

**NANYANG  
TECHNOLOGICAL  
UNIVERSITY**  
SINGAPORE

# **CE1107/CZ1107: DATA STRUCTURES AND ALGORITHMS**

## **Lecture 4: Linked Lists II**

Dr Owen Noel Newton Fernando

**College of Engineering**  
School of Computer Science and Engineering

- sizeList() function
- Worked example: Using a linked list
- Linked list C struct
- More complex linked lists
  - Doubly-linked lists
  - Circular linked lists
  - Circular doubly-linked lists
- Array-based list storage
- Summary: Linked lists

# LEARNING OBJECTIVES

After this lesson, you should be able to:

- Understand (conceptually) and use (C implementation) a LinkedList struct
- Choose between an array and a linked list for data storage
- Describe (and implement) more complex linked list variants

- **sizeList() function**

- Worked example: Using a linked list
- Linked list C struct
- More complex linked lists
  - Doubly-linked lists
  - Circular linked lists
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- Core linked list data structure functions
  - printList();
  - findNode();
  - insertNode()
  - removeNode()
- Recall prototypes for insertNode() and removeNode()
  - Need to be able to modify the address stored in the head pointer
  - Pass a pointer to the head pointer into functions

```
int insertNode(ListNode **ptrHead, int index, int value);  
int removeNode(ListNode **ptrHead, int index);
```

# sizeList() FUNCTION

- One more function
    - Return the number of nodes in a linked list
- ```
int sizeList(ListNode *head);
```
- Use the head pointer to get to the first node
  - Keep following the next pointer until next == NULL
    - Increment counter
  - Return the counter

# sizeList()

- Should be quite easy to understand what's happening here

```
1  int sizeList(ListNode *head){
2
3      int count = 0;
4
5      if (head == NULL){
6          return 0;
7      }
8
9      while (head != NULL){
10         head = head->next;
11         count++;
12     }
13
14     return count;
15 }
```

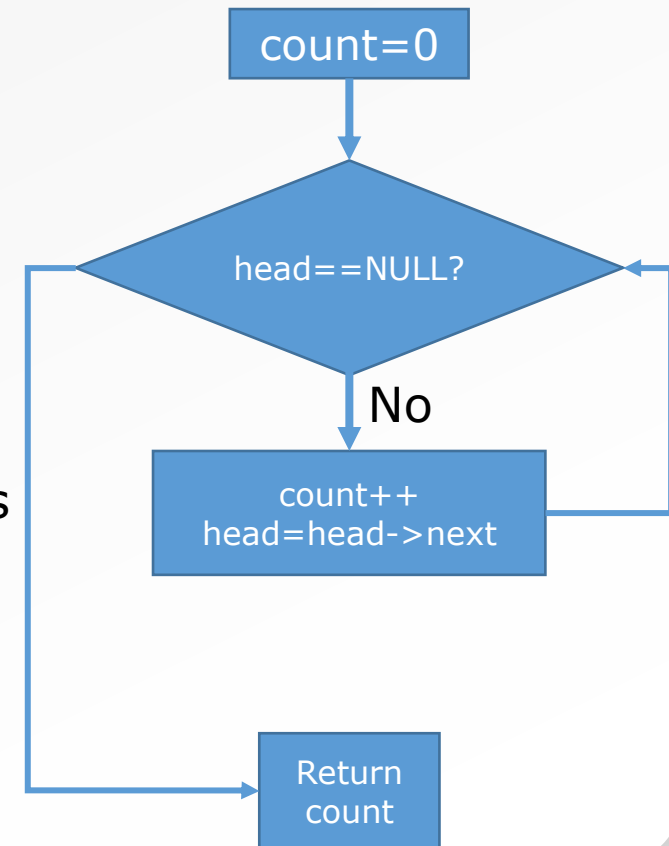
```
typedef struct _listnode{
    int item;;
    struct _listnode *next;
}LinkedList;
```



# sizeList()

- Should be quite easy to understand what's happening here

```
1  int sizeList(ListNode *head){
2
3      int count = 0;
4
5      if (head == NULL){
6          return 0;
7      }
8
9      while (head != NULL){
10         head = head->next;
11         count++;
12     }
13
14     return count;
15 }
```





- sizeList() function
- **Worked example: Using a linked list**
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## WORKED EXAMPLE: LINKED LIST APPLICATION

- Use the `sizeList()`, `insertNode()` and `printList()` functions
- Generate a list of 10 numbers by inserting random numbers (0-99) to the beginning of the list until it has 10 nodes

# WORKED EXAMPLE: LINKED LIST APPLICATION

```
1  int main(){
2
3      ListNode *head = NULL;
4
5      srand(time(NULL));
6      while (sizeList(head) < 10){
7          insertNode(&head, 0, rand() % 100);
8          printf("List: ");
9          printList(head);
10         printf("\n");
11     }
12     printf("%d nodes\n", sizeList(head));
13
14     while (sizeList(head) > 0){
15         removeNode(&head, sizeList(head)-1);
16         printf("List: ");
17         printList(head);
18         printf("\n");
19     }
20     printf("%d nodes\n", sizeList(head));
21
22     return 0;
23 }
```

# WORKED EXAMPLE: LINKED LIST APPLICATION

```
1 int main(){
2
3     ListNode *head = NULL;
4
5     srand(time(NULL));
6     while (sizeList(head) < 10){
7         insertNode(&head, 0, rand() % 100);
8         printf("List: ");
9         printList(head);
10        printf("\n");
11    }
12    printf("%d nodes\n", sizeList(head));
13
14    while (sizeList(head) > 0){
15        removeNode(&head, sizeList(head)-1);
16        printf("List: ");
17        printList(head);
18        printf("\n");
19    }
20    printf("%d nodes\n", sizeList(head));
21
22    return 0;
23}
```

```
int insertNode(ListNode **ptrHead, int index, int value);
int removeNode(ListNode **ptrHead, int index);
int sizeList(ListNode *head)
void printList(ListNode *head)
```

```
typedef struct _listnode{
    int item;;
    struct _listnode *next;
}LinkedList;
```



# LINKED LIST APPLICATION

- How many times does `sizeList()` get called?
- Whole list has to be traversed every time

# LINKED LIST APPLICATION

```
1  int main(){
2
3      ListNode *head = NULL;
4
5      srand(time(NULL));
6      while (sizeList(head) < 10){
7          insertNode(&head, 0, rand() % 100);
8          printf("List: ");
9          printList(head);
10         printf("\n");
11     }
12     printf("%d nodes\n", sizeList(head));
13
14     while (sizeList(head) > 0){
15         removeNode(&head, sizeList(head)-1);
16         printf("List: ");
17         printList(head);
18         printf("\n");
19     }
20     printf("%d nodes\n", sizeList(head));
21
22     return 0;
23 }
```

```
typedef struct _listnode{
    int item;;
    struct _listnode *next;
}LinkedList;
```



