with slopes smaller than 1.0, whereas the VT-CPFM model produces better approximation to measurements with higher slope values. MOVES has extremely low slope values given that the MOVES database has no trucks as heavy as the combination of the test truck plus the MERL trailer. The researchers at UC Riverside used MERL to collect data which was accounted for as part of truck load, which makes the total truck load extremely high.

6.2. Optimum Cruise Speed

In validating the proposed model, the variation of fuel predictions over cruise speed was compared against CMEM estimates, as illustrated in Fig. 9 which gives one example result. The two models have highly consistent bowl shaped curves as a function of cruise speed, demonstrating that the proposed model can produce robust fuel estimates. Specifically, the optimum cruise speed ranges between 32~52 km/h (lower than LDVs: 60~80 km/h) for all of the test trucks varying the grade level from 0% to 8%, and moves towards the negative direction with the increase of vehicle load and grade level.



(a) HDDT1



(b) HDDT2

Fig. 8: Instantaneous model validation

Table 5: Comparison of model performance

Truck classification	VT-CPFM (concave)		VT-CPFM (convex)		CMEM		MOVES	
	R^2	Slope	R^2	Slope	R^2	Slope	R^2	Slope
HDDT 1	0.82	0.93	0.80	0.87	0.87	0.78	0.72	0.42
HDDT 2	0.83	0.81	0.81	0.76	0.87	0.75	0.76	0.39
HDDT 3	0.84	0.92	0.83	0.81	0.90	0.78	0.77	0.42
HDDT 4	0.87	0.91	0.86	0.88	0.90	0.77	0.78	0.42
HDDT 5	0.66	0.75	0.64	0.69	0.71	0.65	0.57	0.39
HDDT 6	0.78	0.89	0.77	0.86	0.83	0.72	0.72	0.38
HDDT 7	0.81	0.82	0.81	0.78	0.85	0.64	0.74	0.35
HDDT 8	0.84	0.86	0.84	0.84	0.89	0.79	0.78	0.43

