

Its output is 0 when at least one of its input is 0. What gate is it?

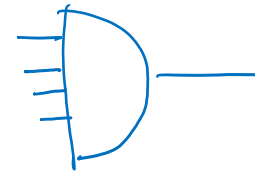
A. NOT

B. OR

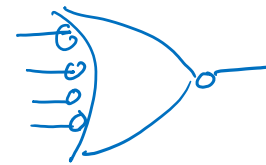
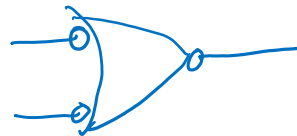
✓ C. AND



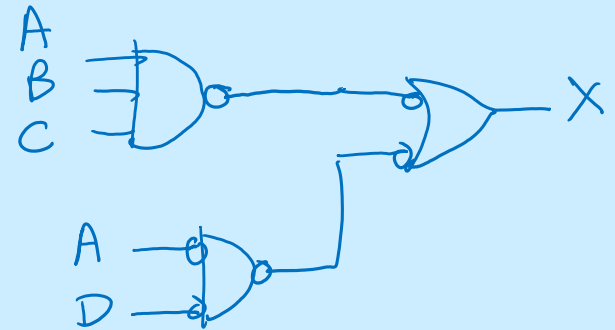
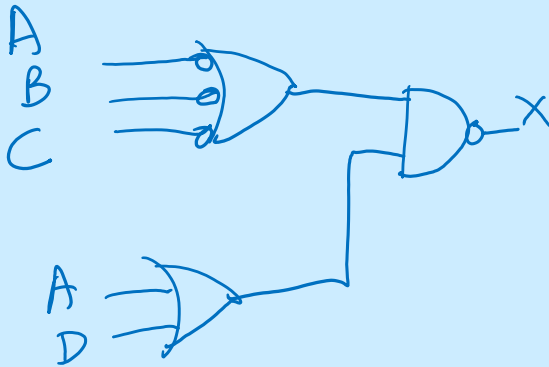
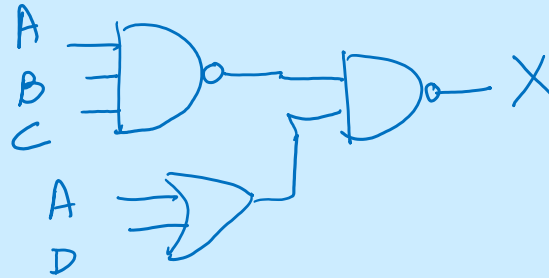
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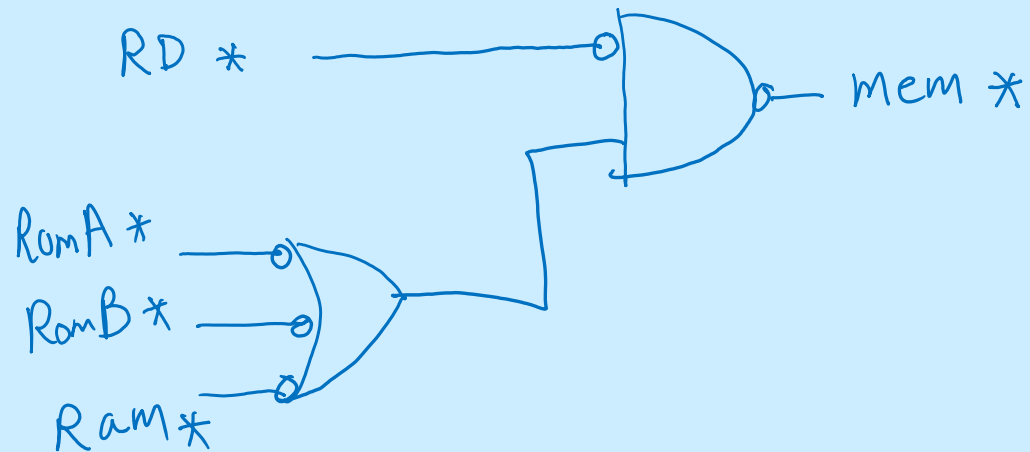
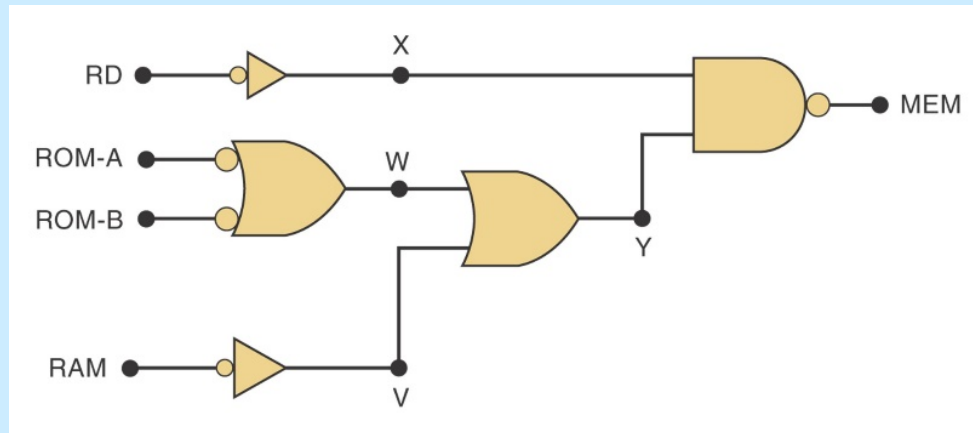
a) $X = [(ABC)' (A+D)]'$



