

Lecture 3 key concepts

- Alternate logic symbols can be used to describe logic circuits more clearly
- With bubble: interpret as 0; without bubble: interpret as 1
- AND shape: interpret as “and”; OR shape: interpret as “or”
- XOR, XNOR, bitwise comparison, parity circuit
- Logic ICs: circuit connection diagram - physical pinout, power and ground
- Applied in Experiment 1

Which concepts are unclear to you after viewing L3?

- A. Alternate logic symbols
- B. XOR, XNOR
- C. Parity circuit
- D. Logic circuit connections
- E. None

Its output is 0 when at least one of its input is 0. What gate is it?

A. NOT

B. OR

C. AND

Will you be attending the concert?

“I won’t attend if I don’t have a free ticket and no one goes with me”

- Alternate symbol for 2-input OR gate

Alternatively, it is the same as

“I will attend if I have a free ticket or someone goes with me”

- Standard symbol for 2-input OR gate

Alternate symbols example 1

Given $X = [(ABC)' (A+D)]'$

How to draw the logic circuit diagram?

3 ways:

- a) Use standard logic symbols only**
- b) Show clearly how X can go Low using appropriate symbols**
- c) Show clearly how X can go High using appropriate symbols**

a) $X = [(ABC)' (A+D)]'$

b) $X=0$ requires (either $A=0$, or $B=0$, or $C=0$) and ($A=1$ or $D=1$)

c) $X=1$ requires $(A=B=C=1)$ or $(A=D=0)$

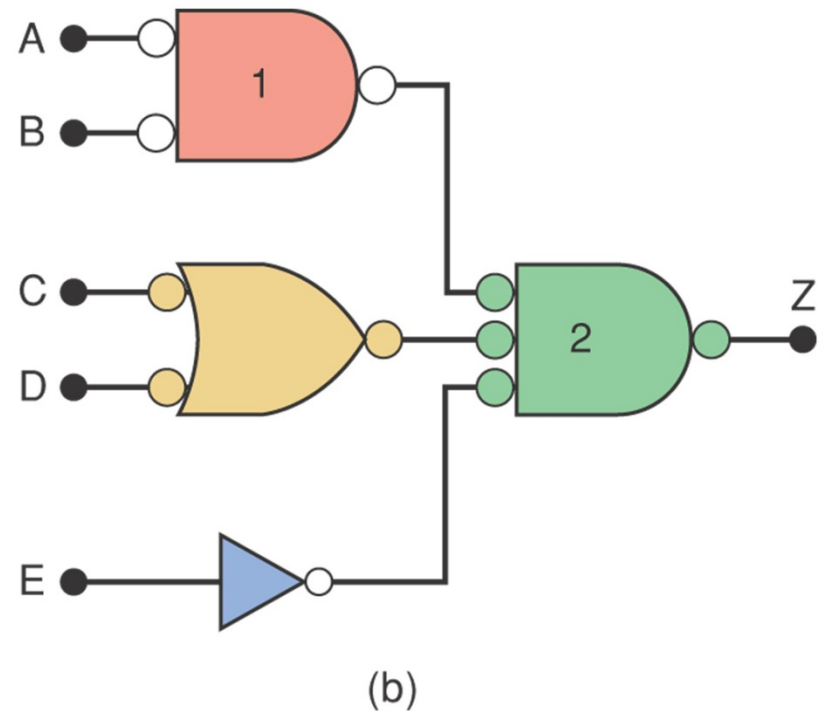
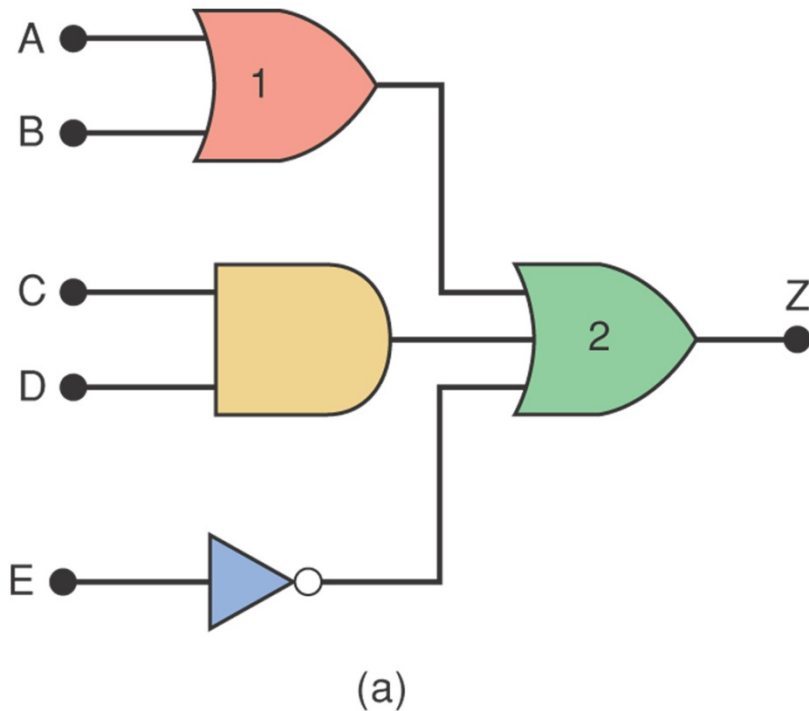
Alternate symbols example 2