# LINKED LIST APPLICATION

- Very inefficient!
- How often does the number of nodes change?
  - Only when you do the following
    - Add a node
    - Remove a node
  - So why recalculate every single time?
- Add a variable to store the number of nodes

```
ListNode *head;  
int listsize;
```

- Update the size variable whenever we add or remove a node

# LINKED LIST APPLICATION [VERSION 2]

```
1  int main(){
2      ListNode *head = NULL;
3      int listsize = 0;
4      srand(time(NULL));
5      while (listsize < 10){
6          insertNode(&head, 0, rand() % 100);
7          listsize++;
8          printf("List: ");
9          printList(head);
10         printf("\n");
11     }
12     printf("%d nodes\n", listsize);
13
14     while (size > 0){
15         removeNode(&head, listsize-1);
16         listsize--;
17         printf("List: ");
18         printList(head);
19         printf("\n");
20     }
21     printf("%d nodes\n", listsize);
22
23     return 0;
24 }
```



- Now `sizeList()` is redundant AND we have to manually manage the count of nodes in the list
- Still not a complete solution to our problems

- sizeList() function
- Worked example: Using a linked list
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# EXISTING LINKED LIST STRUCTURE

- Consider the “big picture” structure of our linked list
- Head pointer
- int listsize
- Problems
  - Multiple things to manage
    - We now have to pass listsize variable into functions
  - Functions that modify linked list structure need to be given pointer to head pointer

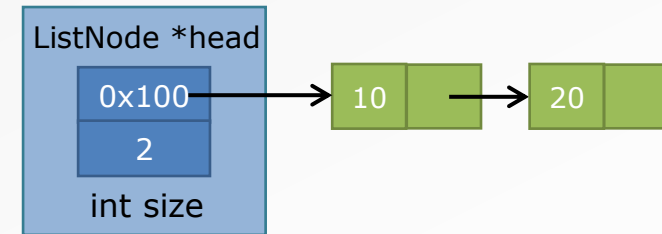


# LinkedList C STRUCT

- Solution

- Define another C struct, LinkedList
- Wrap up (encapsulate) all elements that are required to implement the linked list data structure

```
typedef struct _linkedlist{  
    ListNode *head;  
    int size;  
} LinkedList;
```



- Why is this useful?

- Consider the rewritten linked list functions

# LINKED LIST FUNCTIONS USING `LinkedList` STRUCT

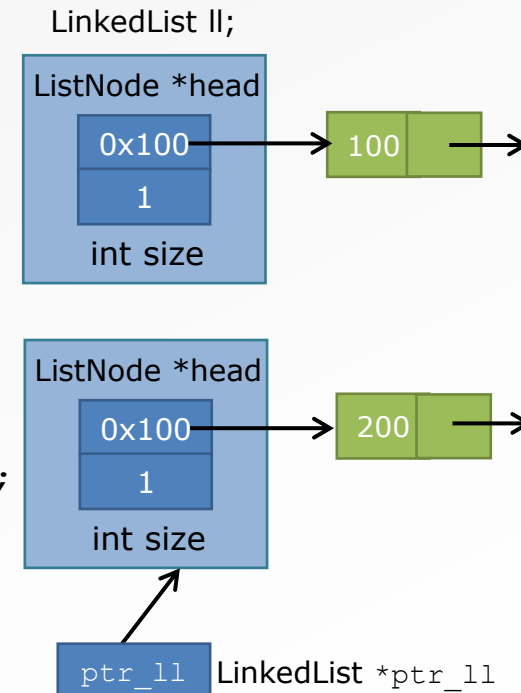
- Original function prototypes
  - `void printList(ListNode *head);`
  - `ListNode * findNode(ListNode *head);`
  - **`int insertNode(ListNode **ptrHead, int index, int value);`**
  - **`int removeNode(ListNode **ptrHead, int index);`**
- New function prototypes
  - `void printList(LinkedList *ll);`
  - `ListNode * findNode(LinkedList *ll, int index);`
  - **`int insertNode(LinkedList *ll, int index, int value);`**
  - **`int removeNode(LinkedList *ll, int index);`**

# CALLING NEW VERSION OF LINKED LIST FUNCTIONS

- Two versions of a small application

```
1 int main() {
2
3     LinkedList ll;
4     LinkedList *ptr_ll;
5
6     insertNode(&ll, 0, 100);
7     printList(&ll);
8     printf("%d nodes\n", ll.size);
9     removeNode(&ll, 0);
10
11    ptr_ll = malloc(sizeof(LinkedList));
12    insertNode(ptr_ll, 0, 200);
13    printList(ptr_ll);
14    printf("%d nodes\n", ptr_ll->size);
15    removeNode(ptr_ll, 0);
16 }
```

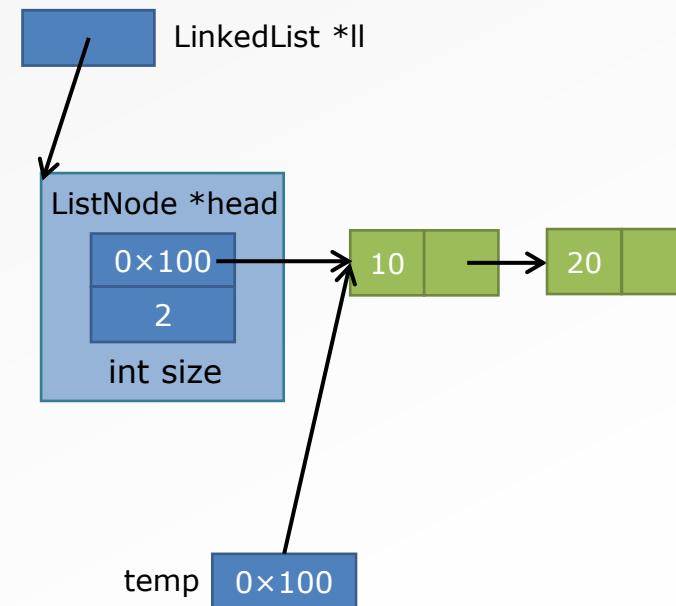
```
int insertNode(LinkedList *ll, int index, int value);
int removeNode(LinkedList *ll, int index);
void printList(ListNode *head)
```



