



## Management Science

Publication details, including instructions for authors and subscription information:  
<http://pubsonline.informs.org>

### The Short-Run and Long-Run Components of Idiosyncratic Volatility and Stock Returns

Yunting Liu

To cite this article:

Yunting Liu (2021) The Short-Run and Long-Run Components of Idiosyncratic Volatility and Stock Returns. Management Science

Published online in Articles in Advance 15 Feb 2021

. <https://doi.org/10.1287/mnsc.2020.3884>

Full terms and conditions of use: <https://pubsonline.informs.org/Publications/Librarians-Portal/PubsOnLine-Terms-and-Conditions>

This article may be used only for the purposes of research, teaching, and/or private study. Commercial use or systematic downloading (by robots or other automatic processes) is prohibited without explicit Publisher approval, unless otherwise noted. For more information, contact [permissions@informs.org](mailto:permissions@informs.org).

The Publisher does not warrant or guarantee the article's accuracy, completeness, merchantability, fitness for a particular purpose, or non-infringement. Descriptions of, or references to, products or publications, or inclusion of an advertisement in this article, neither constitutes nor implies a guarantee, endorsement, or support of claims made of that product, publication, or service.

Copyright © 2021, INFORMS

Please scroll down for article—it is on subsequent pages



With 12,500 members from nearly 90 countries, INFORMS is the largest international association of operations research (O.R.) and analytics professionals and students. INFORMS provides unique networking and learning opportunities for individual professionals, and organizations of all types and sizes, to better understand and use O.R. and analytics tools and methods to transform strategic visions and achieve better outcomes.

For more information on INFORMS, its publications, membership, or meetings visit <http://www.informs.org>

# The Short-Run and Long-Run Components of Idiosyncratic Volatility and Stock Returns

Yunting Liu<sup>a,\*</sup>

<sup>a</sup> Department of Finance, School of Economics, Peking University, 100871 Beijing, China

\*Corresponding author

Contact: [yuntingliu@pku.edu.cn](mailto:yuntingliu@pku.edu.cn),  <https://orcid.org/0000-0003-2319-6598> (YL)

Received: April 23, 2019

Revised: June 10, 2020; September 10, 2020

Accepted: October 3, 2020

Published Online in *Articles in Advance*:  
February 15, 2021

<https://doi.org/10.1287/mnsc.2020.3884>

Copyright: © 2021 INFORMS

**Abstract.** To capture the dynamics of idiosyncratic volatility of stock returns over different horizons and investigate the relationship between idiosyncratic volatility and expected stock returns, this paper develops and estimates a parsimonious model of idiosyncratic volatility consisting of a short-run and a long-run component. The conditional short-run and long-run components are found to be positively and negatively related to expected stock returns, respectively. The positive relation between the short-run component and stock returns may be caused by investors requiring compensation for bearing idiosyncratic volatility risk when facing trading frictions and hold underdiversified portfolios. The negative relationship between the long-run component and stock returns may reflect the fact that stocks with high long-run idiosyncratic volatility are less exposed to systematic risk factors and, hence, earn lower returns. Moreover, the low-risk exposure of stocks characterized by high idiosyncratic volatility lends support to real-option-based mechanisms to explain this negative relation. In particular, the systematic risk of a firm with abundant growth options crucially depends upon the risk exposure of these options. The value of growth options could rise significantly because of convexity when the increase in idiosyncratic volatility occurs over long horizons. And growth options' systematic risk could fall because the relative magnitude of their value in relation to systematic risk factors decreases.

**History:** Accepted by David Simchi-Levi, finance.

**Funding:** This work was supported by the National Natural Science Foundation of China [Grant 71903004] and the Seed Fund (School of Economics, Peking University).

**Supplemental Material:** Data and the online appendix are available at <https://doi.org/10.1287/mnsc.2020.3884>.

**Keywords:** idiosyncratic volatility • short-run • long-run • cross-sectional stock returns • risk factors • real options

## 1. Introduction

The question of whether a stock's expected return depends on idiosyncratic volatility has been a central theme of the asset pricing literature. In an influential paper, Ang et al. (2006) present evidence that stocks with high realized idiosyncratic volatility have anomalously low returns in the subsequent month. This phenomenon is challenging to interpret because traditional asset pricing theories predict no relation between idiosyncratic volatility and expected returns when investors are well-diversified and markets are complete and frictionless, or a positive relation when investors do not hold well-diversified portfolios and face trading frictions (e.g., Merton 1987).

Ang et al. (2006) define idiosyncratic volatility as the standard deviation of the residuals from the Fama and French (1993) (hereafter FF-3) model estimated using daily returns from the previous month. Because idiosyncratic volatility is time-varying, lagged idiosyncratic volatility may not be a good proxy for

the conditional idiosyncratic volatility. However, the dynamics of conditional idiosyncratic volatility and its relationship with cross-sectional stock returns remain unclear. Fu (2009) constructs measures of conditional idiosyncratic volatility using exponential generalized autoregressive processes (EGARCH) and instead finds a strong positive relationship between conditional idiosyncratic volatility and average returns. Nonetheless, Guo et al. (2014) caution that the EGARCH approach used by Fu (2009) may be subject to substantial look-ahead bias. Once the look-ahead bias is addressed, Fink et al. (2012) also do not find a positive relationship between idiosyncratic volatility and expected returns using the EGARCH model. Finally, Ang et al. (2009) demonstrate that lagged realized idiosyncratic volatility possesses strong explanatory power for one-month-ahead realized idiosyncratic volatility, indicating that lagged realized volatility may serve as a useful proxy for the conditional idiosyncratic volatility. However, they do not

provide a structural model for the dynamics of idiosyncratic volatility.

This paper mainly makes three contributions to the literature. First, I document empirical evidence that idiosyncratic volatility decays quickly between one and three months, while persisting over longer horizons. To capture the dynamics of idiosyncratic volatility over short and long horizons, I develop a parsimonious model of idiosyncratic volatility featuring two components differing in persistence. This modeling approach is in line with the work of Adrian and Rosenberg (2008), Christoffersen et al. (2008), and Corsi (2009). The more persistent component is termed the long-run component and could be modeled as containing a unit root. The other component is referred to as the short-run component and is less persistent. I use both portfolio analysis and Fama and MacBeth (1973) regressions to investigate the cross-sectional relationship between these two components and stock returns. Results from both types of methods indicate a significant negative relation between the conditional long-run idiosyncratic volatility and expected returns, and a significant positive relation between the conditional short-run idiosyncratic volatility and expected returns. Therefore, accounting for the dynamics of idiosyncratic volatility over short and long horizons is crucial to the measurement of conditional idiosyncratic volatility and understanding of the relationship between idiosyncratic volatility and expected stock returns.

Moreover, the return spread between the lowest and highest quintile portfolio sorted by the conditional long-run idiosyncratic volatility is correlated with the return spread sorted by the realized idiosyncratic volatility, with a coefficient of 0.95. And the averages of these return spreads are also quantitatively close, with  $-0.79\%$  per month for the realized volatility and  $-0.73\%$  for the conditional long-run idiosyncratic volatility. This finding suggests that the negative relationship between realized idiosyncratic volatility and stock returns is limited to the long-run idiosyncratic volatility and provides a new dimension for investigating potential mechanisms behind this negative relationship.

Second, this paper provides empirical evidence suggesting that the cross-sectional relationship between conditional long-run idiosyncratic volatility and stock returns may be risk-driven, whereas the relationship between conditional short-run idiosyncratic volatility and stock returns is not. I include three different predictive horizons (1, 12, and 24 months) in the portfolio analysis and find that the predictive relationship between conditional long-run idiosyncratic volatility and expected returns holds for the 1-, 12-, and 24-month horizons. In contrast, the predictive relationship

of conditional short-run idiosyncratic volatility only holds for the one-month horizon. This finding highlights that there are persistent variations in expected returns that are negatively related to conditional long-run idiosyncratic volatility. As Cochrane (1999) explains, if predictability reflects risk, it is likely to persist. Therefore, a risk-based explanation may be an effective means of explaining the persistent negative relationship between the conditional long-run volatility and expected returns, whereas the positive relationship between the conditional short-run idiosyncratic volatility and expected stock returns may not be driven by exposure to systematic risk factors.

Furthermore, I investigate whether the difference in portfolio returns sorted by the short-run and long-run components of idiosyncratic volatility might be explained by exposure to systematic risk factors. The return difference in portfolios sorted by the conditional short-run idiosyncratic volatility is not found to be correlated with common systematic risk factors. This lack of correlations with systematic risk factors is direct evidence against risk-based explanations for the predictability of short-run idiosyncratic volatility. The positive relationship between conditional short-run idiosyncratic volatility and stock returns may arise because investors require compensation for bearing idiosyncratic risk when facing trading frictions in short horizons and, hence, hold underdiversified portfolios (Merton 1987). In contrast, the difference in portfolio returns sorted by the conditional long-run idiosyncratic volatility comoves with systematic risk factors. In particular, I find that portfolios with high idiosyncratic volatility are less exposed to the profitability factor in the five-factor model of Fama and French (2015).

Third, the finding that the negative relation between realized idiosyncratic volatility and stock returns is limited to the long-run idiosyncratic volatility lends support to real-option-based mechanisms as means of explaining the low risk exposure to systematic risk factors of stocks with high long-run idiosyncratic volatility. Real-option-based theories, following Berk et al. (1999) and Carlson et al. (2004), model the value of firms deriving from assets in place and growth options. Firms could exploit valuable investment opportunities by making irreversible investments. Bhamra and Shim (2017) introduce stochastic idiosyncratic cash flow risk into a real-option model with growth options to explain the negative relationship between idiosyncratic volatility and stock returns. For a firm with abundant growth options, its systematic risk crucially depends upon the risk exposure of such options. When idiosyncratic volatility increases, the value of growth options could rise significantly because of convexity. But growth options' exposure to

systematic risk factors could fall, because of the decrease in the relative magnitude of the value of options related to systematic risk. I also outline a model similar to that of Bhamra and Shim (2017) in the online appendix to illustrate this mechanism.