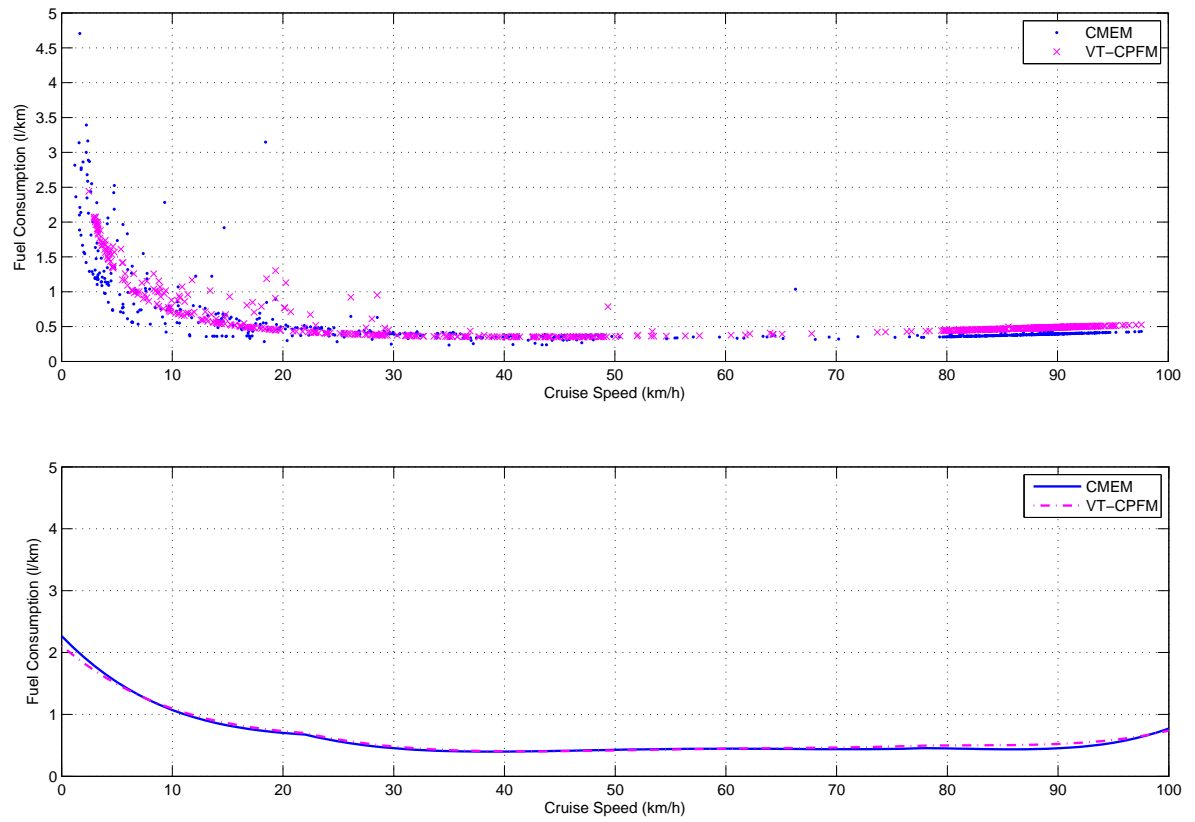


Fig. 9: Impact of cruise speed on fuel consumption levels: VT-CPFM vs. CMEM

Table 6: The performance of CO_2 models

Truck Classification	Coefficients of determination (R^2)	Slope
HDDT 1	0.78	0.95
HDDT 2	0.85	0.72
HDDT 3	0.81	0.82
HDDT 4	NA^a	NA^a
HDDT 5	NA^a	NA^a
HDDT 6	0.74	0.73
HDDT 7	0.81	0.65
HDDT 8	0.79	0.82

^a CO_2 model cannot be validated due to the invalid CO_2 in-field measurements.

6.3. CO_2 Emissions

CO_2 can be estimated from the carbon balance equation using the fuel consumption, HC and CO estimates. Given that the magnitude of CO_2 emissions is significantly higher than HC and CO emissions, the fuel consumption level is thus the primary factor that affects CO_2 emissions. As demonstrated in Rakha et al. (2011), CO_2 emission is linearly related to fuel consumption. Eq.(9) was used to capture the relationship between CO_2 and fuel predictions. The model was firstly calibrated for each truck with CO_2 in g/s and fuel consumption in l/s , and the values of θ were then averaged over individual models to generate the average model given that the relationship between CO_2 and fuel consumption is only related to fuel type rather than vehicle type. The value of 2070 was used to compute CO_2 emissions from fuel consumption estimates. It is found that model estimates are in general consistent with field measurements, as the example results illustrated in Fig. 10. The results of other validation efforts are summarized in Table 6 which has an R^2 values ranging between 0.74 and 0.85. In general, the model provides reliable CO_2 predictions. Noticeably, the model cannot be validated for HDDT 4 and HDDT 5 due to a lack of valid CO_2 field measurements, and the model performance is thus not discussed for these vehicles.

$$\theta = \frac{CO_2(t)}{FC(t)} \quad (9)$$

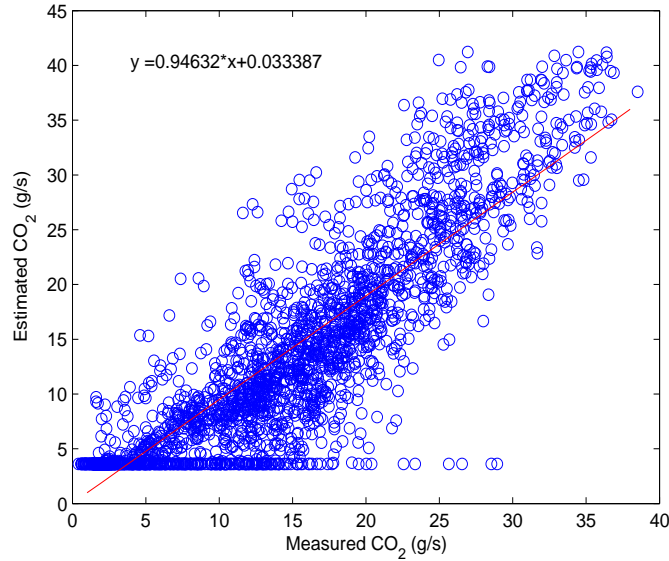


Fig. 10: CO₂ estimation using fuel consumption model (HDDT 1)