# printList() USING LinkedList STRUCT

- Declare a temp pointer instead of using head (it is no longer a local variable; it is the actual head pointer)

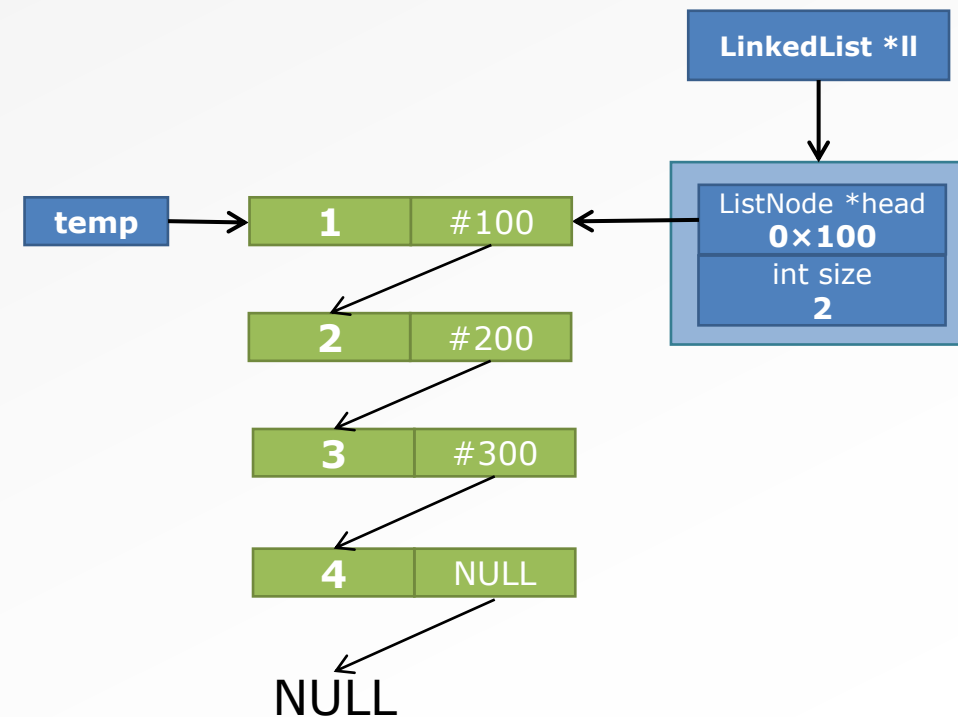
```
1 void printList(LinkedList *ll){
2     ListNode *temp = ll->head;
3
4     if (temp == NULL)
5         return;
6
7     while (temp != NULL){
8         printf("%d ", temp->item);
9         temp = temp->next;
10    }
11    printf("\n");
12 }
```



# printList() USING LinkedList STRUCT

- Declare a temp pointer instead of using head  
(it is no longer a local variable; it is the actual head pointer)

```
1 void printList(LinkedList *ll){
2
3     ListNode *temp;
4     temp = ll->head;
5
6     if (temp == NULL)
7         return;
8
9     while (temp != NULL){ ←
10         printf("%d ", temp->item);
11         temp = temp->next;
12     }
13     printf("\n");
14 }
```



**Print: 1 2 3 4**



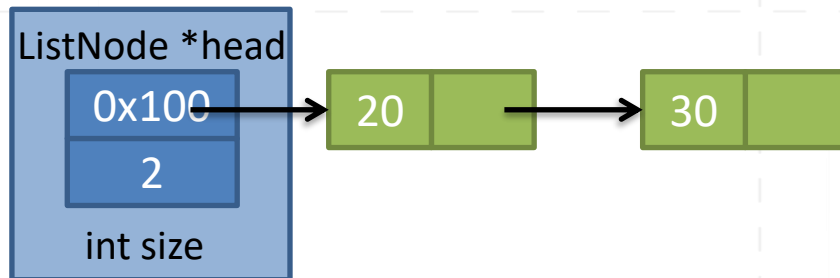
# printList() Versions

```
typedef struct _listnode{
    int item;;
    struct _listnode *next;
}LinkedList;
```



```
1 void printList(ListNode *head){
2
3     if (head == NULL)
4         return;
5
6     while (head != NULL){
7         printf("%d ", head->item);
8         head = head->next;
9     }
10    printf("\n");
11 }
```

```
typedef struct _linkedlist{
    int size;
    ListNode *head;
}LinkedList;
```

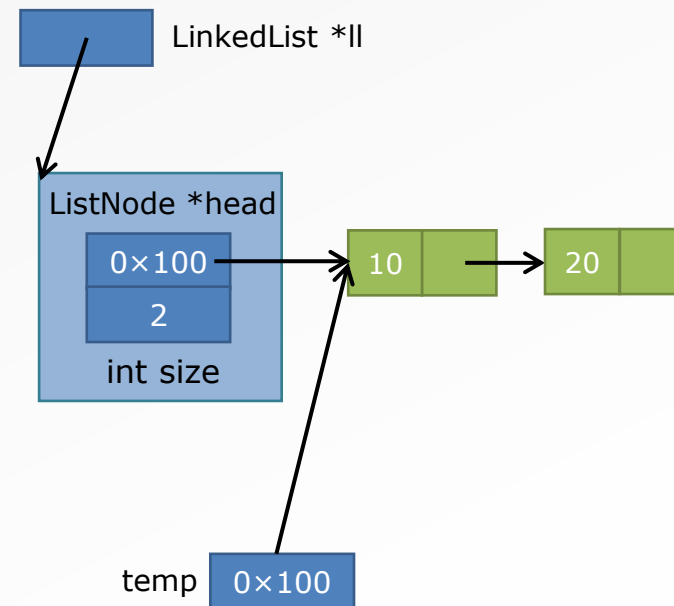


```
1 void printList(LinkedList *ll){
2     ListNode *temp = ll->head;
3
4     if (temp == NULL)
5         return;
6
7     while (temp != NULL){
8         printf("%d ", temp->item);
9         temp = temp->next;
10    }
11    printf("\n");
12 }
```

# findNode() USING LinkedList STRUCT

- Again, declare a temp pointer to track the node we are looking at
- Also not much change/improvement in development time here

