## MAXIMIZE THE SCORE

## Editorial

May 2025

## 1 Key Observations

Since each operation is either multiplication or addition, the more nodes we traverse in a path, the more our score can increase.

If we choose a node x with an incoming edge from y, we can potentially obtain a higher score by choosing node y first. Therefore, we should start from nodes with no incoming edges. Let us call these nodes **Good** nodes.

We can use topological sorting to sort all the nodes and then traverse them in that order. There may be more than one **Good** node.

Let dp[i] represent the maximum score that can be achieved by traveling from any Good node to the *i*-th node.

Then, for each node x in topological order, we examine all the nodes j that have edges leading to x (using the reve rse adjacency list).

The state dp[i] can then be defined as the maximum of all dp[j] values, followed by the maximum score from applying either of the two operations at node i.

## 2 Complexity Analysis

- Topological Sort: O(n+m)
- **DP Computation:** For each node, we iterate over its predecessors also O(n+m)

Hence, the overall time complexity is efficient for the given constraints:  $n \le 30, \, m \le \frac{n(n-1)}{2}.$