Given another circuit $Z = (A+B)+CD+E'$

Figure shows how to make output Z goes

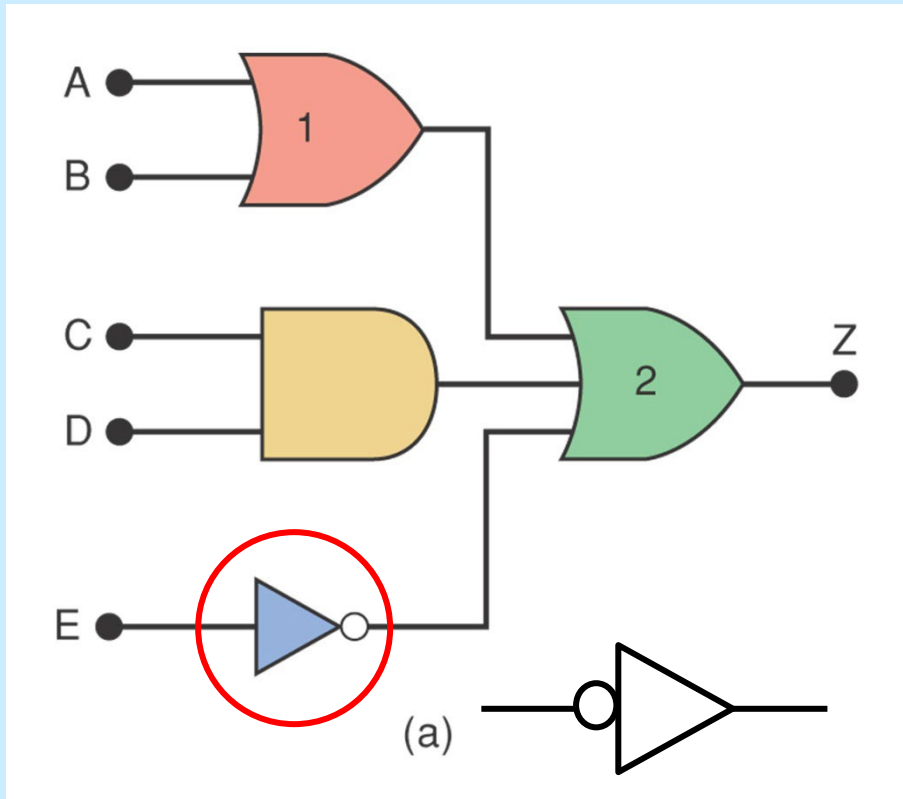
(a) High

(b) Low



Example 2 (cont)

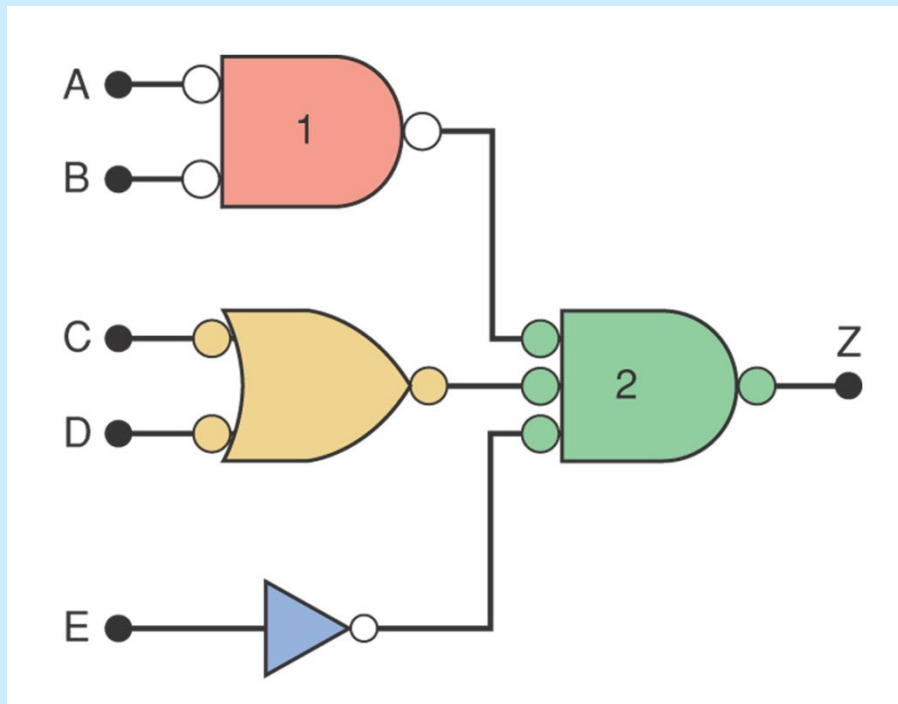
Interpretation of circuit diagram (a):



$Z = 1$ when
 $A=1$ or $B=1$,
or
 $C=1$ and $D=1$,
or
 $E=0$

Example 2 (cont)

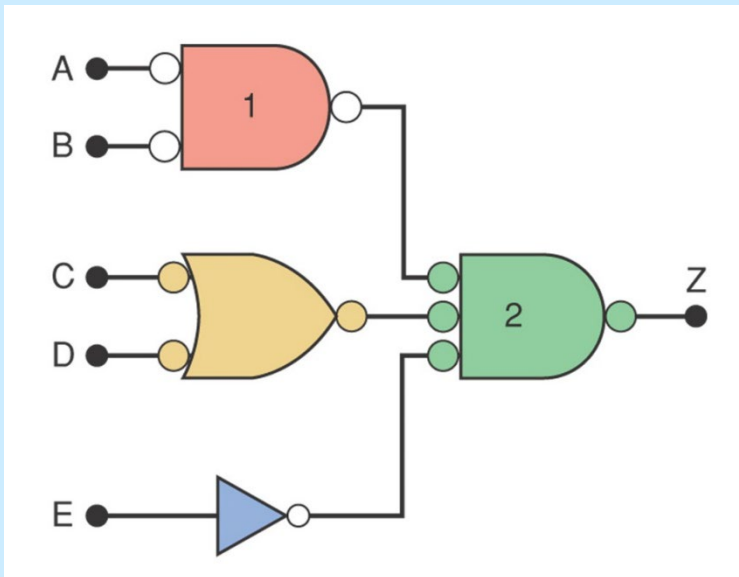
Interpretation of circuit diagram (b):



