Initialization

Welcome to the first assignment of "Improving Deep Neural Networks".

Training your neural network requires specifying an initial value of the weights. A well chosen initialization method will help learning.

If you completed the previous course of this specialization, you probably followed our instructions for weight initialization, and it has worked out so far. But how do you choose the initialization for a new neural network? In this notebook, you will see how different initializations lead to different results.

A well chosen initialization can:

- · Speed up the convergence of gradient descent
- Increase the odds of gradient descent converging to a lower training (and generalization) error

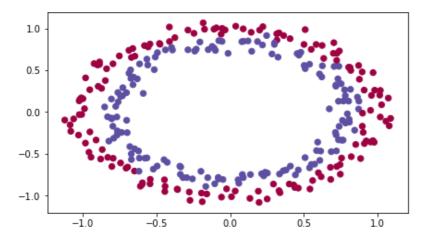
To get started, run the following cell to load the packages and the planar dataset you will try to classify.

In [18]:

```
import numpy as np
import matplotlib.pyplot as plt
import sklearn
import sklearn.datasets
from init_utils import sigmoid, relu, compute_loss, forward_propagation, backward_propag
ation
from init_utils import update_parameters, predict, load_dataset, plot_decision_boundary,
predict_dec

%matplotlib inline
plt.rcParams['figure.figsize'] = (7.0, 4.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# load image dataset: blue/red dots in circles
train_X, train_Y, test_X, test_Y = load_dataset()
```



You would like a classifier to separate the blue dots from the red dots.

1 - Neural Network model

You will use a 3-layer neural network (already implemented for you). Here are the initialization methods you will experiment with:

- Zeros initialization -- setting initialization = "zeros" in the input argument.
- Random initialization -- setting initialization = "random" in the input argument. This initializes the weights to large random values.

• *He initialization* -- setting initialization = "he" in the input argument. This initializes the weights to random values scaled according to a paper by He et al., 2015.

Instructions: Please quickly read over the code below, and run it. In the next part you will implement the three initialization methods that this <code>model()</code> calls.

```
In [19]:
```

```
def model(X, Y, learning rate = 0.01, num iterations = 15000, print cost = True, initial
    11 11 11
   Implements a three-layer neural network: LINEAR->RELU->LINEAR->RELU->LINEAR->SIGMOID.
   X -- input data, of shape (2, number of examples)
   Y -- true "label" vector (containing 0 for red dots; 1 for blue dots), of shape (1,
number of examples)
   learning rate -- learning rate for gradient descent
   num iterations -- number of iterations to run gradient descent
   print cost -- if True, print the cost every 1000 iterations
   initialization -- flag to choose which initialization to use ("zeros", "random" or "he
")
   Returns:
   parameters -- parameters learnt by the model
   qrads = \{\}
   costs = [] # to keep track of the loss
   m = X.shape[1] # number of examples
   layers dims = [X.shape[0], 10, 5, 1]
    # Initialize parameters dictionary.
   if initialization == "zeros":
       parameters = initialize parameters zeros(layers dims)
   elif initialization == "random":
       parameters = initialize parameters random(layers dims)
   elif initialization == "he":
       parameters = initialize parameters he(layers dims)
   # Loop (gradient descent)
   for i in range(0, num iterations):
        # Forward propagation: LINEAR -> RELU -> LINEAR -> RELU -> LINEAR -> SIGMOID.
       a3, cache = forward propagation(X, parameters)
        # Loss
       cost = compute loss(a3, Y)
        # Backward propagation.
       grads = backward_propagation(X, Y, cache)
        # Update parameters.
       parameters = update parameters (parameters, grads, learning rate)
        # Print the loss every 1000 iterations
       if print cost and i % 1000 == 0:
            print("Cost after iteration {}: {}".format(i, cost))
            costs.append(cost)
   # plot the loss
   plt.plot(costs)
   plt.ylabel('cost')
   plt.xlabel('iterations (per hundreds)')
   plt.title("Learning rate =" + str(learning_rate))
   plt.show()
   return parameters
```

