# Online Appendix

## A Discussions on generalizations

The logic in the main text can be generalized. In particular, the discrepancy between the IU outcome (Section 3.1) and the complete-market EU outcome (Section 3.2) would generalize to broader situations. The logic is simple. The IU outcome, by construction, has no structure that makes the marginal rate of substitution (between a state that involves the MIT shock and a state that does not) equal across consumers. The complete-market EU outcome has this equivalence built in, as long as the solutions for the consumers' problems are interior, no matter how small the shock probabilities are.

The equivalence results in Section 3.3 requires some qualifications in a more general setting. First, one can generally find an incomplete-market EU setting that delivers the same outcome as the IU allocation in the probability-zero limit; one can simply construct an EU setting where all contingency on the MIT-shock state is taken away and the rest of the asset structure is the same as in the IU economy. The EU allocation constructed in this manner would converge to the IU allocation (if the limit exists), as long as the equilibrium in the constructed EU economy and the equilibrium in the IU economy are both unique and the decision rules are continuous with respect to the change in environment. Second, multiple incomplete-market EU settings that are consistent with a particular IU allocation can exist. Appendix C constructs an EU economy where the asset-market structure differs from the setting of Section 3.3 and it still delivers the allocation in Section 3.1 as a limit. (Appendix C considers a bond economy.) Third, what kind of market incompleteness in the EU economy corresponds to the IU outcome depends on what kind of asset structure is assumed in the IU setting.

To see the third point more formally, Appendix D modifies the model in Section 3 and repeats the analysis. The modification in Appendix D is that the consumers' equilibrium savings are nonzero, so that carrying assets (and liabilities) into the irregular state is possible. Appendix D shows that for the limit equivalence to hold, the asset holding that can be carried into the irregular state has to be consistent between the EU economy and the IU economy.

Note the values of the assets also have to be recalculated carefully when computing each consumer's asset holding upon the occurrence of the MIT shock. In models with a simple asset structure as in Huggett (1993) and Aiyagari (1994), reevaluating the assets that the consumers can carry over to the MIT-shock state is fairly straightforward. Young (2004) is such an example, where Aiyagari's (1994) model is extended to incorporate an endogenous job search.

However, one has to be more careful in a more complex economy such as Krusell et al.'s (2010). Mukoyama (2013) is an example of an MIT-shock analysis of such a model. There,

<sup>&</sup>lt;sup>1</sup>One can use a similar logic as the one used for the proof of Proposition 10 in Krusell et al. (2011).

first, reevaluating the stock (the ownership value of firms) is necessary when the government policy changes, because the stock price jumps when the policy change (which is treated as an MIT shock) occurs.

In addition, in Mukoyama (2013), making an assumption about the composition of each consumer's portfolio before the MIT shock is necessary. When consumers don't anticipate the policy change, they are indifferent between which asset to hold in an IU economy, because the return structures are identical. However, because one asset incurs capital gain/loss with the policy change whereas the other does not, each consumer's asset holding after an MIT shock is affected by the portfolio composition before the shock. Mukoyama (2013) assumes a proportional portfolio (i.e., all consumers have the same portfolio ratio) before the shock. The same consideration applies in Kaplan et al. (2018).<sup>2</sup> This assumption may not be appropriate in interpreting the experiment as a limit of an EU economy, if the portfolio decision in the corresponding EU economy is different from the proportional rule. Boar and Midrigan (2020) also implicitly assume a proportional portfolio, because their setting features a financial intermediary that combines different assets into one asset that consumers hold.

Another potential situation where a particular care is necessary in reevaluating the asset upon an MIT shock is when some consumers default on their debt under certain states. In such a case, the balance of asset and liability may not carry over into certain specific states.

In sum, from a practical viewpoint, three principles must be followed when an MIT-shock analysis is employed. First, one must recognize that in the background EU economy, the state-contingent claim to the MIT shock is missing. Second, the assets that can be carried into the MIT-shock state in an IU economy have to be consistent with the contingency description in the corresponding EU economy. Third, when an asset is carried into the MIT-shock state in an IU economy, the value of an asset has to be carefully reevaluated.

