

Spring 2025  
Stanford CS231n 10th Anniversary

# Lecture 15: 3D Vision

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May 22, 2025









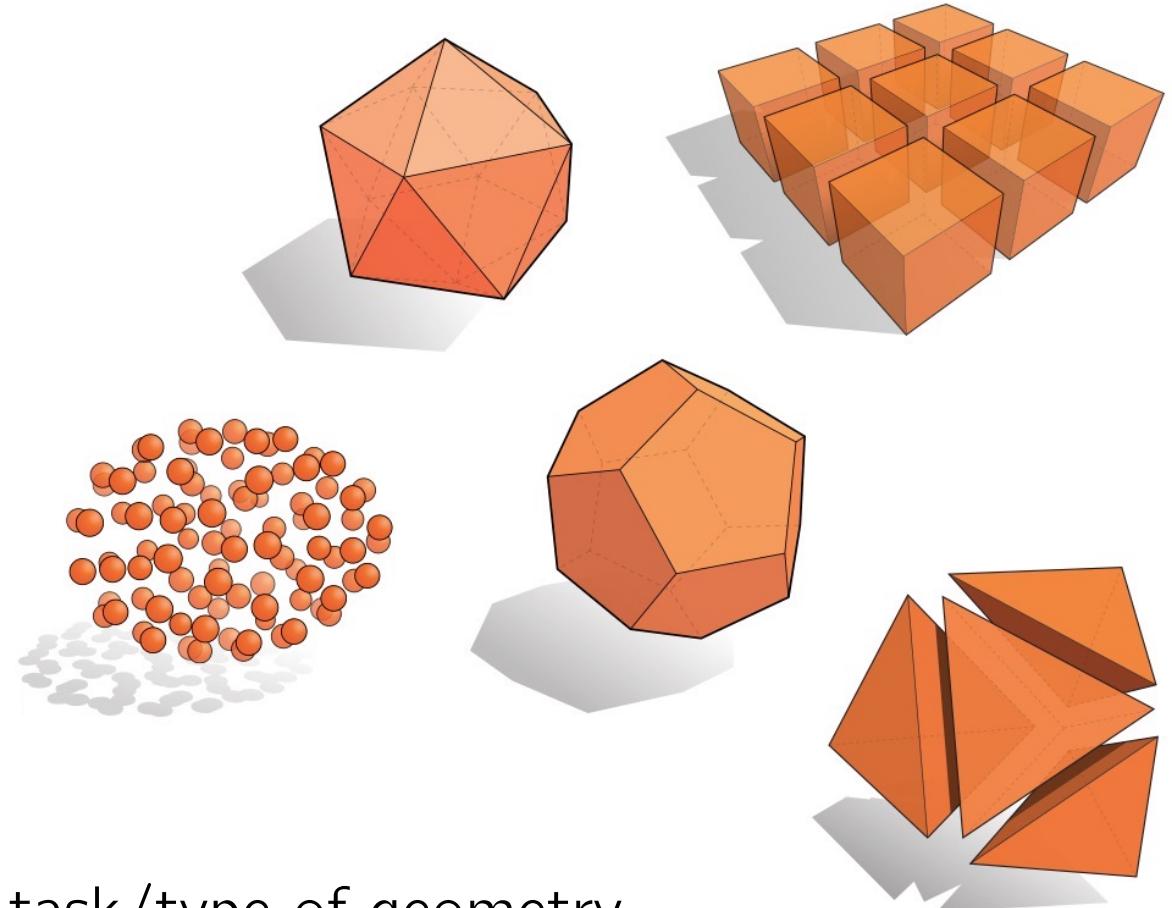
NATIONAL  
GEOGRAPHIC

Photograph by Adriana Franco, Your Shot

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# Many Ways to Represent Geometry

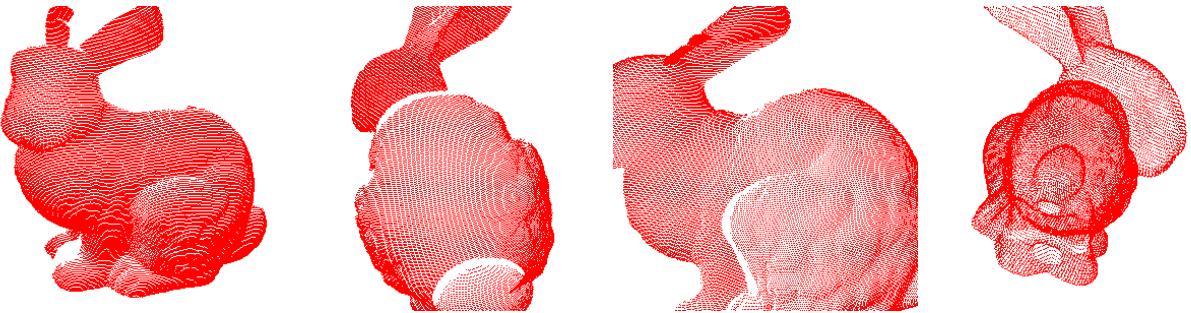
- Explicit
  - Point cloud
  - Polygon mesh
  - Subdivision, NURBS
  - ...
- Implicit
  - Lever sets
  - Algebraic surface
  - Distance functions
  - ...
- Each choice best suited to a different task/type of geometry



