


How many different 2-input truth tables can be constructed? Assume each has 1 output.

A. 4

B. 8

C. 12

 **D. 16**

Inputs		Possible outputs							
a	b	trivial			trivial				
0	0	0	0	0					
0	1	0	0	0					
1	0	0	0	1					
1	1	0	1	0					

2^n
rows

$2^{(2^n)}$ columns

Commonly-used 2-input logic gates:

- AND, NAND
- OR, NOR
- XOR, XNOR

Can the truth table be obtained from a timing diagram?

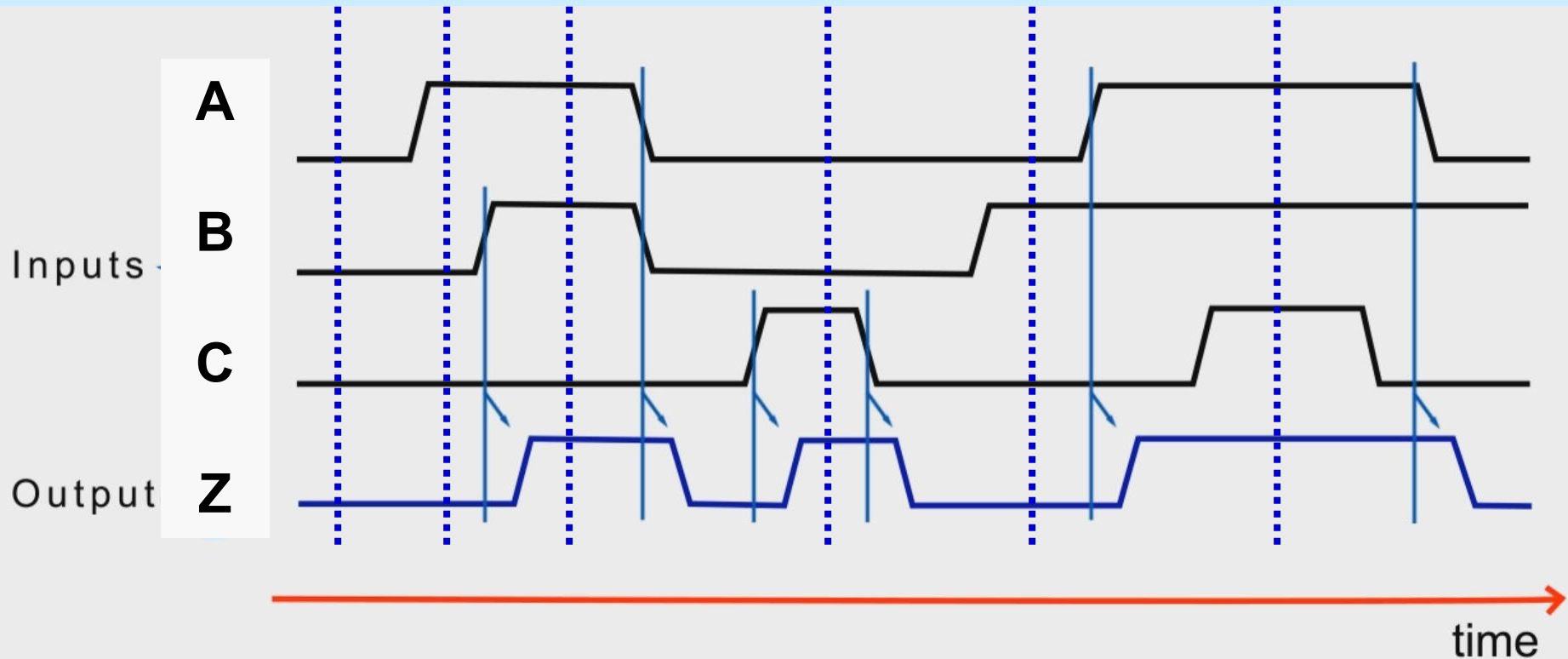


Fig. 3.17 (taken from Wakerly)

Truth table from timing diagram

inputs			output
A	B	C	Z
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

Incomplete truth table

These input combinations did not happen in the timing diagram

inputs			output
A	B	C	Z
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	?
1	0	0	0
1	0	1	?
1	1	0	1
1	1	1	1

$$A(B+C)' = AB' + AC'$$

True or false?