## B Implications

In the context of policy design, if one believes a particular event is truly unanticipated, the MIT-shock analysis using an IU economy framework, as in Section 3.1, can be a useful benchmark.<sup>3</sup> In this case, the analysis in Section 3 has some practical implications. In such an environment, because the background EU economy is an incomplete-market economy, the IU allocation with MIT shocks suffers from an inherent inefficiency, even if the IU economy appears efficient absent MIT shocks. Ex-post government interventions, such as transfers to the most affected sectors and consumers, can be justified from an ex-ante Pareto-efficiency perspective in the corresponding EU economy. In other words, this paper reconciles the apparent need for the government intervention of the IU economy ex post, even when the IU economy appears efficient before the shock, by showing the background EU economy is

<sup>&</sup>lt;sup>2</sup>See their footnote 23.

<sup>&</sup>lt;sup>3</sup>Alternatively, one can imagine a situation where writing a contract with many contingencies is costly, as in Dye (1985).

indeed inefficient.

From a purely theoretical perspective, the lesson is that one has to be careful when conducting an analysis of an economy after an MIT shock. Recall that the outcomes after the MIT shock and the small-probability limit of a complete-market EU model are different. Given that the effect of the missing market is typically distributional, the (positive) aggregate consequences are often unaffected by the underlying assumptions on the asset market if Gorman preferences are assumed. Even with Gorman preferences, however, in an environment where the markets have other imperfections, such as market power, sticky prices, and search frictions, the positive predictions can be affected. Many macroeconomic analyses consider a complete-market outcome as a benchmark, and one has to be aware that the analysis of the MIT shock may not deliver an approximate solution to this benchmark scenario even when the probability is small. As I discussed in Appendix A, even with an analysis that explicitly treats market incompleteness, the modeling decision of what asset can be carried into the shock state would have a nontrivial effect on the ex-post outcome.

In conducting normative analysis, the asset distribution after the shock can have a profound effect on the conclusions concerning the welfare effects of the shocks to individuals. In the example in Sections 3.1 and 3.2, having an Arrow security to carry into the after-the-shock state would change the individual welfare ex post. For example, in Mukoyama (2010), after establishing general results that allows for an arbitrary wealth distribution after the shock, I provide an example under the implicit assumption that the consumers are allowed to bring the asset ("trees") into the post-shock state, whereas they cannot bring in other securities. As I argued in Appendix A (and Appendix D), the limit result can differ depending on what kind of assets can be carried into the state after the shock. In this sense, the implicit assumption in that example (that no assets other than the trees can be brought in) is not innocuous when discussing the distributional effect of policy from a normative perspective.

The fact that an MIT shock "adds" an extra state ex post could cause a conceptual dilemma in the analysis of a redistribution policy. For example, in Boar and Midrigan's (2020) setting, the financial intermediary may incur a capital loss because the value of the production firm may fall as a result of the redistribution policy. To maintain zero profit ex post, the intermediary has to pass the capital loss to the consumer. This outcome implies that, ex ante, this type of provision has to be present in the contract between the consumers and the intermediary. To write down this type of provision, however, (i) the contract has to recognize that a capital-loss event may occur in future and (ii) different types of assets have to be treated differently in the contract. These two elements in the contract are difficult to square with the fact that the intermediary is content to offer only one type of asset to the consumers, because it can, in principle, offer different mixes of assets to different consumers so that the consumers can better hedge the risk of redistribution policy.

## C Incomplete market: Bond economy

Here, consider another incomplete-market EU economy. Specifically, the consumers are only allowed to trade noncontingent bonds. For the ease of computation, I assume the utility function is quadratic:

 $u(c) = \alpha c - \frac{\gamma}{2}c^2,\tag{2}$ 

where  $\alpha > 0$  and  $\gamma > 0$ . The value of  $\alpha$  is assumed to be sufficiently large so that utility is increasing in c over the relevant range.