In addition, this real-option-based mechanism highlights the importance of long-run idiosyncratic volatility in explaining the negative relationship between idiosyncratic volatility and stock returns. The rise in growth option values could be pronounced when the increase in idiosyncratic volatility is over long horizons and there is a possibility of waiting to invest. The impact of short-run variations of volatility on option values could be limited. Therefore, only the persistent part of idiosyncratic volatility, that is, long-run idiosyncratic volatility, is negatively related to cross-sectional stock returns.

The remainder of this paper is organized as follows. Section 2 describes how to measure the idiosyncratic volatilities of stocks and decompose them into short-run and long-run components. Section 3 explores the cross-sectional relationship between conditional short-run and long-run idiosyncratic volatility and stock returns using portfolio analysis. Section 4 examines such relationships via cross-sectional regressions. Section 5 investigates risk exposures of stocks with different levels of idiosyncratic volatility and discusses underlying mechanisms behind the cross-sectional relationship between idiosyncratic volatility and stock returns. In particular, the discussion sheds light on the implications of long-run idiosyncratic volatility for mechanisms behind the negative relationship between idiosyncratic volatility and stock returns. Section 6 concludes.

## 2. Estimating Idiosyncratic Volatilities

In this section, I describe the data and methods used to estimate idiosyncratic volatilities.

### 2.1. Data

My data set includes monthly and daily return data on stocks traded in the NYSE, AMEX, and NASDAQ return files from the Center for Research in Security Prices (CRSP). The accounting variables are from COMPUSTAT's annual industrial files of income-statement and balance-sheet data.

The CRSP returns cover NYSE and AMEX stocks until 1973 when NASDAQ returns also come online. The COMPUSTAT data covers the period from 1963 to 2017. The 1963 start date reflects the fact that the book value of common equity (COMPUSTAT item 60) is not generally available prior to 1962. More importantly, COMPUSTAT data from earlier years have a serious selection bias: the pre-1962 data are tilted toward big, historically successful firms.

The procedures below are standard in the literature following Fama and French (1992). To ensure that the accounting variables are known before the returns they are used to explain, I match the accounting data for all fiscal year ends in calendar year  $t - 1$  with the returns for July of year  $t$  to June of year  $t + 1$ . The six-month (minimum) gap between fiscal year end and the return tests is conservative. I use a firm's market equity at the end of December of year  $t - 1$  to compute its book-to-market ratio for year  $t - 1$ .

### 2.2. Idiosyncratic Volatility Definition

Following Ang et al. (2006) and Bali and Cakici (2008), I concentrate on idiosyncratic volatility defined and measured relative to the Fama and French (1993) three-factor (FF-3) model.<sup>1</sup> Specifically, I consider the following specification for each firm at each month:

$$r_{t,d}^i = \alpha_t^i + \beta_{MKT}^i MKT_{t,d} + \beta_{SMB}^i SMB_{t,d} + \beta_{HML}^i HML_{t,d} + \sigma_t^i \epsilon_{t,d}^i, \quad (1)$$

where for day  $d$  in month  $t$ ,  $r_{t,d}^i$  is stock  $i$ 's excess return,  $MKT_{t,d}$  is the market excess returns, and  $SMB_{t,d}$  and  $HML_{t,d}$  capture size and book-to-market effects, respectively. The residuals  $\eta_{t,d}^i \equiv \sigma_t^i \epsilon_{t,d}^i$  are the idiosyncratic risk for month  $t$ . I define the idiosyncratic volatility of stock returns for firm  $i$  in month  $t$  as

$$v_t^i = \sigma_t^i \sqrt{N_m}, \quad (2)$$

where  $N_m$  is the number of trading days in month  $t$  for firm  $i$ . It is useful to note that the idiosyncratic volatility  $v_t^i$  is the daily standard deviation of residuals times the square root of the number of trading days in that month. The inclusion of  $N_m$  transforms the daily return residuals into monthly residuals. This procedure can be seen in French et al. (1987) and Fu (2009).

Because the latent conditional volatility  $v_t^i$  cannot be directly observed, I use realized volatility: squared daily return residuals in month  $t$  obtained through the cross-sectional regression of Equation (1) to measure the individual stock's idiosyncratic volatility for month  $t$ . Specifically,

$$IV_t^i \equiv \sqrt{\sum_{d=1}^{N_m} (\eta_{t,d}^i)^2}. \quad (3)$$

When I refer to idiosyncratic volatility in this paper, I mean idiosyncratic volatility relative to the FF-3 model.

### 2.3. Time-Series Properties of Realized Idiosyncratic Volatility

Table 1 presents the time-series properties of the realized idiosyncratic volatility (IV). I first compute



**Table 1.** Time Series Properties of Idiosyncratic Volatility

Panel A: Some summary statistics of idiosyncratic volatility						
Mean	Standard deviation	Skewness	Kurtosis			
15.54	9.21	2.00	8.23			
Panel B: Autocorrelations of idiosyncratic volatility						
ACF(1)	ACF(2)	ACF(3)	ACF(4)	ACF(5)	ACF(10)	ACF(12)
0.39	0.31	0.28	0.23	0.21	0.12	0.12

*Notes.* This table summarizes the time-series statistics for idiosyncratic volatility. I first compute the statistics for each stock and then average the statistics across all stocks. The sample period is July 1963 to December 2017. The ACF stands for estimated autocorrelations at different lags. The unit of the mean and standard deviation is percentage points.

the time-series statistics of idiosyncratic volatility for each firm and then summarize the mean statistics across about 22,000 firms. The mean of IV is 15.54% across stocks, and the mean standard deviation for IV is 9.21%. The skewness is 2.00, and kurtosis is 8.23, which suggests that the idiosyncratic volatility is positively skewed and fat-tailed. The autocorrelation for realized idiosyncratic volatility is 0.39 with 1-month lag, 0.31 with 2-month lag, 0.21 with 5-month lag, 0.12 with 10-month lag, and 0.12 with one-year lag. The autocorrelation of 0.39 with 1-month lag and 0.31 with 2-month lag suggests that shocks to idiosyncratic volatility are not very persistent within short horizons (a quarter). However, the autocorrelations decay slowly over longer periods, for example, over a year. The autocorrelation of realized idiosyncratic volatility with a lag period of 12 months is still more than 0.1. In comparison, the autocorrelation of an AR(1) process with first-order autocorrelation of 0.39 would predict that the autocorrelation with 12-month lag is less than 0.2 basis points.<sup>2</sup>

This pattern of a relatively quick initial decline in the autocorrelation function followed by a slower decay is sufficient evidence to dismiss using the simple Autoregressive moving average (ARMA) model to model idiosyncratic volatility (e.g., Barndorff-Nielsen and Shephard 2002). Corsi (2009) proposes that the aggregate stock return volatility could be captured by an additive cascade model of volatility defined over different time periods. The empirical evidence in this section suggests that the idiosyncratic volatility of stock returns could also be better captured by a process with components of different persistence. Therefore, I model the log of idiosyncratic volatility as the sum of a short-run and a long-run component. The short-run component is less persistent and has a large impact on the autocorrelations of

idiosyncratic volatility over short horizons (a quarter). And the more persistent long-run component dominates the autocorrelations over longer horizons (a year or longer).

#### 2.4. Decomposing Idiosyncratic Volatility

To decompose idiosyncratic volatilities into short-run and long-run components, I model the idiosyncratic volatility  $v_t^i$  as follows:

$$\text{Idiosyncratic Volatility : } \log v_t^i = s_t^i + l_t^i,$$

$$\text{Short-Run Component : } s_{t+1}^i = \rho_s^i s_t^i + \sigma_s^i \epsilon_{s,t}^i,$$

$$\text{Long-Run Component : } l_{t+1}^i = \phi_i + \rho_l^i l_t^i + \sigma_l^i \epsilon_{l,t}^i. \quad (4)$$

I refer to this model as the short- and long-run (SL) model hereafter. In Equation (4), the log-volatility is the sum of two components,  $s_t$  and  $l_t$ . Each component follows a first-order autoregressive process AR(1) with its own rate of mean reversion. The short-run component  $s_t$  has a mean of zero, whereas the long-run component  $l_t$  contains a constant  $\phi_i$ .<sup>3</sup> I normalize the mean reversion parameters such that  $\rho_l > \rho_s$ . This restriction identifies the model, as otherwise, the two components can be interchangeable. Moreover, parameters  $\sigma_s$  and  $\sigma_l$  denote the volatility of shocks to the short-run and long-run components. Shocks to the short- and long-run components  $\epsilon_{s,t}$  and  $\epsilon_{l,t}$  are normal independently and identically distributed with zero expectation and unit variance.

For each firm, Equation (4) is readily in a state space form, and the unobserved short-run and long-run components can be directly estimated via a Kalman filter. I consider  $\hat{s}_t \equiv \mathbb{E}_{t-1}(s_t | y_1, y_2, \dots, y_{t-1})$  and  $\hat{l}_t \equiv \mathbb{E}_{t-1}(l_t | y_1, y_2, \dots, y_{t-1})$  as the expectations for the short-run and long-run components at time  $t$  based on information available at time  $t-1$ . The smoothed estimates  $\tilde{s}_t = \mathbb{E}(s_t | y_1, y_2, \dots, y_T)$  and  $\tilde{l}_t = \mathbb{E}(l_t | y_1, y_2, \dots, y_T)$ , which use all the sample information, may produce

more precise estimates for the expectation of unobserved components  $s_t$  and  $l_t$  at each point in time. Therefore, full information set estimates are appropriate for asset pricing tests because of the gain in accuracy. However, in terms of evaluating trading strategies, incorporating future observations directly in forecasts may lead to using substantial information beyond what investors are aware of.<sup>4</sup> Thus, I report results using filtered estimates in the subsequent empirical analysis. Empirical results using smoothed estimates are statistically more significant but are nevertheless included in the online appendix.

Starting with Engle and Lee (1999), a number of studies find that two-component volatility models outperform one-component specifications in explaining equity market volatility. Adrian and Rosenberg (2008) consider a two-component model for aggregate stock market volatility and find that the prices of risk are different for the short-run and long-run components. In addition, two-component volatility models perform well in the option pricing literature. For example, Christoffersen et al. (2008) show that modeling stock return volatility with short- and long-run components perform well for option pricing. My paper differs from Adrian and Rosenberg (2008) in both the estimation method and the focus on idiosyncratic volatility. Adrian and Rosenberg (2008) estimate volatilities using a maximum-likelihood method on daily stock returns and then aggregate volatilities to monthly frequencies. I use a state-space model on realized idiosyncratic volatility to decompose realized idiosyncratic volatility into short-run and long-run components. This method is convenient for extracting filtered and smoothed estimates of conditional idiosyncratic volatility.