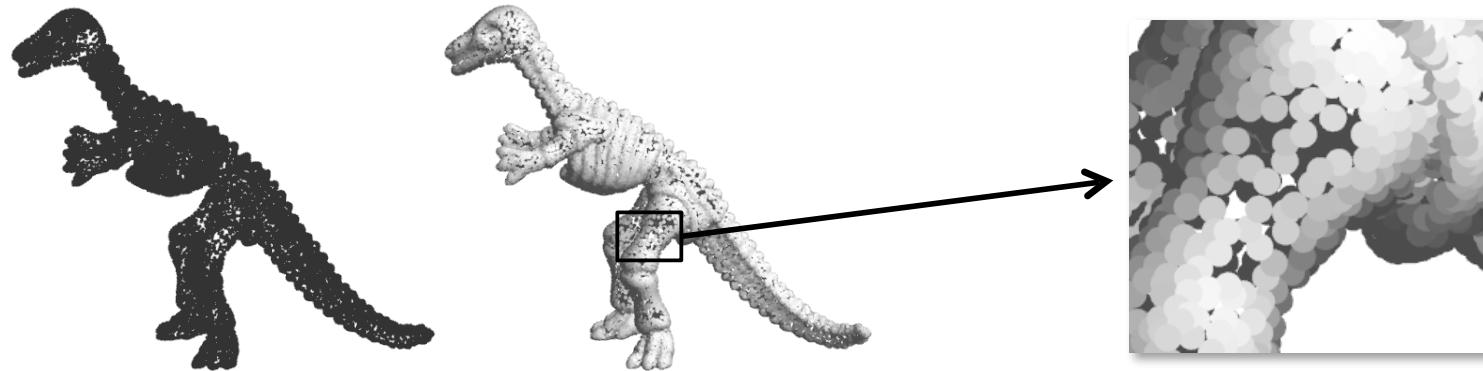
# Representation Considerations

- Needs to be stored in the computer
- Creation of new shapes
  - Input metaphors, interfaces...
- Operations
  - Editing, simplification, smoothing, filtering, repairing...
- Rendering
  - Rasterization, ray tracing, neural rendering...
- Animation

