## Waterloo White (2015-16)

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## 1 Algorithms

#### 1.1 Mo.cpp

```
// Determining the number of distinct numbers in a subsequence
#include <bits/stdc++.h>
#define SIZE 30010
#define MAX_VALUE 1000010
#define QUERIES 200010
using namespace std;
int N, M, sz, res, cnt[MAX_VALUE], a[SIZE], ans[QUERIES];
struct Query {
   int l, r, index;
   Query () {}
   Query (int l, int r, int index): l(l), r(r), index(index) {}
```

```
bool operator < (const Query& q) const {</pre>
        if ((1 - 1) / sz != (q.1 - 1) / sz)
           return (1 - 1) / sz > (q.1 - 1) / sz;
        return r < q.r;
} q[QUERIES];
void update (int i) {
    if (!cnt[i]++)
        res++;
void remove (int i) {
    if (!--cnt[i])
        res--:
int main () {
    scanf("%d", &N);
    sz = (int)sqrt(N);
    for (int i = 1; i \le N; i++)
        scanf("%d", &a[i]);
    scanf("%d", &M);
    for (int i = 0; i < M; i++) {
        int 1, r;
        scanf("%d%d", &1, &r);
        q[i] = Query(1, r, i);
    }
    sort(q, q + M);
    int 1 = 1, r = 0;
    for (int i = 0; i < M; i++) {
        while (r > q[i].r)
           remove(a[r--]);
        while (r < q[i].r)
           update(a[++r]);
        while (1 < q[i].1)
           remove(a[1++]);
        while (1 > q[i].1)
            update(a[--1]);
        ans[q[i].index] = res;
    for (int i = 0; i < M; i++)
        printf("%d\n", ans[i]);
    return 0;
}
```

#### 2 Data Structures

## 2.1 BIT.cpp

```
#include <bits/stdc++.h>
using namespace std;
struct BIT {
    int N;
    vector < int > val;
    BIT (int N) : N(N), val(N) {}
    void update (int idx, int v) {
        for (int x = idx; x < N; x += (x & -x))
            val[x] += v;
    int query (int idx) {
        int ret = 0;
        for (int x = idx; x > 0; x -= (x & -x))
            ret += val[x];
        return ret;
    }
};
```

#### 2.2 BIT\_Range.cpp

```
#include <bits/stdc++.h>
using namespace std;
struct BIT_Range {
    int N;
    vector < int > val1, val2;
   BIT_Range (int N): N(N), val1(N), val2(N) {}
    void update (vector<int> &val, int idx, int v) {
        for (int x = idx; x < N; x += (x & -x))
            val[x] += v;
   }
    void update (int x1, int x2, int val) {
        update(val1, x1, val);
        update(val1, x2 + 1, -val);
        update(val2, x1, val * (x1 - 1));
        update(val2, x2 + 1, -val * x2);
   }
    int query (vector < int > &val, int idx) {
        int ret = 0;
        for (int x = idx; x > 0; x -= (x & -x))
            ret += val[x]:
        return ret;
    int query (int x) {
        return query(val1, x) * x - query(val2, x);
    int query (int x1, int x2) {
        return query(x2) - query(x1 - 1);
};
```

#### 2.3 Treap.cpp

```
#include <bits/stdc++.h>
using namespace std;
int randomPriority () {
   return rand() * 65536 + rand();
struct Node {
   int val, p;
    Node *left, *right;
   Node (int val): val(val), p(randomPriority()) {
       left = nullptr;
        right = nullptr;
struct Treap {
   Node* root:
   Treap () {
        root = nullptr;
    // precondition: all values of u are smaller than all values of v
   Node* join (Node* u, Node* v) {
       if (u == nullptr)
            return v;
        if (v == nullptr)
            return u;
        if (u->p < v->p) {
            u->right = join(u->right, v);
            return u:
        v->left = join(u, v->left);
        return v:
   }
   pair < Node*, Node*> split (Node* u, int k) {
        if (u == nullptr)
```

```
return make_pair(nullptr, nullptr);
        if (u->val < k) {
            auto res = split(u->right, k);
            u->right = res.first;
            res.first = u:
            return res:
        } else if (u->val > k) {
            auto res = split(u->left, k);
            u->left = res.second;
            res.second = u;
            return res:
        } else {
            return make_pair(u->left, u->right);
    }
    bool contains (int val) {
        return contains (root, val);
    bool contains (Node* u, int val) {
        if (u == nullptr)
            return false;
        if (u->val < val)
            return contains(u->right, val);
        else if (u->val > val)
            return contains(u->left, val);
        return true;
    }
    void insert (int val) {
        if (contains(root, val))
            return;
        auto nodes = split(root, val);
        root = join(nodes.first, join(new Node(val), nodes.second));
    void remove (int val) {
        if (root == nullptr)
            return;
        auto nodes = split(root, val);
        root = join(nodes.first, nodes.second);
};
```