## 2.5. A Permanent and Transitory Special Case

In my empirical work, I also investigate a special case of Equation (4) where the long-run component contains a unit root, and the short-run component follows a white noise process. I refer to this model as the permanent and transitory (PT) model:

$$\begin{aligned} \text{Idiosyncratic Volatility : } \log v_t^i &= s_t^i + l_t^i, \\ \text{Short-run Component : } s_{t+1}^i &= \sigma_s^i \epsilon_{s,t}^i, \\ \text{Long-run component : } l_{t+1}^i &= l_t^i + \sigma_l^i \epsilon_{l,t}^i. \end{aligned} \quad (5)$$

Equation (5) may be viewed as a special case of (4) with the restriction that  $\rho_s = 0$  and  $\rho_l = 1$ . The log-volatility is the sum of two components,  $s_t$  and  $l_t$ . The long-run component  $l_t$  follows a random walk. Thus, changes to the long-run volatility could be permanent and are persistent over time. For each firm, Equation (5) can also be estimated using a Kalman filter. Because the long-run component  $l_t$

follows a random walk, the one-step-ahead conditional expectation of the long-run component  $\mathbb{E}_t(l_{t+1}|y_1, y_2, \dots, y_t) = \mathbb{E}_t(l_t|y_1, y_2, \dots, y_t)$  and that of the short-run component  $\mathbb{E}_{t-1}(s_t|y_1, y_2, \dots, y_{t-1})$  trivially equal zero. Therefore, for the permanent and transitory (PT) model, I only consider the expectation of the long-run component  $\hat{l}_t = \mathbb{E}_{t-1}(l_t|y_1, y_2, \dots, y_{t-1})$  and  $\tilde{l}_t = \mathbb{E}(l_t|y_1, y_2, \dots, y_T)$  and investigate their relationship with expected returns.

## 2.6. Parameter Estimates of the Idiosyncratic Volatility Model

In practice, the true conditional idiosyncratic volatility  $v_t$  cannot be directly observed. Consequently, the realized volatility  $IV_t$  is a proxy for the latent volatility subject to measurement errors. Because measurement errors are largely identically and independently distributed over time, it has little forecasting power for forming conditional expectations. In empirical studies, realized volatilities are usually treated as measuring latent volatilities without errors (e.g., Bollerslev and Zhou 2002, Chua et al. 2010). In this paper, I report results using this approach because it massively simplifies subsequent estimation and analysis. The results with identically and independently distributed measurement errors are quantitatively close and are reported in the online appendix.

Table 2 summarizes parameter estimates for the short- and long-run volatility (SL) model with Equation (4) and the permanent transitory volatility (PT) model with Equation (5). Both the SL and the PT model are estimated using the maximum likelihood method. For the SL model, the mean AR(1) parameter for the short-run component is  $-0.07$ , while the median is  $-0.003$ . The long-run component is more persistent, with a mean AR(1) coefficient of  $0.79$  and a median of  $0.94$ . The mean volatility of shocks to the

**Table 2.** Parameter Estimates for Idiosyncratic Volatility Model

Panel A: The short- and long-run volatility (SL) model				
Variables	$\rho_s$	$\rho_l$	$\sigma_s$	$\sigma_l$
Mean	$-0.07$	$0.79$	$0.29$	$0.20$
Median	$-0.003$	$0.94$	$0.31$	$0.15$
Panel B: The permanent and transitory volatility model				
Variables	$\sigma_s$	$\sigma_l$		
Mean	$0.36$	$0.14$		
Median	$0.34$	$0.10$		

*Notes.* This table summarizes the properties of parameter estimates for the short- and long-run idiosyncratic volatility processes. I first compute parameter estimates for each stock and then construct the mean and median statistics across all stocks. The sample period is July 1963 to December 2017.

short-run component is 0.29, and the median is 0.31. For the long-run component, the mean volatility is 0.20, and the median is 0.15. Therefore, the short-run component does not persist long, but shocks to it are relatively bigger. It mostly fluctuates around the mean, zero. Despite shocks to the long-run component tending to be smaller, the long-run component is relatively persistent, which means that the level of the long-run component can display substantial variations over time. In the online appendix, I also plot estimates of the short-run and long-run components of idiosyncratic volatility for a few randomly selected firms.

The permanent and transitory (PT) model can be viewed as a special case of the SL model with  $\rho_s = 0$  and  $\rho_l = 1$ . Given that the median estimate of  $\rho_s$  is  $-0.003$  and  $\rho_l$  is  $0.94$  from the SL model, the PT model can be a plausible model to capture the dynamics of idiosyncratic volatility. For the PT model, the only parameters to be estimated are the volatility of shocks to the short-run and long-run components. The mean volatility of shocks to the short-run component is  $0.36$ , and the median is  $0.34$ . As for the volatility of shocks to the long-run component, the mean is  $0.14$ , and the median is  $0.10$ . The magnitude of shocks is also largely similar to estimates from the SL model.

### 3. Portfolio Sorts of Idiosyncratic Volatility and Cross-Sectional Stock Returns

This section considers the performance of portfolios formed by different measures of idiosyncratic volatilities and asks whether exposures to different volatilities are systematically important for expected stock returns. To examine trading strategies based on idiosyncratic volatility, I consider the standard portfolio formation strategies following Jegadeesh and Titman (1993) with a holding period of  $N = 1, 12, 24$  months. For strategies with multimonth holding periods, I average across the  $N$  subquintiles formed at the beginning of month  $t - s$ , for  $s = 0, 1, 2, 3, \dots, N - 1$ , as the return for a given quintile.

#### 3.1. Patterns in Average Returns for Idiosyncratic Volatility

I first consider value-weighted quintile portfolios formed every month by sorting stocks based on realized idiosyncratic volatility relative to the FF-3 model. Portfolios are formed every month based on realized volatility computed using daily data of the previous month. Panel A in Table 3 shows that the average return increases slightly from  $0.96\%$  per month to  $1.05\%$  going from the quintile 1 (low idiosyncratic volatility stocks) to quintile 3. Then portfolios' returns drop tremendously going to quintile 5.

The portfolio with the highest idiosyncratic volatility (quintile 5) has a surprisingly low average return of  $0.17\%$  per month. The difference in returns between the highest and lowest portfolios is as large as  $-0.79\%$  per month, which is statistically significant, with a robust  $t$ -statistic of  $-2.84$ . These numbers are similar to the findings of Ang et al. (2006), who find a return spread of  $-0.97\%$  between quintile 5 and quintile 1 portfolios, with a significance of  $-2.97$ , in a July 1963–December 2000 sample.

The FF3-alpha for the quintile 5 portfolio is  $-1.21\%$  per month, with a robust  $t$ -statistic of  $-7.15$ . Therefore, the difference in quintile portfolio returns cannot be explained by our standard FF-3 model. The difference in average returns in Table 3 indicates a significant negative relationship between expected return and idiosyncratic volatility. Panel B in Table 3 also reports average portfolio returns with holding periods of  $N = 12, 24$  months. For the holding period of  $N = 12$  months, the average return decreases from  $0.91\%$  per month for the quintile 1 portfolio (low idiosyncratic volatility stocks) to  $0.58\%$  for the quintile 5 portfolio (high idiosyncratic volatility stocks). The difference in returns is  $-0.33\%$ , with a robust  $t$ -statistic of  $-2.89$ . Similarly, when the holding period is  $N = 24$  months, the average return of the quintile 1 portfolio is  $0.89\%$  per month, while it is  $0.72\%$  for the quintile 5 portfolio. The difference in returns is  $-0.17\%$ , with a robust  $t$ -statistic of  $-2.12$ . Therefore, the negative relation between lagged idiosyncratic volatility and stocks returns holds for longer holding periods, suggesting that the cross-sectional relationship is persistent and expected returns have a persistent component.

#### 3.2. Portfolios Sorted by Short-Run and Long-Run Volatilities

Estimating the state-space model of (4) and (5) produces estimates of the conditional short-run and long-run volatilities at the monthly frequency. I form value-weighted quintile portfolios sorting by the filtered short-run volatility  $\hat{s}_t$  and long-run volatility  $\hat{l}_t$ .

First, I consider the performance of portfolios sorted by the filtered estimates of the conditional long-run component with a holding period of one month. Table 4 reveals substantial spreads in average returns across quintile portfolios. For both the SL model and the PT model, the portfolio with the highest long-run volatilities earns particularly low average returns. The average return of the quintile 5 portfolio with the highest long-run idiosyncratic volatility is as low as  $0.18\%$  per month for the SL model and  $0.25\%$  for the PT model. The spread in average returns between the portfolios with the lowest and highest long-run volatility is  $-0.73\%$  per month for the SL model and  $-0.68\%$  for the PT model. The difference in returns

**Table 3.** Portfolios Sorted by Idiosyncratic Volatility

Panel A: Ranking on realized idiosyncratic volatility						
Rank	Mean	Standard deviation	% Market share	FF-3 alpha		
1 (low)	0.96	3.65	43.8%	0.11 (3.14)		
2	0.96	4.59	31.3%	0.00 (0.08)		
3	1.05	5.69	15.3%	−0.01 (−0.17)		
4	0.76	7.03	7.1%	−0.37 (−3.82)		
5 (high)	0.17	8.38	2.5%	−1.10 (−7.40)		
5 − 1	−0.79 (−2.84)	6.66		−1.21 (−7.15)		
Panel B: Ranking on realized idiosyncratic volatility with multiple holding periods						
Period	1 Low	2	3	4	5 High	5 − 1
N = 1	0.96	0.96	1.05	0.76	0.17	−0.79 (−2.84)
N = 12	0.91	0.95	0.97	0.89	0.58	−0.33 (−2.89)
N = 24	0.89	0.94	0.97	0.94	0.72	−0.17 (−2.12)

*Notes.* I form value-weighted quintile portfolios every month by sorting stocks based on idiosyncratic volatility relative to the FF-3 model. Portfolios are formed every month, based on volatility computed using daily data of the previous month. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The statistics in the columns labeled Mean and Standard deviation are measured in monthly percentage terms and apply to total, not excess, returns. The column 5 − 1 refers to the difference in monthly returns between portfolio 5 and portfolio 1. The alpha column reports Jensen's alpha with respect to the FF-3 model. Robust Newey and West (1987) *t*-statistics with up to one lag are reported in square brackets. The sample period is July 1963 to December 2017.

also cannot be explained by the FF-3 model. The highest long-run volatility portfolio has an FF3-alpha of −1.25% for the SL model and −1.19% for the PT model. The alphas are statistically significant, with robust *t*-statistics of −6.06 and −5.72, respectively. Therefore, there is a strong negative relation between conditional long-run volatility and stock returns.