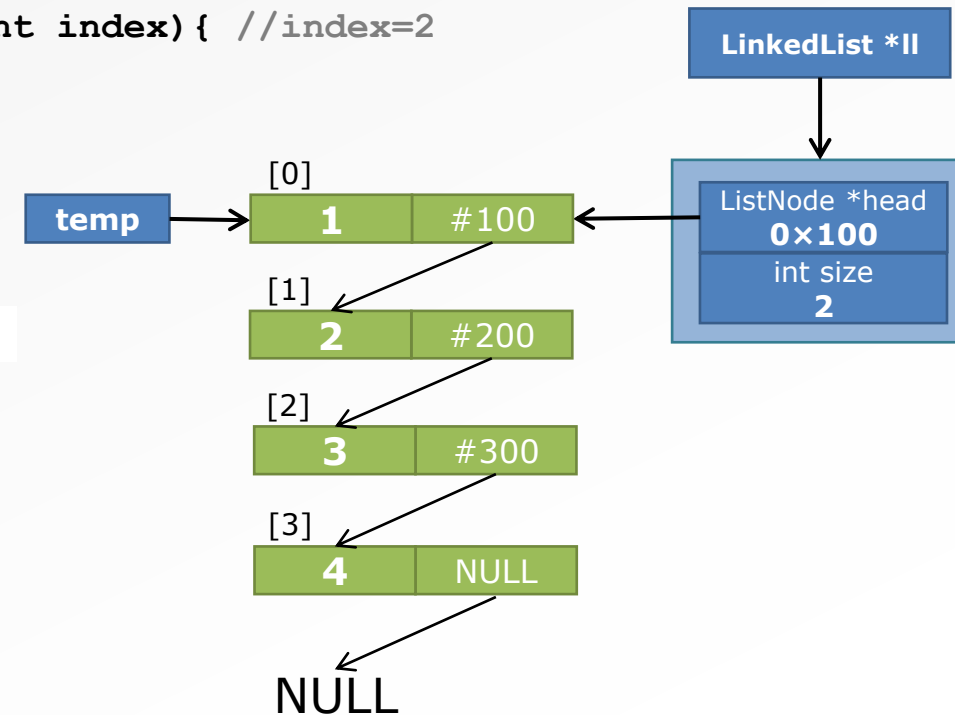
```
1  ListNode * findNode(  
2      LinkedList *ll, int index){  
3      ListNode *temp = ll->head;  
4      if (temp == NULL || index < 0)  
5          return NULL;  
6  
7      while (index > 0){  
8          temp = temp->next;  
9          if (temp == NULL)  
10             return NULL;  
11             index--;  
12     }  
13     return temp;  
14 }
```



# findNode() USING LinkedList STRUCT

- Again, declare a temp pointer to track the node we are looking at
- Also not much change/improvement in development time here

```
1  ListNode * findNode( LinkedList *ll, int index){ //index=2
2      ListNode *temp;
3      temp = ll->head;
4
5      if (temp == NULL || index < 0)
6          return NULL;
7
8      while (index > 0){ ← Index = 0
9          temp = temp->next;
10         if (temp == NULL)
11             return NULL;
12         index--;
13     }
14     return temp;
15 }
```

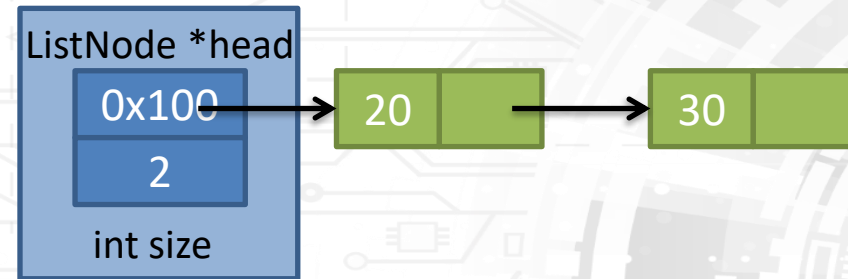


# findNode() Versions

```
typedef struct _listnode{
    int item;;
    struct _listnode *next;
}LinkedList;
```



```
typedef struct _linkedlist{
    int size;
    ListNode *head;
}LinkedList;
```

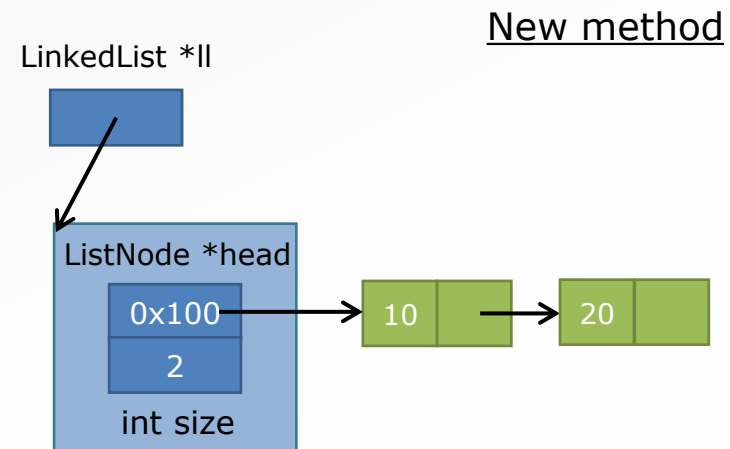
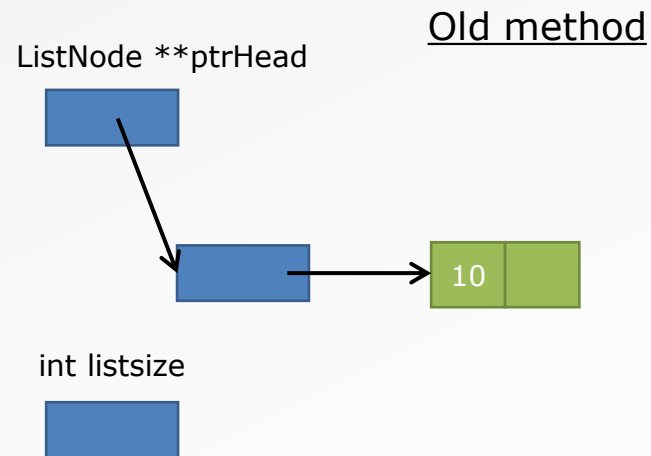


```
1  ListNode * findNode(
2      ListNode *head, int index){
3
4      if (head == NULL || index < 0)
5          return NULL;
6
7      while (index > 0){
8          head = head->next;
9          if (head == NULL)
10             return NULL;
11         index--;
12     }
13     return head;
14 }
```

```
1  ListNode * findNode(
2      LinkedList *ll, int index){
3      ListNode *temp = ll->head;
4      if (temp == NULL || index < 0)
5          return NULL;
6
7      while (index > 0){
8          temp = temp->next;
9          if (temp == NULL)
10             return NULL;
11         index--;
12     }
13     return temp;
14 }
```