## 3 Geometry

### 3.1 Convex\_Hull.cpp

```
#include <bits/stdc++.h>
using namespace std;
struct Point {
    int x, y;
    Point (int x, int y): x(x), y(y) {}
    bool operator < (const Point& p) const {</pre>
        return make_pair(x, y) < make_pair(p.x, p.y);</pre>
};
int ccw (Point p1, Point p2, Point p3) {
        return (p2.x - p1.x) * (p3.y - p1.y) - (p2.y - p1.y) * (p3.x - p1.x);
vector<Point> convexHull (vector<Point> pts) {
    vector < Point > u, 1;
    sort(pts.begin(), pts.end());
    for (int i = 0; i < (int)pts.size(); i++) {
        int j = (int)1.size();
        while (j \ge 2 \&\& ccw(1[j - 2], 1[j - 1], pts[i]) \le 0) {
            1.erase(1.end() - 1);
            j = (int)1.size();
        1.push_back(pts[i]);
    for (int i = (int)pts.size() - 1; i >= 0; i--) {
        int j = (int)u.size();
```

```
while (j >= 2 && ccw(u[j - 2], u[j - 1], pts[i]) <= 0) {
            u.erase(u.end() - 1);
            j = (int)u.size();
        }
        u.push_back(pts[i]);
}
u.erase(u.end() - 1);
l.erase(l.end() - 1);
l.reserve(l.size() + u.size());
l.insert(l.end(), u.begin(), u.end());
return 1;</pre>
```

# 4 Graph Theory

## 4.1 Eulerian.cpp

}

```
#include <bits/stdc++.h>
using namespace std;
struct Edge {
    int dest, index;
    bool used;
struct Euler {
    int N;
    vector < vector < Edge >> adj;
    vector < int > used;
    Euler (int N): N(N), adj(N), used(N) {}
    void addEdge (int u, int v) {
        adj[u].push_back({v, (int)adj[v].size(), 0});
        adj[v].push_back({u, (int)adj[u].size() - 1, 0});
    // precondition: all vertices are connected
    int getEuler () {
        int odd = 0;
        for (int i = 0; i < N; i++)
            if ((int)adj[i].size() & 1)
                odd++;
        if (odd > 2)
            return -1;
        return odd == 0 ? 0 : 1;
    bool isEulerianPath () {
        return getEuler() != -1;
    bool isEulerianCycle () {
        return getEuler() == 0;
    void printEulerianPath () {
        if (!isEulerianPath()) {
            printf("No Eulerian Path Exists.");
            return:
        stack<int> order;
        int curr = 0;
        for (int i = 0; i < N; i++)
            if ((int)adj[i].size() & 1)
                curr = i;
        while (true) {
            if ((int)adj[curr].size() - used[curr] == 0) {
                printf("%d ", curr);
                if (order.size() == 0)
                    break;
                curr = order.top();
                order.pop();
            } else {
```

```
order.push(curr);
                for (int i = 0; i < (int)adj[curr].size(); i++) {
                    if (!adj[curr][i].used) {
                        int dest = adj[curr][i].dest;
                        int index = adj[curr][i].index;
                        adj[curr][i].used = true;
                        adj[dest][index].used = true;
                        used[curr]++:
                        used[dest]++:
                        curr = dest;
                        break;
               }
            }
        }
    }
};
4.2 SCC.cpp
#include <bits/stdc++.h>
using namespace std;
struct SCC {
    int N, cnt, idCnt;
    vector < int > disc, lo, id;
    vector < bool > inStack;
    vector < vector < int >> adi:
    stack<int> s;
    SCC (int N): N(N), disc(N), lo(N), id(N), inStack(N), adj(N) {}
    void addEdge (int u, int v) {
        adj[u].push_back(v);
    void dfs (int i) {
        disc[i] = lo[i] = ++cnt;
        inStack[i] = true;
        s.push(i);
        for (int j : adj[i]) {
            if (disc[j] == 0) {
                dfs(j);
                lo[i] = min(lo[i], lo[j]);
            } else if (inStack[j]) {
                lo[i] = min(lo[i], disc[j]);
        if (disc[i] == lo[i]) {
            while (s.top() != i) {
                inStack[s.top()] = false;
                id[s.top()] = idCnt;
                s.pop();
            inStack[s.top()] = false;
            id[s.top()] = idCnt++;
            s.pop();
        }
    }
    void compute () {
        for (int i = 0; i < N; i++)
            if (disc[i] == 0)
                dfs(i):
};
4.3 Biconnected_Components.cpp
#include <bits/stdc++.h>
```