# Point Clouds

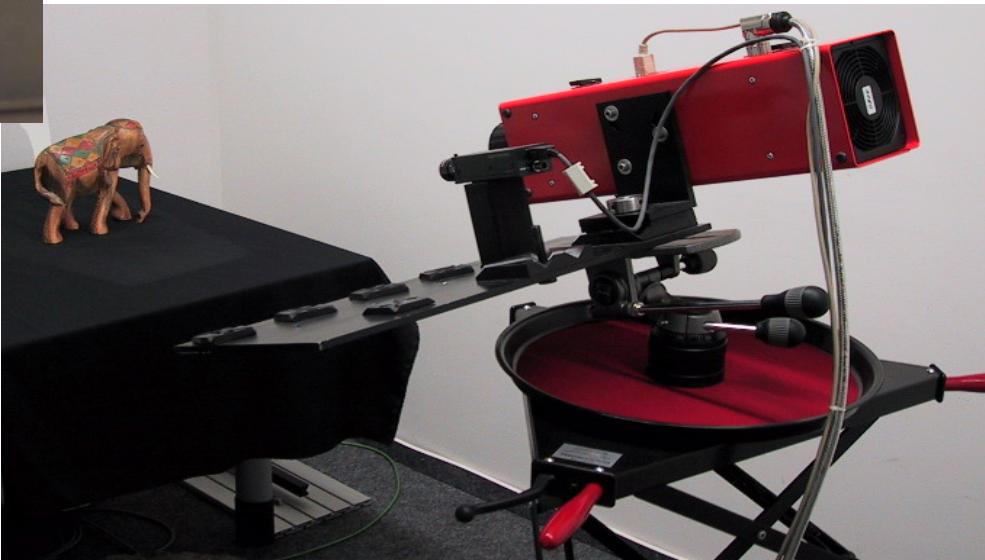
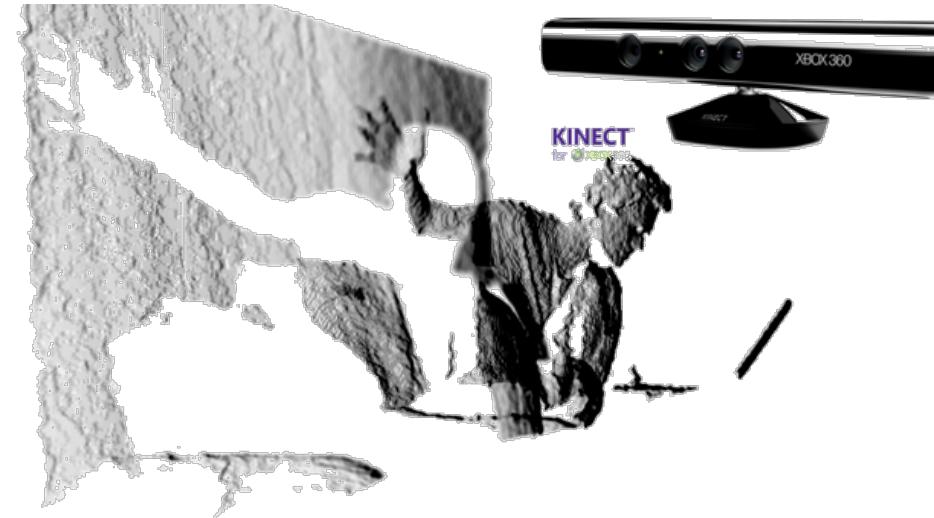
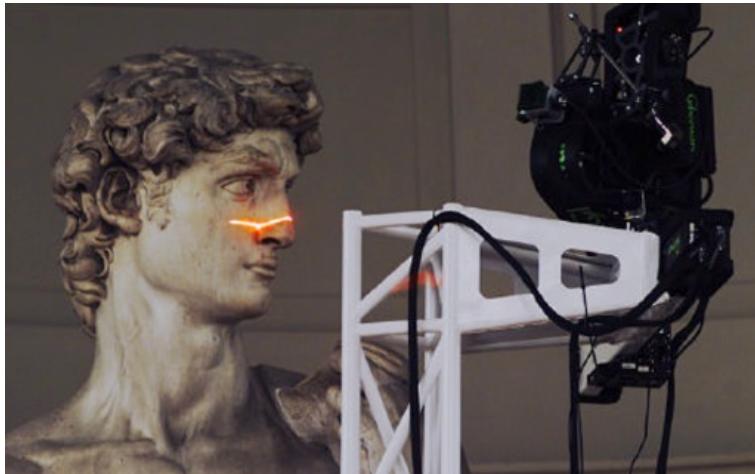


- Simplest representation: **only points**, no connectivity
- Collection of  $(x, y, z)$  coordinates, possibly with normal
- Points with orientation are called **surfels**



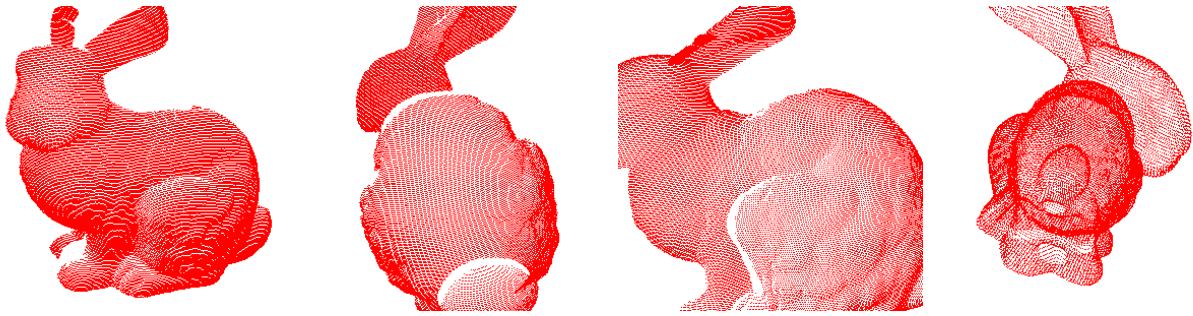
Shading needs normals!