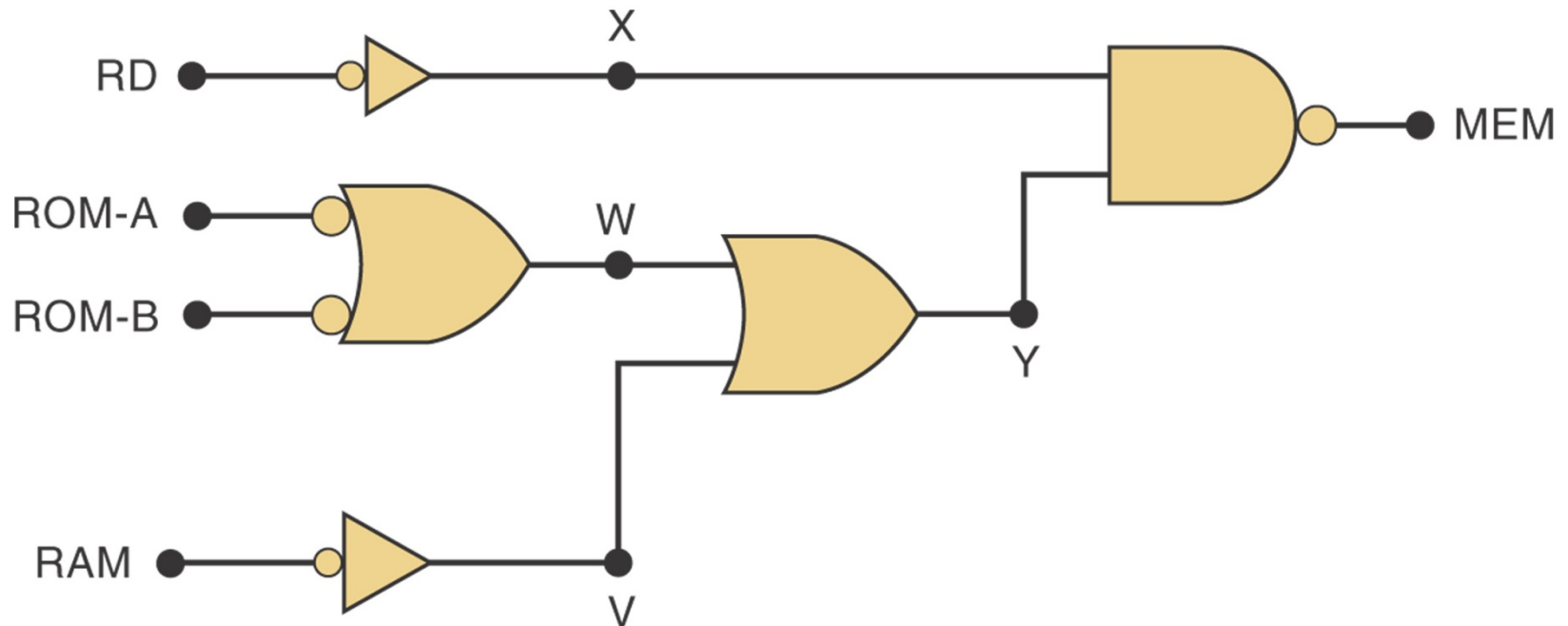
$Z = 0$ when
 $A=0$ and $B=0$,
and
 $C=0$ or $D=0$,
and
 $E=1$

Example 2 (cont)

What if we remove pairs of matched-bubbles?



Alternate symbols example 3

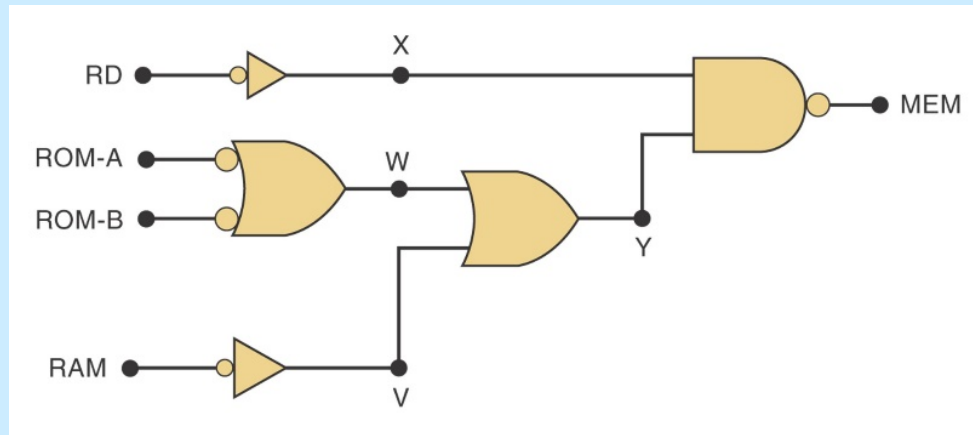


**RD=0 and (ROM-A=0 or
ROM-B=0 or
RAM=0)**

**will make
MEM = 0**

Figure 3-39 Tocci, Widmer, Moss. 10th ed.

Possible to draw simpler diagram



Exclusive OR/NOR

$$A \text{ XOR } B = AB' + A'B = A \oplus B$$

$$A \text{ XNOR } B = A'B' + AB = (A \oplus B)'$$

$$\begin{aligned} A \text{ XOR } B \text{ XOR } C &= (A \oplus B) \oplus C \\ &= A \oplus (B \oplus C) \end{aligned}$$

XOR is commutative and associative

$$(A \oplus B)' = A \oplus B' = A' \oplus B$$

True or false?