#include <bits/stdc++.h>
using namespace std;
typedef pair<int, int> edge;
struct BiconnectedComponents {
 int N, cnt = 0;

```
vector<edge> bridges;
vector < vector < edge >> components;
vector < vector < int >> adj;
stack < edge > s;
vector < int > lo, disc;
vector < bool > vis, cutVertex;
BiconnectedComponents (int N): N(N), adj(N), lo(N), disc(N), vis(N),
     cutVertex(N) {}
void addEdge (int u, int v) {
    adj[u].push_back(v);
    adj[v].push_back(u);
}
void dfs (int u, int prev) {
    disc[u] = lo[u] = cnt++;
    vis[u] = true;
    int children = 0;
    for (int v : adj[u]) {
        if (!vis[v]) {
            children++;
             s.push({u, v});
            dfs(v, u);
            lo[u] = min(lo[u], lo[v]);
             if ((disc[u] == 0 \&\& children > 1) \mid | (disc[u] > 0 \&\& lo[v]
                 >= disc[u])) {
                 cutVertex[u] = true;
                 components.push_back(vector<edge>());
                 while (s.top().first != u && s.top().second != v) {
                     components.back().push_back(edge(s.top().first, s.top
                          ().second));
                     s.pop();
                 components.back().push_back(edge(s.top().first, s.top().
                     second));
                 s.pop();
            if (lo[v] > disc[u])
                bridges.push_back(edge(s.top().first, s.top().second));
        } else if (v != prev && disc[v] < lo[u]) {</pre>
            lo[u] = disc[v];
            s.push({u, v});
        }
    }
}
void compute () {
    for (int i = 0; i < N; i++)
        if (!vis[i])
             dfs(i, -1);
```

#### 4.4 MaxFlow.cpp

};

```
#include <bits/stdc++.h>
using namespace std;
struct Edge {
   int dest, cost, next;
   Edge (int dest, int cost, int next): dest(dest), cost(cost), next(next)
        {};

struct Network {
   int N, src, sink;
   vector<int> last, dist;
   vector<Edge> e;

   Network (int N, int src, int sink): N(N), src(src), sink(sink), last(N),
        dist(N) {
        fill(last.begin(), last.end(), -1);
   }
```

```
void AddEdge (int x, int y, int xy, int yx) {
        e.push_back(Edge(y, xy, last[x]));
        last[x] = (int)e.size() - 1;
        e.push_back(Edge(x, yx, last[y]));
        last[v] = (int)e.size() - 1;
    bool getPath () {
        fill(dist.begin(), dist.end(), -1);
        queue <int> q;
        q.push(src);
        dist[src] = 0;
        while (!q.empty()) {
            int curr = q.front(); q.pop();
            for (int i = last[curr]; i != -1; i = e[i].next) {
                if (e[i].cost > 0 && dist[e[i].dest] == -1) {
                    dist[e[i].dest] = dist[curr] + 1;
                    q.push(e[i].dest);
        return dist[sink] != -1;
    int dfs (int curr, int flow) {
        if (curr == sink)
           return flow;
        int ret = 0;
        for (int i = last[curr]; i != -1; i = e[i].next) {
            if (e[i].cost > 0 && dist[e[i].dest] == dist[curr] + 1) {
                int res = dfs(e[i].dest, min(flow, e[i].cost));
                ret += res:
                e[i].cost -= res;
                e[i ^ 1].cost += res;
                flow -= res;
                if (flow == 0)
                    break;
            }
        return ret:
    int getFlow () {
        int res = 0;
        while (getPath())
            res += dfs(src, 1 << 30);
        return res:
};
```

