

Data Structures and Algorithms

Lecture 4: **Queues**

Department of Computer Science & Technology
United International College

Outline

- Queue ADT
- Basic operations of queue
 - enqueue, dequeue
- Applications of queue
- Implementation of queue
 - Array
 - Linked list

Queue ADT

- Like a stack, a *queue* is also a list.
- However, with a queue
 - insertion is done at one end
 - The rear
 - while deletion is performed at the other end.
 - The front



Queue Animation

- <http://liveexample.pearsoncmg.com/liang/animation/animation.html>
- Queues are known as **FIFO** (First In, First Out) lists.

Enqueue and Dequeue

- Primary operations: Enqueue and Dequeue
- Enqueue
 - insert an element at the rear of the queue
- Dequeue
 - remove an element from the front of the queue

Enqueue and Dequeue



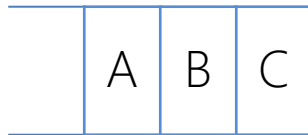
Empty queue



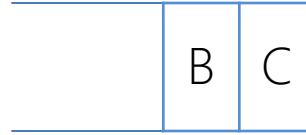
Enqueue(A)



Enqueue(B)



Enqueue(C)



Dequeue()



Dequeue()

Queue Applications

- Printer Queue
- Web Crawler
- System Buffer
- Any sequence maintained in a FIFO order

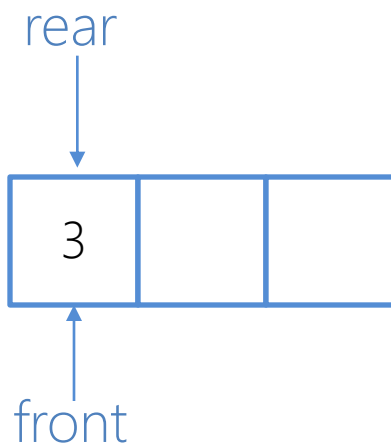
Implementation of Queue

- Recall the reason why we usually
 - implement a [list using links](#)?
 - implement a [stack using array](#)?

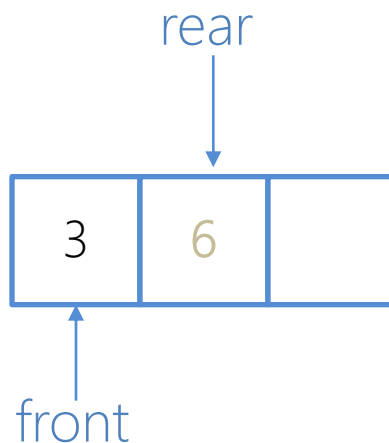
Topic		Array	Linked List
Efficiency	Enqueue		
	Dequeue		
space			

Queue Implementation Using Array

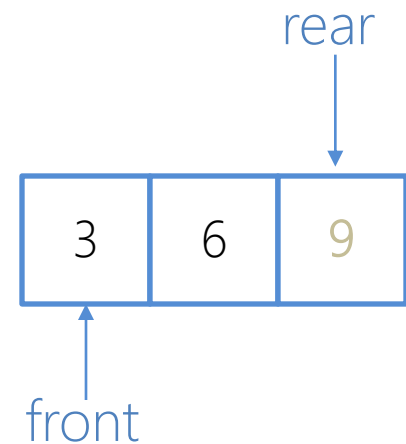
- There are several different algorithms to implement **Enqueue** and **Dequeue**
- Naive way: **Enqueue**
 - the **front index** is always fixed
 - the **rear index** moves forward in the array.