# insertNode() USING LinkedList STRUCT

- Pass in pointer to LinkedList struct
- Function has full access to read and write address in head pointer
- Function can also update the number of nodes in the size variable; no need to pass in and listsize
- No need to think about double dereferencing



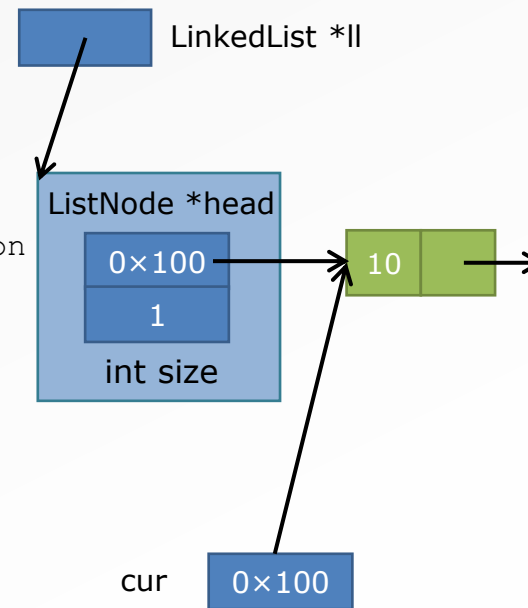
# insertNode() Using ListNode STRUCT

```
1  int insertNode(ListNode **ptrHead, int index, int value){
2
3      ListNode *pre, *cur;
4
5      // If empty list or inserting first node, need to update head pointer
6      if (*ptrHead == NULL || index == 0){
7          cur = *ptrHead;
8          *ptrHead = malloc(sizeof(ListNode));
9          (*ptrHead)->item = value;
10         (*ptrHead)->next = cur;
11         return 1;
12     }
13
14     // Find the nodes before and at the target position
15     // Create a new node and reconnect the links
16     if ((pre = findNode(*ptrHead, index-1)) != NULL){
17         cur = pre->next;
18         pre->next = malloc(sizeof(ListNode));
19         pre->next->item = value;
20         pre->next->next = cur;
21         return 1;
22     }
23
24     return 0;
25 }
```



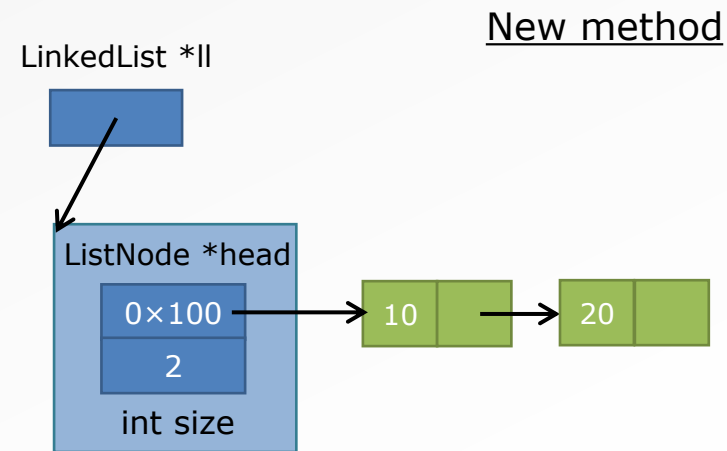
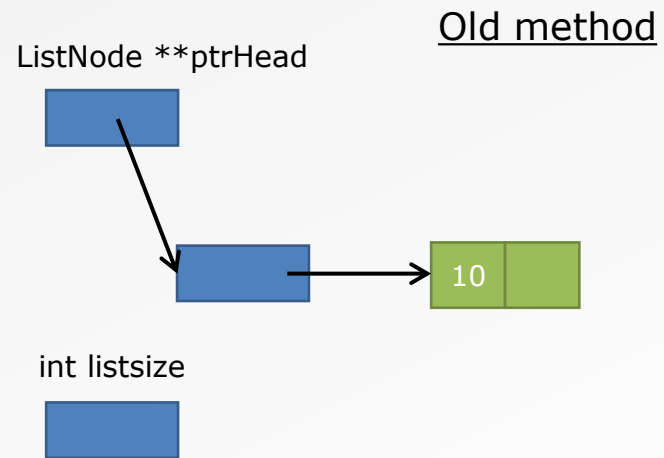
# insertNode() LinkedList STRUCT

```
1 int insertNode(LinkedList *ll, int index, int value){
2     ListNode *pre, *cur;
3
4     if (ll == NULL || index < 0 || index > ll->size + 1)
5         return 0;
6 // If empty list or inserting first node, need to update head pointer
7     if (ll->head == NULL || index == 0){
8         cur = ll->head;
9         ll->head = malloc(sizeof(ListNode));
10        ll->head->item = value;
11        ll->head->next = cur;
12        ll->size++;
13        return 1;
14    }
15 // Find the nodes before and at the target position
16 // Create a new node and reconnect the links
17     if ((pre = findNode(ll, index - 1)) != NULL){
18         cur = pre->next;
19         pre->next = malloc(sizeof(ListNode));
20         pre->next->item = value;
21         pre->next->next = cur;
22         ll->size++;
23         return 1;
24     }
25     return 0;
26 }
```



# removeNode() USING LinkedList STRUCT

- Rewriting the removeNode() functions is left as an exercise for you
- MUCH simpler than writing the original versions with pointer to head pointer

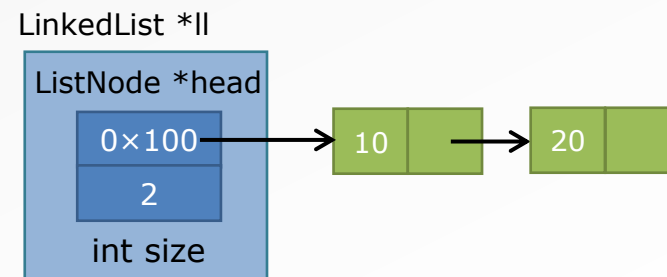


**-int insertNode(ListNode \*\*ptrHead, int index, int value);**   **-int insertNode(LinkedList \*ll, int index, int value);**



# LinkedList STRUCT

- Allows us to think of LinkedList as an object on its own
- Each LinkedList object has the following components
  - Head pointer that stores the address of the first node
  - Size variable that tracks the number of nodes in the linked list
- Conceptually much cleaner
- Practically much cleaner too
  - Easy to pass the entire LinkedList struct into a function