#### 4.5 MaxFlowMinCost.cpp

```
#include <bits/stdc++.h>
using namespace std;
struct Edge {
    int orig, dest, origCost, cost, flow, last;
    Edge (int orig, int dest, int cost, int flow, int last): orig(orig), dest
         (dest), origCost(cost), cost(cost), flow(flow), last(last) {}
};
struct Vertex {
    int index, cost;
    Vertex (int index, int cost): index(index), cost(cost) {}
    bool operator < (const Vertex& v) const {</pre>
        return cost < v.cost;
};
struct MaxFlowMinCost {
    int N, src, sink, cnt = 0;
    vector < Edge > e;
    vector<int> last, phi, prev, dist, index;
    MaxFlowMinCost (int N, int src, int sink): N(N), src(src), sink(sink),
         last(N), phi(N), prev(N), dist(N), index(N) {
```

```
fill(last.begin(), last.end(), -1);
void addEdge (int u, int v, int flow, int cost) {
    e.push_back({u, v, cost, flow, last[u]});
    last[u] = (int)e.size() - 1;
    e.push_back({v, u, -cost, 0, last[v]});
    last[v] = (int)e.size() - 1;
void reduceCost () {
    for (int i = 0; i < (int)e.size(); i += 2) {
        e[i].cost += phi[e[i].orig] - phi[e[i].dest];
        e[i ^ 1].cost = 0;
}
void bellmanFord () {
    fill(phi.begin(), phi.end(), 1 << 25);
    phi[src] = 0;
    for (int j = 0; j < N - 1; j++)
        for (int i = 0; i < (int)e.size(); i++)
            if (e[i].flow > 0)
                phi[e[i].dest] = min(phi[e[i].dest], phi[e[i].orig] + e[i
                     1.cost):
}
bool dijkstra () {
    fill(dist.begin(), dist.end(), 1 << 30);
    fill(prev.begin(), prev.end(), -1);
    fill(index.begin(), index.end(), -1);
    dist[src] = 0;
    priority_queue < Vertex > pq;
    pq.push({src, 0});
    while (!pq.empty()) {
        Vertex curr = pq.top();
        pq.pop();
        for (int next = last[curr.index]; next != -1; next = e[next].last
            if (e[next].flow == 0 || dist[e[next].dest] <= dist[curr.</pre>
                 index] + e[next].cost)
                continue;
            dist[e[next].dest] = dist[curr.index] + e[next].cost;
            prev[e[next].dest] = curr.index;
            index[e[next].dest] = next;
            pq.push({e[next].dest, dist[e[next].dest]});
    return dist[sink] != 1 << 30;
pair<int, int> getMaxFlowMinCost () {
    int flow = 0;
    int cost = 0;
    bellmanFord();
    reduceCost();
    while (dijkstra()) {
        for (int i = 0; i < N; i++)
            phi[i] = dist[i];
        reduceCost();
        int aug = 1 << 30;
        int curr = sink;
        while (prev[curr] != -1) {
            aug = min(aug, e[index[curr]].flow);
            curr = prev[curr];
        flow += aug;
        curr = sink;
        while (prev[curr] != -1) {
            e[index[curr]].flow -= aug;
            e[index[curr] ^ 1].flow += aug;
            cost += aug * e[index[curr]].origCost;
            curr = prev[curr];
        }
```

```
return {flow, cost};
}
```

#### 4.6 MaxMatching.cpp

```
#include <bits/stdc++.h>
using namespace std;
struct MaxMatching {
    vector < vector < int >> adj;
    vector <bool> mark, used;
    vector<int> match, par, id;
    MaxMatching (int N): N(N), adj(N), mark(N), used(N), match(N), par(N), id
    void addEdge (int u, int v) {
        adj[u].push_back(v);
        adj[v].push_back(u);
    void markPath (vector < bool > & blossom, int i, int b, int j) {
        for (; id[i] != b; i = par[match[i]]) {
            blossom[id[i]] = blossom[id[match[i]]] = true;
            par[i] = j;
            j = match[i];
    }
    int lca (int i, int j) {
        vector < bool > v(N):
        while (true) {
            i = id[i]:
            used[i] = true;
            if (match[i] == -1)
                break;
            i = par[match[i]];
        while (true) {
            j = id[j];
            if (v[j])
                return j;
            j = par[match[j]];
    int getAugmentingPath (int src) {
        fill(par.begin(), par.end(), -1);
        fill(used.begin(), used.end(), 0);
        for (int i = 0; i < N; i++)
            id[i] = i;
        used[src] = true;
        queue <int> q;
        q.push(src);
        while (!q.empty()) {
            int curr = q.front();
            q.pop();
            for (int next : adj[curr]) {
                if (id[curr] == id[next] || match[curr] == next)
                     continue;
                 if (next == src || (match[next] != -1 && par[match[next]] !=
                     -1)) {
                     int newBase = lca(curr, next);
                    vector < bool > blossom(N);
                    markPath(blossom, curr, newBase, next);
                    markPath(blossom, next, newBase, curr);
                    for (int i = 0; i < N; i++) {
                         if (blossom[id[i]]) {
                            id[i] = newBase;
                             if (!used[i]) {
```

used[i] = true;

```
q.push(i);
                        }
                    }
                }
            } else if (par[next] == -1) {
                par[next] = curr;
                if (match[next] == -1)
                    return next;
                next = match[next]:
                used[next] = true;
                q.push(next);
            }
       }
   }
}
int getMaxMatching () {
    fill(match.begin(), match.end(), -1);
    fill(par.begin(), par.end(), 0);
    fill(id.begin(), id.end(), 0);
    fill(used.begin(), used.end(), 0);
    for (int i = 0; i < N; i++) {
        if (match[i] == -1){
            int v = getAugmentingPath(i);
            while (v != -1) {
                int pv = par[v];
                int ppv = match[pv];
                match[v] = pv;
                match[pv] = v;
                v = pp\bar{v};
            }
        }
    }
    int res = 0;
    for (int i = 0; i < N; i++)
        if (match[i] != -1)
            res++;
    return res / 2;
}
```