Enqueue(3)



Enqueue(6)

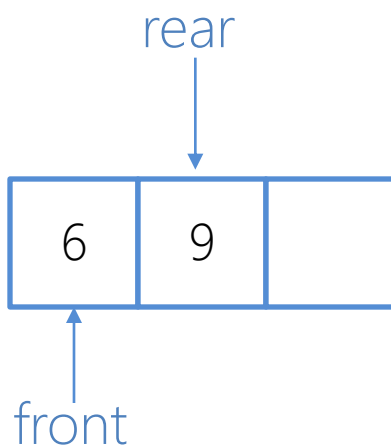


Enqueue(9)

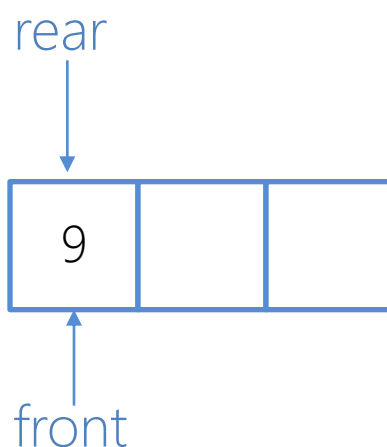


Queue Implementation Using Array

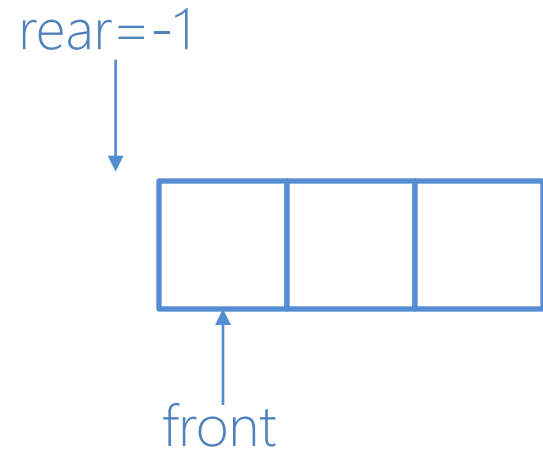
- Naive way: Dequeue
 - the front index is fixed
 - the element at the front the queue is removed
 - Move all the elements after it by one position.



Dequeue()



Dequeue()

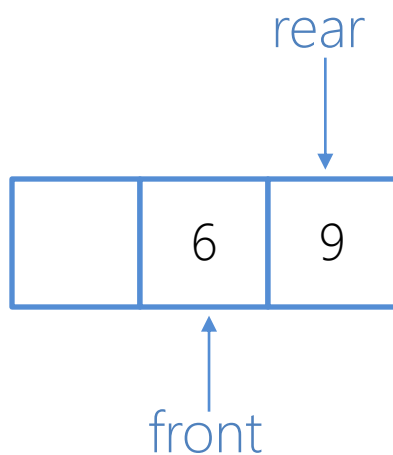


Dequeue()

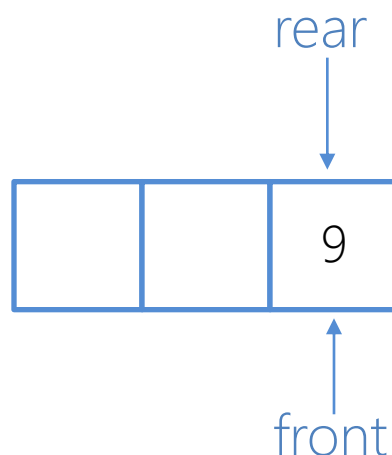
NO GOOD

A Better Array Implementation

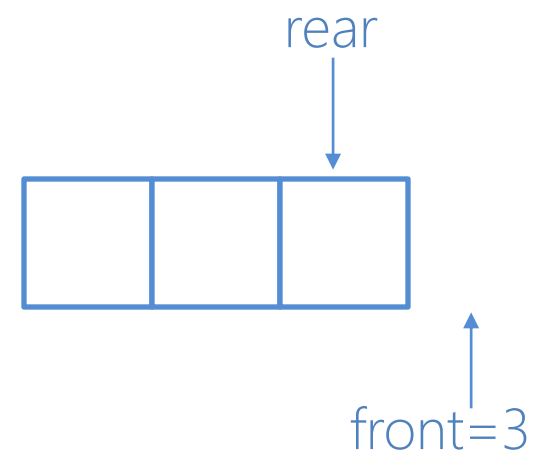
- When an item is **enqueued**, the **rear index** moves forward.
- When an item is **dequeued**, the **front index** also moves forward by one element



