

Tutorial 8

- ① Construct a Moore machine that takes set of all strings over $\Sigma = \{a, b\}$ as input & prints 1 as a output for every occurrence of baa as substring.

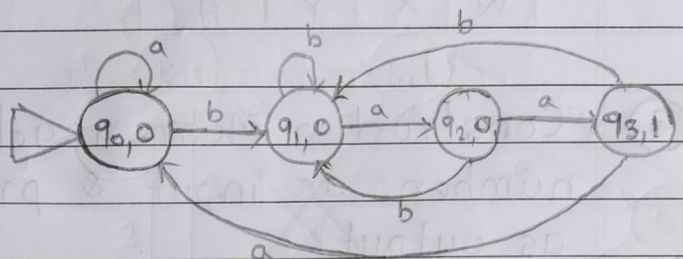
→ $M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$

$Q = \{q_0, q_1, q_2, q_3\}$

$\Sigma = \{a, b\}$

$q_0 - q_0$

$\Delta = \{0, 1\}$



transition table

	δ	a	b	o/p
→	q_0	q_0	q_1	0
	q_1	q_2	q_1	0
	q_2	q_3	q_1	0
	q_3	q_0	q_1	1

$q_0 \xrightarrow{a} q_0$	$q_0 \xrightarrow{b} q_1$	$q_1 \xrightarrow{a} q_2$	$q_2 \xrightarrow{a} q_3$
0	0	0	1

- ② Construct a Moore machine that takes set of strings over $\Sigma = \{0, 1\}$ & produce 'A' as output if input string end with 10 or produce 'B' as as output if input ends with 11 otherwise 'c'.

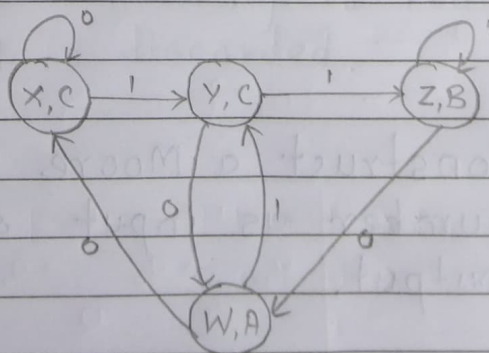
→ $M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$

$Q = \{w, x, y, z\}$

$\Sigma = \{0, 1\}$

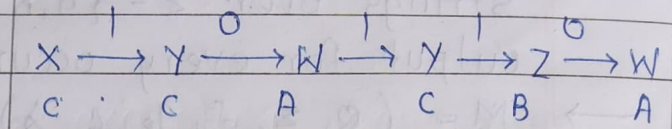
$q_0 - x$

$\Delta = \{A, B, c\}$



transition table

	δ	0	1	O/P
\rightarrow	X	X	Y	C
	Y	W	Z	C
	Z	W	Z	B
	W	X	Y	A



- ③ Construct a Moore machine that takes binary number as input & produces 'residue modulo 3' as output.

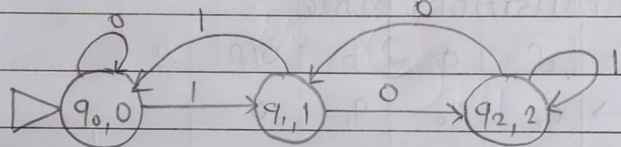
$$\rightarrow M = (Q, \Sigma, q_0, \delta, \Delta, \lambda)$$

$$Q = \{q_0, q_1, q_2\}$$

$$\Sigma = \{0, 1\}$$

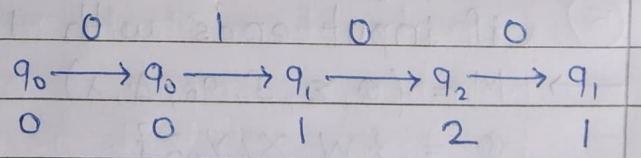
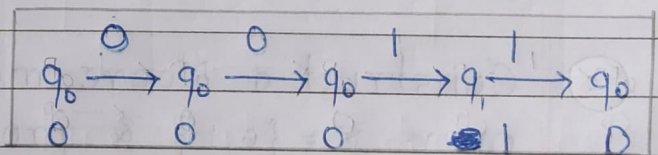
$$q_0 = q_0$$

$$\Delta = \{0, 1, 2\}$$



transition table

	δ	0	1	O/P
\rightarrow	q_0	q_0	q_1	0
	q_1	q_2	q_0	1
	q_2	q_1	q_2	2



- ④ Construct a Moore machine that takes base 4 number as input & produces modulo 5 as output.