#### 4.7 Stoer\_Wagner.cpp

}:

```
#include <bits/stdc++.h>
using namespace std;
struct MinCut {
   int N;
    vector < vector < int >> adj;
    vector < int > weight;
    vector < bool > inContraction, used;
   MinCut (int N): N(N), adj(N, vector<int>(N)), weight(N, 0), inContraction
        (N, 0), used(N, 0) {}
   void addEdge (int u, int v, int c) {
        adj[u][v] = c;
        adj[v][u] = c;
   }
   int getMinCut () {
        int minCut = 1 << 30;
        for (int v = N - 1; v >= 0; v --) {
            for (int i = 1; i < N; i++) {
                used[i] = inContraction[i];
                weight[i] = adj[0][i];
            int prev = 0, curr = 0;
            for (int sz = 1; sz <= v; sz++) {
                prev = curr;
                curr = -1;
                for (int i = 1; i < N; i++)
                    if (!used[i] && (curr == -1 || weight[i] > weight[curr]))
                        curr = i:
```

```
if (sz != v) {
                    for (int i = 0; i < N; i++)
                        weight[i] += adj[curr][i];
                    used[curr] = true:
                    for (int i = 0; i < N; i++)
                        adj[prev][i] = adj[i][prev] += adj[i][curr];
                     inContraction[curr] = true;
                    minCut = min(minCut, weight[curr]);
            }
        }
        return minCut;
};
4.8 LCA.cpp
#include <bits/stdc++.h>
using namespace std;
struct LCA {
    int N, LN;
    vector < int > depth;
    vector < vector < int >> pa;
    vector < vector < int >> adj;
    LCA (int N): N(N), LN(ceil(log(N) / log(2) + 1)), depth(N), pa(N), vector < 1
         int>(LN)), adj(N) {
        for (auto &x : pa)
            fill(x.begin(), x.end(), -1);
    void addEdge (int u, int v) {
        adj[u].push_back(v);
        adj[v].push_back(u);
    void dfs (int u, int d, int prev) {
        depth[u] = d;
        pa[u][0] = prev;
        for (int v : adj[u])
            if (v != prev)
                dfs(v, d + 1, u);
    void precompute () {
        for (int i = 1; i < LN; i++)
            for (int j = 0; j < N; j++)
                if (pa[j][i - 1] != -1)
                    pa[j][i] = pa[pa[j][i - 1]][i - 1];
    }
    int getLca (int u, int v) {
        if (depth[u] < depth[v])</pre>
            swap(u, v);
        for (int k = LN - 1; k >= 0; k--)
            if (pa[u][k] != -1 && depth[pa[u][k]] >= depth[v])
                u = pa[u][k];
        if (u == v)
            return u;
        for (int k = LN - 1; k >= 0; k--)
            if (pa[u][k] != -1 && pa[v][k] != -1 && pa[u][k] != pa[v][k])
                u = pa[u][k], v = pa[v][k];
        return pa[u][0];
};
4.9 HLD.cpp
#include <bits/stdc++.h>
using namespace std;
```

struct HLD {

int N, chainIndex;

```
vector < vector < int >> adj;
vector < int > sz, depth, chain, par, head;
HLD (int N): N(N), adj(N), sz(N), depth(N), chain(N), par(N), head(N) {
    fill(head.begin(), head.end(), -1);
void addEdge (int u, int v) {
    adj[u].push_back(v);
    adj[v].push_back(u);
void dfs (int u, int p, int d) {
    par[u] = p;
    depth[u] = d;
    sz[u] = 1;
    for (int v : adj[u]) {
        if (v != p) {
            dfs(v, u, d + 1);
            sz[u] += sz[v];
        }
    }
}
void build (int u, int p) {
    if (head[chainIndex] == -1)
        head[chainIndex] = u;
    chain[u] = chainIndex;
    int maxIndex = -1;
    for (int v : adj[u])
        if (v != p \&\& (maxIndex == -1 || sz[v] > sz[maxIndex]))
            maxIndex = v;
    if (maxIndex != -1)
        build(maxIndex, u);
    for (int v : adj[u])
        if (v != p && v != maxIndex) {
            chainIndex++:
            build(v, u);
        }
}
void precompute () {
    dfs(0, -1, 0);
    build(0, -1);
}
int getLca (int u, int v) {
    while (chain[u] != chain[v]) {
        if (depth[head[chain[u]]] < depth[head[chain[v]]])</pre>
            v = par[head[chain[v]]];
        else
            u = par[head[chain[u]]];
    return depth[u] < depth[v] ? u : v;
```