A Type-I consumer's problem is

$$\max_{c_1,c_2,\tilde{c}_2,b} u(c_1) + (1-\pi)u(c_2) + \pi u(\tilde{c}_2),$$

subject to

$$c_1 + qb = 1$$
,

$$c_2 = 1 + b$$
,

and

$$\tilde{c}_2 = 1 - \tau + b,$$

where q is the bond price and b is the bond holding. After solving for the first-order condition, the bond demand of Type-I consumers is

$$b = \frac{q(\gamma - \alpha) + \alpha - \gamma(1 - \pi\tau)}{\gamma(q^2 + 1)}.$$

Similarly, the Type-II consumer's problem is

$$\max_{c_1',c_2',\tilde{c}_2',b'}\ u(c_1') + (1-\pi)u(c_2') + \pi u(\tilde{c}_2'),$$

subject to

$$c_1' + qb' = 1,$$

$$c_2' = 1 + b',$$

and

$$\tilde{c}_2' = 1 + \tau + b',$$

The bond demand of the Type-II consumers is

$$b = \frac{q(\gamma - \alpha) + \alpha - \gamma(1 + \pi\tau)}{\gamma(q^2 + 1)}.$$

The bond price q is set so that the excess bond demand is zero:

$$b + b' = 0$$
.

It is straightforward to derive that, in equilibrium,

$$q = 1$$

and

$$(b,b') = \left(\frac{\pi}{2}\tau, -\frac{\pi}{2}\tau\right)$$

hold. The resulting consumptions are:

$$(c_1, c_1', c_2, c_2', \tilde{c}_2, \tilde{c}_2') = \left(1 - \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, 1 - \frac{\pi}{2}\tau, 1 + \left(\frac{\pi}{2} - 1\right)\tau, 1 + \left(1 - \frac{\pi}{2}\right)\tau\right),$$

which achieves some but not perfect consumption smoothing.

In the limit of  $\pi \to 0$ , the consumption profile when the irregular state takes place in period 2 would approach

$$\lim_{\tau \to 0} (c_1, c_1', \tilde{c}_2, \tilde{c}_2') = (1, 1, 1 - \tau, 1 + \tau),$$

which is identical to (1). In the current example, the incomplete-market structure that delivers the equivalence to the MIT-shock outcome is not unique. The following section looks at the economy with one Arrow security.

## D When the type of asset structures matters

For simplicity, in the main text (Section 3), I considered a setting where in both the IU economy (Section 3.1) and the EU economies (Sections 3.3 and Appendix C), the equilibrium security holdings are zero. This assumption has two consequences: (i) For the IU economy, the outcome is identical regardless of whether the assumption is that the existing security is (a) an Arrow security for the regular state or (b) a state-noncontingent bond. (ii) The limiting outcome of the EU economies in the Arrow-security economy (Section 3.3) and the bond economy (Appendix C) are both consistent with the IU outcome. Here, I consider a setting where the equilibrium security holdings in these situations are nonzero, and show that the type of asset structures in both the IU economies and the EU economies matters.

Consider the same setting as in Section 3, except for the endowments. A Type-I consumer receives the endowment of 0 in period 1 and 2 in the period-2 regular state. In the period-2 irregular state, a Type-I consumer receives  $(2 - \tau)$ , where  $\tau \in (0, 1)$ . A Type-II consumer receives 2 in period 1 and 0 in the period-2 regular state. In the period-2 irregular state, a Type-II consumer receives  $\tau$ .

Below, I show several IU outcomes can exist depending on the asset structure, because the level of asset that can be carried into the MIT-shock state can differ depending on the assumed asset structure. I show several (incomplete-market) EU allocations can also exist depending on the asset structure, and one can map an EU allocation to a corresponding IU allocation.

The lesson of this section is that, when an MIT-shock experiment is conducted, one has to use the underlying asset structure that is consistent with a particular background EU economy. If the background EU economy is an incomplete-market economy with bonds, the consumers have to be allowed to carry over the bond holdings after the MIT shock. If the background EU economy features state-by-state Arrow security, one has to think carefully about whether to allow for a similar ex-ante arrangement for the MIT-shock state.

#### D.1 MIT shock: Arrow security economy

First, consider an MIT shock (IU) economy. Suppose that, before the shock, the economy permits an Arrow security contingent on the regular state. The problem for a Type-I consumer is

$$\max_{c_1,c_2,a} u(c_1) + u(c_2),$$

subject to

$$c_1 + pa = 0$$

and

$$c_2 = 2 + a$$
,

where p is the price of the Arrow security that pays out one unit of the consumption good in the regular state period 2. Because the consumers perceive only the regular state, the IU economy has a complete asset market with one Arrow security. The consumption in period 1 and 2 is denoted as  $c_1$  and  $c_2$ , respectively, and the security holding is represented by a.

