## **Contents**

```
      1 Misc
      1

      1.1 Makefile
      1

      2 Math
      1

      2.1 Number Theory
      1

      2.1.1 Modular
      1

      2.1.2 Extended GCD
      1

      2.1.3 Chinese Remainder
      1

      2.1.4 Tonelli-Shanks
      1

      3 Numeric
      1

      3.1 FFT
      1
```

## 1 Misc

### 1.1 Makefile

```
.PRECIOUS: ./p%
%: p%
   ulimit -s unlimited &6 ./$<
p%: p%.cpp
   g+ -std=gnu+17 -Wall -Wextra -Wshadow \
   -fsanitize=address -fsanitize=undefined \
   -o $0 $<
init:
   for i in a b c d e f g h; do \
        cp default.cpp "p$$i.cpp"; \
        done</pre>
```

# 2 Math

# 2.1 Number Theory

### 2.1.1 Modular

```
template<typename T> struct M {
  static T MOD;
  Τv;
  M() : v(0) \{ \}
  M(T x) {
   v = (-MOD \leqslant x \& x < MOD) ? x : x % MOD;
   if (v < \emptyset) v += MOD;
  }
  explicit operator T() const { return v; }
  bool operator=(const M\delta b) const { return v = b.v; }
  bool operator\neq(const M\delta b) const { return v \neq b.v; }
  M operator-() { return M(-v); }
  M operator+(M b) { return M(v + b.v); }
  M operator-(M b) { return M(v - b.v); }
  M operator*(M b) { return M((__int128)v * b.v % MOD); }
  M operator/(M b) { return *this * (b ^ (MOD - 2)); }
  friend M operator^(M a, ll b) {
    M ans(1);
    for(; b; b \gg 1, a *= a) if(b & 1) ans *= a;
   return ans:
  friend M& operator+=(M& a, M b) { return a = a + b; }
  friend Mô operator-=(Mô a, M b) { return a = a - b; }
  friend M& operator*=(M& a, M b) { return a = a * b; }
  friend M\delta operator\not= (M\delta a, M b) { return a = a / b; }
};
using Mod = M<ll>;
templatell Mod::MOD = 10000000007;
/* Safe primes
 * 21673, 26497, 22621, 21817, 28393, 26821, 30181, 22093
 * 977680993, 971939533, 970479637, 910870273, 1041012121
```

```
* 741266610070171837, 1110995545625882557
* NTT prime
                       p - 1
                                     primitive root
                       (2^16)
* 65537
                                     3
* 998244353
                       (2^23)*119
                                     3
* 2748779069441
                       (2^39)*5
                                     3
* 1945555039024054273
                       (2^56)*27
                                    5
```

#### 2.1.2 Extended GCD

```
tuple<ll, ll, ll> extgcd(ll a, ll b) {
  if (b = 0) return { 1, 0, a };
  else {
    auto [p, q, g] = extgcd(b, a % b);
    return { q, p - q * (a / b), g };
  }
}
```

### 2.1.3 Chinese Remainder

```
ll crt(ll a, ll m, ll b, ll n) {
  if (n > m) swap(a, b), swap(m, n);
  auto [x, y, g] = extgcd(m, n);
  assert((a - b) % g = 0); // no solution
  x = (x * (b - a) / g) % (n / g) * m + a;
  return x < 0 ? x + m * n / g : x;
}</pre>
```

### 2.1.4 Tonelli-Shanks

```
int legendre(Mod a) {
  if (a = 0) return 0;
  return (a ^ ((a.MOD - 1) / 2)) = 1 ? 1 : -1;
// O(\log^2(p)) worst, O(\log(p)) most of the time
Mod sqrt(Mod a) {
  assert(legendre(a) \neq -1); // no solution
  ll p = a.MOD, s = p - 1;
  if (a = 0) return 0;
  if (p = 2) return 1;
  if (p \% 4 = 3) return a ((p + 1) / 4);
  int r, m;
  for (r = 0; !(s & 1); r++) s >= 1;
  Mod n = 2;
  while (legendre(n) \neq -1) n += 1;
  Mod x = a ^ ((s + 1) / 2), b = a ^ s, g = n ^ s;
  while (b \neq 1) {
    Mod t = b;
    for (m = 0; t \neq 1; m++) t *= t;
    Mod gs = g^{(1)}(1LL \ll (r - m - 1));
    g = gs * gs, x *= gs, b *= g, r = m;
  }
  return x;
```

# 3 Numeric

### 3.1 FFT

```
#include <complex>
#include <vector>

template<typename T>
void work(int n, vector<T>& a, vector<T>& rt, bool inv) {
    for (int i = 1, r = 0; i < n; i++) {
        for (int bit = n; !(r & bit); bit >= 1, r ^= bit);
        if (r > i) swap(a[i], a[r]);
    }
    for (int len = 2; len & n; len <= 1) {
        for (int i = 0; i < n; i += len) {
            for (int j = 0; j < len / 2; j++) {
                int pos = n / len * (inv ? len - j : j);
            T u = a[i + j], v = a[i + j + len / 2] * rt[pos];
            a[i + j] = u + v, a[i + j + len / 2] = u - v;</pre>
```

```
}
}
if (inv) for (T minv = T(1) / T(n); T& x : a) x *= minv;
}

void FFT(vector<complex<double>>& a, bool inv) {
    int n = a.size();
    vector<complex<double>>> rt(n + 1);
    double arg = acos(-1) * 2 / n;
    for (int i = 0; i < n; i++)
        rt[i] = { cos(arg * i), sin(arg * i) };
    work(n, a, rt, inv);
}

void NTT(vector<Mod>& a, bool inv, Mod root) {
    int n = a.size();
    vector<Mod> rt(n + 1, 1);
    for (int i = 0; i < n; i++) rt[i + 1] = rt[i] * root;
    work(n, a, rt, inv);
}
</pre>
```