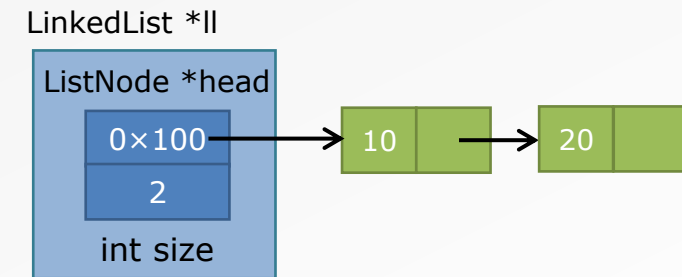


# NEW sizeList() FUNCTION

- sizeList() just became a trivial function!

```
1 int sizeList(LinkedList *ll) {  
2     return ll->size;  
3 }
```

- This is not a bad thing!
  - No need to recalculate size every time
  - Size only changes when adding/removing nodes
- There is a tradeoff here
  - Sometimes it is better to use some memory to store a value
  - While other times, it is better to use some computation time to calculate it
  - Again, you will encounter this in Algorithms



- sizeList() function
- Worked example: Using a linked list
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- **More complex linked lists**
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  - Circular linked lists
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# MORE COMPLEX LINKED LISTS

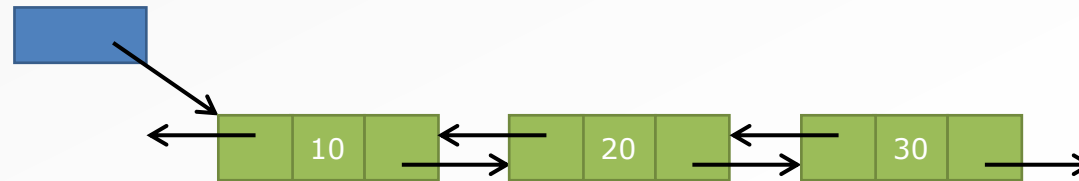
- So far, singly-linked list
  - Each ListNode is linked to at most one other ListNode
  - Traversal of the list is one-way only
    - Cannot go backwards
- Idea: Allow two-way traversal of a list
  - Maybe we want to start from a given node and search EITHER backwards OR forward
  - Each node now has to connect to the previous node as well

# DOUBLY LINKED LIST

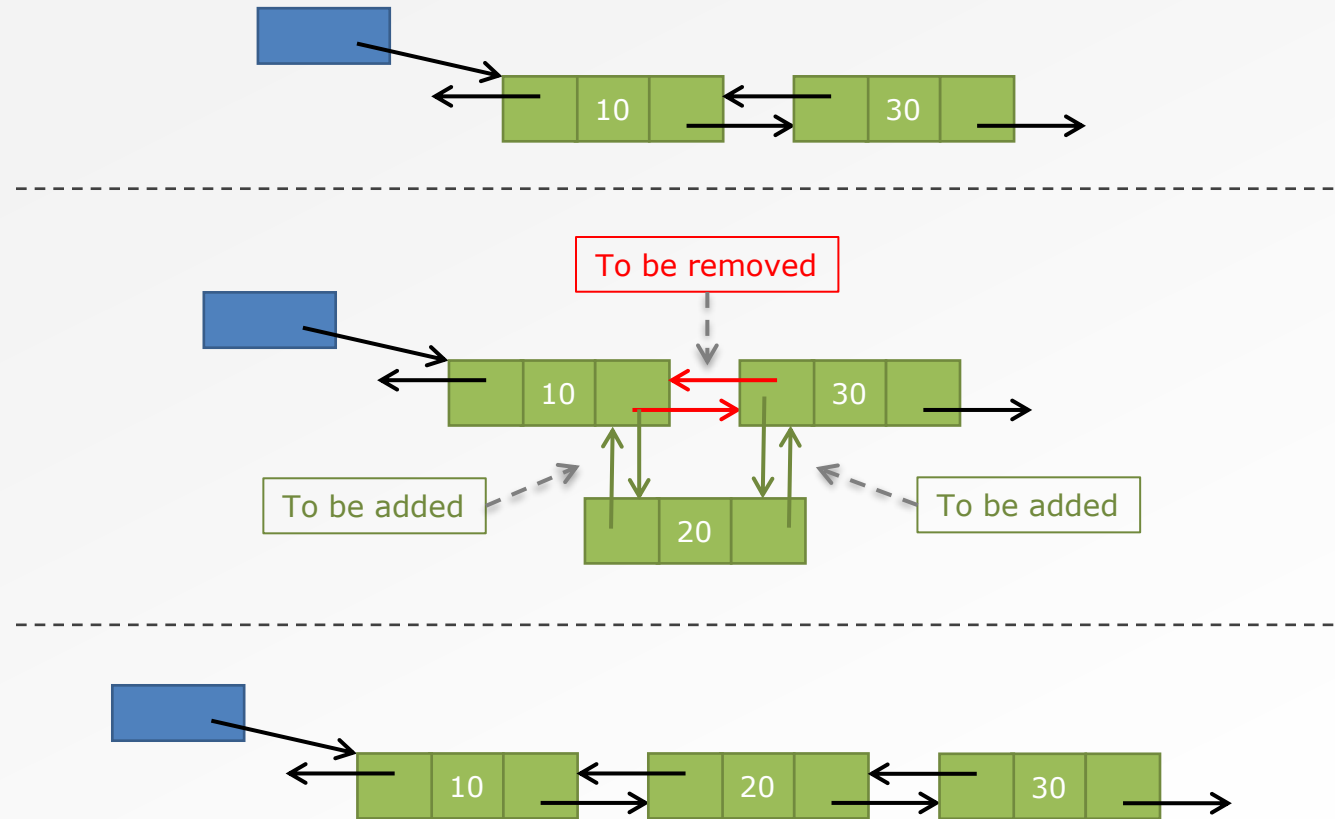
- Modify the ListNode struct

```
typedef struct _dbllistnode{  
    int item;  
    struct _dbllistnode *prev;  
    struct _dbllistnode *next;  
} DbListNode;
```

- Note that first node has prev == NULL
- Inserting a node
  - Have to set the prev and next pointers accordingly for all nodes involved
  - Included in practice questions for Lab 1