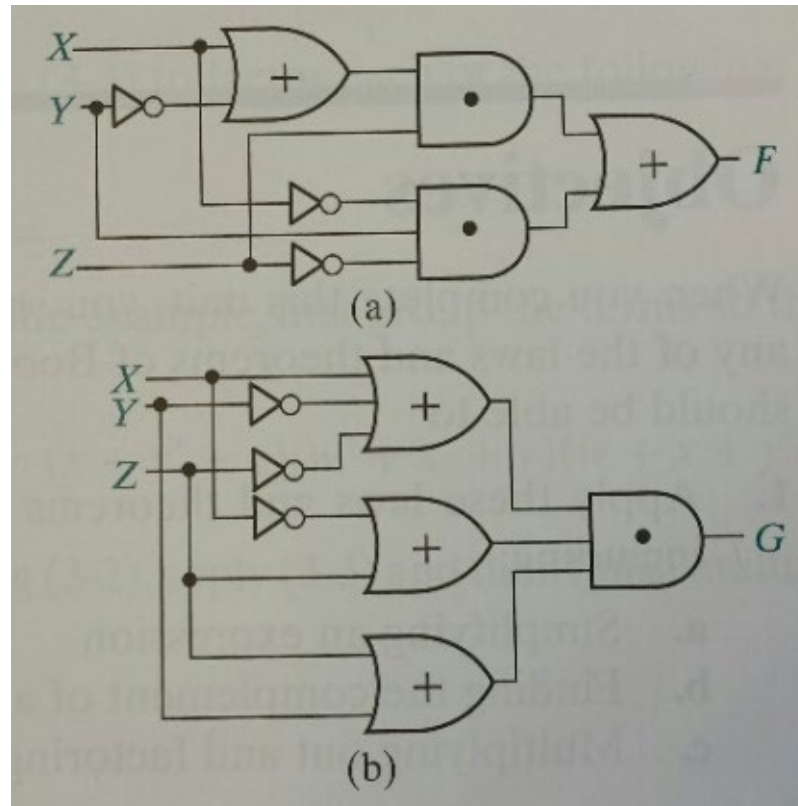
A. True

 **B. False**

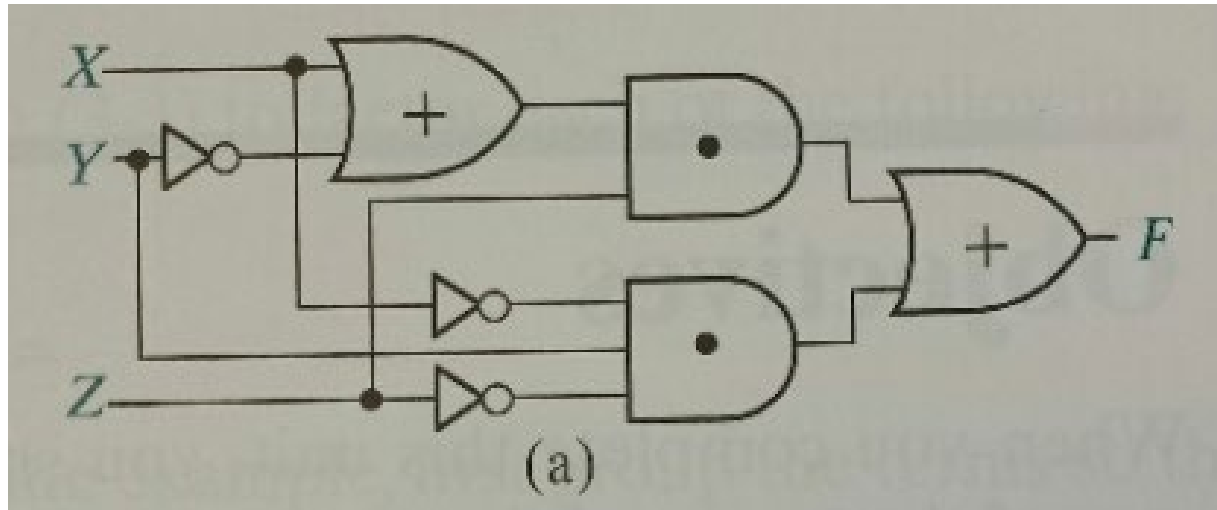
$$\begin{aligned} A (B + C)' \\ &= A (B' C') \\ &= A B' C' \end{aligned}$$

Are these two circuits algebraically equivalent?