# Output of Acquisition

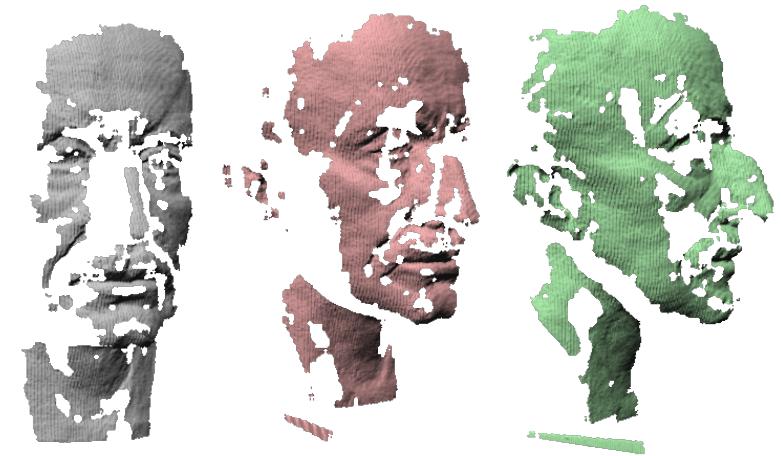


Slide credit: Hao Su

# Point Clouds

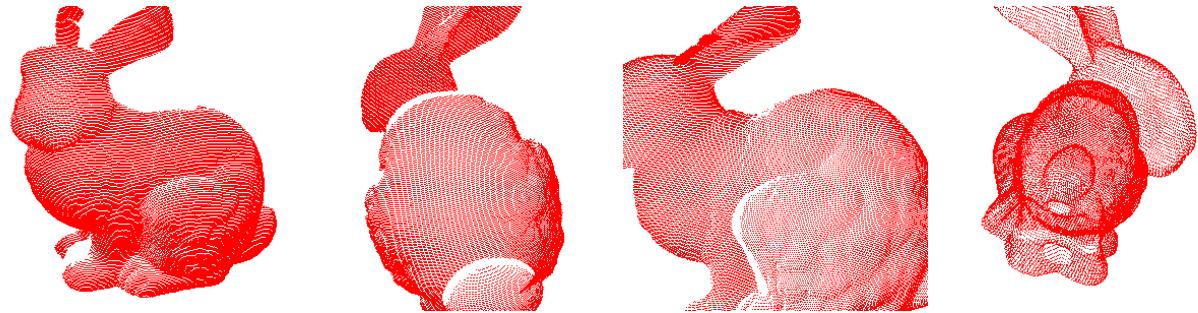


- Simplest representation: **only points**, no connectivity
- Collection of  $(x, y, z)$  coordinates, possibly with normal
- Points with orientation are called **surfels**
  
- Often results from scanners
- Potentially noisy
- Registration of multiple images

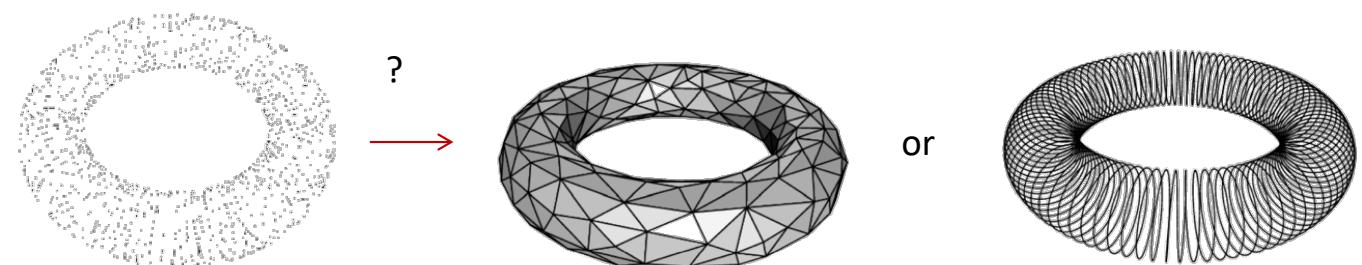


Set of raw scans

# Point Clouds

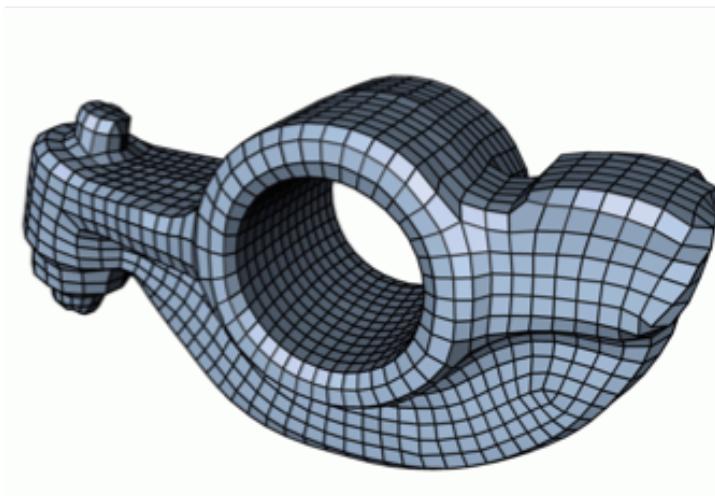
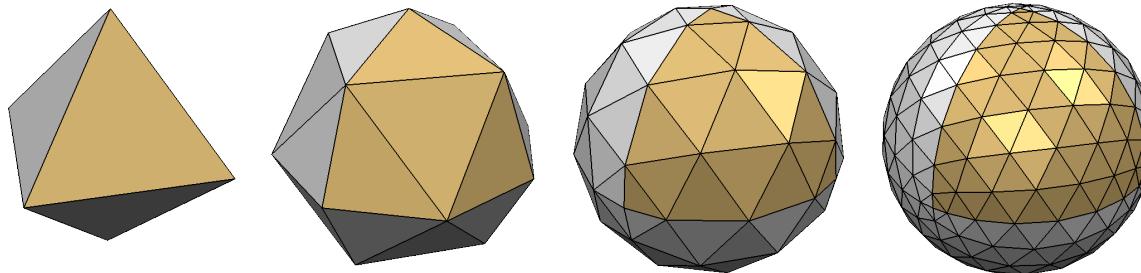