Dequeue()



Dequeue()

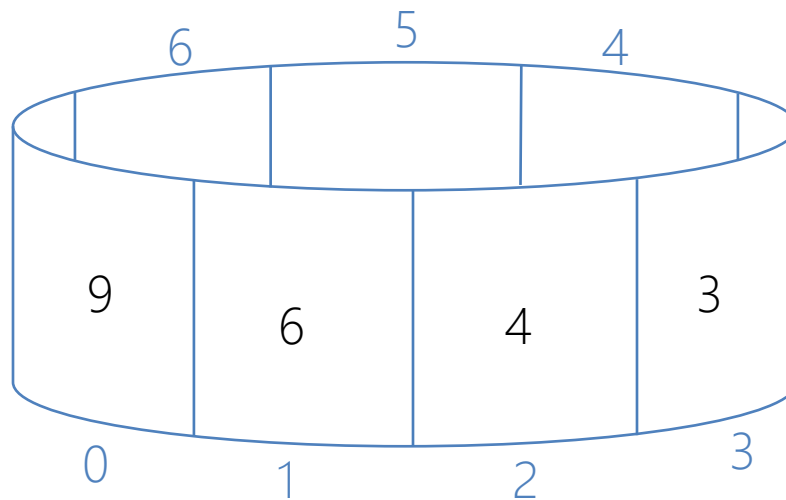


Dequeue()

Efficient...but
what is the
PROBLEM?

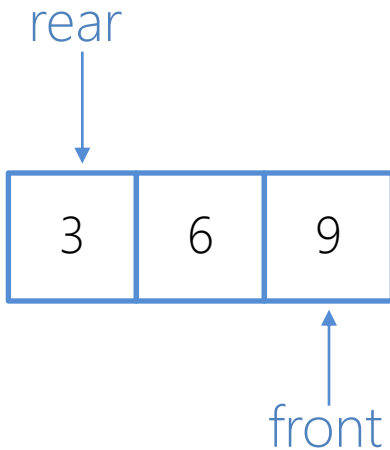
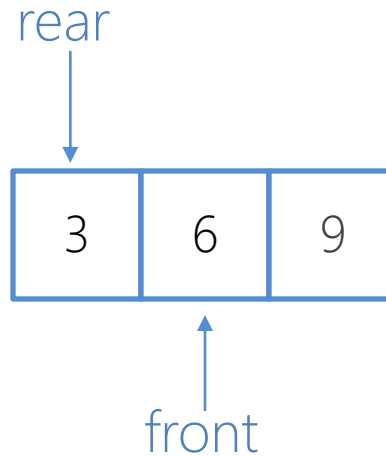
Final Solution: A Circular Array

- Circular array
 - When an element moves past the end of a circular array, it wraps around to the beginning

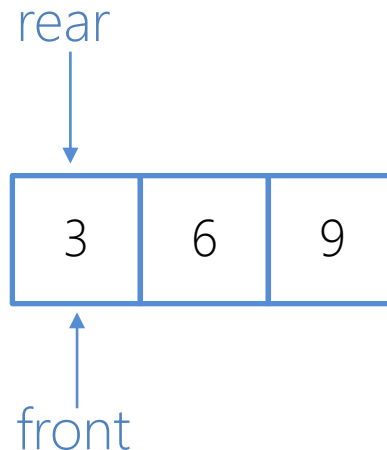


Index Growth: $0 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 0 \rightarrow \dots$

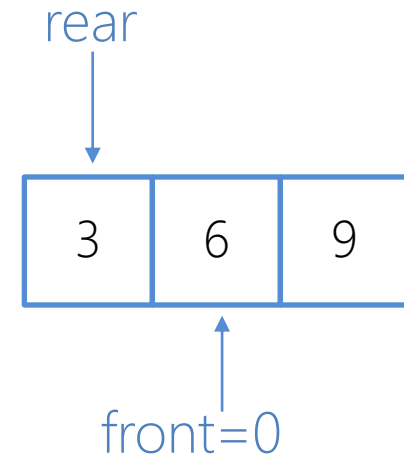
Deque in a Circular Array



Deque()