# INSERTING A NODE INTO A DOUBLY LINKED LIST



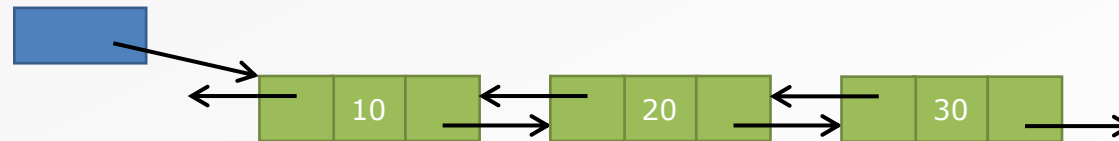
# DOUBLY LINKED LIST

- Traversing a doubly linked list in forward direction

```
temp = temp->next;
```

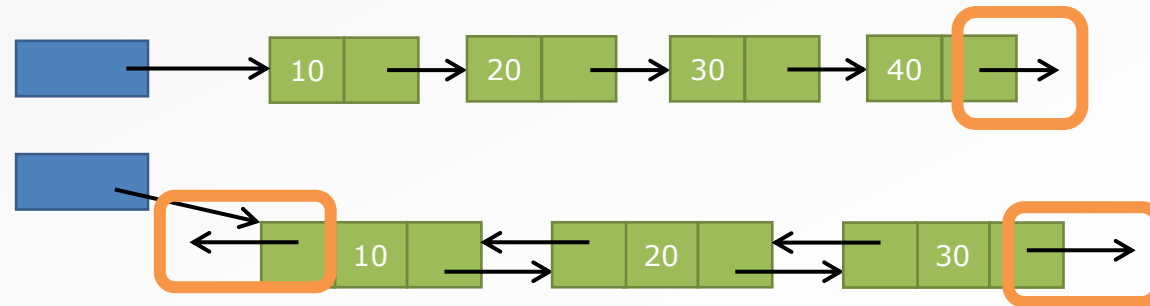
- Traversing a doubly linked list in backward direction

```
temp = temp->prev;
```



## MORE COMPLEX LINKED LISTS (PART II)

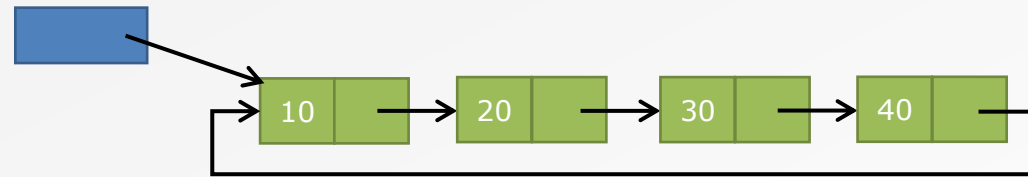
- So far, linked list has a fixed end (or ends)
- No way to loop around
- Might be useful to allow looping traversal
  - Circular linked lists
- No extra variables needed in the ListNode struct
  - Just have to add connections



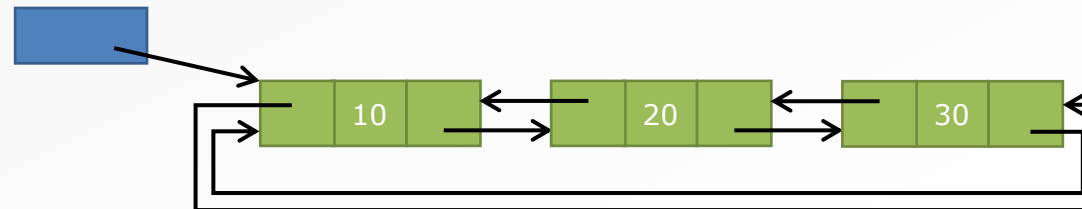


# CIRCULAR LINKED LISTS

- Circular singly-linked lists
  - Last node has next pointer pointing to first node

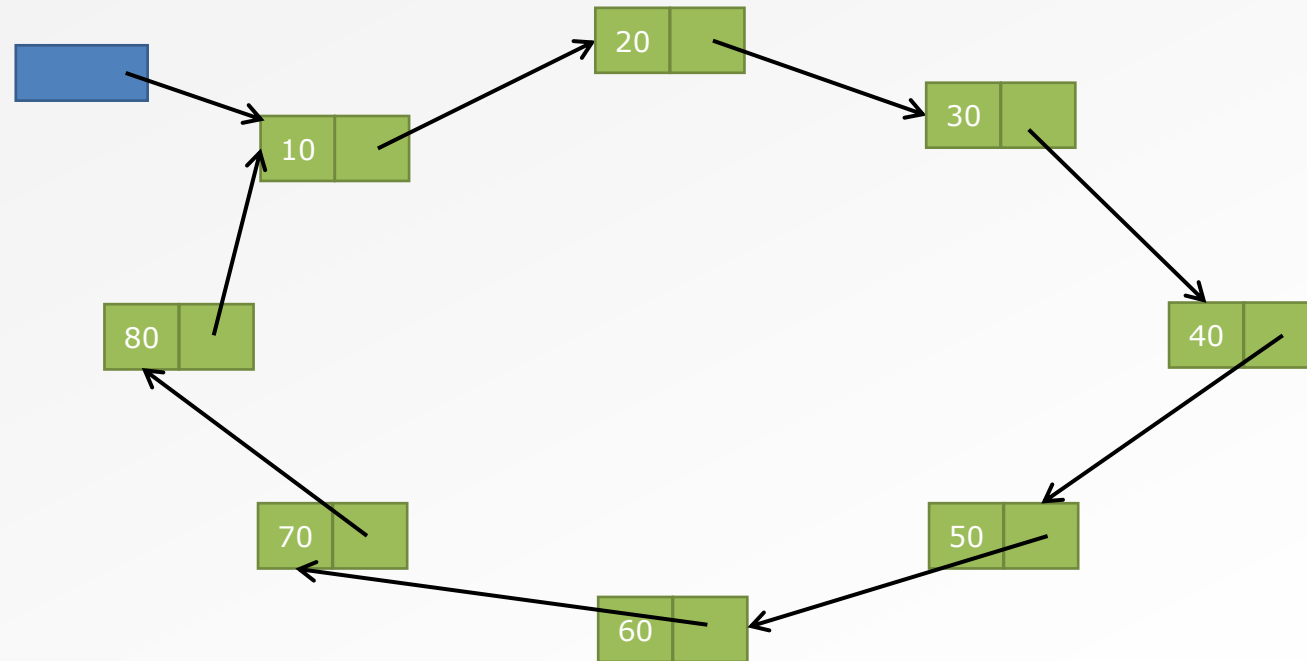


- Circular doubly-linked lists
  - Last node has next pointer pointing to first node
  - First node has prev pointer pointing to last node



# CIRCULAR LINKED LISTS

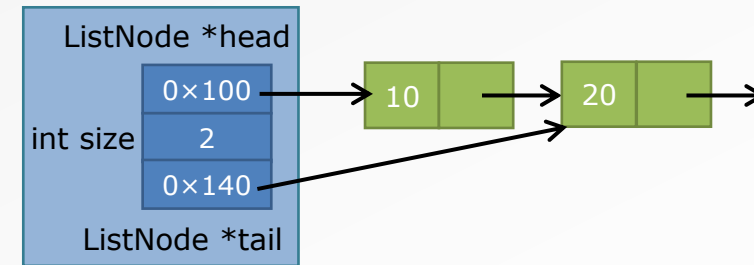
- Effectively we will have this (singly-linked version)



# LinkedList C STRUCT: ONE MORE THING

- Alternative version of our LinkedList struct

```
typedef struct _linkedlist{  
    struct ListNode *head;  
    struct ListNode *tail;  
    int size;  
} LinkedList;
```



- Tail pointer
  - Always points to the last node of the linked list
- Why is this useful?