A. True

B. False

Example: Construct the truth table for F:

$$F = W (X \oplus Y \oplus Z \oplus W') + (X \oplus Y \oplus Z)$$

W	X	Y	Z	F
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	
0	1	0	1	
0	1	1	0	
0	1	1	1	
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	

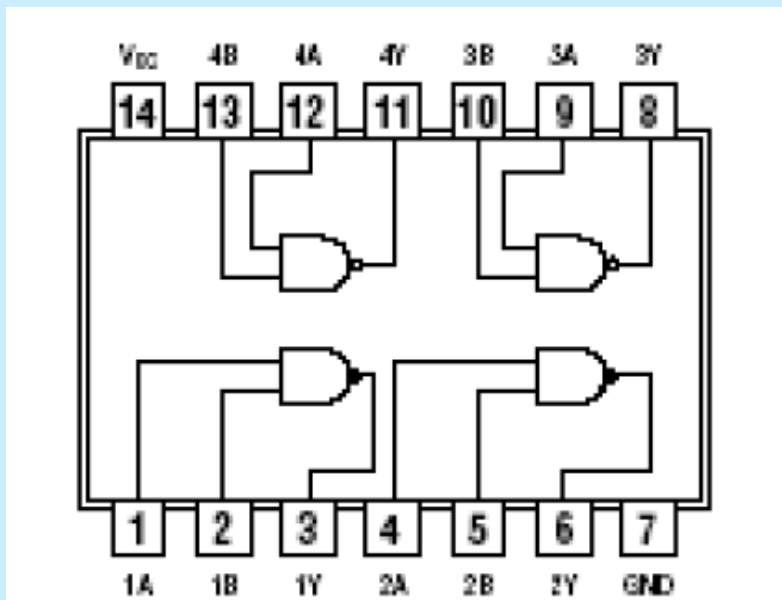
How many 2-input XOR gates are needed to generate the parity bit from an 8-bit data?

- A. 4**
- B. 6**
- C. 8**
- D. 10**

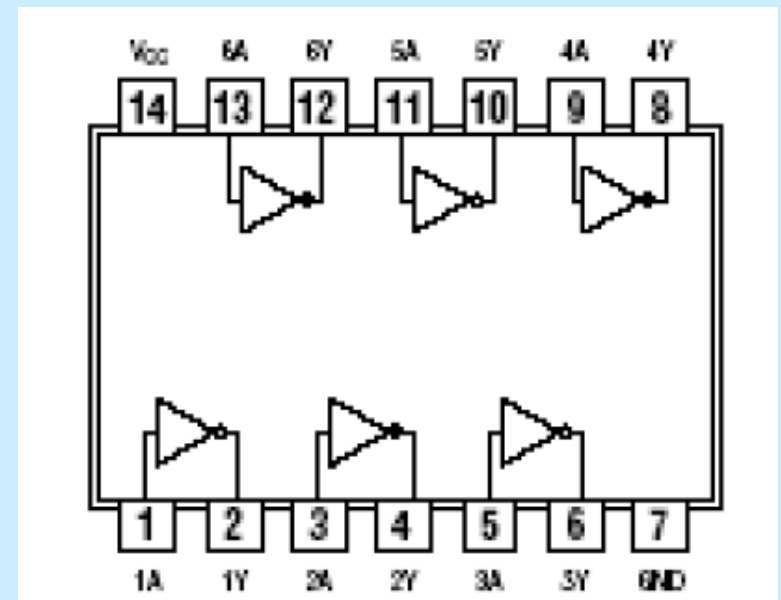
Logic devices

Component pin assignment

Quad-NAND



Hex-NOT



Logic devices (cont)