- ✓ A. Yes
- B. No

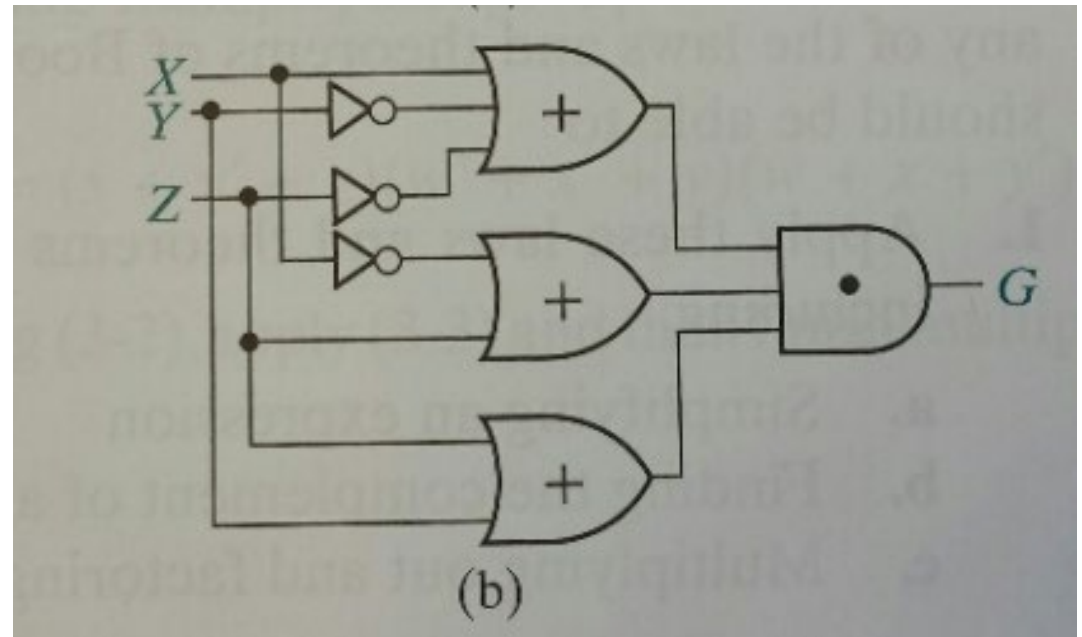


The answer is Yes.



$$F = (X + Y')Z + X'YZ'$$

$$\begin{aligned}
G &= (X+Y'+Z')(X'+Z)(Y+Z) \\
&= (X+Y'+Z')(X'Y + X'Z + YZ + ZZ) \\
&= (X+Y'+Z')[X'Y + Z(X'+Y+1)] \\
&= (X+Y'+Z')[X'Y + Z] \\
&= XZ + Y'Z + X'YZ' \\
&= (X+Y')Z + X'YZ' \\
&= F
\end{aligned}$$



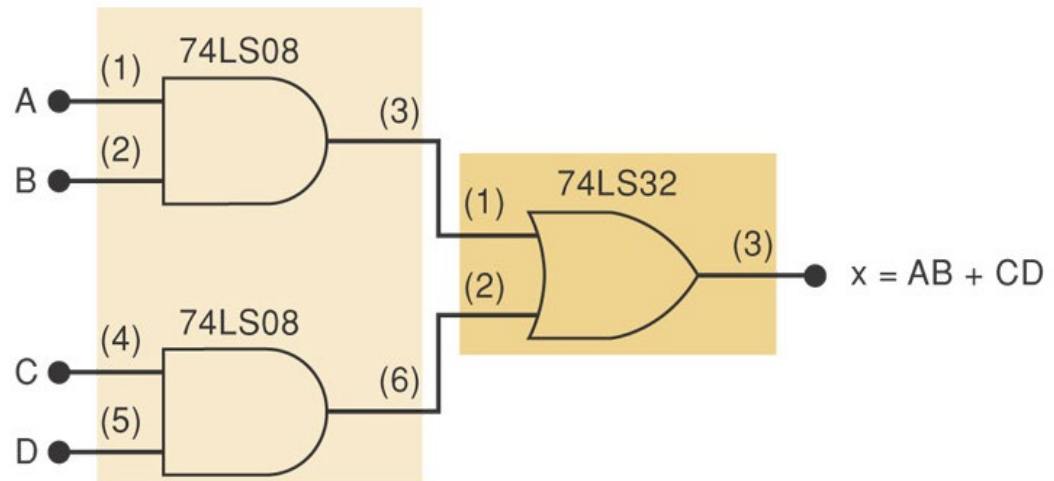
How many NAND gates are needed in total to replace all the gates?