- Easily represent any kind of geometry
- Useful for large datasets
- Difficult to draw in undersampled regions
- Other limitations:
  - No simplification or subdivision
  - No direction smooth rendering
  - No topological information



# Polygonal Meshes

- Boundary representations of objects



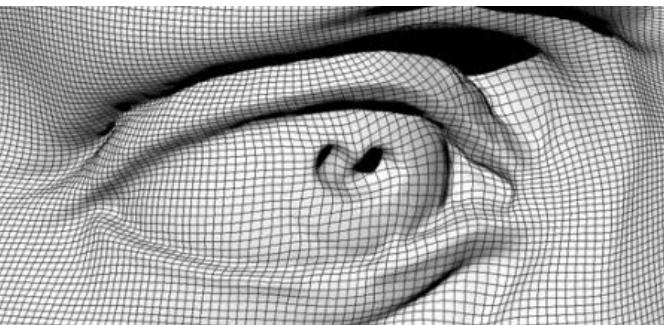
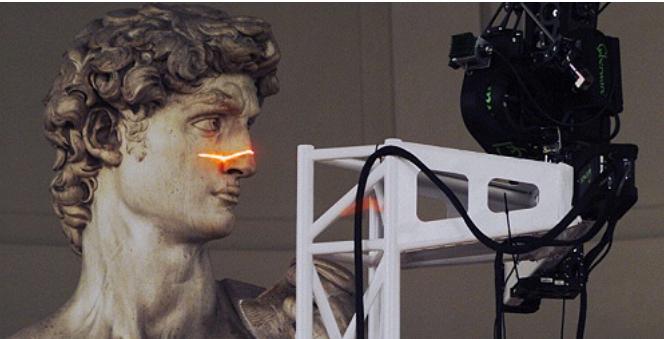
# A Large Triangle Mesh