The Type-II consumer faces the problem:

$$\max_{c'_1, c'_2, s'} \ u(c'_1) + u(c'_2),$$

subject to

$$c_1' + pa' = 2$$

and

$$c_2' = a',$$

where prime  $(\prime)$  denotes variables for the Type-II consumers.

The unique competitive equilibrium is with p=1, a=-1, a'=1, and  $c_1=c_1'=c_2=c_2'=1$ . Now suppose the MIT shock hits the economy. Because the irregular state is not spanned by the Arrow security, the ex-post allocation will be  $\tilde{c}_2=2-\tau$  and  $\tilde{c}_2'=\tau$ . (As in the main text, a tilde () denotes the irregular state.) Thus, the entire ex-post allocation ends up with

$$(c_1, c'_1, \tilde{c}_2, \tilde{c}'_2) = (1, 1, 2 - \tau, \tau).$$
 (3)

#### D.2 MIT shock: Bond economy

Second, alternatively, consider another MIT shock (IU) economy with a different asset structure. Suppose, instead, the asset in the economy is a noncontingent bond. The problem for a Type-I consumer is

$$\max_{c_1, c_2, a} u(c_1) + u(c_2),$$

subject to

$$c_1 + qb = 0$$

and

$$c_2 = 2 + b$$
,

where q is the price of the bond that pays out one unit of the consumption good in the regular state period 2. Once again, because the consumers perceive only the regular state, the IU economy's asset market is complete. The consumption in period 1 and 2 is denoted as  $c_1$  and  $c_2$ , respectively, and the bond holding is represented by b.

The Type-II consumer faces the identical problem:

$$\max_{c_1',c_2',s'}\ u(c_1')+u(c_2'),$$

subject to

$$c_1' + pb' = 2$$

and

$$c_2' = b',$$

where prime  $(\prime)$  denotes variables for the Type-II consumers.

The unique competitive equilibrium is with q=1, b=-1, b'=1, and  $c_1=c_1'=c_2=c_2'=1$ . Now suppose the MIT shock hits the economy. Now, in contrast to the previous case, the noncontingent bond remains in the economy, and the ex-post allocation will be  $\tilde{c}_2=1-\tau$  and  $\tilde{c}_2'=1+\tau$ . A tilde () denotes the irregular state. Thus, the entire ex-post allocation ends up with

$$(c_1, c'_1, \tilde{c}_2, \tilde{c}'_2) = (1, 1, 1 - \tau, 1 + \tau).$$
 (4)

Thus, comparing (3) and (4), one can see that the allocation after the MIT shock is different depending on the asset structure.

### D.3 Complete market

The next three sections consider EU economies. That is, I consider a situation where the irregular state occurs with probability  $\pi$ , and the consumers perceive that event. First, suppose the existence of a full set of Arrow securities. The notations are the same as in Section 3.2. A Type-I consumer's problem is

$$\max_{c_1, c_2, \tilde{c}_2, a, \tilde{a}} u(c_1) + (1 - \pi)u(c_2) + \pi u(\tilde{c}_2),$$

subject to

$$c_1 + pa + \tilde{p}\tilde{a} = 0,$$
$$c_2 = 2 + a,$$

and

$$\tilde{c}_2 = 2 - \tau + \tilde{a},$$

where a and  $\tilde{a}$  denote the holding of Arrow securities.

A Type-II consumer's problem is (with the same notation convention as in the last section)

$$\max_{c_1',c_2',\tilde{c}_2',a',\tilde{a}'}\ u(c_1') + (1-\pi)u(c_2') + \pi u(\tilde{c}_2'),$$

subject to

$$c'_1 + pa' + \tilde{p}\tilde{a}' = 2,$$
  
$$c'_2 = a',$$

and

$$\tilde{c}_2' = \tau + \tilde{a}'.$$

One can confirm the competitive equilibrium, where the consumer's first-order conditions are satisfied and the market-clearing conditions

$$a + a' = 0$$

and

$$\tilde{a} + \tilde{a}' = 0$$

have the following solution:

$$p = 1 - \pi$$

and

$$\tilde{p} = \pi$$

with

$$(a, a', \tilde{a}, \tilde{a}') = \left(-1 - \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, -1 + \frac{2-\pi}{2}\tau, 1 - \frac{2-\pi}{2}\tau\right).$$

The resulting consumptions is:

$$(c_1, c'_1, c_2, c'_2, \tilde{c}_2, \tilde{c}'_2) = \left(1 - \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, 1 - \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, 1 - \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau\right);$$

that is, each consumer can smooth consumption across time and state.