$$\rightarrow M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$$

$$Q = \{q_0, q_1, q_2, q_3, q_4\}$$

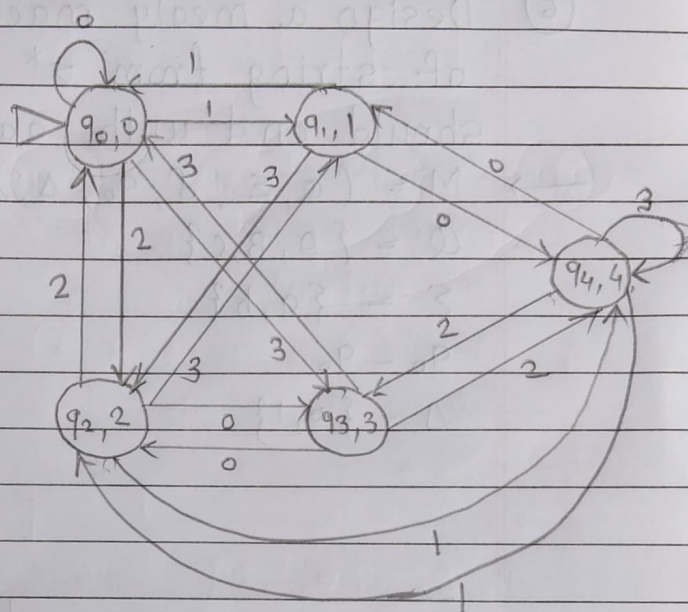
$$\Sigma = \{0, 1, 2, 3\}$$

$$q_0 - q_0$$

$$\Delta = \{0, 1, 2, 3, 4\}$$

transition table

δ	0	1	2	3	o/p
q_0	q_0	q_1	q_2	q_3	0
q_1	q_4	q_0	q_1	q_2	1
q_2	q_3	q_4	q_0	q_1	2
q_3	q_2	q_3	q_4	q_0	3
q_4	q_1	q_2	q_3	q_4	4



1	1	0	
$q_0 \rightarrow q_1 \rightarrow q_0 \rightarrow q_0$			
0	1	0	0

	1	1	1			
q_0	\rightarrow	q_1	\rightarrow	q_0	\rightarrow	q_1
0		1		0		0

- ⑤ Construct a Mealy machine that takes binary number as input & produces 2's complement of that number as output assume the string is read from LSB to MSB & end carry is discarded.

$$\rightarrow M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$$

$$Q = \{q_0, q_1\}$$

$$\Sigma = \{0, 1\}$$

$$q_0 - q_0$$

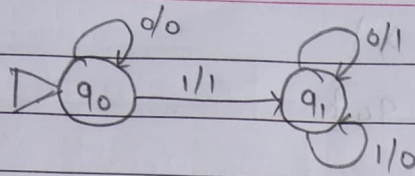
$$\Delta = \{0, 1\}$$

Ex. - 1101 \rightarrow binary no.

0010 \rightarrow 1's complement

+ 0001

0011 \rightarrow 2's complement



- ⑥ Design a mealy machine accepting language consisting of string from Σ^* where $\Sigma = \{a, b\}$ & string should end with aa or bb.

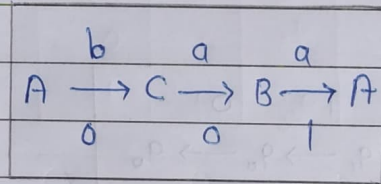
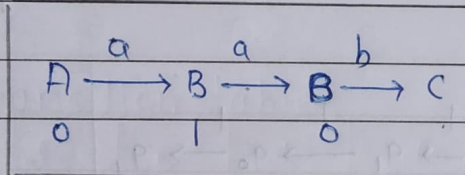
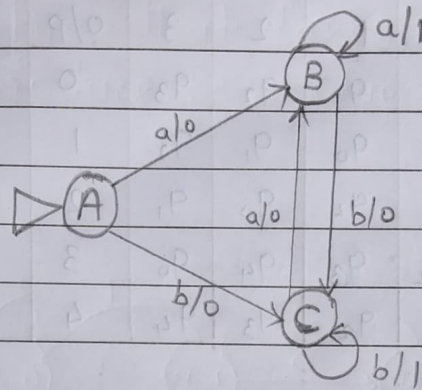
→ $M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$

$Q = \{A, B, C\}$

$\Sigma = \{a, b\}$

$q_0 = A$

$\Delta = \{0, 1\}$



- ⑦ Construct a mealy machine that produces the 1's complement of any binary input number.

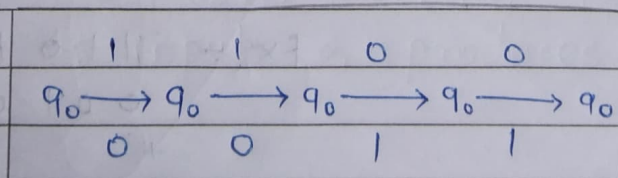
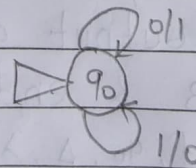
→ $M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$

$Q = \{q_0\}$

$\Sigma = \{0, 1\}$

$q_0 = q_0$

$\Delta = \{0, 1\}$



⑧ Construct a mealy machine that prints 'a' whenever the sequence '01' is encountered in any binary input string.

→ $M = (Q, \Sigma, \delta, q_0, \Delta, \lambda)$

$\Sigma = \{q_0, q_1, q_2\}$

$\Sigma = \{0, 1\}$

$q_0 - q_0$

$\Delta = \{a\}$