Next, Panels A and B in Table 6 report the portfolio performance of sorting on long-run idiosyncratic volatility for holding periods of  $N = 12, 24$  on the filtered estimates of long-run idiosyncratic volatility. Statistical significance actually increases for longer holding periods. For the SL model, return spreads are −0.73%, −0.38%, and −0.22%, respectively, for  $N = 1, 12, 24$ . The corresponding *t*-statistics are −2.10, −2.67, and −2.22. Higher statistical significance suggests that conditional long-run idiosyncratic volatility plays a crucial role behind the persistent negative relationship between idiosyncratic volatility and stock returns.

Last, Table 5 and Panel C in Table 6 report the performance of portfolios sorted by the filtered estimates of conditional short-run idiosyncratic volatility. The high

minus low short-run volatility portfolio earns an average monthly return of 0.19%, with a *t*-statistic of 2.81, which indicates that there is a significant positive relation between conditional short-run idiosyncratic volatility and expected stock returns. Extending the strategy for multiple holding periods of  $N = 12$  and  $N = 24$  reveals that this positive relationship is not persistent over time. Panel C in Table 6 reports that the average spread is 0.03, and the significance is 1.40 over 12-month holding periods. Moreover, the average spread over the 24-month holding period even becomes negative, namely, −0.02, with a significance of −0.99. These results suggest that stock prices go up when the conditional idiosyncratic volatility increases. However, as the short-run volatility dies off, stock prices revert back over time. Given the low average persistence parameter  $\rho_s$  estimated, the speed of reversion in stock prices may be slow to some extent. Holding periods of 12 and 24 months seem to be relatively long. This suggests that there may be some degree of friction (limited investor attention or trading friction, for example) in slowing the reversion of stock prices.



**Table 4.** Portfolios Sorted by the Filtered Estimates of Conditional Long-Run Volatility

Panel A: Short and long-run volatility (SL) model				
Rank	Mean	Standard deviation	% Market share	FF-3 alpha
1 (low)	0.92	3.68	47.2%	0.09 (2.50)
2	1.00	4.77	32.0%	0.00 (0.06)
3	1.05	6.21	13.7%	−0.01 (−0.1)
4	0.86	7.98	5.6%	−0.31 (−2.73)
5 (high)	0.18	9.88	1.5%	−1.15 (−6.26)
5 − 1	−0.73 (−2.10)	8.26		−1.25 (−6.06)
Panel B: Permanent and transitory volatility (PT) model				
Rank	Mean	Standard deviation	% Market share	FF-3 alpha
1 (low)	0.93	3.67	46.8%	0.10 (2.90)
2	1.00	4.75	32.0%	−0.00 (−0.09)
3	1.05	6.14	13.9%	−0.01 (−0.17)
4	0.84	7.91	5.7%	−0.33 (−2.88)
5 (high)	0.25	9.84	1.6%	−1.09 (−5.79)
5 − 1	−0.68 (−1.94)	8.23		−1.19 (−5.72)

*Notes.* Portfolios are formed every month based on the filtered estimates of conditional short-run idiosyncratic volatility  $\hat{l}_t$ . Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The statistics in the columns labeled Mean and Standard deviation are measured in monthly percentage terms and apply to total, not excess, returns. The column 5 − 1 refers to the difference in monthly returns between portfolio 5 and portfolio 1. The alpha column reports Jensen's alpha with respect to the FF-3 model. Robust Newey and West (1987)  $t$ -statistics with up to one lag are reported in square brackets. The sample period is July 1963 to December 2017.

#### 4. Cross-Sectional Regressions

My empirical analysis thus far is based on portfolio sorts. In this section, I investigate the cross-sectional relationship between average stock returns and estimated conditional idiosyncratic volatilities. I follow Fama and MacBeth (1973) by regressing cross-sectional stock returns on idiosyncratic volatilities and other firm characteristics on a monthly basis and calculate the time-series averages of the coefficients. My goal is to test whether the coefficient on idiosyncratic volatility in explaining cross-sectional stock returns is significantly different from zero.

Specifically, I run the following cross-sectional regressions each month for the SL and PT model:

$$R_{i,t+1}^e = \gamma_{l,t} \hat{l}_t + \gamma_{s,t} \hat{s}_t + \epsilon_{i,t+1}, \quad (6)$$

$$R_{i,t+1}^e = \gamma_{l,t} \tilde{l}_t + \gamma_{s,t} \tilde{s}_t + \epsilon_{i,t+1}, \quad (7)$$

where  $r_{t+1,i}^e$  is stock  $i$ 's excess return in month  $t + 1$  minus its Fama and French (1993) factor adjustments.

Volatilities with tildes are smoothed estimates, and those with hat signs are filtered estimates.

Table 7 shows time-series averages of the coefficients from the month-by-month Fama–MacBeth (FM) regressions of the cross-section of stock returns on different measures of idiosyncratic volatility. The average coefficient on variables used to explain expected returns provides standard FM tests for determining which variables on average have explanatory power during the July 1963 to December 2017 period.<sup>5</sup>

The average coefficient on the log of realized idiosyncratic volatility (IV) is  $-0.52$ , with a  $t$ -statistic of  $-5.66$ . The finding confirms the negative relationship between idiosyncratic volatility and expected return found by Ang et al. (2006).

Subsequently, I include measures of conditional short-run and long-run idiosyncratic volatility into FM regressions. Regressions using the SL model are reported in Table 7. The regression results indicate that there exists a negative (positive) relationship

**Table 5.** Portfolios Sorted by Filtered Estimates of Expected Short-Run Volatility

Rank	Mean	Standard deviation	% Market share	FF-3 alpha
1 (low)	0.77	4.63	12.3%	−0.16 (−2.84)
2	0.89	4.44	23.4%	−0.02 (−0.44)
3	0.98	4.42	28.2%	0.07 (2.31)
4	0.91	4.45	23.4%	0.01 (0.39)
5 (high)	0.96	4.66	12.7%	0.01 (0.25)
5 − 1	0.19 (2.81)	1.74		0.17 (2.40)

*Notes.* Portfolios are formed every month based on the filtered conditional short-run idiosyncratic volatility  $\hat{s}_t$ . Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The statistics in the columns labeled Mean and Standard deviation are measured in monthly percentage terms and apply to total, not excess, returns. The column 5 − 1 refers to the difference in monthly returns between portfolio 5 and portfolio 1. The alpha column reports Jensen's alpha with respect to the FF-3 model. Robust Newey and West (1987)  $t$ -statistics with up to one lag are reported in square brackets. The sample period is July 1963 to December 2017.

between conditional long-run (short-run) volatility and expected returns. The average coefficient is −0.50 (2.41), with a significant  $t$ -statistic of −4.01 (6.10) for the filter long-run (short-run) component. The statistical significance is also higher for the smoothed estimates. These FM regression results lend support to the finding in Section 3.2 with stocks sorted by  $\hat{s}_t$  and  $\hat{l}_t$ . It is also useful to explain the finding using the PT model to measure conditional long-run idiosyncratic volatility. Table 8 shows that the average coefficient on the filtered estimates of conditional long-run volatility  $\hat{l}_t$  is −0.49, with a  $t$ -statistic of −4.11.

#### 4.1. Additional Robustness Check

As robustness checks, I include two additional controls in the Fama–MacBeth regressions—return reversals and unexpected idiosyncratic volatility—in this section. The findings in the previous section remain robust when controlling for these two channels.

**4.1.1. Controlling for Return Reversals.** Stock returns display short-term reversals (Jegadeesh 1990; Lehmann 1990). Return reversal describes the phenomenon that if a stock's previous-month return is too high (low), it will tend to reverse the following month and earn a low (high) return. Following Huang et al. (2010), I use the returns of individual stocks in the prior month to control for return reversals. Therefore, Equation (7) is modified to allow for the previous month's stock return:

$$r_{t,d}^i = \gamma_{l,t} \hat{l}_t + \gamma_{s,t} \hat{s}_t + \beta_{r,t-1} r_{t-1}^i + v_{t,d}^i e_{t,d}^i. \quad (8)$$

Without the previous month's stock return  $r_{t-1}^i$ , the relationship between idiosyncratic risk and expected stock returns may be negatively biased because the coefficient incorporates part of the return reversal that should have been captured by the stock return of the previous month. Including return reversals in the FM regression, Table 7 shows that the coefficient on the log of realized volatility is reduced to −0.42 with a  $t$ -statistic of −4.55. This finding is consistent with the finding in Huang et al. (2010) that part of the finding by Ang et al. (2006) can be explained by return reversals. And the coefficient on the lagged month return is statistically significant, with a statistic of −10.59.

However, accounting for return reversals does not quite reduce the coefficients of the conditional short-run and long-run components. Some of the coefficients become even more significant after the lagged month return control is added. Still, the coefficient on lagged month return is significant for both the SL and the PT models, with  $t$ -statistics of −11.36 and −12.23. Therefore, return reversals are not the key driver of the relationship between short-run and long-run conditional idiosyncratic volatility and expected returns.

**4.1.2. Controlling for Unexpected Idiosyncratic Volatility.** In the spirit of the argument of French et al. (1987), the relationship between expected idiosyncratic volatility and expected returns in the above regression may be clouded by the relationship between unexpected idiosyncratic volatility and unexpected stock returns. To control for this effect, I add unexpected idiosyncratic volatility to the FM regression. I define the unexpected idiosyncratic volatility as

$$\mu_t = \log v_t - \hat{s}_t - \hat{l}_t,$$

where  $\log v_t$  is the log of realized volatility at time  $t$ , and  $\hat{s}_t$  and  $\hat{l}_t$  are filtered volatility estimates made at time  $t - 1$  for the short-run and long-run components at time  $t$ . The average of first-order autocorrelations of  $\mu_t$  is 0.003, suggesting  $\mu_t$  has no time-series predictability. The average of correlations between  $s_t$  and  $\mu_t$  is 0.07, and it is −0.06 between  $s_t$  and  $l_t$ . These statistics justify  $\mu_t$  as being unexpected. When the unexpected idiosyncratic volatility is added to the regression, cross-sectional relationships between conditional short-run and long-run idiosyncratic volatility and expected stock returns remain robust.