David

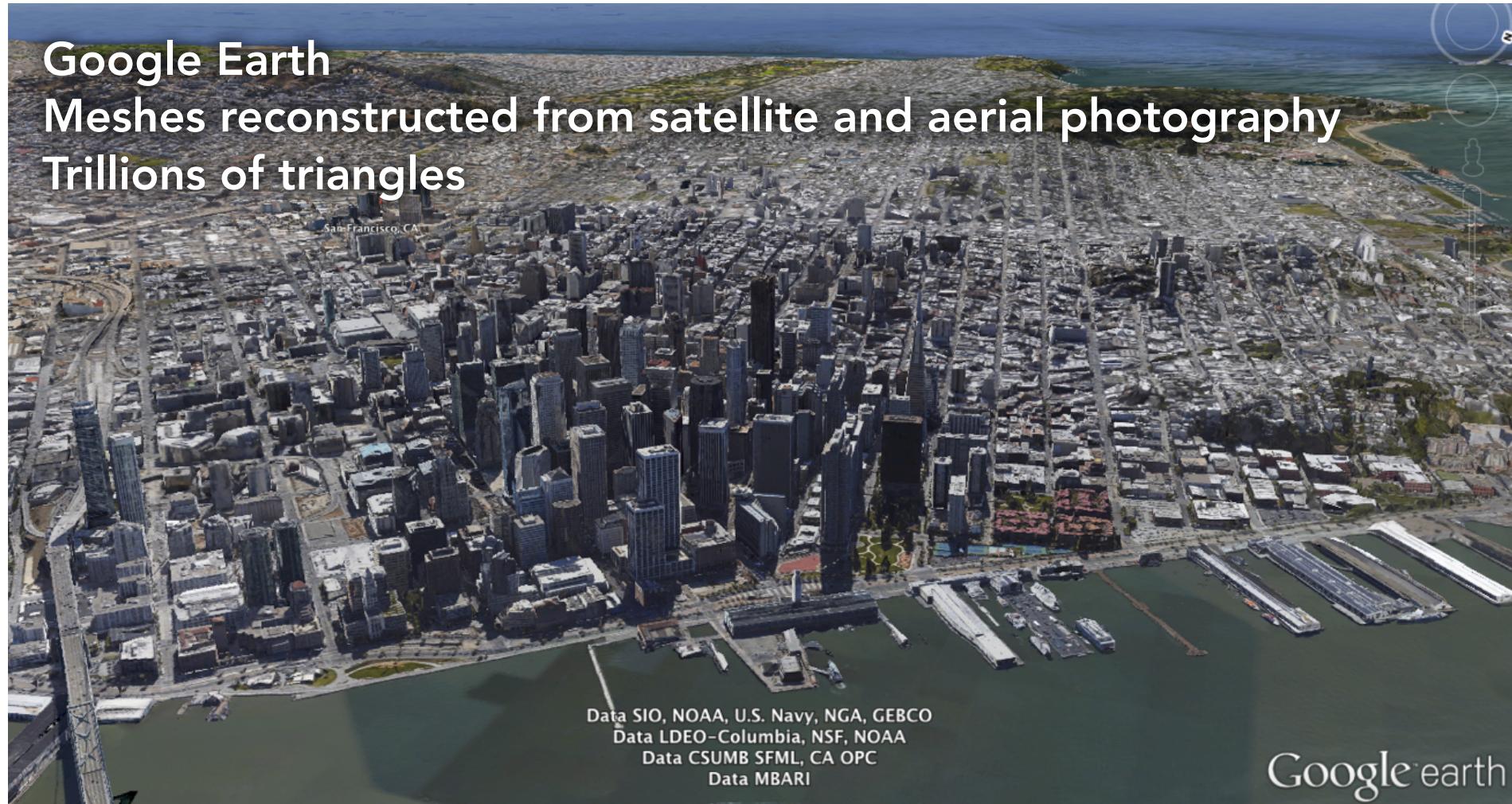
Digital Michelangelo Project

28,184,526 vertices

56,230,343 triangles

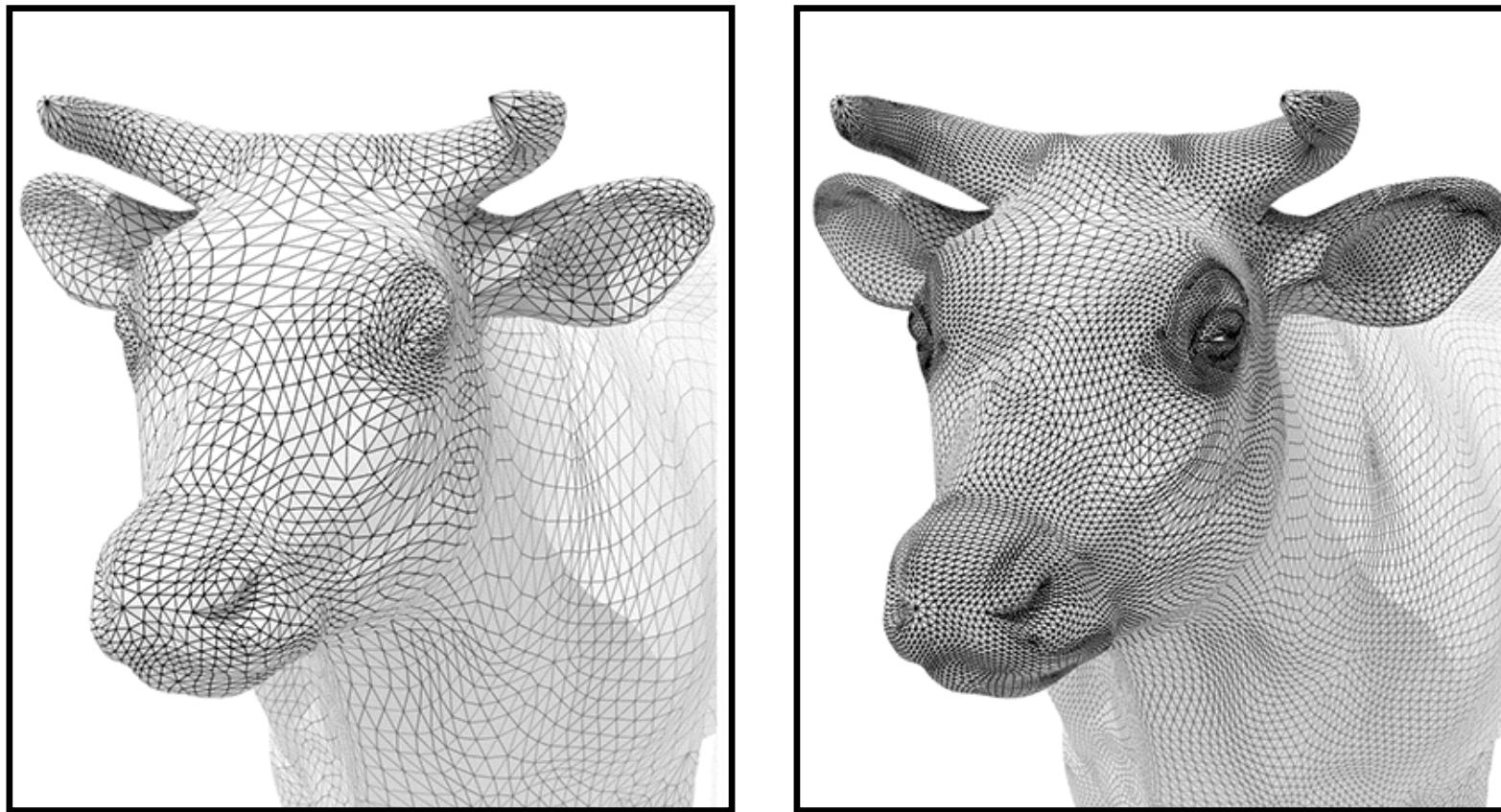