7. Conclusions and Recommendations for Further Research

The model developed in this paper circumvents the bang-bang type of control in the family of HDDT fuel consumption models. Given a lack of publicly available data, field measurements are used for model development. The model is calibrated for each individual truck and validated by comparing model estimates against in-field measurements as well as CMEM and MOVES model predictions.

The results of the study demonstrate that the model should be convex, although empirical fuel consumption do seem to point to a concave function of vehicle power, in order to provide realistic driving recommendations from the system perspective. The convex model is demonstrated to estimate fuel consumption levels consistent with in-field measurements and provides better predictions than the CMEM and MOVES models. The optimum fuel economy cruise speed ranges between 32 and 52 *km/h* for all of the test vehicles with grade levels ranging from 0% to 8%, and moves towards the negative direction with an increase in the vehicle load and grade level; namely, steeper roads and heavier vehicles result in lower optimum cruise speeds. The model also generates accurate CO₂ predictions that are consistent with field data.

Finally, it is recommended that EPA require HDDT manufacturers report their fuel economy in the future so that the models can be calibrated using publicly available data without mass in-field data collection, which can maximize the cost-effectiveness of model

341 development. Although NHTSA provides new fuel efficiency standards, these standards,
342 however, are designed for each truck class (e.g. class 7, class 8) rather than specific truck
343 models. Fuel consumption behavior may differ for different vehicle models within the
344 same class. Consequently, the models developed based on class-specific fuel efficiency
345 data may not adequately capture fuel behavior of each individual truck model.

346 8. Acknowledgements

347 This research effort was sponsored by the TranLIVE University Transportation Cen-
348 ter. The authors would like to thank University of California at Riverside researchers for
349 providing the field data used in the model development.

350 9. References

- 351 Ahn, K., Rakha, H., 2008. [The effects of route choice decisions on vehicle energy con-](#)
352 [sumption and emissions](#). Transp Res Part D 13 (3), 151–167.
- 353 Ahn, K., Rakha, H., Moran, K., 2011. Eco-cruise control: Feasibility and initial testing.
354 In: Transportation Research Board 90th Annual Meeting. No. 11-1031.
- 355 Ahn, K., Rakha, H. A., 2013. [Network-wide impacts of eco-routing strategies: a large-](#)
356 [scale case study](#). Transp Res Part D 25, 119–130.
- 357 Arbor, A., 2003. User's guide to MOBILE 6.1 and MOBILE 6.2. Assessment and Standard
358 Division, Office of Transportation and Air Quality, USEPA, Mich.
- 359 Balat, M., Balat, H., 2009. [Recent trends in global production and utilization of bio-ethanol](#)
360 [fuel](#). Appl energy 86 (11), 2273–2282.
- 361 Barkenbus, J. N., 2010. [Eco-driving: An overlooked climate change initiative](#). Energy
362 Policy 38 (2), 762–769.
- 363 Barth, M., An, F., Younglove, T., Levine, C., Scora, G., Ross, M., Wenzel, T., 2000. De-
364 velopment of a comprehensive modal emissions model. National Cooperative Highway
365 Research Program, Transportation Research Board of the National Academies.
- 366 Barth, M., Scora, G., Younglove, T., 2004. [Modal emissions model for heavy-duty diesel](#)
367 [vehicles](#). Transp Res Rec: J of the Transp Res Board (1880), 10–20.
- 368 Boriboonsomsin, K., Barth, M. J., Zhu, W., Vu, A., 2012. [Eco-routing navigation system](#)
369 [based on multisource historical and real-time traffic information](#). Intell Transp Syst,
370 IEEE Trans on 13 (4), 1694–1704.