Table 7 reports results for the SL model. The coefficient on the filtered short-run (long-run) idiosyncratic volatility is 3.52 (−0.34) with a robust  $t$ -statistic of 8.92 (−2.66), which further supports that there is a strong negative (positive) relationship between the conditional long-run (short-run) component and average

**Table 6.** Portfolios Sorted by Idiosyncratic Volatility with Multiple Holding Periods

Panel A: Ranking on conditional long-run idiosyncratic volatility: PT						
Period	1 Low	2	3	4	5 High	5 – 1
$N = 1$	0.93	1.00	1.05	0.84	0.25	–0.68 (–1.94)
$N = 12$	0.89	0.99	1.01	0.94	0.55	–0.34 (–2.46)
$N = 24$	0.87	0.98	1.03	0.99	0.69	–0.19 (–1.96)
Panel B: Ranking on conditional long-run idiosyncratic volatility: SL						
Period	1 Low	2	3	4	5 High	5 – 1
$N = 1$	0.92	1.00	1.05	0.86	0.18	–0.73 (–2.10)
$N = 12$	0.89	0.99	1.02	0.94	0.51	–0.38 (–2.67)
$N = 24$	0.87	0.98	1.03	0.99	0.66	–0.22 (–2.22)
Panel C: Ranking on conditional short-run idiosyncratic volatility: SL						
Period	1 Low	2	3	4	5 High	5 – 1
$N = 1$	0.77	0.89	0.98	0.91	0.96	0.19 (2.81)
$N = 12$	0.87	0.90	0.94	0.89	0.90	0.03 (1.40)
$N = 24$	0.90	0.89	0.93	0.89	0.88	–0.02 (–0.99)

*Notes.* Panel A reports the performance of portfolios sorted by conditional long-run idiosyncratic volatility for the permanent and transitory (PT) model. Panel B and Panel C report the performance of portfolio sorted by the conditional short-run and long-run idiosyncratic volatility for the short- and long-run (SL) model. I form value-weighted quintile portfolios every month by sorting stocks based on idiosyncratic volatility relative to the FF-3 model. The holding period is 1 month, 12 months, or 24 months. Portfolio 1 (5) is the portfolio of stocks with the lowest (highest) volatilities. The statistics in the columns labeled Mean and Standard deviation are measured in monthly percentage terms and apply to total, not excess, returns. The column 5 – 1 refers to the difference in monthly returns between portfolio 5 and portfolio 1. The alpha column reports Jensen's alpha with respect to the FF-3 model. Robust Newey and West (1987)  $t$ -statistics with up to one lag are reported in square brackets. The sample period is July 1963 to December 2017.

stock returns. The coefficient on the unexpected idiosyncratic volatility is also significant. For the filtered idiosyncratic volatility estimates group, the coefficient of unexpected idiosyncratic volatility is 4.81, with a high  $t$ -statistic of 22.61. The positive relationship between unexpected idiosyncratic volatility and stock returns is consistent with the positive contemporaneous relationship between stock returns and firm-level idiosyncratic volatility found by Duffee (1995) and Grullon et al. (2012).<sup>6</sup> Table 8 reports similar results of adding unexpected idiosyncratic volatility to the PT model.

## 5. The Cross-Sectional Relationships Between Short-Run and Long-Run Idiosyncratic Volatility and Expected Stock Returns

In this section, I examine the risk exposures of portfolios sorted by short-run and long-run idiosyncratic

volatility. Then I attempt to interpret these results through possible channels through which idiosyncratic volatility is related to stock returns.

### 5.1. Investigating Risk Exposures

To investigate whether the cross-sectional relationship between short- or long-run idiosyncratic volatility and stock returns can be explained by risk exposures, I examine return differences between portfolios sorted by short-run and long-run idiosyncratic volatility. If these return differences are driven by risk, they should comove with systematic risk factors. If no significant correlations are found, the relation could then be non-risk-based and driven by forces such as market frictions.

To this end, I compute the correlations between the returns of the high minus low (5 – 1) portfolio sorted by conditional short-run idiosyncratic volatility,

**Table 7.** Relationship between Idiosyncratic Volatility and Expected Returns: SL Model

Short and long-run volatility (SL) model				
$\log v_t$	$\hat{s}_t$	$\hat{l}_t$	$Ret(-1)$	$\mu_t$
-0.52 (-5.66)	2.41 (6.10)	-0.50 (-4.01)		
-0.42 (-4.46)			-4.82 (-10.67)	
	2.70 (6.81)	-0.48 (-3.74)	-5.16 (-11.43)	
	3.52 (8.93)	-0.34 (-2.66)	-4.34 (-10.19)	4.81 (22.61)

Notes. The average coefficient is the time-series average of monthly regression coefficients from July 1963 to December 2017, and the  $t$ -statistic is the average coefficient divided by its time-series standard error. The  $t$ -statistic is reported in brackets.

long-run idiosyncratic volatility, and lagged realized volatility, and the five factors of Fama and French (2015) (FF-5). Based on the evidence of Novy-Marx (2013) and Titman et al. (2004), the profitability factor Robust Minus Weak (RMW) and investment factor Conservative Minus Aggressive (CMA) are added in addition to the three factors of Fama and French (1993).<sup>7</sup> As for the short-run and long-run components, I use the filtered estimates here, which use information at time  $t - 1$  to predict the conditional volatility at time  $t$ .

Table 9 reports the correlations between portfolio spreads sorted by idiosyncratic volatility and the five factors. It is found that the return spread sorted by the conditional short-run component, denoted by IVFS, is not correlated with the spread sorted by the conditional long-run idiosyncratic volatility IVFL, realized

**Table 8.** Relationship Between Idiosyncratic Volatility and Expected Returns: PT Model

Permanent and transitory volatility (PT) model			
$\log v_t$	$\hat{l}_t$	$Ret(-1)$	$\mu_t$
-0.52 (-5.73)	-0.49 (-4.11)		
-0.42 (-4.55)		-4.79 (-10.59)	
	-0.48 (-3.88)	-5.07 (-11.21)	
	-0.26 (-2.12)		4.88 (23.34)
	-0.26 (-2.08)	-4.19 (-9.72)	4.75 (22.90)

Notes. The average coefficient is the time-series average of monthly regression coefficients from July 1963 to December 2017, and the  $t$ -statistic is the average coefficient divided by its time-series standard error. The  $t$ -statistic is reported in brackets.

idiosyncratic volatility IVFR, or the five factors of Fama and French (2015). The correlation is  $-0.04$  with the IVFL portfolio,  $0.02$  with the excess market return,  $0.06$  with the size factor SMB,  $0.04$  with the value factor HML,  $0.04$  with the RMW factor, and  $0.04$  with the CMA factor. The lack of correlations with systematic risk factors further suggests that the cross-sectional relationship between the conditional short-run component and stock returns is not likely driven by risk.

In the meantime, the return spread sorted by the conditional long-run component, denoted as IVFL, is strongly correlated with the return spread sorted by realized idiosyncratic volatility, denoted as IVFR, with a correlation of  $0.95$ . Therefore, the cross-sectional relationship between realized idiosyncratic volatility and stock returns found by Ang et al. (2006) is mostly captured by the long-run idiosyncratic volatility. Besides, the return spread IVFL correlates with the book-to-market factor HML, profitability factor RMW, and investment factor CMA with a negative sign. The correlation with the profitability factor is especially strong, with a coefficient of  $-0.62$ . Given that these factors may earn positive risk premiums, low exposure to them could help explain why stocks with high conditional long-run idiosyncratic volatility earn low returns.

Table 10 systematically examines how these five factors are useful to explain the portfolio returns sorted by the realized idiosyncratic volatility beyond the FF-3 model. The test assets used here are the 25 portfolios formed monthly on size and realized idiosyncratic volatility (Size-IV), provided on Kenneth French's website.<sup>8</sup> Similar to the findings of Fama and French (2016), the FF-5 model provides a better description of average returns on these 25 portfolios. Table 12 reports the Gibbons et al. (1989) GRS statistic, which is reduced from  $6.76$  for the three-factor model to  $5.56$  for the five-factor model. The average absolute alpha is also reduced significantly from  $0.24$  to  $0.13$ . In particular, Table 10 shows that stocks with high idiosyncratic volatility have significant negative exposure to the profitability factor RMW.

While the profitability factor is useful to explain the negative relationship between idiosyncratic volatility and the cross section of stock returns, it does not fully capture it. Strong exposure to RMW still misses part of the low average returns of high realized idiosyncratic volatility small stocks. Therefore, I investigate whether there is an additional factor structure behind the negative relationship between idiosyncratic volatility and the cross section of stock returns. In particular, I investigate whether IVFL is a useful factor in explaining the cross-sectional relationship between idiosyncratic volatility and stock returns.



**Table 9.** Correlations of Return Spreads with the Five Factors of Fama and French (2015)

	IVFS	IVFL	IVFR	$R_M - R_F$	SMB	HML	RMW	CMA
IVFS	1.00	-0.04	-0.00	0.02	0.06	0.04	0.04	0.04
IVFL	-0.04	1.00	0.95	0.52	0.68	-0.33	-0.62	-0.37
IVFR	-0.00	0.95	1.00	0.50	0.66	-0.31	-0.58	-0.36
$R_M - R_F$	0.02	0.52	0.50	1.00	0.28	-0.26	-0.23	-0.38
SMB	0.06	0.68	0.66	0.28	1.00	-0.07	-0.35	-0.10
HML	0.04	-0.33	-0.31	-0.26	-0.07	1.00	0.06	0.70
RMW	0.04	-0.62	-0.58	-0.23	-0.35	0.06	1.00	-0.04
CMA	0.04	-0.37	-0.36	-0.38	-0.10	0.70	-0.04	1.00

Notes. The table reports pairwise correlations between return spreads of the high minus low portfolio and the five factors of Fama and French (2015). IVFS, return spread of sorting stocks by the conditional short-run idiosyncratic volatility; IVFL, return spread sorted by the conditional long-run idiosyncratic volatility; IVFR, return spread sorted by lagged realized idiosyncratic volatility;  $R_M - R_F$ , excess market return; SMB, size factor; HML, book-to-market factor; RMW, profitability factor; CMA, investment factor.