2 - Zero initialization

There are two types of parameters to initialize in a neural network:

```
 \begin{array}{c} \bullet \ \ \text{the weight matrices} \ (W^{[1]},W^{[2]},W^{[3]},\dots\\ & \cdot,W^{[L-1]},W^{[L]}) \\ \bullet \ \ \text{the bias vectors} \ (b^{[1]},b^{[2]},b^{[3]},\dots,\\ & b^{[L-1]},b^{[L]}) \end{array}
```

Exercise: Implement the following function to initialize all parameters to zeros. You'll see later that this does not work well since it fails to "break symmetry", but lets try it anyway and see what happens. Use np.zeros((..,..)) with the correct shapes.

```
In [20]:
```

```
# GRADED FUNCTION: initialize parameters zeros
def initialize parameters zeros(layers dims):
    11 11 11
   Arguments:
   layer dims -- python array (list) containing the size of each layer.
   Returns:
    parameters -- python dictionary containing your parameters "W1", "b1", ..., "WL", "b
L''' .
                    W1 -- weight matrix of shape (layers dims[1], layers dims[0])
                    b1 -- bias vector of shape (layers dims[1], 1)
                    WL -- weight matrix of shape (layers dims[L], layers dims[L-1])
                    bL -- bias vector of shape (layers dims[L], 1)
    11 11 11
   parameters = {}
   L = len(layers dims)
                                   # number of layers in the network
    for l in range(1, L):
        ### START CODE HERE ### (≈ 2 lines of code)
       parameters['W' + str(l)] = np.zeros((layers_dims[l], layers_dims[l-1]))
       parameters['b' + str(l)] = np.zeros((layers_dims[l], 1))
        ### END CODE HERE ###
    return parameters
```

In [21]:

Expected Output:

```
**W1** [[ 0. 0. 0.] [ 0. 0. 0.]]

**b1** [[ 0.] [ 0.]]

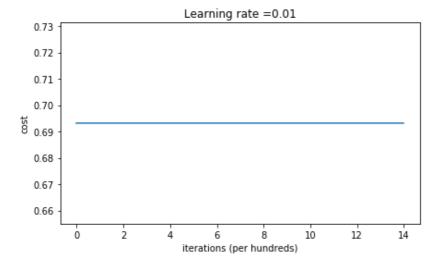
**W2** [[ 0. 0.]]

**b2** [[ 0.]]
```

```
In [22]:
```

```
parameters = model(train_X, train_Y, initialization = "zeros")
print ("On the train set:")
predictions_train = predict(train_X, train_Y, parameters)
print ("On the test set:")
predictions_test = predict(test_X, test_Y, parameters)
```

```
Cost after iteration 0: 0.6931471805599453
Cost after iteration 2000: 0.6931471805599453
Cost after iteration 2000: 0.6931471805599453
Cost after iteration 3000: 0.6931471805599453
Cost after iteration 4000: 0.6931471805599453
Cost after iteration 5000: 0.6931471805599453
Cost after iteration 6000: 0.6931471805599453
Cost after iteration 7000: 0.6931471805599453
Cost after iteration 8000: 0.6931471805599453
Cost after iteration 9000: 0.6931471805599453
Cost after iteration 10000: 0.6931471805599453
Cost after iteration 10000: 0.6931471805599453
Cost after iteration 12000: 0.6931471805599453
Cost after iteration 12000: 0.6931471805599453
Cost after iteration 12000: 0.6931471805599453
Cost after iteration 13000: 0.6931471805599453
Cost after iteration 13000: 0.6931471805599453
```



On the train set: Accuracy: 0.5 On the test set: Accuracy: 0.5

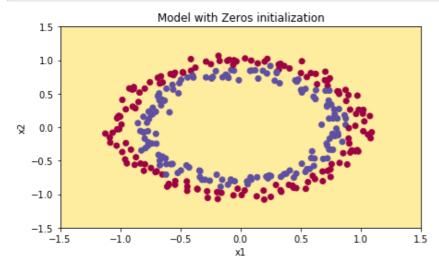
The performance is really bad, and the cost does not really decrease, and the algorithm performs no better than random guessing. Why? Lets look at the details of the predictions and the decision boundary:

```
In [23]:
```

In [24]:

```
print ("predictions train = " + str(predictions train))
print ("predictions test = " + str(predictions_test))
0 0 0 0
0 0 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
        0
        0 0 0
          0
0 0 0 011
0 0 0 0
```

```
plt.title("Model with Zeros initialization")
axes = plt.gca()
axes.set_xlim([-1.5,1.5])
axes.set_ylim([-1.5,1.5])
plot_decision_boundary(lambda x: predict_dec(parameters, x.T), train_X, train_Y)
```



The model is predicting 0 for every example.