b) $X=0$ requires (either $A=0$, or $B=0$, or $C=0$) and ($A=1$ or $D=1$)

c) $X=1$ requires ($A=B=C=1$) or ($A=D=0$)

Possible to draw simpler diagram



$$(A \oplus B)' = A \oplus B' = A' \oplus B$$

True or false?

 A. True

B. False

Construct the truth tables and compare:

A	B	$(A \oplus B)'$	$A \oplus B'$	$A' \oplus B$
0	0	1	1	1
0	1	0	0	0
1	0	0	0	0
1	1	1	1	1

Or use Boolean algebra:

$$(A \oplus B)' = A'B' + AB$$

$$A \oplus B' = A(B')' + A'(B') = AB + A'B'$$

$$A' \oplus B = (A')B' + (A')'B = A'B' + AB$$

Example: Construct the truth table for F:

$$F = W (X \oplus Y \oplus Z \oplus W') + (X \oplus Y \oplus Z)$$

W	X	Y	Z	F
0	0	0	0	
0	0	0	1	1
0	0	1	0	1
0	0	1	1	
0	1	0	0	1
0	1	0	1	
0	1	1	0	
0	1	1	1	1
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	

Continue:

$$F = W (X \oplus Y \oplus Z \oplus W') + (X \oplus Y \oplus Z) = (X \oplus Y \oplus Z)$$

W	X	Y	Z	F
0	0	0	0	
0	0	0	1	1
0	0	1	0	1
0	0	1	1	
0	1	0	0	1
0	1	0	1	
0	1	1	0	
0	1	1	1	1
1	0	0	0	
1	0	0	1	1
1	0	1	0	1
1	0	1	1	
1	1	0	0	1
1	1	0	1	
1	1	1	0	
1	1	1	1	1

How many 2-input XOR gates are needed to generate the parity bit from an 8-bit data?