This is testing whether there is a “slope” structure between portfolios sorted by idiosyncratic volatility.

Tables 11 and 12 report the results of adding the IVFL factor to the FF-5 model. As Table 12 shows, adding the IVFL factor does not lead to substantial gains beyond the FF-5 model. The GRS statistic is reduced from 5.55 to 5.15, and the average absolute alpha decreases from 0.13 to 0.11. However, Table 11 also shows that, after the IVFL factor is added, coefficients on the RMW factor become almost insignificant. This pattern suggests that the information of RMW is largely captured by the IVFL factor. Therefore, it may be worthwhile for future research to investigate additional risk factor structures behind the negative relationship between conditional long-run idiosyncratic volatility and stock returns.

The empirical analysis in this section complements the paper by Guo and Savickas (2010). Guo and Savickas (2010) demonstrate that the difference in returns between low and high realized idiosyncratic volatility stocks is a priced factor in the cross-section of stock returns. And this factor is correlated with the value factor HML defined by Fama and French (1993). However, they have not examined risk exposures to the FF-5 model. This paper examines whether return differences between low and high conditional short-run and long-run volatility are priced factors and whether they are related to the five factors of Fama and French (2015).

## 5.2. Why Is Short-Run Idiosyncratic Volatility Related to Stock Returns?

Traditional asset pricing theories assuming full information and frictionless and complete markets predict no relationship between idiosyncratic volatility and expected returns when agents are rational. In reality, investors may not hold perfectly diversified portfolios. Various theories assuming underdiversification predict that idiosyncratic risk is positively related to

expected stock returns, such as informational frictions (Merton 1987) and transaction costs (Hirshleifer 1988). However, frictions that prevent investors from adjusting portfolios to perfectly diversify risk are more significant over short horizons. Moreover, the difficulty of achieving perfect diversification is more evident over short horizons when shocks to idiosyncratic volatility have a relatively large and short-lived component. In the SL model, the median estimate of the volatility of shocks to the short-run component  $\theta_s$  is more than 50% larger than that of the long-run component  $\theta_l$ .

For returns measured over long horizons, frictions such as transaction costs and limited attention tend to play restricted roles, which is consistent with the reporting in Section 3.2. The return spread sorted by the conditional short-run idiosyncratic volatility is found not to hold for long holding periods of 12 and 24 months. Therefore, the positive relationship between conditional short-run idiosyncratic volatility and cross-sectional stock returns might arise because investors face frictions and hold underdiversified portfolios.

## 5.3. Why Is Long-Run Idiosyncratic Volatility Related to Stock Returns?

Ang et al. (2006) find that stocks with high realized idiosyncratic volatility in one month earn extremely low average returns in the next month. One reason for this novel finding is that earlier studies do not sort stocks or examine idiosyncratic volatility at the stock level. In Section 5.1, I present empirical evidence that the return spreads between the lowest and highest quintile portfolios sorted by the conditional long-run idiosyncratic volatility and lagged realized idiosyncratic volatility are strongly correlated with a coefficient of 0.95. Additionally, Section 3.2 shows that the magnitude of the return spreads is also quantitatively close, with  $-0.79\%$  for the realized volatility and  $-0.73\%$  for the conditional long-run idiosyncratic

**Table 10.** Regression Tests for the FF-5 Model

IVOL→	Low	2	3	4	High	Low	2	3	4	High
Panel A: Three-factor $R_{i,t} - R_{F,t} = a_i + b_i(R_{M,t} - R_{F,t}) + s_iSMB_t + h_iHML_i + \epsilon_{i,t}$										
	$a$					$t$				
Small	0.38	0.33	0.10	-0.19	-1.24	5.30	4.55	1.41	-2.19	-8.36
2	0.28	0.24	0.19	0.03	-0.73	4.25	3.46	2.61	0.38	-7.59
3	0.17	0.20	0.12	0.09	-0.47	2.56	2.86	1.72	1.10	-4.93
4	0.19	0.15	0.07	0.04	-0.33	2.44	1.96	0.96	0.56	-3.26
Big	0.09	0.10	0.02	-0.06	-0.09	1.57	1.88	0.35	-1.00	-1.00
Panel B: Five-factor $R_{i,t} - R_{F,t} = a_i + b_i(R_{M,t} - R_{F,t}) + s_iSMB_t + h_iHML_i + r_iRMW_i + c_iCMA_i\epsilon_{i,t}$										
	$a$					$t(a)$				
Small	0.27	0.19	0.05	-0.10	-0.87	3.78	2.56	0.53	-0.90	-5.56
2	0.14	0.06	0.02	-0.08	-0.47	2.32	0.98	0.36	-1.12	-5.47
3	0.03	0.04	-0.05	-0.05	-0.25	0.41	0.61	-0.74	-0.63	-2.84
4	0.04	-0.03	-0.09	-0.07	-0.10	0.47	-0.36	-1.29	-0.91	-1.06
Big	0.01	-0.04	-0.09	-0.05	0.12	0.14	-0.74	-1.75	-0.86	1.45
	$b$					$t(b)$				
Small	0.71	0.98	1.09	1.15	1.13	35.36	45.24	38.38	29.88	21.22
2	0.78	1.01	1.12	1.24	1.27	45.88	55.58	54.33	49.29	34.55
3	0.79	0.99	1.10	1.19	1.25	46.95	45.34	51.49	47.21	39.80
4	0.82	0.99	1.13	1.20	1.26	36.27	42.61	52.37	48.92	42.61
Big	0.83	0.97	1.05	1.11	1.18	56.75	66.03	75.18	69.87	46.26
	$s$					$t(s)$				
Small	0.67	0.93	1.04	1.19	1.35	25.22	26.10	22.92	18.90	16.48
2	0.56	0.75	0.83	0.94	1.12	23.03	27.37	24.24	22.13	24.05
3	0.31	0.47	0.57	0.69	0.82	12.59	13.91	16.42	16.61	19.64
4	0.10	0.18	0.23	0.32	0.51	3.16	4.98	6.15	8.29	13.93
Big	-0.28	-0.25	-0.17	-0.12	0.03	-13.11	-12.65	-7.28	-4.84	0.75
	$h$					$t(h)$				
Small	0.40	0.35	0.34	0.28	0.22	9.72	6.79	4.50	2.82	1.93
2	0.34	0.33	0.26	0.18	-0.07	10.55	7.18	4.93	2.84	-0.88
3	0.33	0.35	0.28	0.17	-0.16	8.78	6.65	5.24	2.72	-2.51
4	0.30	0.26	0.21	0.12	-0.18	5.63	4.57	3.92	2.28	-3.25
Big	0.12	-0.04	0.05	0.06	-0.19	3.91	-1.55	1.38	1.68	-3.28
	$r$					$t(r)$				
Small	0.28	0.35	0.17	-0.15	-0.83	4.94	5.22	1.97	-1.31	-6.32
2	0.32	0.42	0.41	0.32	-0.53	8.92	7.80	6.37	4.17	-7.79
3	0.31	0.41	0.43	0.35	-0.45	7.58	6.54	7.29	5.43	-7.99
4	0.31	0.40	0.37	0.27	-0.51	6.51	6.62	6.27	4.73	-8.81
Big	0.18	0.26	0.25	0.00	-0.42	4.59	7.23	5.55	0.11	-7.72
	$c$					$t(c)$				
Small	0.07	0.08	-0.02	-0.22	-0.42	1.24	1.30	-0.24	-1.71	-2.05
2	0.14	0.15	0.10	-0.03	-0.39	3.07	3.03	1.86	-0.49	-4.11
3	0.19	0.05	0.10	0.02	-0.32	3.64	0.95	1.93	0.32	-3.67
4	0.21	0.15	0.12	0.07	-0.25	2.96	2.51	1.95	0.99	-2.79
Big	0.08	0.22	0.12	-0.05	-0.34	1.54	4.11	2.47	-1.03	-4.12

Notes. The left-hand side variables in each set of 25 regressions are monthly excess returns on the 25 Size-IV portfolios. The right-hand side variables are excess market return  $R_M - R_F$ , the size factor SMB, the value factor HML, the profitability factor RMW, and the investment factor CMA. Panel A shows intercepts from the three-factor model, and Panel B shows intercepts and slopes from the five-factor model. The sample period is July 1963 to December 2017.

volatility. This finding suggests that long-run idiosyncratic volatility plays a crucial role in the negative relationship between realized idiosyncratic volatility and stock returns.