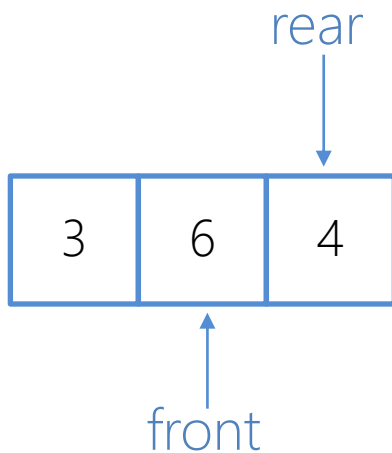
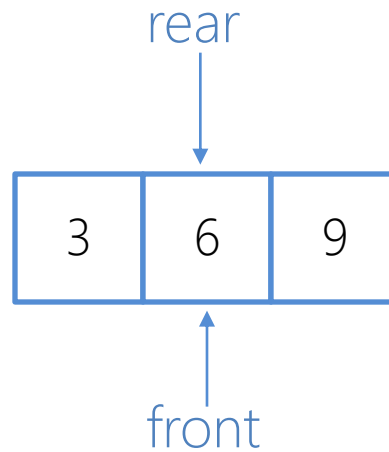


Deque()

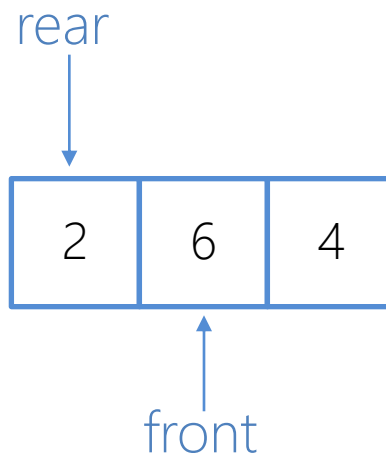


Deque()

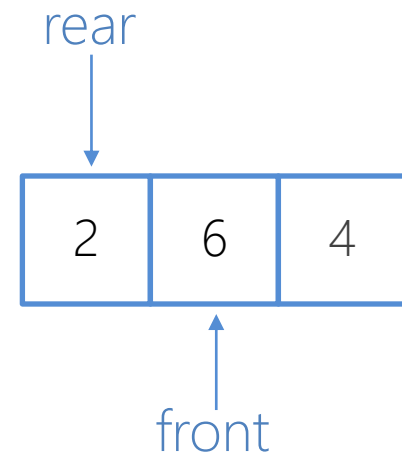
Enqueue in a Circular Array



Enqueue(4)



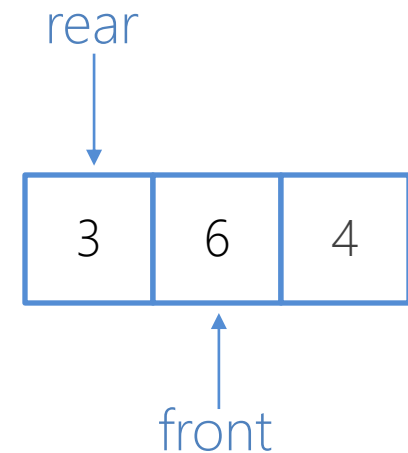
Enqueue(2)



Enqueue(1) Fails

Question to Ponder

- How to detect an **empty** or **full** queue using a circular array?
 - Empty
 - rear is **one position before** front
 - Full
 - rear is **one position before** front
 - Is this queue empty or full?



Question to Ponder

- How to detect an **empty** or **full** queue, using a circular array algorithm?

Use a **counter** which records **number of elements** in the queue.