- 371 Cocker, D. R., Shah, S. D., Johnson, K., Miller, J. W., Norbeck, J. M., 2004. [Development](#)
372 [and application of a mobile laboratory for measuring emissions from diesel engines. 1.](#)
373 [Regulated gaseous emissions](#). Environ Sci & Technol 38 (7), 2182–2189.
- 374 Davis, S. C., Diegel, S. W., Boundy, R. G., 2015. [Transportation energy data book](#). Oak
375 Ridge National Laboratory.
- 376 Demirbas, A., 2007. [Importance of biodiesel as transportation fuel](#). Energy policy 35 (9),
377 4661–4670.
- 378 Dzenisiuk, K., 2012. [Eco-driving-changing truck driver behavior to achieve long-term sus-](#)
379 [tainability results](#). Master's thesis, Copenhagen Business School, 2012.
- 380 Edwardes, W., Rakha, H., 2014. [Virginia Tech Comprehensive Power-Based Fuel Con-](#)
381 [sumption Model: Modeling diesel and hybrid buses](#). Transp Res Rec: J of the Transp
382 Res Board (2428), 1–9.
- 383 EPA, 2015. [Inventory of US greenhouse gas emissions and sinks: 1990-2013](#). Tech. rep.,
384 EPA 430-R-15-004.
- 385 Feng, C., 2007. Transit bus load-based modal emission rate model development. Ph.D.
386 thesis, Georgia Institute of Technology.
- 387 Fitch, J. W., 1994. Motor truck engineering handbook. Technology 2004, 03–08.
- 388 Guo, J., Ge, Y., Hao, L., Tan, J., Peng, Z., Zhang, C., 2015. [Comparison of real-world fuel](#)
389 [economy and emissions from parallel hybrid and conventional diesel buses fitted with](#)
390 [selective catalytic reduction systems](#). Appl Energy 159, 433–441.
- 391 Harrington, W., Krupnick, A., 2012. [Improving fuel economy in heavy-duty vehicles](#).
392 Resources for the Future DP, 12–02.
- 393 Hausberger, S., Rexeis, M., Zallinger, M., Luz, R., 2010. PHEM user guide for version 10.
394 TUG/FVT Report, 1–57.
- 395 Lattemann, F., Neiss, K., Terwen, S., Connolly, T., 2004. The predictive cruise control:
396 A system to reduce fuel consumption of heavy duty trucks. SAE transactions 113 (2),
397 139–146.
- 398 López, J. M., Gómez, Á., Aparicio, F., Sánchez, F. J., 2009. [Comparison of GHG emis-](#)
399 [sions from diesel, biodiesel and natural gas refuse trucks of the City of Madrid](#). Appl
400 Energy 86 (5), 610–615.