#### 5 Mathematics

#### 5.1 Euclid.cpp

};

```
#include <bits/stdc++.h>
using namespace std;
int mod (int a, int b) {
    return ((a % b) + b) % b;
}
int gcd (int a, int b) {
    return b == 0 ? a : (gcd(b, a % b));
}
```

```
int lcm (int a, int b) {
    return a / gcd(a, b) * b;
// returns (d, x, y) such that d = qcd(a, b) and d = ax * by
vector<int> euclid (int a, int b) {
    int x = 1, y = 0, x1 = 0, y1 = 1, t;
    while (b != 0) {
        int q = a / b;
        t = \hat{x};
        x = x1;
        x1 = t - q * x1;
        t = y;
        y = y1;
        y1 = t - q * y1;
        t = b;
        b = a - q * b;
        a = t;
    vector<int> ret = {a, x, y};
    if (a \le 0) ret = \{-a, -x, -y\};
    return ret:
// finds all solutions to ax = b \mod n
vector<int> linearEquationSolver (int a, int b, int n) {
    vector < int > ret:
    vector<int> res = euclid(a, b);
    int d = res[0], x = res[1];
    if (b \% d == 0) {
        x = mod(x * (b / d), n);
        for (int i = 0; i < d; i++)
            ret.push_back(mod(x + i * (n / d), n));
    }
    return ret;
}
// computes x and y such that ax + by = c; on failure, x = y = -1 << 30
void linearDiophantine (int a, int b, int c, int &x, int &y) {
    int d = gcd(a, b);
    if (c % d != 0) {
       x = y = -1 << 30;
    } else {
        a /= d;
        b /= d;
        c /= d:
        vector<int> ret = euclid(a, b);
        x = ret[1] * c;
        y = ret[2] * c;
    }
}
// precondition: m > 0 \& gcd(a, m) = 1
int modInverse (int a. int m) {
    a = mod(a, m);
    return a == 0 ? 0 : mod((1 - modInverse(m % a, a) * m) / a, m);
}
// precondition: p is prime
vector<int> generateInverse (int p) {
    vector < int > res(p);
    res[1] = 1;
    for (int i = 2; i < p; ++i)
       res[i] = (p - (p / i) * res[p % i] % p) % p;
    return res;
}
// solve x = a[i] \pmod{p[i]}, where qcd(p[i], p[j]) == 1
int simpleRestore (vector<int> a, vector<int> p) {
   int res = a[0];
    int m = 1;
    for (int i = 1; i < (int)a.size(); i++) {
        m *= p[i - 1];
```

```
while (res % p[i] != a[i])
            res += m;
    return res;
}
int garnerRestore (vector<int> a, vector<int> p) {
    vector < int > x(a.size());
    for (int i = 0; i < (int)x.size(); ++i) {
        x[i] = a[i];
        for (int j = 0; j < i; ++j) {
            x[i] = (int) modInverse(p[j], p[i]) * (x[i] - x[j]);
            x[i] = (x[i] \% p[i] + p[i]) \% p[i];
        }
    }
    int res = x[0];
    int m = 1;
    for (int i = 1; i < (int)a.size(); i++) {
        m *= p[i - 1];
        res += x[i] * m;
    return res:
}
```