Queue Implementation

- Data are stored in an array
 - **values**: the array of data items. The data can be of any type but we use **Double** for demonstration
 - **front**: index of the front
 - **rear**: index of the rear
 - **counter**: number of elements in the queue

Queue Implementation

Queue
<ul style="list-style-type: none">- values: Double[]- front: int- rear: int- counter: int
<ul style="list-style-type: none">+ Queue(int size)+ isEmpty(): boolean+ isFull(): boolean+ enqueue(double x): Double+ dequeue(): Double+ displayQueue(): void

Methods

- `public Queue(int size)`
 - Creates an empty queue whose capacity is *size*
- `public boolean isEmpty()`
 - Returns true if the queue is empty and false otherwise
- `public boolean isFull()`
 - Returns true if the queue is full and false otherwise

Methods

- `public Double enqueue(double x)`
 - Adds a new element with value x after the rear of the queue
 - Returns the new element if the operation is successful and null otherwise
- `public Double dequeue()`
 - Removes and returns the (old) front element of the queue
 - Returns null if the operation fails
- `public void displayQueue()`

```
front-> |          -2.0000          |  
        |          3.0000          |  
        |          1.0000          |  
        |          8.0000          |<-rear
```

The Constructor

```
public Queue(int size) {  
    values = new Double[size];  
    front = 0;  
    rear = -1;  
    counter = 0;  
}
```

Why?
Any other valid
initialization values?

Enqueue

```
public Double enqueue(double x) {  
    if(isFull())  
        return null;  
    rear = (rear + 1) % values.length;  
    values[rear] = Double.valueOf(x);  
    counter ++;  
    return values[rear];  
}
```

Circular
index
increase

Using Queue

```
public static void main(String[] args) {  
    Queue myQueue = new Queue(4);  
    System.out.println(myQueue.isEmpty());  
    myQueue.enqueue(-2);  
    myQueue.enqueue(3);  
    myQueue.enqueue(1);  
    System.out.println("The queue has 3 items: -2, 3, 1");  
    myQueue.displayQueue();  
    myQueue.enqueue(8);  
    myQueue.enqueue(6);  
    System.out.println("The queue has 4 items: -2, 3, 1, 8");  
    System.out.println(myQueue.isFull());  
    myQueue.displayQueue();  
    myQueue.dequeue();  
    myQueue.dequeue();  
    System.out.println("The queue has 2 items: 1, 8");  
    myQueue.displayQueue();  
    myQueue.dequeue();  
    myQueue.dequeue();  
    myQueue.dequeue();  
    System.out.println("The queue is empty:");  
    myQueue.displayQueue();  
}
```

Using Queue

```
public static void main(String[] args) {  
    Queue myQueue = new Queue(4);  
    System.out.println(myQueue.isEmpty());  
    myQueue.enqueue(-2);  
    myQueue.enqueue(3);  
    myQueue.enqueue(1);  
    System.out.println("The queue has 3 items: -2, 3, 1");  
    myQueue.displayQueue();  
    myQueue.enqueue(8);  
    myQueue.enqueue(6);  
    System.out.println("The queue has 4 items: -2, 3, 1, 8");  
    System.out.println(myQueue.isFull());  
    myQueue.displayQueue();  
    myQueue.dequeue();  
    myQueue.dequeue();  
    System.out.println("The queue has 2 items: 1, 8");  
    myQueue.displayQueue();  
    myQueue.dequeue();  
    myQueue.dequeue();  
    myQueue.dequeue();  
    System.out.println("The queue is empty:");  
    myQueue.displayQueue();  
}
```

```
true  
The queue has 3 items: -2, 3, 1  
front-> |          -2.0000          |  
         |          3.0000          |  
         |          1.0000          |<-rear  
The queue has 4 items: -2, 3, 1, 8  
true  
front-> |          -2.0000          |  
         |          3.0000          |  
         |          1.0000          |  
         |          8.0000          |<-rear  
The queue has 2 items: 1, 8  
front-> |          1.0000          |  
         |          8.0000          |<-rear  
The queue is empty:  
Empty queue!
```

Note

- The main function on page 26-27 is for demonstration.
- When you write your own main function, you should **design testing cases** like the ones you've learnt in the OOP course.

Task

- Complete *Queue.java* which implements the queue class
 - The class is defined on slide 21.
 - A *main* function has been given for the class which tests 5 functions: enqueue, dequeue, isEmpty, isFull, displayQueue
- Submit *Queue.java* to iSpace.