- 401 Onat, N. C., Kucukvar, M., Tatari, O., 2015. [Conventional, hybrid, plug-in hybrid or](#)
402 [electric vehicles? State-based comparative carbon and energy footprint analysis in the](#)
403 [United States](#). Appl Energy 150, 36–49.
- 404 Park, S., Rakha, H., Ahn, K., Moran, K., 2011. [Predictive eco-cruise control: Algorithm](#)
405 [and potential benefits](#). In: Integrated and Sustainable Transportation System (FISTS),
406 2011 IEEE Forum on. IEEE, pp. 394–399.
- 407 Park, S., Rakha, H., Ahn, K., Moran, K., 2013. [Virginia Tech Comprehensive Power-based](#)
408 [Fuel Consumption Model \(VT-CPFM\): Model validation and calibration considerations](#).
409 Int J of Transp Sci and Technol 2 (4), 317–336.
- 410 Pindilli, E., 2012. Applications for the environment: Realtime information synthesis
411 (AERIS) benefit-cost analysis. Prepared by United States Department of Transporta-
412 tion, Federal Highway Administration Office.
- 413 Pontryagin, L. S., 1987. Mathematical theory of optimal processes. CRC Press.
- 414 Rakha, H., Ahn, K., Moran, K., 2012. [Integration framework for modeling eco-routing](#)
415 [strategies: logic and preliminary results](#). Int J of Transp Sci and Technol 1 (3), 259–274.
- 416 Rakha, H., Ahn, K., Trani, A., 2004. [Development of VT-Micro model for estimating hot](#)
417 [stabilized light duty vehicle and truck emissions](#). Transp Res Part D 9 (1), 49–74.
- 418 Rakha, H., Lucic, I., Demarchi, S. H., Setti, J. R., Aerde, M. V., 2001. [Vehicle dynamics](#)
419 [model for predicting maximum truck acceleration levels](#). J of Transp Eng 127 (5), 418–
420 425.
- 421 Rakha, H. A., Ahn, K., Moran, K., Suerens, B., Van den Bulck, E., 2011. [Virginia tech](#)
422 [comprehensive power-based fuel consumption model: model development and testing](#).
423 Transp Res Part D 16 (7), 492–503.
- 424 Rakopoulos, D. C., Rakopoulos, C. D., Giakoumis, E. G., 2015. [Impact of properties of](#)
425 [vegetable oil, bio-diesel, ethanol and n-butanol on the combustion and emissions of](#)
426 [turbocharged HDDI diesel engine operating under steady and transient conditions](#). Fuel
427 156, 1–19.
- 428 Saboohi, Y., Farzaneh, H., 2009. [Model for developing an eco-driving strategy of a pas-](#)
429 [senger vehicle based on the least fuel consumption](#). Appl Energy 86 (10), 1925–1932.
- 430 Suerens, B., Diehl, M., Van den Bulck, E., 2010. Optimal control using pontryagin’s max-
431 imum principle and dynamic programming. In: Automotive Model Predictive Control.
432 Springer, pp. 119–138.

- 433 Schall, D. L., Mohnen, A., 2015. [Incentivizing energy-efficient behavior at work: An](#)
434 [empirical investigation using a natural field experiment on eco-driving](#). Appl Energy (In
435 press).
- 436 Smit, R., Smokers, R., Rabé, E., 2007. [A new modelling approach for road traffic emis-](#)
437 [sions: VERSIT+](#). Transp Res Part D 12 (6), 414–422.
- 438 Soylu, S., 2014. [The effects of urban driving conditions on the operating characteristics of](#)
439 [conventional and hybrid electric city buses](#). Appl Energy 135, 472–482.
- 440 Takada, Y., Ueki, S., Saito, A., Sawazu, N., Nagatomi, Y., 2007. Improvement of fuel
441 economy by eco-driving with devices for freight vehicles in real traffic conditions. Tech.
442 rep., SAE Technical Paper.
- 443 U.S. EPA, NHTSA, 2011. Final rules: Greenhouse gas emissions standards and fuel effi-
444 ciency standards for medium and heavy-duty engines and vehicles. Tech. rep., Federal
445 Register 76: 57106.
- 446 Wang, J., Rakha, H. A., 2016a. Fuel consumption model for conventional diesel buses.
447 Applied Energy 170, 394–402.
- 448 Wang, J., Rakha, H. A., 2016b. Modeling fuel consumption of hybrid electric buses:
449 Model development and comparison with conventional buses. Transportation Research
450 Record: Journal of the Transportation Research Board (2539), 94–102.
- 451 Wayne, W. S., Clark, N. N., Nine, R. D., Elefante, D., 2004. [A comparison of emissions](#)
452 [and fuel economy from hybrid-electric and conventional-drive transit buses](#). Energy &
453 fuels 18 (1), 257–270.
- 454 Wong, J. Y., 2001. Theory of ground vehicles. John Wiley & Sons.