In general, initializing all the weights to zero results in the network failing to break symmetry. This means that every neuron in each layer will learn the same thing, and you might as well be training a neural network with $n^{[l]}=1$ for every layer, and the network is no more powerful than a linear classifier such as logistic regression.

What you should remember:

- The weights $W^{[l]}$ should be initialized randomly to break symmetry.
- It is however okay to initialize the biases $b^{[l]}$ to zeros. Symmetry is still broken so long as $W^{[l]}$ is initialized randomly.

3 - Random initialization

To break symmetry, lets intialize the weights randomly. Following random initialization, each neuron can then proceed to learn a different function of its inputs. In this exercise, you will see what happens if the weights are intialized randomly, but to very large values.

Exercise: Implement the following function to initialize your weights to large random values (scaled by *10) and your biases to zeros. Use <code>np.random.randn(..,.) * 10</code> for weights and <code>np.zeros((.., ..))</code> for biases. We are using a fixed <code>np.random.seed(..)</code> to make sure your "random" weights match ours, so don't worry if running several times your code gives you always the same initial values for the parameters.

In [31]:

```
np.random.seed(3)  # This seed makes sure your "random" numbers will be
the as ours
parameters = {}
L = len(layers_dims)  # integer representing the number of layers

for 1 in range(1, L):
    ### START CODE HERE ### (* 2 lines of code)
    parameters['W' + str(1)] = np.random.randn(layers_dims[1], layers_dims[1-1]) * 1

0  parameters['b' + str(1)] = np.zeros((layers_dims[1], 1))
    ### END CODE HERE ###

return parameters
```

In [32]:

Expected Output:

```
**W1** [[ 17.88628473 4.36509851 0.96497468] [-18.63492703 -2.77388203 -3.54758979]]

**b1** [[ 0.] [ 0.]]

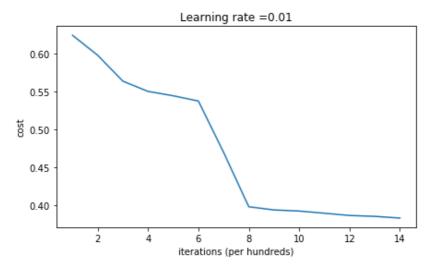
**W2** [[-0.82741481 -6.27000677]]

**b2**
```

Run the following code to train your model on 15,000 iterations using random initialization.

```
In [33]:
```

```
parameters = model(train X, train Y, initialization = "random")
print ("On the train set:")
predictions train = predict(train X, train Y, parameters)
print ("On the test set:")
predictions test = predict(test X, test Y, parameters)
/home/jovyan/work/week5/Initialization/init utils.py:145: RuntimeWarning: divide by zero
encountered in log
  logprobs = np.multiply(-np.log(a3), Y) + np.multiply(-np.log(1 - a3), 1 - Y)
/home/jovyan/work/week5/Initialization/init utils.py:145: RuntimeWarning: invalid value e
ncountered in multiply
  logprobs = np.multiply(-np.log(a3), Y) + np.multiply(-np.log(1 - a3), 1 - Y)
Cost after iteration 0: inf
Cost after iteration 1000: 0.6242434241539614
Cost after iteration 2000: 0.5978811277755388
Cost after iteration 3000: 0.5636242569764779
Cost after iteration 4000: 0.5500958254523324
Cost after iteration 5000: 0.544339206192789
Cost after iteration 6000: 0.5373584514307651
Cost after iteration 7000: 0.469574666760224
Cost after iteration 8000: 0.39766324943219844
Cost after iteration 9000: 0.3934423376823982
Cost after iteration 10000: 0.3920158992175907
Cost after iteration 11000: 0.38913979237487845
Cost after iteration 12000: 0.3861261344766218
Cost after iteration 13000: 0.3849694511273874
Cost after iteration 14000: 0.3827489017191917
```



On the train set: Accuracy: 0.83 On the test set: Accuracy: 0.86

If you see "inf" as the cost after the iteration 0, this is because of numerical roundoff; a more numerically sophisticated implementation would fix this. But this isn't worth worrying about for our purposes.