Furthermore, as shown in Sections 3.2 and 5.1, the cross-sectional relationship between long-run idiosyncratic volatility and stock returns persists over

multiperiod holding returns. And stocks with high long-run idiosyncratic volatility may be less exposed to systematic factors, especially the profitability factor RMW. All this empirical evidence lends support to risk-based explanations of the negative relationship between idiosyncratic volatility and cross-sectional stock returns. Moreover, risk-based mechanisms should

**Table 11.** Regression Tests for the FF-5-plus-IVFL Model

Five-factor plus IVFL: $R_{i,t} - R_{F,t} = a_i + b_i(R_{M,t} - R_{F,t}) + s_iSMB_t + h_iHML_t + r_iRMW_t + c_iCMA_t + v_iIVFL_t\epsilon_{i,t}$										
	$a$					$t(a)$				
Small	0.23	0.17	0.09	0.02	-0.61	3.25	2.33	1.00	0.15	-4.19
2	0.07	0.00	-0.01	-0.07	-0.33	1.22	0.07	-0.16	-0.94	-3.90
3	-0.05	-0.01	-0.07	-0.05	-0.12	-0.78	-0.14	-1.02	-0.71	-1.47
4	-0.04	-0.08	-0.11	-0.07	0.04	-0.56	-1.13	-1.65	-0.92	0.43
Big	-0.05	-0.07	-0.11	-0.04	0.26	-0.92	-1.48	-1.95	-0.64	3.40
	$b$					$t(b)$				
Small	0.74	0.99	1.06	1.07	0.94	36.29	48.77	41.31	32.23	19.59
2	0.83	1.05	1.14	1.23	1.16	53.42	64.33	62.59	53.95	47.78
3	0.84	1.02	1.11	1.20	1.16	53.67	55.37	52.28	47.62	46.81
4	0.88	1.03	1.15	1.20	1.16	39.94	50.03	56.69	48.60	45.35
Big	0.88	1.00	1.06	1.10	1.08	59.36	64.61	74.01	70.45	53.65
	$s$					$t(s)$				
Small	0.76	0.96	0.94	0.92	0.71	14.81	15.48	13.57	11.04	8.66
2	0.73	0.89	0.92	0.91	0.75	17.62	17.66	15.75	14.74	12.47
3	0.49	0.60	0.62	0.71	0.50	11.17	9.52	11.25	12.78	10.44
4	0.29	0.31	0.29	0.33	0.18	5.75	5.33	5.39	6.33	3.01
Big	-0.13	-0.15	-0.13	-0.15	-0.31	-4.69	-5.38	-3.62	-3.91	-4.93
	$h$					$t(h)$				
Small	0.38	0.35	0.36	0.33	0.35	8.33	6.14	4.76	3.59	3.70
2	0.30	0.30	0.25	0.19	0.00	8.52	5.90	4.18	2.86	0.04
3	0.29	0.32	0.27	0.17	-0.10	7.36	5.49	4.80	2.64	-1.96
4	0.27	0.23	0.20	0.12	-0.12	4.83	3.87	3.57	2.22	-2.18
Big	0.09	-0.06	0.04	0.07	-0.12	3.25	-2.29	1.15	1.85	-2.10
	$r$					$t(r)$				
Small	0.16	0.31	0.30	0.21	-0.02	1.81	3.16	2.76	1.73	-0.16
2	0.10	0.25	0.30	0.35	-0.06	1.44	2.71	2.97	3.55	-0.69
3	0.08	0.25	0.37	0.34	-0.05	1.07	2.43	4.45	4.31	-0.76
4	0.07	0.24	0.30	0.27	-0.09	0.93	2.57	3.77	3.96	-1.04
Big	-0.00	0.14	0.21	0.05	-0.00	-0.04	3.90	4.23	0.93	-0.01
	$c$					$t(c)$				
Small	0.00	0.06	0.05	-0.04	0.02	0.07	0.97	0.58	-0.34	0.12
2	0.02	0.05	0.04	-0.01	-0.14	0.37	1.17	0.84	-0.17	-2.02
3	0.06	-0.03	0.07	0.01	-0.10	1.44	-0.59	1.29	0.16	-1.43
4	0.08	0.07	0.08	0.07	-0.03	1.25	1.17	1.35	0.94	-0.33
Big	-0.02	0.15	0.10	-0.03	-0.12	-0.45	3.30	2.05	-0.57	-1.77
	$v$					$t(v)$				
Small	-0.07	-0.03	0.08	0.22	0.52	-2.80	-0.83	2.17	4.48	10.33
2	-0.14	-0.11	-0.07	0.02	0.29	-6.88	-4.52	-2.79	0.73	6.28
3	-0.15	-0.10	-0.04	-0.01	0.26	-7.08	-3.63	-1.64	-0.47	8.13
4	-0.15	-0.10	-0.05	-0.00	0.27	-6.52	-4.14	-2.16	-0.16	8.80
Big	-0.12	-0.08	-0.03	0.03	0.27	-7.86	-5.17	-1.52	1.45	8.96

Notes. The left-hand side variables in each set of 25 regressions are the monthly excess returns on the 25 Size-IV portfolios. The right-hand side variables are the excess market return  $R_M - R_F$ , the size factor SMB, the value factor HML, the profitability factor RMW, the investment factor CMA and IVFL, the return spread in univariate sort on conditional long-run idiosyncratic volatility. The sample period is July 1963 to December 2017.

explain why this relationship is limited to the long-run component.

There are several risk-based explanations for the negative relationship between idiosyncratic volatility and stock returns in the literature. For this type of explanation, idiosyncratic volatility can serve as a proxy for either exposure to systematic risk factors or sensitivity to fluctuations in changing investment opportunities as in Merton (1973).

Babenko et al. (2016) view firms as portfolios of separate systematic and idiosyncratic divisions and rely on the additivity of systematic and idiosyncratic

cash flow shocks in the valuation of firms. Hence, favorable idiosyncratic shocks decrease the importance of systematic cash flows, leading to lower risk premia and higher idiosyncratic stock return volatility. Similarly, Chen et al. (2020) study a risk-shifting problem of equity householders who take on more investments with high idiosyncratic risk when firms are in distress and when the aggregate economy is in a bad state. Thus, the negative covariance between the equity beta and market risk premium in the conditional CAPM may explain the negative excess returns and negative CAPM alphas in the high-idiosyncratic-volatility firms.

**Table 12.** Summary Statistics for Tests of the FF-3, FF-5, and FF-5-plus-IVFL Models

Model factors	GRS	$p(\text{GRS})$	$A a_i $	$\frac{A a_i }{A \bar{r}_i }$	$\frac{Aa_i^2}{A\bar{r}_i^2}$	$\frac{As^2(a_i)}{A \bar{r}_i }$	$A(R^2)$
MKT SMB HML	6.76	0.0	0.24	0.77	0.91	0.05	0.88
MKT SMB HML RMW CMA	5.55	0.0	0.13	0.43	0.37	0.12	0.9
MKT SMB HML RMW CMA IVFL	5.15	0.0	0.11	0.36	0.21	0.2	0.91

*Notes.* This table reports statistics summarizing how well the FF-3, FF-5, and FF-5-plus-IVFL models explain monthly excess returns on the 25 Size-IV portfolios. The table shows (1) the GRS statistics testing whether the expected values of all 25 intercept estimates are zero; (2)  $p(\text{GRS})$ , the  $p$ -value for the GRS statistic; (3) the average absolute value of the intercepts,  $A|a_i|$ ; (4) the average absolute value of the intercepts over the average absolute value of  $\bar{r}_i$ , which is the average excess returns on portfolio  $i$  minus the average market portfolio excess returns; (5)  $Aa_i^2/A\bar{r}_i^2$ , the average squared intercept over the average squared value of  $\bar{r}_i$ ; (6)  $As^2(a_i)/A|\bar{r}_i|$ , the average of the estimates of the variances of the sampling errors of the estimated intercepts over  $A\bar{r}_i^2$ ; and (7)  $A(R^2)$ , the average value of the regression  $R^2$  corrected for degrees of freedom. The sample period is July 1963 to December 2017.

Recent studies such as Cao et al. (2008) and Grullon et al. (2012) find that firms with high idiosyncratic volatility usually possess abundant growth options. Real options models, following Berk et al. (1999) and Carlson et al. (2004), establish links between expected returns and the riskiness of assets in place and growth options. The firm's systematic risk could crucially depend upon the risk exposure of its growth options, when such options' value consists of a large proportion of the firm's value. Bhamra and Shim (2017) introduce stochastic cash flow risks into an equity evaluation model with growth options to explain the negative relationship between idiosyncratic volatility and expected stock returns. This real-option-based mechanism highlights the importance of long-run idiosyncratic volatility in explaining the negative relationship between idiosyncratic volatility and stock returns. When idiosyncratic volatility increases, the value of growth options could rise because of convexity. Moreover, such a rise in the value of growth options could be significant if the increase in idiosyncratic volatility occurs over long horizons and there is a possibility of delaying investment. Short-run variations in idiosyncratic volatility that level off quickly over time may have a very limited impact on option values.

In the meantime, growth options' sensitivity to systematic risk factors could decrease because the relative magnitude of such options' value that is related to systematic risk falls. This channel drives down the expected return when idiosyncratic volatility is higher. Therefore, long-run idiosyncratic volatility serves as a proxy for exposure to systematic risk factors. A simple model similar to that of Bhamra and Shim (2017) is also provided in the online appendix to shed light on the real-option-based channel to explain the negative relationship between idiosyncratic volatility and stock returns.

Guo and Savickas (2008, 2010), motivated by the reasoning that idiosyncratic volatility could be related to growth options and investment opportunities,

show that CAPM, FF-3 model, and other asset pricing models may suffer from omitted variable bias because they do not include a measure of the set of investment opportunities proposed in Merton's (1973) Intertemporal Capital Asset Pricing Model (ICAPM). As a result, their pricing relationships assign too high a price of risk to the changes in aggregate investment opportunities, which imparts a negative expected return on idiosyncratic volatility. Along with this argument, if long-run idiosyncratic volatility is a good proxy for changing investment opportunities, this mechanism may also explain the negative relationship between long-run idiosyncratic volatility and cross-sectional stock returns.

As for the non-risk-based explanations, the list of them could include lottery preferences (Bali et al. 2011), limits to arbitrage (Stambaugh et al. 2015), and so forth. In a recent paper, Stambaugh et al. (2015) argue that costly arbitrage leads to the pricing of idiosyncratic risk, but the cost is higher for overpriced stocks than for underpriced ones. Because the negative relation among overpriced stocks is stronger, especially for stocks less easily shorted, the overall relation between idiosyncratic volatility and stock returns is negative. Because mispricing tends to be corrected over the long run, it is unclear whether this explanation could generate a persistent negative relation between idiosyncratic volatility and stock returns. It is thus worth investigating whether their findings hold over longer return horizons. Furthermore, non-risk-based explanations may be challenged to reconcile the finding in this paper that the relationship between idiosyncratic volatility and cross-sectional stock return is limited to the long-run component.

Therefore, there are two real-option-related mechanisms that may explain the negative relation between long-run idiosyncratic volatility and stock returns. One possible avenue for future research is to rigorously test these real-option-based and other mechanisms in explaining the negative relationship between



long-run idiosyncratic volatility and cross-sectional stock returns.

## 6. Conclusion

The paper develops and estimates a model that better captures the dynamics of idiosyncratic volatility. I decompose the volatility of idiosyncratic stock returns into short-run and long-run components and find that there is a significant negative (positive) relationship between conditional long-run (short-run) idiosyncratic volatility and expected stock returns. And the negative relationship between lagged realized volatility and expected returns is captured by the long-run component. These results highlight that idiosyncratic volatility variations over short and long horizons have important implications for cross-sectional stock returns.