Circuit connection diagram

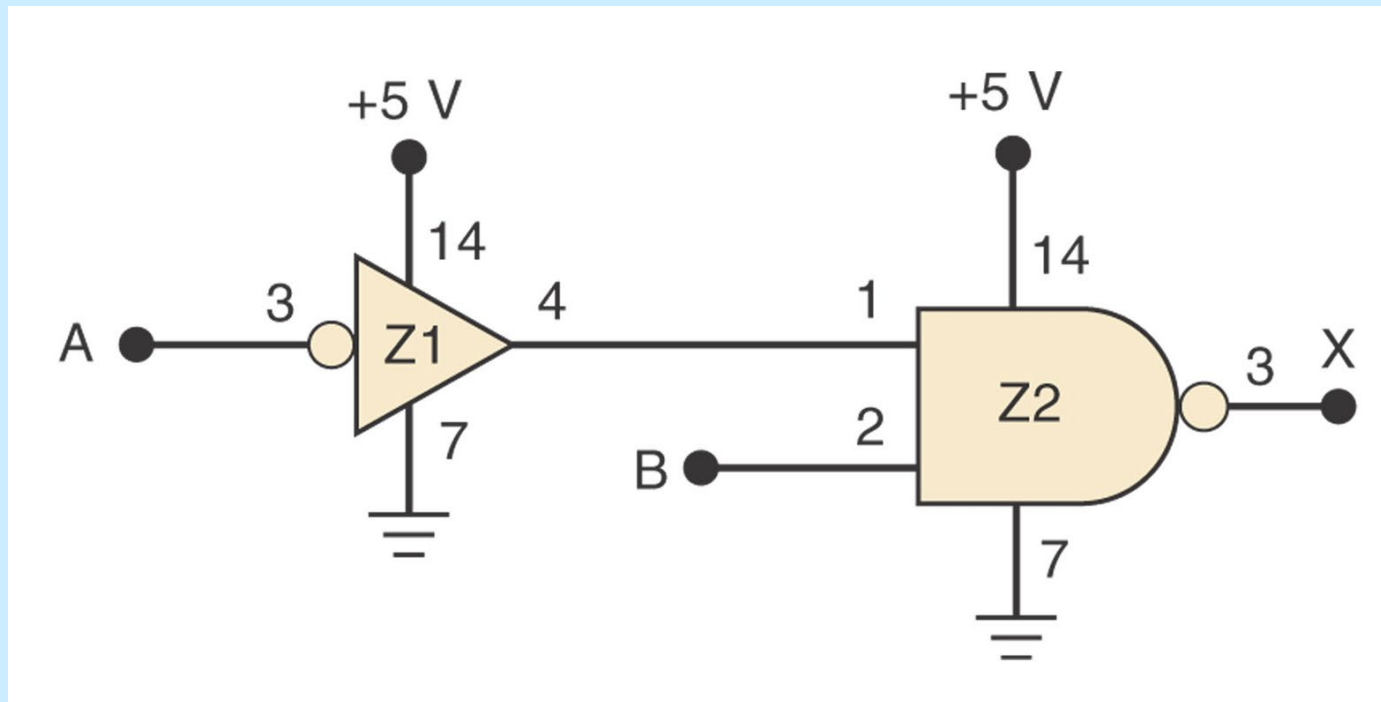


Figure 4-36 Tocci, Widmer, Moss. 10th ed.

Lecture 4 key concepts

- **Binary addition and subtraction**
- **Half adder and full adder**
- **Carry and sum**
- **4-bit parallel adder with 4 full adders**
- **Carry propagation**
- **Sign-magnitude representation**
- **2's complement representation**
- **<http://www.falstad.com/circuit/e-fulladd.html>**

Which concepts are unclear to you after viewing L4?

- A. Half adder, full adder
- B. Parallel adders
- C. Carry propagation
- D. Sign-magnitude
- E. 2's complement
- F. None

Carry and Sum

Logical addition and arithmetic addition are different:

$$1 + 1 = 1$$

Logical addition

$$1 + 1 = 1\ 0$$

Arithmetic addition

$$1 + 1 + 1 = 1\ 1$$

Arithmetic addition

$$\text{e.g. } 21(\text{dec}) + 7(\text{dec}) = 28(\text{dec})$$

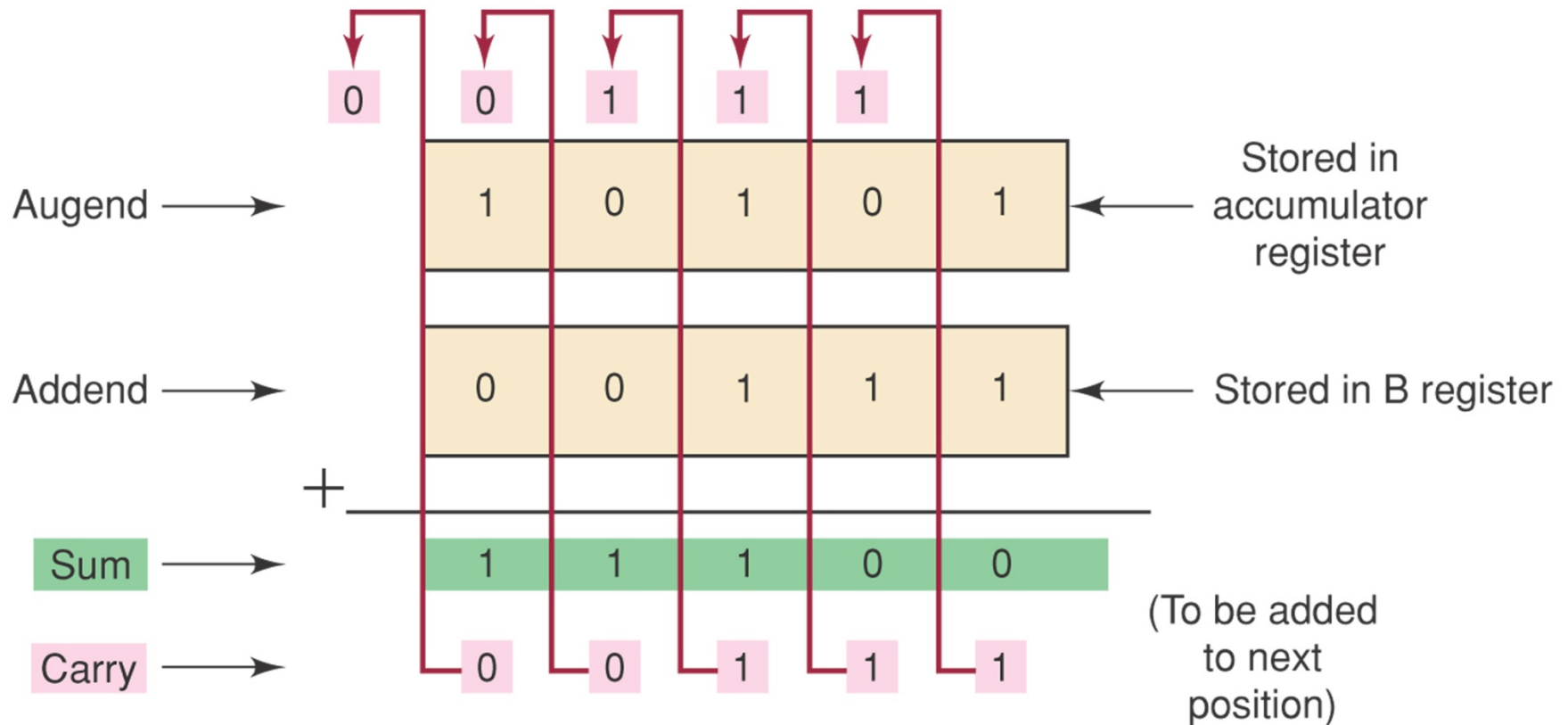


Figure 6-5 Tocci, Widmer, Moss. 10th ed.

