

Assignment 3 – ELEC ENG 3TQ3
Due Date: Nov 27th , 11:59 P.M.

1. (5 points) Consider two independent Gaussian random variables with expected values of 0 and variances 1. Let random variable $U = 2X + 3Y$ and random variable $V = X + 2Y$. Find the bivariate distribution of U, V . Hint: you can either calculate covariances and corresponding correlation coefficients or use matrix transformation as discussed in lectures.
2. (5 points) Consider two Gaussian random variables U and V such that: a) the expected value of U is 2 and variance of U is 9 and b) the expected value of V is 1 and variance is 16. In addition the covariance $\text{cov}(U, V)$ is 3. Find coefficients a, b, c and d so that $X = aU + bV$ and $Y = cU + dV$ are jointly Gaussian and independent. What are the corresponding distributions of X and Y . Note: there may be multiple solutions but you need to find only one.