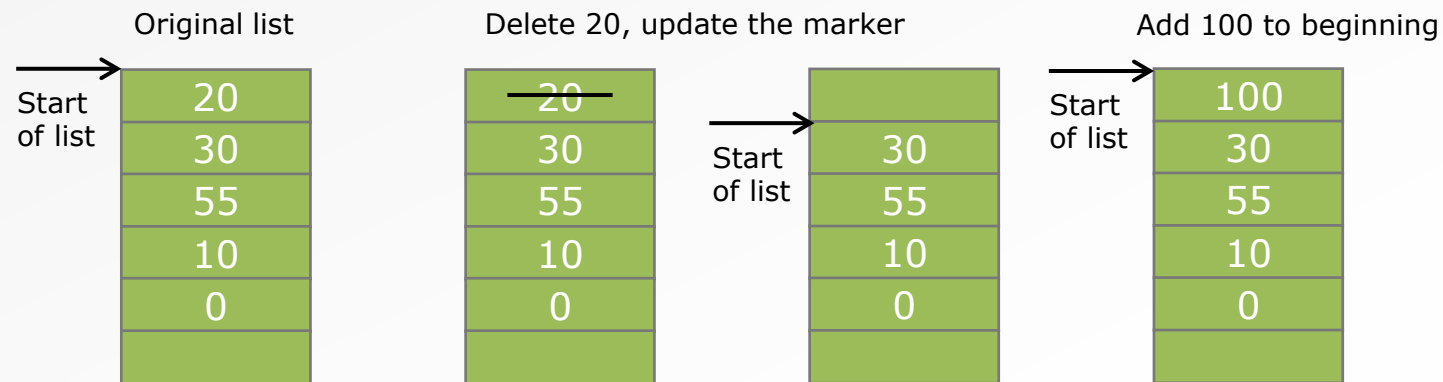
- sizeList() function
- Worked example: Using a linked list
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- **Array-based list storage**
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# ARRAY-BASED LISTS

- Back to arrays as list storage
- Try to implement “smarter” array-based list
- Avoid some of the problems we saw earlier with using arrays to store lists
  - Key is to minimize shifting operations

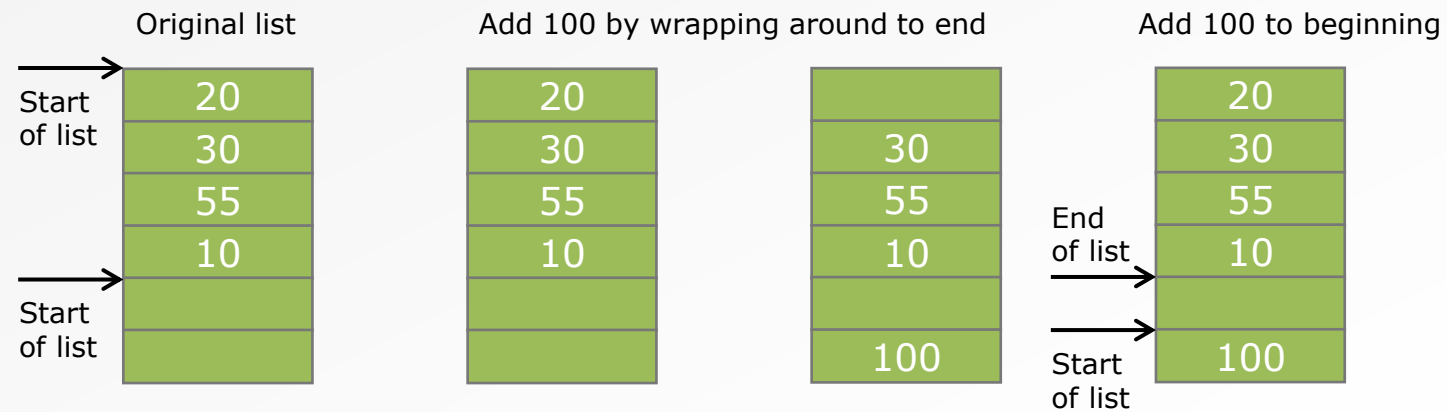
# ARRAY-BASED LISTS

- Delete an item from the beginning of a list
  - Key idea: Leave the empty space, do not shift everything down
  - In future, empty space gets used if we add to the beginning
  - Use a marker (or index number) to store location of first actual item
- Try: Delete 20 from index 0, then add 100 to index 0



# ARRAY-BASED LISTS

- Unfortunately, this doesn't help once you run out of space at the beginning
- Idea: Wrap around to the other end; circular array



# ARRAYS VS. LINKED LISTS

- Array-based lists allow random access
  - No need to traverse list until you reach the node index that you want
  - Much more efficient lookup compared to linked lists
- Previous slides show how clever tricks can be used to overcome some shortcomings of array-based list storage
- Important to know what arrays and linked lists are good and bad for



# ARRAYS VS. LINKED LISTS

- **Arrays**

- Efficient random access
- Difficult to expand, rearrange
- When inserting/removing items in the middle or at the beginning, computation time scales with size of list
- Generally, a better choice when data is immutable

- **Linked Lists**

- “Random access” can be implemented, but more inefficient than arrays
- Excellent for dynamic lists
- Easy to expand, shrink, rearrange
- Insert/remove operations only require fixed number of operations regardless of list size

- Know when to choose an array or a linked list

- sizeList() function
- Worked example: Using a linked list
- Linked list C struct
- More complex linked lists
  - Doubly-linked lists
  - Circular linked lists
  - Circular doubly-linked lists
- Array-based list storage
- Summary: Linked lists