To see whether this allocation corresponds to one of the IU allocations, take  $\pi \to 0$  and look at the consumption when the irregular shock hits. The result is

$$\lim_{\pi \to 0} (c_1, c_1', \tilde{c}_2, \tilde{c}_2') = (1, 1, 1, 1).$$

The outcome is different from both (3) and (4).

#### D.4 Incomplete market: Arrow security economy

Now, consider another EU economy. Suppose, as in Section 3.3, the Arrow security does not exist for the irregular state although the consumers recognize the possibility of the irregular state in the future. A Type-I consumer's problem is

$$\max_{c_1, c_2, \tilde{c}_2, a} u(c_1) + (1 - \pi)u(c_2) + \pi u(\tilde{c}_2),$$

subject to

$$c_1 + pa = 0,$$

$$c_2 = 2 + a,$$

and

$$\tilde{c}_2 = 2 - \tau.$$

For Type-II consumers,

$$\max_{c'_1, c'_2, \tilde{c}'_2, a'} u(c'_1) + (1 - \pi)u(c'_2) + \pi u(\tilde{c}'_2),$$

subject to

$$c_1' + pa' = 2,$$

$$c_2' = a',$$

and

$$\tilde{c}_2' = \tau$$
.

The competitive equilibrium is  $p = 1 - \pi$ , a = -1, a' = 1. The resulting consumption is:

$$(c_1, c'_1, c_2, c'_2, \tilde{c}_2, \tilde{c}'_2) = (1, 1, 1, 1, 2 - \tau, \tau).$$

Thus, in the limit of  $\pi \to 0$ ,

$$\lim_{\tau \to 0} (c_1, c_1', \tilde{c}_2, \tilde{c}_2') = (1, 1, 2 - \tau, \tau),$$

which is identical to (3).

#### D.5 Incomplete market: Bond economy

For yet another EU economy, consider an economy with only a state-noncontingent bond. Similarly to Appendix C, I assume the utility function is quadratic:

$$u(c) = \alpha c - \frac{\gamma}{2}c^2,\tag{5}$$

where  $\alpha > 0$  and  $\gamma > 0$ . The value of  $\alpha$  is assumed to be sufficiently large so that utility is increasing in c over the relevant range.

A Type-I consumer's problem is

$$\max_{c_1, c_2, \tilde{c}_2, b} u(c_1) + (1 - \pi)u(c_2) + \pi u(\tilde{c}_2),$$

subject to

$$c_1 + qb = 0,$$

$$c_2 = 2 + b$$
,

and

$$\tilde{c}_2 = 2 - \tau + b,$$

where q is the bond price and b is the bond holding. After solving for the first-order condition, the bond demand of Type-I consumers is

$$b = \frac{-q\alpha + \alpha - \gamma(2 - \pi\tau)}{\gamma(q^2 + 1)}.$$

Similarly, the Type-II consumer's problem is

$$\max_{c_1', c_2', \tilde{c}_2', b'} \ u(c_1') + (1 - \pi)u(c_2') + \pi u(\tilde{c}_2'),$$

subject to

$$c_1' + qb' = 2,$$

$$c_2' = b',$$

and

$$\tilde{c}_2' = \tau + b',$$

The bond demand of the Type-II consumers is

$$b = \frac{q(2\gamma - \alpha) + \alpha - \gamma \pi \tau}{\gamma(q^2 + 1)}.$$

The bond price q is set so that

$$b + b' = 0,$$

and therefore, in equilibrium,

$$q = 1$$

and

$$(b,b') = \left(\frac{\pi}{2}\tau - 1, 1 - \frac{\pi}{2}\tau\right)$$

hold. The resulting consumptions are

$$(c_1, c_1', c_2, c_2', \tilde{c}_2, \tilde{c}_2') = \left(1 - \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, 1 + \frac{\pi}{2}\tau, 1 - \frac{\pi}{2}\tau, 1 + \left(\frac{\pi}{2} - 1\right)\tau, 1 + \left(1 - \frac{\pi}{2}\right)\tau\right).$$

In the limit of  $\pi \to 0$ , the consumption profile when the irregular state takes place in period 2 would approach

$$\lim_{\tau \to 0} (c_1, c'_1, \tilde{c}_2, \tilde{c}'_2) = (1, 1, 1 - \tau, 1 + \tau),$$

which is identical to (4).