#### 5.2 Combinatorics.cpp

```
#include <bits/stdc++.h>
typedef long long 11;
ll modpow (ll base, ll pow, ll mod) {
    if (pow == 0)
        return 1L:
    if (pow == 1)
        return base;
    if (pow % 2)
        return base * modpow(base * base % mod, pow / 2, mod) % mod;
    return modpow(base * base % mod, pow / 2, mod);
}
11 factorial (11 n, 11 m) {
    ll ret = 1;
    for (int i = 2; i \le n; i++)
        ret = (ret * i) % m;
}
// precondition: p is prime
11 divMod (11 i, 11 j, 11 p) {
    return i * modpow(j, p - 2, p) % p;
// precondition: p is prime; O(log P) if you precompute factorials
11 fastChoose (ll n, ll k, ll p) {
    return divMod(divMod(factorial(n, p), factorial(k, p), p), factorial(n -
        k, p), p);
// number of partitions of n
ll partitions (ll n, ll m) {
    11 dp[n + 1];
    memset(dp, 0, sizeof dp);
    dp[0] = 1;
    for (int i = 1; i <= n; i++)
        for (int j = i; j \le n; j++)
            dp[j] = (dp[j] + dp[j - 1]) \% m;
    return dp[n] % m;
}
11 stirling1 (int n, int k, long m) {
    ll dp[n + 1][k + 1];
    memset(dp, 0, sizeof dp);
    dp[0][0] = 1;
    for (int i = 1; i <= n; i++)
        for (int j = 1; j \le k; j++) {
```

```
dp[i][j] = ((i - 1) * dp[i - 1][j]) % m;
            dp[i][j] = (dp[i][j] + dp[i - 1][j - 1]) \% m;
        }
    return dp[n][k];
}
11 stirling2 (int n, int k, 11 m) {
    11 dp[n + 1][k + 1];
    memset(dp, 0, sizeof dp);
    dp[0][0] = 1;
    for (int i = 1; i \le n; i++)
        for (int j = 1; j <= k; j++) {
    dp[i][j] = (j * dp[i - 1][j]) % m;
            dp[i][j] = (dp[i][j] + dp[i - 1][j - 1]) \% m;
    return dp[n][k];
}
ll eulerian1 (int n, int k, ll m) {
    if (k > n - 1 - k)
        k = n - 1 - k;
    11 dp[n + 1][k + 1];
    memset(dp, 0, sizeof dp);
    for (int j = 1; j \le k; j++)
        dp[0][j] = 0;
    for (int i = 1; i \le n; i++)
        for (int j = 1; j \le k; j++) {
            dp[i][j] = ((i - j) * dp[i - 1][j - 1]) % m;
            dp[i][j] = (dp[i][j] + ((j + 1) * dp[i - 1][j]) % m) % m;
        }
    return dp[n][k] % m;
11 eulerian2 (int n, int k, 11 m) {
    11 dp[n + 1][k + 1];
    memset(dp, 0, sizeof dp);
    for (int i = 1; i \le n; i++)
        for (int j = 1; j \le k; j++) {
            if (i == j) {
                dp[i][j] = 0;
                 dp[i][j] = ((j + 1) \% dp[i - 1][j]) \% m;
                dp[i][j] = (((2 * i - 1 - j) * dp[i - 1][j - 1]) % m + dp[i][
                     j]) % m;
        }
    return dp[n][k] % m;
}
// precondition: p is prime
11 catalan (int n, ll p) {
    return fastChoose(2 * n, n, p) * modpow(n + 1, p - 2, p) % p;
      Gauss_Jordon.cpp
5.3
* 1) Solving system of linear equations (AX=B), stored in B
 * 2) Inverting matrices (AX=I), stored in A
 st 3) Computing determinants of square matrices, returned as T
#include <bits/stdc++.h>
#define EPS 1e-10
using namespace std;
typedef vector <int> VI;
typedef double T;
typedef vector <T> VT;
typedef vector < VT > VVT;
T GaussJordan(VVT &a, VVT &b) {
    const int n = a.size();
    const int m = b[0].size();
    VI irow(n), icol(n), ipiv(n);
```

```
T det = 1;
for (int i = 0; i < n; i++) {
    int pj = -1, pk = -1;
    for (int j = 0; j < n; j++) if (!ipiv[j])
        for (int k = 0; k < n; k++) if (!ipiv[k])
            if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk
    if (fabs(a[pj][pk]) < EPS)
        return 0;
    ipiv[pk]++;
    swap(a[pj], a[pk]);
    swap(b[pj], b[pk]);
    if (pj != pk) det *= -1;
    irow[i] = pj;
    icol[i] = pk;
    T c = 1.0 / a[pk][pk];
    det *= a[pk][pk];
    a[pk][pk] = 1.0;
    for (int p = 0; p < n; p++) a[pk][p] *= c;
    for (int p = 0; p < m; p++) b[pk][p] *= c;
    for (int p = 0; p < n; p++) if (p != pk) {
        c = a[p][pk];
        a[p][pk] = 0;
        for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
        for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
}
for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
return det:
```