$$\text{e.g. } 9(\text{dec}) + 7(\text{dec}) = 16(\text{dec})$$

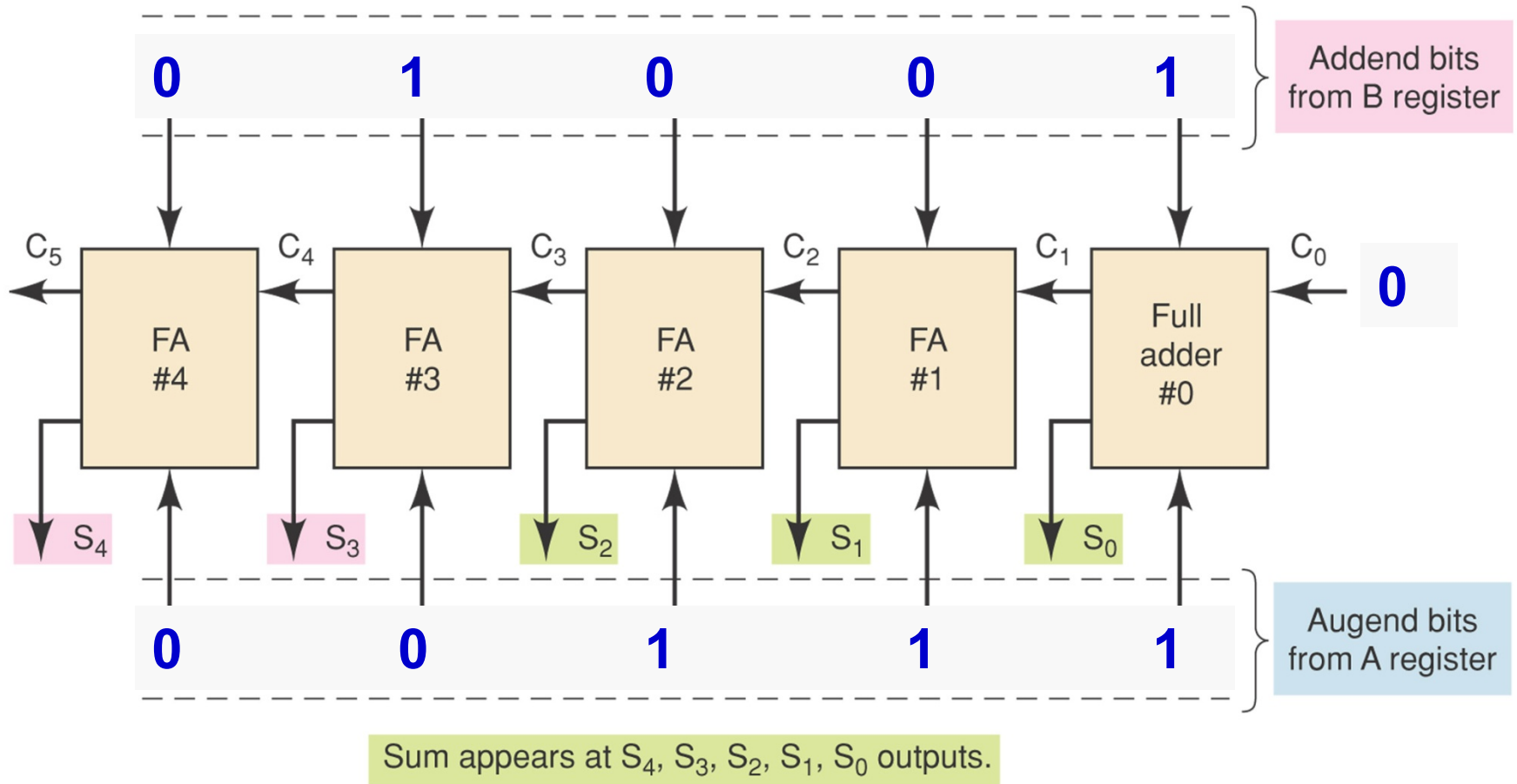


Figure 6-6 Tocci, Widmer, Moss. 10th ed.