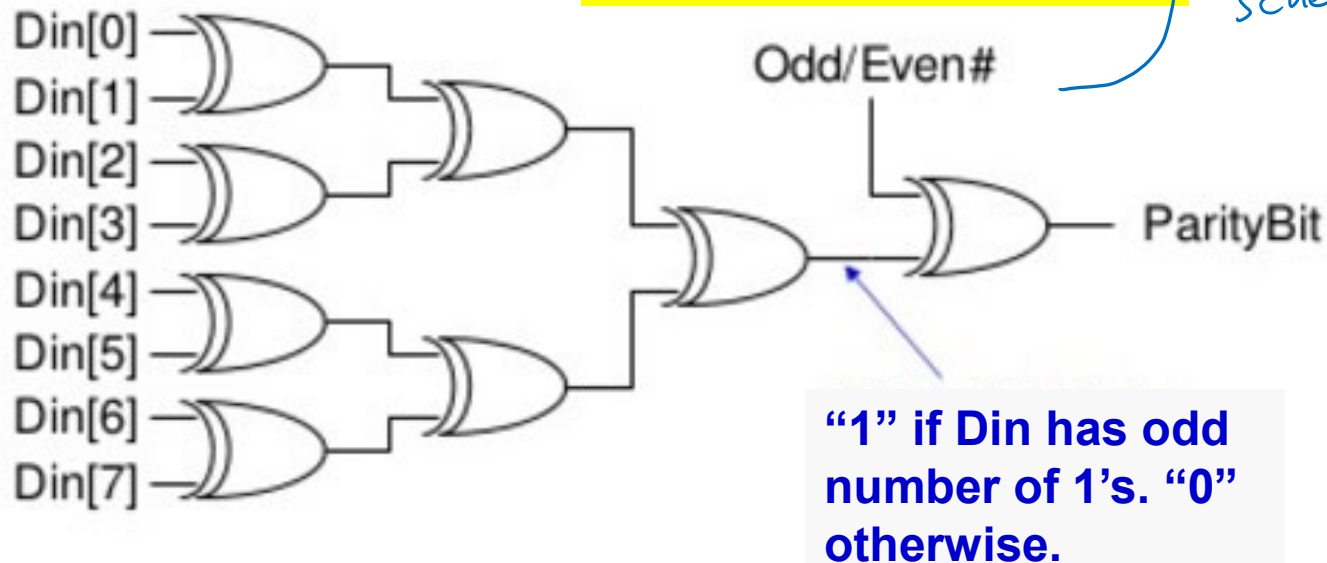
A. 4

B. 6

 **C. 8**

D. 10

An 8-Bit Parity Generator



For 7-bit parity, tie Din[7] to a '0'

Re-write the following in hexadecimal:

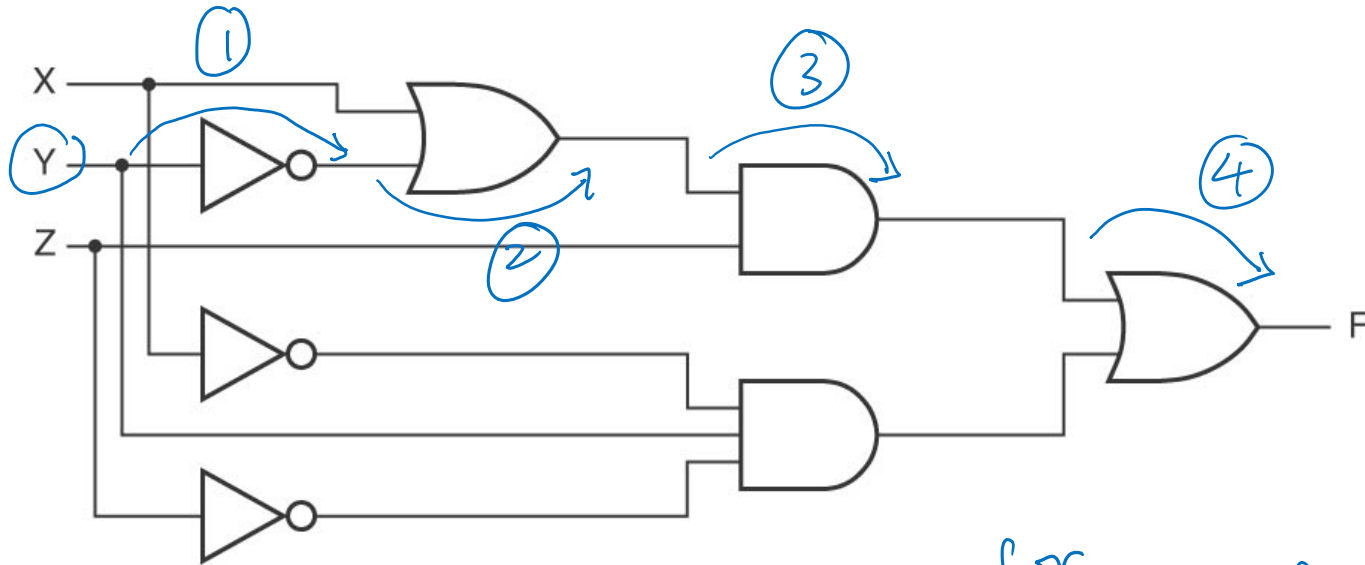
$$\mathbf{9(dec) + 7(dec) = 16(dec)}$$

$$9h + 7h = 10h$$

$$\mathbf{21(dec) + 7(dec) = 28(dec)}$$

$$15h + 7h = 1Ch$$

How many units of gate delay in total?