# A Very Large Triangle Mesh



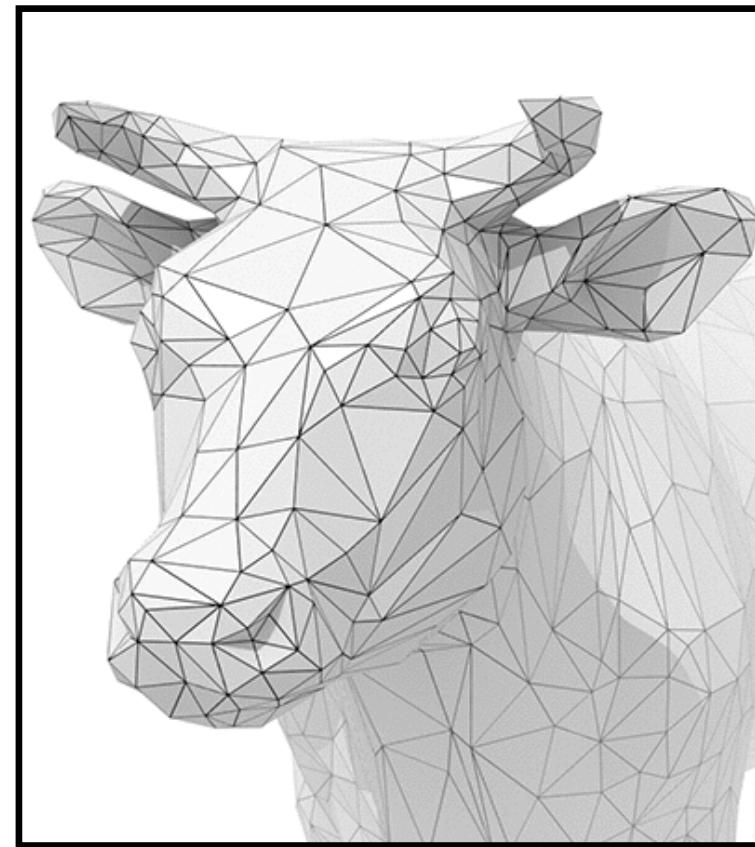
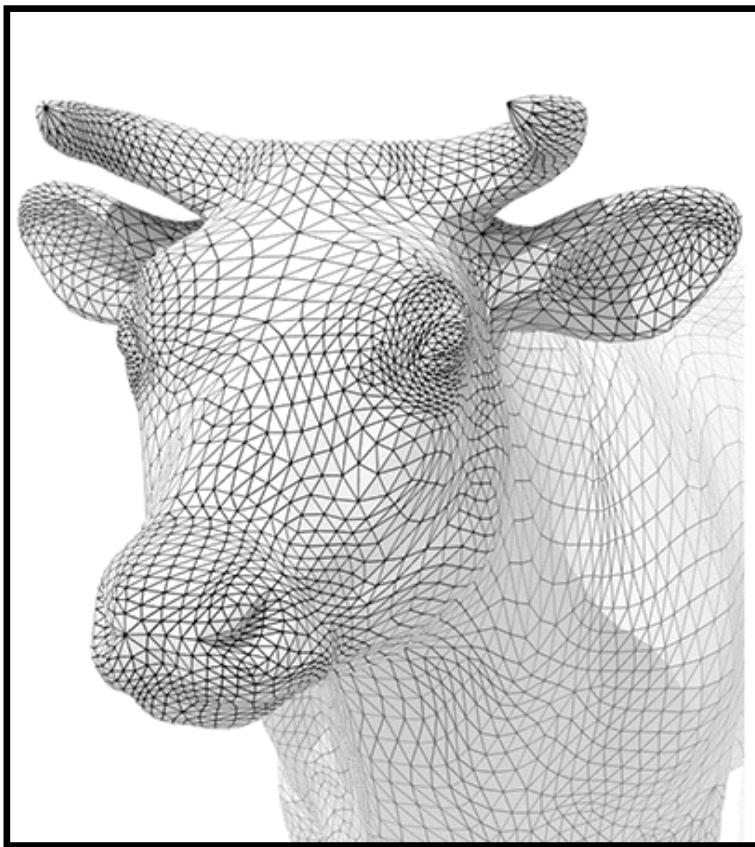
Slide credit: Ren Ng