Further empirical tests suggest the positive relationship between short-run idiosyncratic volatility and stock returns is not risk-driven, while the negative relationship between long-run idiosyncratic volatility and stock returns may be driven by risk. Moreover, the finding that the negative relationship between realized idiosyncratic volatility and stock returns is limited to the long-term component suggests two types of real-option-based mechanisms to explain the negative relationship between long-run idiosyncratic volatility and stock returns.

One explanation is that stocks with high long-run idiosyncratic volatility are less exposed to systematic risk factors. The systematic risk of a firm is determined by the risk of its assets in place and growth options. When idiosyncratic volatility increases, growth options rise in value because of convexity. And the exposure of growth options to systematic risk factors could fall because of the decrease in the relative magnitude of option values related to systematic risk factors. The other explanation is related to Merton's (1973) ICAPM. Long-run idiosyncratic volatility might be proxying for sensitivity to fluctuations in changing investment opportunities.

## Acknowledgments

The author thanks the associate editor and two anonymous referees for insightful and constructive comments, which greatly improved the exposition of the paper. The author also thanks comments from Federico Bandi, Gregory Duffee, Jon Faust, and seminar participants at the CCEER Summer Institute. Yixuan Di provided excellent research assistance.

## Endnotes

<sup>1</sup> I also consider defining the idiosyncratic volatility relative to the Carhart (1997) four-factor model and Fama and French (2015) five-factor model. The negative relationship between lagged realized volatility and average stock returns also holds. These results are available upon request.

<sup>2</sup> One basis point equals one hundredth of one percentage point.

<sup>3</sup> The constant term should be excluded from the short-run component mainly for two reasons. First, a constant term is capturing a very "persistent" part of idiosyncratic volatility. If a firm has a high constant  $\phi_i$ , it tends to have high idiosyncratic volatility for long periods of time. This implication also plays an important role in interpreting the negative relationship between long-run idiosyncratic volatility and stock returns through real-option-based channels in Section 5.3. Second, the constant term in the long-run component makes the SL model to some extent comparable to the limiting case when the long-run component contains a unit root and does not have a mean.

<sup>4</sup> Filtered estimates may still use future information if parameters are estimated based on whole sample information.

<sup>5</sup> All results with smoothed estimates are reported in the online appendix.

<sup>6</sup> The convexity-based real-option explanation in Section 5.3 may be useful to explain the positive sign on unexpected idiosyncratic volatility. The average of correlations between the conditional long-run volatility at  $t + 1$ ,  $\hat{v}_{t+1}$ , and unexpected idiosyncratic volatility  $\mu_t$  is about 0.4. This suggests that a positive unexpected change in  $\mu_t$  is associated with an upward revision in the conditional long-run volatility  $\hat{v}_{t+1}$ . When the long-run idiosyncratic volatility  $\hat{v}_{t+1}$  is expected to increase, the stock price at  $t$  may rise as growth options become more valuable. The expected return at  $t + 1$  falls as the exposure of growth options to systematic risk factors decreases, though.

<sup>7</sup> The question investigated here is not related to momentum. Including the momentum factor of Carhart (1997) does not impact the main results of this paper, and the results are available upon request.

<sup>8</sup> According to information on Kenneth French's website, the portfolios, which are constructed monthly, are the intersections of five portfolios formed on size (market equity, ME) and five portfolios formed on the variance of the residuals from the FF-3 model.

## References

- Adrian T, Rosenberg J (2008) Stock returns and volatility: Pricing the short-run and long-run components of market risk. *J. Finance* 63(6):2997–3030.
- Ang A, Hodrick RJ, Xing Y, Zhang X (2006) The cross-section of volatility and expected returns. *J. Finance* 61(1):259–299.
- Ang A, Hodrick RJ, Xing Y, Zhang X (2009) High idiosyncratic volatility and low returns: International and further us evidence. *J. Financial Econom.* 91(1):1–23.
- Babenko I, Boguth O, Tserlukevich Y (2016) Idiosyncratic cash flows and systematic risk. *J. Finance* 71(1):425–456.
- Bali TG, Cakici N (2008) Idiosyncratic volatility and the cross section of expected returns. *J. Financial Quant. Anal.* 43(01):29–58.
- Bali TG, Cakici N, Whitelaw RF (2011) Maxing out: Stocks as lotteries and the cross-section of expected returns. *J. Financial Econom.* 99(2):427–446.
- Barndorff-Nielsen OE, Shephard N (2002) Econometric analysis of realized volatility and its use in estimating stochastic volatility models. *J. Roy. Statist. Soc. Ser. B. Statist. Methodol.* 64(2):253–280.
- Berk JB, Green RC, Naik V (1999) Optimal investment, growth options, and security returns. *J. Finance* 54(5):1553–1607.
- Bhamra HS, Shim KH (2017) Stochastic idiosyncratic cash flow risk and real options: Implications for stock returns. *J. Econom. Theory* 168:400–431.
- Bollerslev T, Zhou H (2002) Estimating stochastic volatility diffusion using conditional moments of integrated volatility. *J. Econometrics* 109(1):33–65.
- Cao C, Simin T, Jing Z (2008) Can growth options explain the trend in idiosyncratic risk? *Rev. Financial Stud.* 21(6):2599–2633.

- Carhart MM (1997) On persistence in mutual fund performance. *J. Finance* 52(1):57–82.
- Carlson M, Fisher A, Giammarino R (2004) Corporate investment and asset price dynamics: Implications for the cross-section of returns. *J. Finance* 59(6):2577–2603.
- Chen Z, Strebulaev IA, Xing Y, Zhang X (2020) Strategic risk shifting and the idiosyncratic volatility puzzle: An empirical investigation. *Management Sci.*, ePub ahead of print July 17, <https://doi.org/10.1287/mnsc.2020.3593>
- Christoffersen P, Jacobs K, Ornathanalai C, Wang Y (2008) Option valuation with long-run and short-run volatility components. *J. Financial Econom.* 90(3):272–297.
- Chua CT, Goh J, Zhang Z (2010) Expected volatility, unexpected volatility, and the cross-section of stock returns. *J. Financial Res.* 33(2):103–123.
- Cochrane JH (1999) Portfolio advice for a multifactor world. *Econom. Perspect.* 23(3):59–78.
- Corsi F (2009) A simple approximate long-memory model of realized volatility. *J. Financial Econom.* 7(2):174–196.
- Duffee GR (1995) Stock returns and volatility a firm-level analysis. *J. Financial Econom.* 37(3):399–420.
- Engle RF, Lee GG (1999) A permanent and transitory component model of stock return volatility. Engle RF, White H, eds. *Cointegration, Causality, and Forecasting: A Festschrift in Honour of Clive W.J. Granger* (Oxford University Press, New York), 475–497.
- Fama EF, French KR (1992) The cross-section of expected stock returns. *J. Finance* 47(2):427–465.
- Fama EF, French KR (1993) Common risk factors in the returns on stocks and bonds. *J. Financial Econom.* 33(1):3–56.
- Fama EF, French KR (2015) A five-factor asset pricing model. *J. Financial Econom.* 116(1):1–22.
- Fama EF, French KR (2016) Dissecting anomalies with a five-factor model. *Rev. Financial Stud.* 29(1):69–103.
- Fama EF, MacBeth JD (1973) Risk, return, and equilibrium: Empirical tests. *J. Political Econom.* 81(3):607–636.
- Fink JD, Fink KE, He H (2012) Expected idiosyncratic volatility measures and expected returns. *Financial Management* 41(3):519–553.
- French KR, Schwert GW, Stambaugh RF (1987) Expected stock returns and volatility. *J. Financial Econom.* 19(1):3–29.
- Fu F (2009) Idiosyncratic risk and the cross-section of expected stock returns. *J. Financial Econom.* 91(1):24–37.
- Gibbons RM, Ross AS, Shanken J (1989) A test of the efficiency of a given portfolio. *Econometrica* 57(5):1121–1152.
- Grullon G, Lyandres E, Zhdanov A (2012) Real options, volatility, and stock returns. *J. Finance* 67(4):1499–1537.
- Guo H, Kassa H, Ferguson MF (2014) On the relation between EGARCH idiosyncratic volatility and expected stock returns. *J. Financial Quant. Anal.* 49(1):271–296.
- Guo H, Savickas R (2008) Average idiosyncratic volatility in G7 countries. *Rev. Financial Stud.* 21(3):1259–1296.
- Guo H, Savickas R (2010) Relation between time-series and cross-sectional effects of idiosyncratic variance on stock returns. *J. Banking Finance* 34(7):1637–1649.
- Hirshleifer D (1988) Residual risk, trading costs, and commodity futures risk premia. *Rev. Financial Stud.* 1(2):173–193.
- Huang W, Liu Q, Rhee SG, Zhang L (2010) Return reversals, idiosyncratic risk, and expected returns. *Rev. Financial Stud.* 23(1):147–168.
- Jegadeesh N (1990) Evidence of predictable behavior of security returns. *J. Finance* 45(3):881–898.
- Jegadeesh N, Titman S (1993) Returns to buying winners and selling losers: Implications for stock market efficiency. *J. Finance* 48(1):65–91.
- Lehmann BN (1990) Fads, martingales, and market efficiency. *Quart. J. Econom.* 105(1):1–28.
- Merton RC (1973) An intertemporal capital asset pricing model. *Econometrica* 41(5):867–887.
- Merton RC (1987) A simple model of capital market equilibrium with incomplete information. *J. Finance* 42(3):483–510.
- Newey WK, West KD (1987) A simple, positive semi-definite, heteroskedasticity and autocorrelation consistent covariance matrix. *Econometrica* 55(3):703–708.
- Novy-Marx R (2013) The other side of value: The gross profitability premium. *J. Financial Econom.* 108(1):1–28.
- Stambaugh RF, Yu J, Yuan Y (2015) Arbitrage asymmetry and the idiosyncratic volatility puzzle. *J. Finance* 70(5):1903–1948.
- Titman S, Wei KJ, Xie F (2004) Capital investments and stock returns. *J. Financial Quant. Anal.* 39(4):677–700.