✓ **A. 4**

B. 5

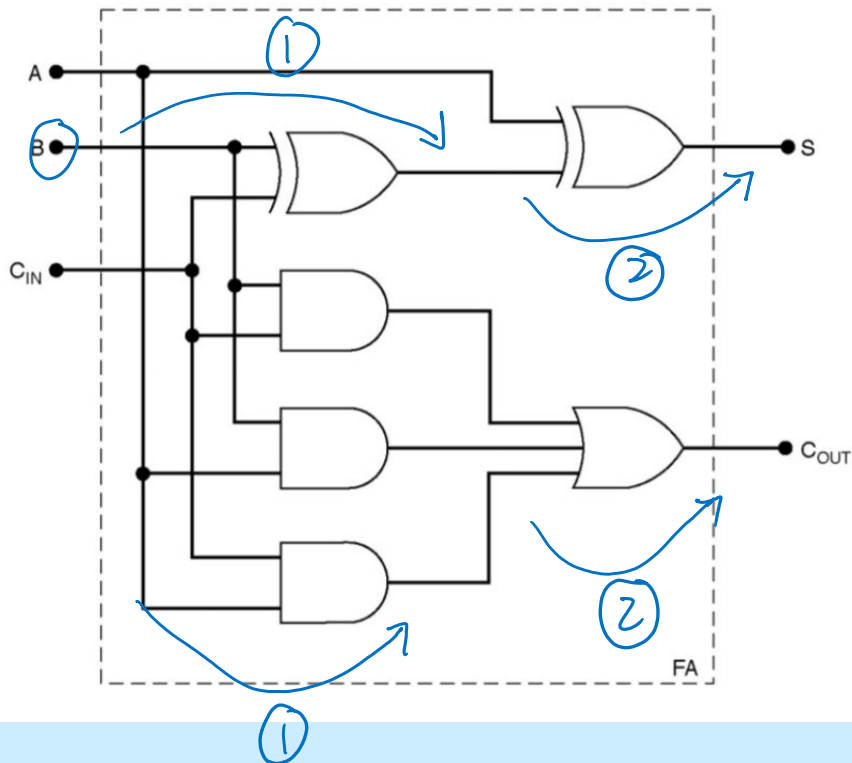
C. 6

D. 7

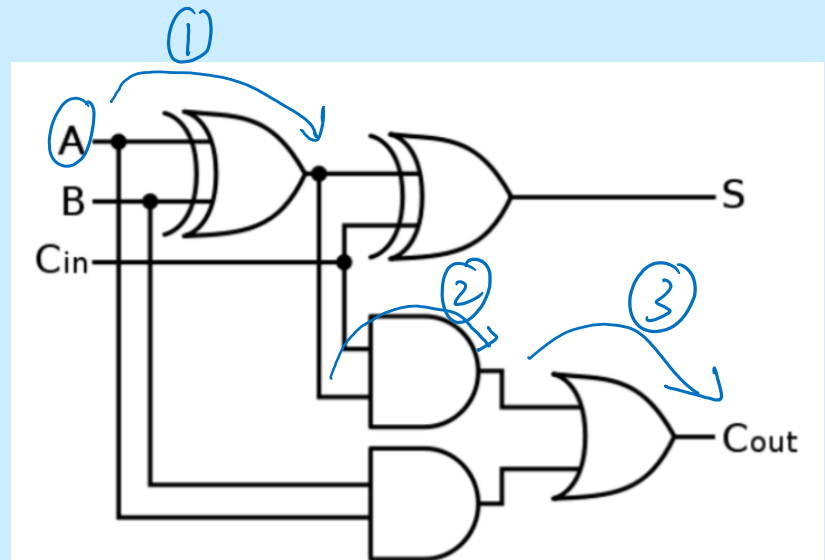
look for
longest path from
input to output

Both are full adders

$t_{pd} = 2$ units



$t_{pd} = 3$ units



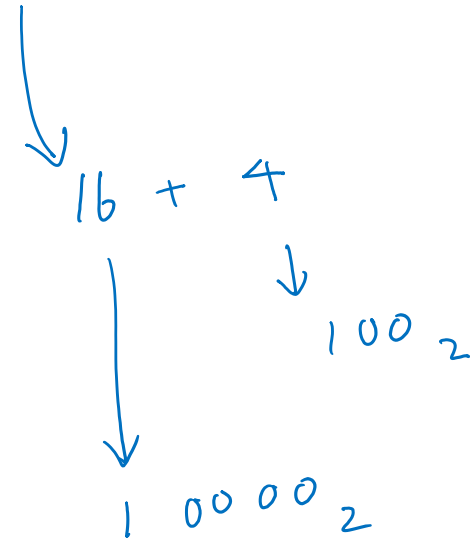
Give the sign-magnitude/2's complement representation of +20 (dec):

A. 1 0 1 0 0

B. 0 1 1 0 0

✓ C. 0 1 0 1 0 0

D. 1 0 1 1 0 0



**Give the sign-magnitude representation of
-20 (dec):**

A. 1 0 1 0 0

B. 0 1 1 0 0

C. 1 0 1 1 0 0

✓ D. 1 1 0 1 0 0

sign

magnitude

Give the 2's complement representation of
-20 (dec):

A. 1 0 1 0 0

B. 0 1 1 0 0

✓ C. 1 0 1 1 0 0

D. 1 1 0 1 0 0

10100

↓ 2's
comp

1 0 1 1 0 0



sign bit has

value of $-(2)^5 = -32_{10}$

$-32_{10} + 12_{10} = -20_{10}$

$1100_2 = 12_{10}$