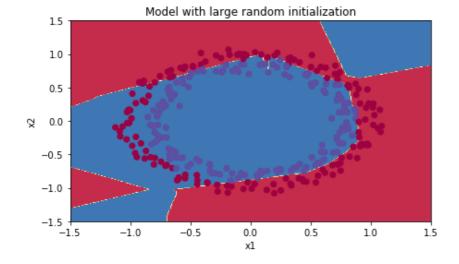
Anyway, it looks like you have broken symmetry, and this gives better results. than before. The model is no longer outputting all 0s.

In [34]:

```
print (predictions train)
print (predictions test)
0
                                  1
                                   1
                                    1
                                      1
  1 1
        1 0 1 1
             1
              1
                0 1
                   0 1
                     1
                       1
                        1
                         0
                           0
                            1
                              1
                               1
                                1
                                  0
                                   1
                                     1
                                      0
                                       1
                                         0
                                          1
                                           1
                                             1
                                              1
     0 1
        0
          1
             0 0
                     1
                        0
                             1
                               0
                                   0
                                          0
         1
            1
                1
                 1
                   1
                    1
                       1
                         0
                           1
                            1
                                1
                                  1
                                    1
                                      0
                                       1
                                         1
                                           1
  0 0
     1
      0
        0
         1
          1
            0
             1
               1
                1
                 0
                   1
                    0
                     0
                       1
                        0
                         1
                           1
                            1
                              1
                               1
                                1
                                  1
                                   0
                                     1
                                      1
                                       0
                                         0
                                          1
  0 1
     0
      1
        1
         1
          0 0
             1
               1
                1
                 1
                   0
                    1
                     1
                       0
                        1
                         0
                           1
                            1
                             0
                               1
                                0
                                  1
                                   1
                                     1
                                       0
  1
     1
      1
        0
         1
          1
            0
             1
              1 0 1
                   1
                    0
                     1
                       0
                        1
                         1
                           1
                            0
                             1
                               1
                                1
                                  0
                                    0
                                       0
       1 1 0 1 1 1 1 0 1 0 0 1 1
                         0 1 1 1 0 0 0 1 1 0 1 1 1 1 0
   1
     0
      1
 1 1 1 011
1 1 1 0 1 0 0 1 0 0 0 1 1 0 1 1 0 0 0 1 1 0 1 1 0 0]
```

In [35]:

```
plt.title("Model with large random initialization")
axes = plt.gca()
axes.set_xlim([-1.5,1.5])
axes.set_ylim([-1.5,1.5])
plot_decision_boundary(lambda x: predict_dec(parameters, x.T), train_X, train_Y)
```



Observations:

- The cost starts very high. This is because with large random-valued weights, the last activation (sigmoid) outputs results that are very close to 0 or 1 for some examples, and when it gets that example wrong it incurs a very high loss for that example. Indeed, when $\log(a^{[3]}) = \log(0)$, the loss goes to infinity.
- Poor initialization can lead to vanishing/exploding gradients, which also slows down the optimization algorithm.
- If you train this network longer you will see better results, but initializing with overly large random numbers slows down the optimization.

In summary:

- Initializing weights to very large random values does not work well.
- Hopefully intializing with small random values does better. The important question is: how small should be these random values be? Lets find out in the next part!

4 - He initialization

Finally, try "He Initialization"; this is named for the first author of He et al., 2015. (If you have heard of "Xavier initialization", this is similar except Xavier initialization uses a scaling factor for the weights $W^{[l]}$ of sqrt(1./layers dims[l-1]) where He initialization would use sqrt(2./layers dims[l-1]).)

Exercise: Implement the following function to initialize your parameters with He initialization.

Hint: This function is similar to the previous <code>initialize_parameters_random(...)</code> . The only difference is that instead of multiplying <code>np.random.randn(...,..)</code> by 10, you will multiply it by $\sqrt{\frac{2}{\text{dimension of the previous layer}}}$, which is what He initialization recommends for layers with a ReLU activation.