# 6 String

#### 6.1 Manacher's.cpp

```
#include <bits/stdc++.h>
using namespace std;
string getLongestPalindrome (string s) {
    int len = (int)s.size() * 2 + 1;
    char text[len];
   for (int i = 0; i < len; i++)
       text[i] = '#';
   for (int i = 1; i < len; i += 2)
        text[i] = s[i / 2];
    int maxLen[len];
   memset(maxLen, 0, sizeof maxLen);
   int c = 0, r = 0;
   for (int i = 1; i < len; i++) {
        int j = (c - (i - c));
        \max Len[i] = r > i ? \min(r - i, \max Len[j]) : 0;
        while (i + 1 + maxLen[i] < len && i - 1 - maxLen[i] >= 0 && text[i +
            1 + maxLen[i]] == text[i - 1 - maxLen[i]])
            maxLen[i]++;
        if (i + maxLen[i] > r) {
            r = i + maxLen[i];
            c = i;
       }
   }
    int maxLength = 0;
   int index = 0;
   for (int i = 1; i < len - 1; i++) {
        int currLen = maxLen[i];
        if (currLen > maxLength) {
            maxLength = currLen;
```

```
index = i;
    }
    maxLength = maxLength + (index - maxLength) % 2;
    return s.substr((index - maxLength + 1) / 2, maxLength);
}
      KMP.cpp
#include <bits/stdc++.h>
using namespace std;
struct KMP {
    string pattern;
    vector < int > lcp;
    KMP (string pattern): pattern(pattern), lcp(pattern.size()) {
        buildLcp();
    void buildLcp () {
        for (int i = 1; i < (int)pattern.size(); i++) {</pre>
            int j = lcp[i - 1];
            while (j > 0 && pattern[j] != pattern[i])
                j = lcp[j - 1];
            if (pattern[j] == pattern[i])
                j++;
            lcp[i] = j;
        }
        for (int i = 0; i < pattern.size(); i++)
            printf("%d\n", lcp[i]);
    int search (string text) {
        int j = 0;
        for (int i = 0; i < (int)text.size(); i++) {
            while (j > 0 && text[i] != pattern[j])
                j = lcp[j - 1];
            if (text[i] == pattern[j])
                j++;
            if (j == (int)pattern.size())
                return i - j + 1;
        return -1;
};
       Rabin_Karp.cpp
#include <bits/stdc++.h>
#define MOD 100000007L
#define R 256L
using namespace std;
typedef long long 11;
struct RabinKarp {
    11 pow, patternHash;
    string pattern;
    RabinKarp (string pattern): pattern(pattern) {
        initialize();
    11 getHash (string s, int len) {
        11 ret = 0;
        for (int i = 0; i < len; i++)
            ret = (R * ret + s[i]) % MOD;
        return ret:
    void initialize () {
        patternHash = getHash(pattern, pattern.size());
        for (int i = 0; i < (int)pattern.size() - 1; i++)
            pow = (pow * R) \% MOD;
    int search (string text) {
```

#### 6.4 Z\_Algorithm.cpp

```
* Produces an array Z where Z[i] is the length of the longest substring
* starting from S[i] which is also a prefix of S.
#include <bits/stdc++.h>
using namespace std;
vector<int> compute (string s) {
   vector < int > z(s.size());
    int 1 = 0, r = 0;
   for (int i = 1: i < (int)s.size(): i++) {
        if (i > r) {
            1 = r = i;
            while (r < (int)s.size() && s[r] == s[r - 1])
           r--; r++;
            z[i] = r - 1 + 1;
       } else {
            int j = i - 1;
            if (z[j] < r - i + 1)
               z[i] = z[j];
            else {
               1 = i;
                while (r < (int)s.size() && s[r] == s[r - 1])
               r--; r++;
               z[i] = r - 1 + 1;
       }
   return z;
```

# 6.5 Suffix\_Array.cpp

}

```
#include <bits/stdc++.h>
using namespace std;
struct Suffix {
    int index;
    pair < int, int > rank;
    Suffix () {}
    Suffix (int index, int rank1, int rank2): index(index), rank{rank1, rank2
        } {}
    bool operator < (const Suffix& s) const {
        return rank < s.rank;
    bool operator == (const Suffix& s) const {
        return rank == s.rank;
}:
vector<int> buildSuffixArray (string s) {
    int N = (int)s.size();
    vector < Suffix > suff(N):
    vector < int > ind(N), ret(N);
    for (int i = 0; i < N; i++)
        suff[i] = Suffix(i, s[i], i + 1 < N ? s[i + 1] : -1);
    for (int i = 2; i <<= 1) {
        sort(suff.begin(), suff.end());
        ind[suff[0].index] = 0;
        for (int j = 1; j < N; j++)
            ind[suff[j].index] = (suff[j] == suff[j - 1]?0:1) + ind[suff[
                j - 1].index];
        for (int j = 0; j < N; j++) {
            suff[j].rank.second = suff[j].index + i < N ? ind[suff[j].index +</pre>
                 i] : -1;
            suff[j].rank.first = ind[suff[j].index];
        if ((*--suff.end()).rank.first == N - 1)
            break;
    for (int i = 0; i < N; i++)
        ret[ind[i]] = i;
    return ret;
}
```