The analysis above first confirms the conclusion of the main text: the probability-zero limit of an EU economy allocation converges to an IU economy allocation only when the asset market is missing for the MIT-shock state. A new point this section makes is that the type of incompleteness matters. Here, the IU outcome in an Arrow-security economy (Section D.1) can be approximated by an appropriate EU economy with an Arrow security (Section D.4), and the outcome in an IU economy with a bond (Section D.2) can be approximated by an incomplete-market EU economy with a bond (Section D.5).

The principle here is that the asset holding that can be carried into the irregular state has to be consistent between the EU economy and the IU economy. The value of the assets also have to be reevaluated carefully when computing each consumer's asset holding upon the occurrence of the MIT shock.

This principle may sound obvious. In some situations, however, reevaluating the asset value coming into the MIT-shock economy requires careful examination. For example, suppose the asset value of a consumer, a, is a sum of a stock px, where p is the stock price and x is the quantity of the stock holding, and a bond b; therefore,

$$a = px + b$$
.

When the realization of the irregular state moves the stock price from p to  $\hat{p}$ , the asset has to be reevaluated as

$$\hat{a} \equiv \hat{p}x + b$$

when starting the MIT-shock state, even though both the stock and bond can be carried into the MIT-shock state. The reevaluation would not be a big issue in an economy with a simple asset structure as in Huggett (1993) and Aiyagari (1994), but would matter in a more complex economy such as Krusell et al.'s (2010) (for which Mukoyama (2013) is an example of an MIT-shock analysis), as discussed above.

### References

- Abel, A. B. and O. J. Blanchard (1983). An Intertemporal Model of Saving and Investment. *Econometrica* 51, 675–692.
- Aiyagari, S. R. (1994). Uninsured Idiosyncratic Risk and Aggregate Saving. Quarterly Journal of Economics 109, 659–684.
- Auerbach, A. J. and L. J. Kotlikoff (1983). National Savings, Economic Welfare, and the Structure of Taxation. In M. Feldstein (Ed.), Behavioral Simulation Methods in Tax Policy Analysis, pp. 459–498. University of Chicago Press.
- Boar, C. and V. Midrigan (2020). Efficient Redistribution. mimeo. New York University.
- Boppart, T., P. Krusell, and K. Mitman (2018). Exploiting MIT Shocks in Heterogeneous-Agent Economies: the Impulse Response as a Numerical Derivative. *Journal of Economic Dynamics and Control* 89, 68–92.
- Dye, R. A. (1985). Costly Contract Contingencies. *International Economic Review 26*, 233–350.
- Guerrieri, V., G. Lorenzoni, L. Straub, and I. Werning (2020). Macroeconomic Implications of COVID-19: Can Negative Supply Shocks Cause Demand Shortages? NBER Working Paper 26918.
- Huggett, M. (1993). The Risk-Free Rate in Heterogeneous-Agent Incomplete-Insurance Economies. *Journal of Economic Dynamics and Control* 17, 953–969.
- Judd, K. L. (1985). Short-Run Analysis of Fiscal Policy in a Simple Perfect Foresight Model. Journal of Political Economy 93, 298–319.
- Kaplan, G., B. Moll, and G. L. Violante (2018). Monetary Policy According to HANK. American Economic Review 108, 697–743.
- Krusell, P., T. Mukoyama, and J. Anthony A. Smith (2011). Asset Prices in a Huggett Economy. *Journal of Economic Theory* 146, 812–844.
- Krusell, P., T. Mukoyama, and A. Şahin (2010). Labour-Market Matching with Precautionary Savings and Aggregate Fluctuations. *Review of Economic Studies* 77, 1477–1507.
- Mukoyama, T. (2010). Welfare Effects of Unanticipated Policy Changes with Complete Asset Markets. *Economics Letters* 109, 134–138.
- Mukoyama, T. (2013). Understanding the Welfare Effects of Unemployment Insurance Policy in General Equilibrium. *Journa of Macroeconomics* 38, 347–368.
- Young, E. R. (2004). Unemployment Insurance and Capital Accumulation. Journa of Monetary Economics 51, 1683–1710.