In [38]:

```
# GRADED FUNCTION: initialize parameters he
def initialize parameters he(layers dims):
    11 11 11
   Arguments:
    layer dims -- python array (list) containing the size of each layer.
    Returns:
   parameters -- python dictionary containing your parameters "W1", "b1", ..., "WL", "b
L":
                    W1 -- weight matrix of shape (layers dims[1], layers dims[0])
                    b1 -- bias vector of shape (layers dims[1], 1)
                    WL -- weight matrix of shape (layers dims[L], layers dims[L-1])
                    bL -- bias vector of shape (layers dims[L], 1)
    11 11 11
    np.random.seed(3)
    parameters = {}
    L = len(layers dims) - 1 # integer representing the number of layers
    for 1 in range (1, L + 1):
        ### START CODE HERE ### (≈ 2 lines of code)
        parameters['W' + str(l)] = np.random.randn(layers dims[l], layers dims[l-1]) * n
p.sqrt(2/layers dims[1-1])
       parameters['b' + str(l)] = np.zeros((layers dims[l], 1))
        ### END CODE HERE ###
    return parameters
```

In [39]:

```
parameters = initialize_parameters_he([2, 4, 1])
print("W1 = " + str(parameters["W1"]))
```

Expected Output:

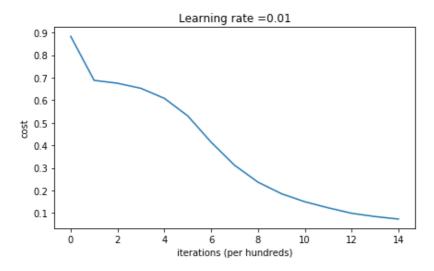
Run the following code to train your model on 15,000 iterations using He initialization.

```
In [40]:
```

```
parameters = model(train_X, train_Y, initialization = "he")
print ("On the train set:")
predictions_train = predict(train_X, train_Y, parameters)
print ("On the test set:")
predictions_test = predict(test_X, test_Y, parameters)
```

```
Cost after iteration 1000: 0.6879825919728063
Cost after iteration 2000: 0.6751286264523371
Cost after iteration 3000: 0.6526117768893807
Cost after iteration 4000: 0.6082958970572938
Cost after iteration 5000: 0.5304944491717495
Cost after iteration 6000: 0.4138645817071794
Cost after iteration 7000: 0.3117803464844441
Cost after iteration 8000: 0.23696215330322562
Cost after iteration 9000: 0.18597287209206834
Cost after iteration 10000: 0.15015556280371806
Cost after iteration 11000: 0.12325079292273546
Cost after iteration 12000: 0.09917746546525934
Cost after iteration 13000: 0.08457055954024278
Cost after iteration 14000: 0.07357895962677369
```

Cost after iteration 0: 0.8830537463419761

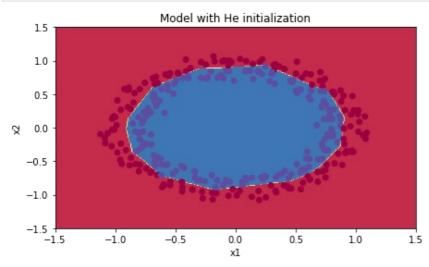


```
On the train set:
Accuracy: 0.993333333333
On the test set:
```

Accuracy: 0.96

```
In [41]:
```

```
plt.title("Model with He initialization")
axes = plt.gca()
axes.set_xlim([-1.5,1.5])
axes.set_ylim([-1.5,1.5])
plot_decision_boundary(lambda x: predict_dec(parameters, x.T), train_X, train_Y)
```



Observations:

• The model with He initialization separates the blue and the red dots very well in a small number of iterations.

5 - Conclusions

You have seen three different types of initializations. For the same number of iterations and same hyperparameters the comparison is:

Problem/Comment	**Train accuracy**	**Model**
fails to break symmetry	50%	3-layer NN with zeros initialization
too large weights	83%	3-layer NN with large random initialization
recommended method	99%	3-layer NN with He initialization

What you should remember from this notebook:

- Different initializations lead to different results
- Random initialization is used to break symmetry and make sure different hidden units can learn different things
- Don't intialize to values that are too large
- He initialization works well for networks with ReLU activations.