✓ A. 3

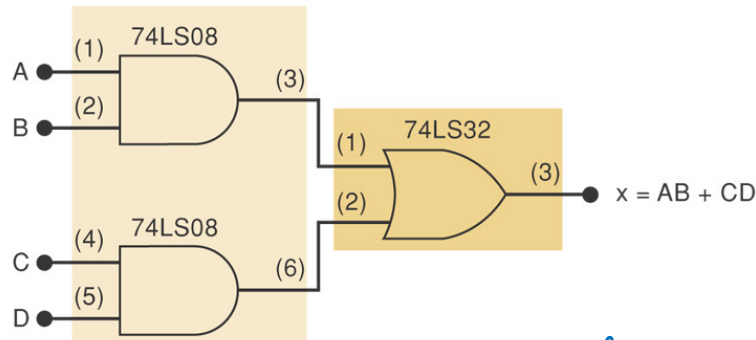
B. 4

C. 5

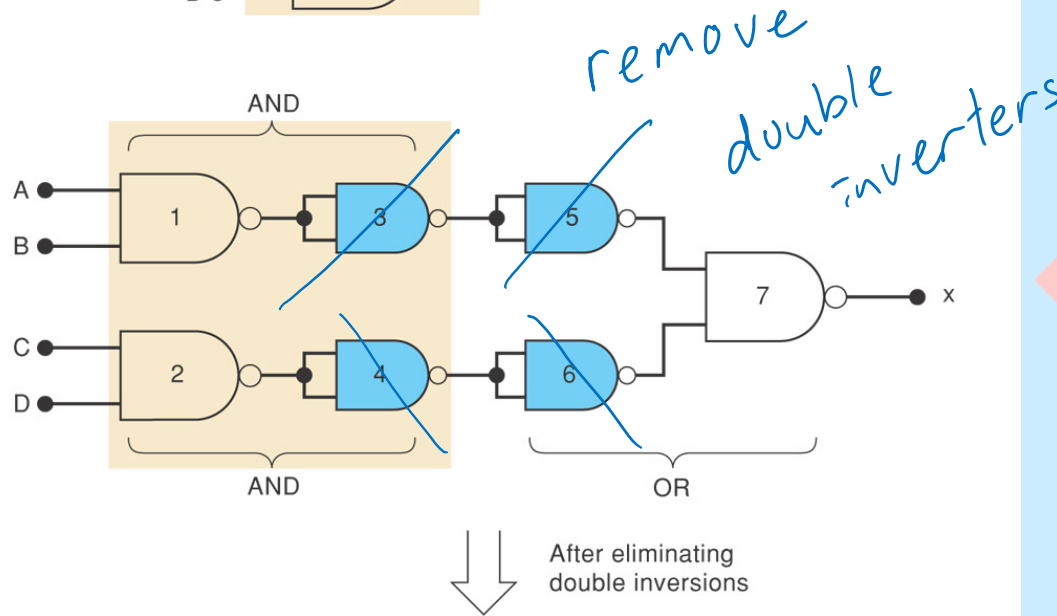
D. 6



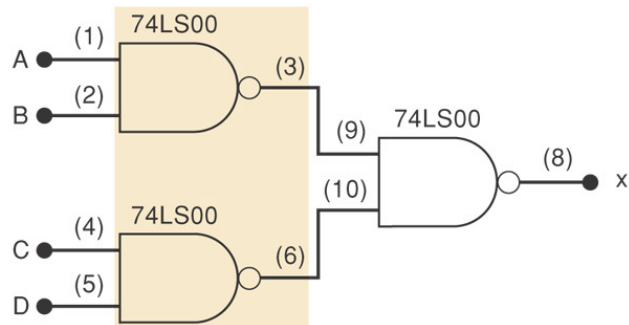
(a)



(b)



(c)

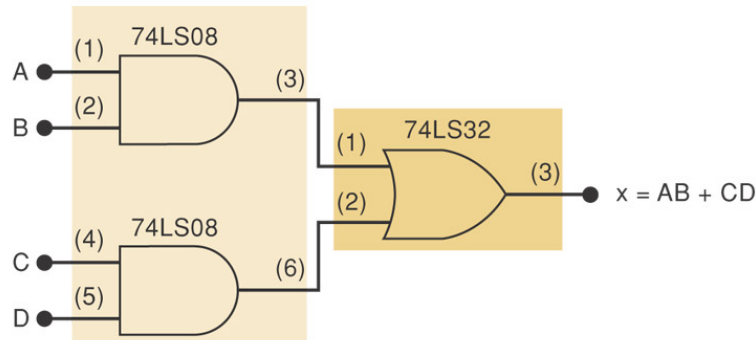


Example:
NAND gates
replace AND,
OR

By diagram

Figure 3-32

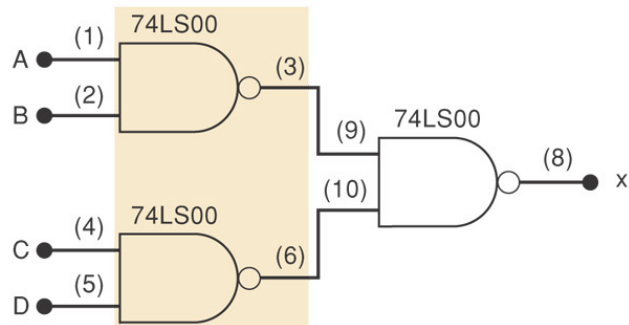
(a)



$$AB + CD = [(AB + CD)']'$$

$$= [\underbrace{(AB)'}_{\text{NAND}} \underbrace{(CD)'}_{\text{NAND}}]' \quad \text{--- NAND}$$

(c)



Example:
NAND gates
replace AND,
OR

By Boolean
expression

Figure 3-32

Tocci, Widmer, Moss. 10th ed.

**Universal gates always reduce
the number of gates used.
True or false?**

A. True

 **B. False**