$$\text{e.g. } 9(\text{dec}) + 7(\text{dec}) = 16(\text{dec})$$

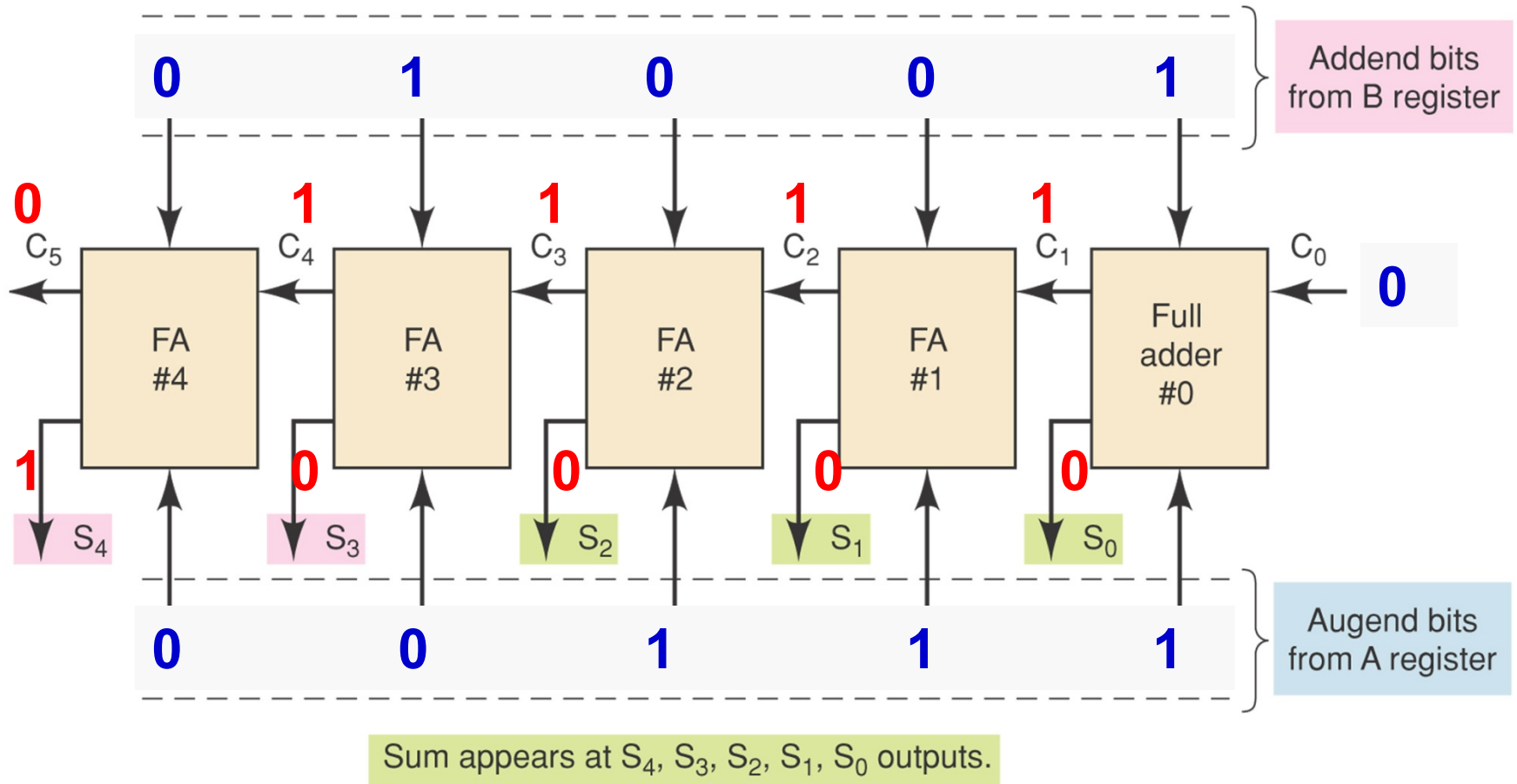


Figure 6-6 Tocci, Widmer, Moss. 10th ed.

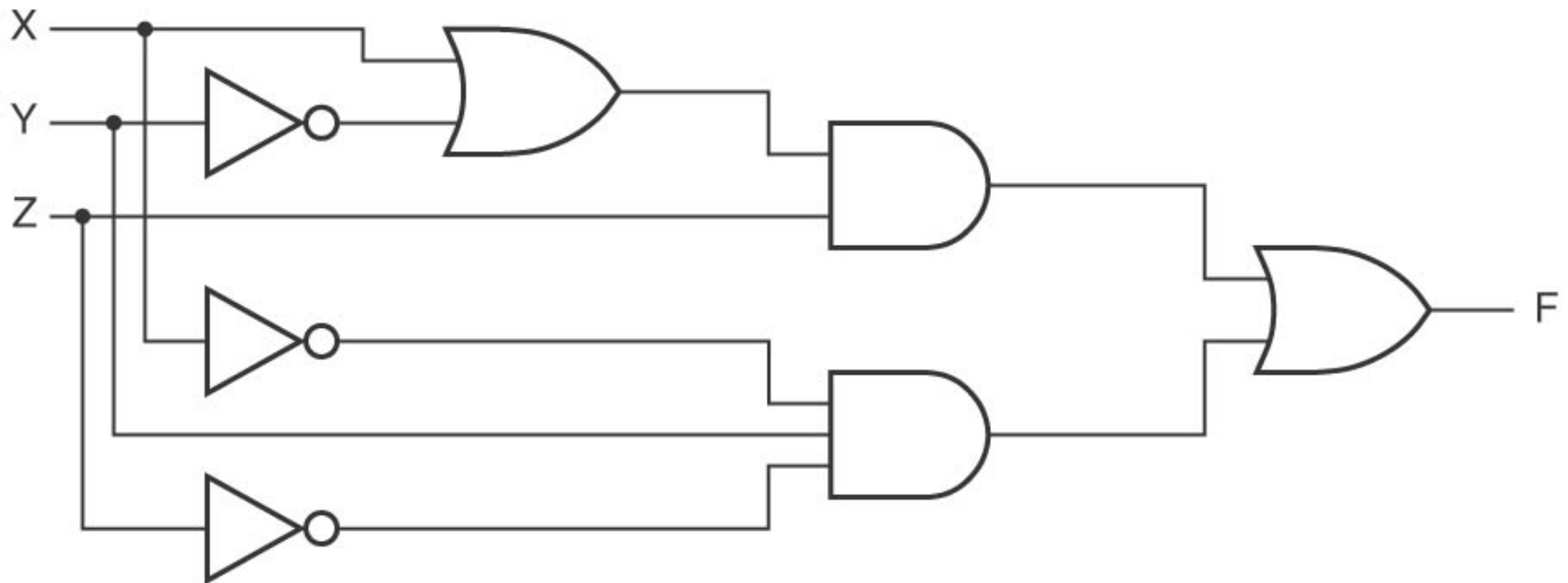
Re-write the following in hexadecimal:

$$9(\text{dec}) + 7(\text{dec}) = 16(\text{dec})$$

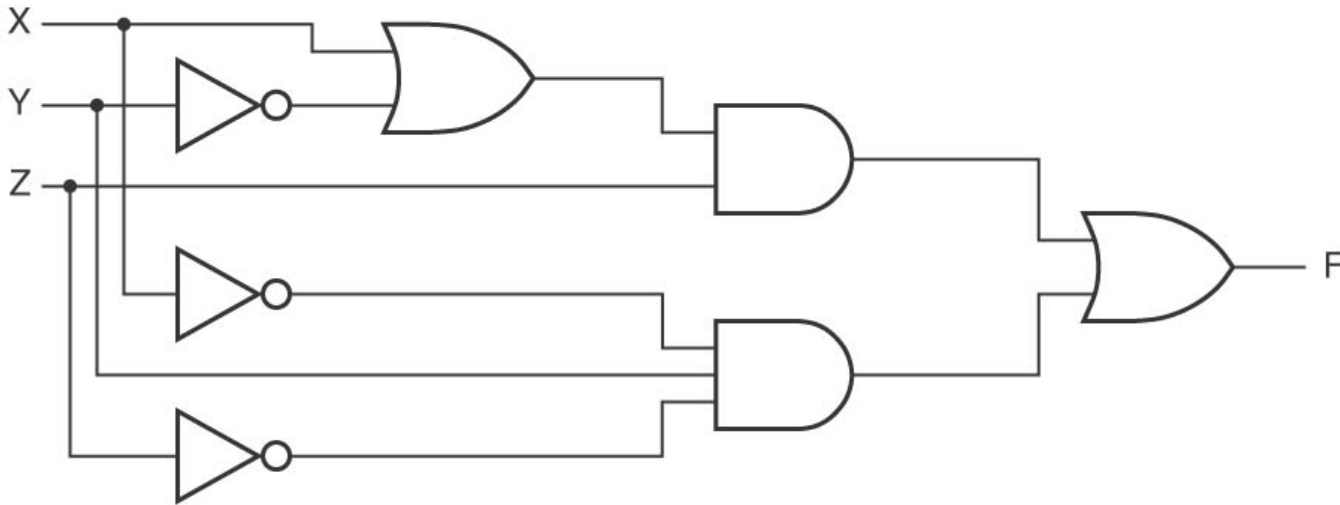
$$21(\text{dec}) + 7(\text{dec}) = 28(\text{dec})$$

Propagation delay example

How many units of gate delays in total from inputs X, Y, Z to output F?



How many units of gate delay in total?



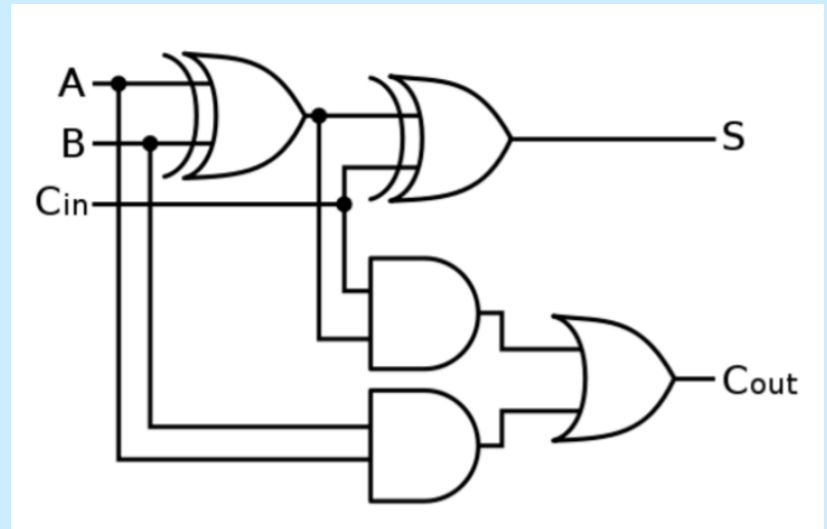
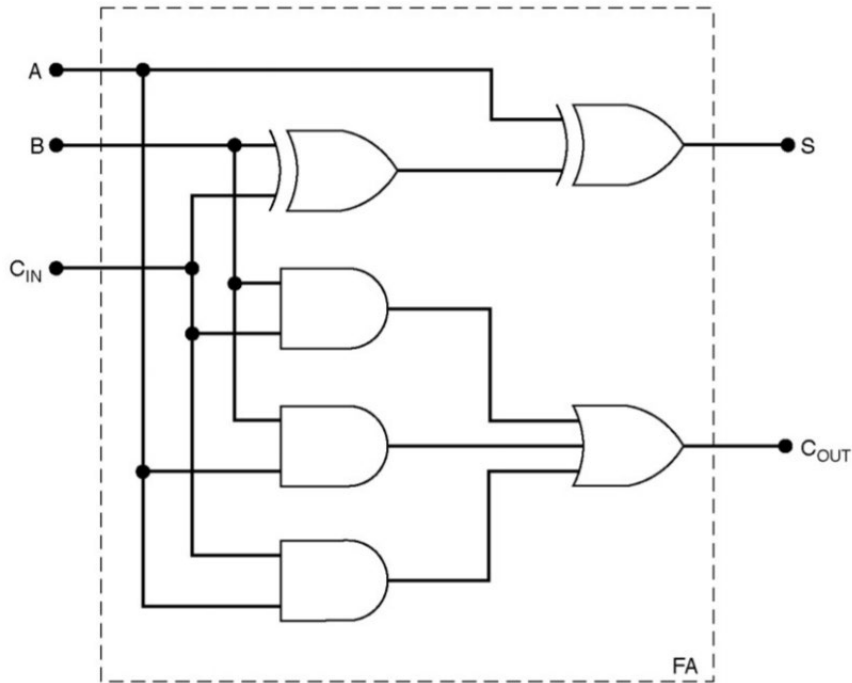
A. 4

B. 5

C. 6

D. 7

Do these circuits perform the same function?
Do they have the same propagation delays?



Give the sign-magnitude/2's complement representation of +20 (dec):

A. 1 0 1 0 0

B. 0 1 1 0 0

C. 0 1 0 1 0 0

D. 1 0 1 1 0 0

**Give the sign-magnitude representation of
-20 (dec):**

A. 1 0 1 0 0

B. 0 1 1 0 0

C. 1 0 1 1 0 0

D. 1 1 0 1 0 0

**Give the 2's complement representation of
-20 (dec):**

A. 1 0 1 0 0

B. 0 1 1 0 0

C. 1 0 1 1 0 0

D. 1 1 0 1 0 0

End of L4 summary