# Mesh Upsampling - Subdivision



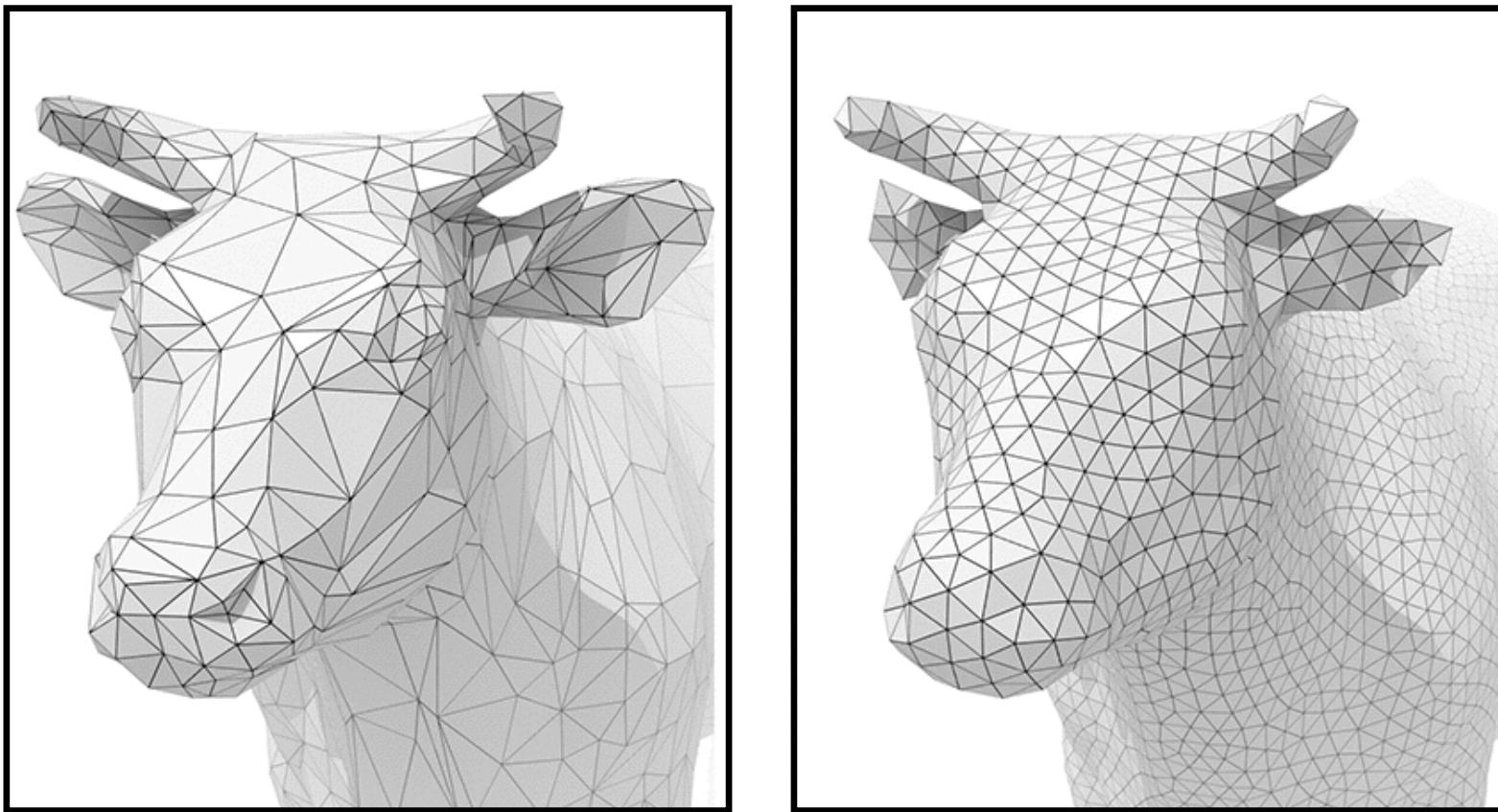
Increase resolution via interpolation

# Mesh Downsampling - Simplification



Decrease resolution; try to preserve shape/appearance

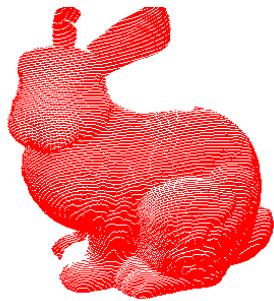
# Mesh Regularization



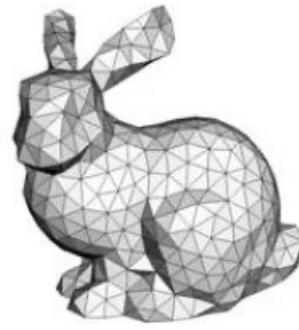
Modify sample distribution to improve quality

# Shape Representations

Non-parametric



Points

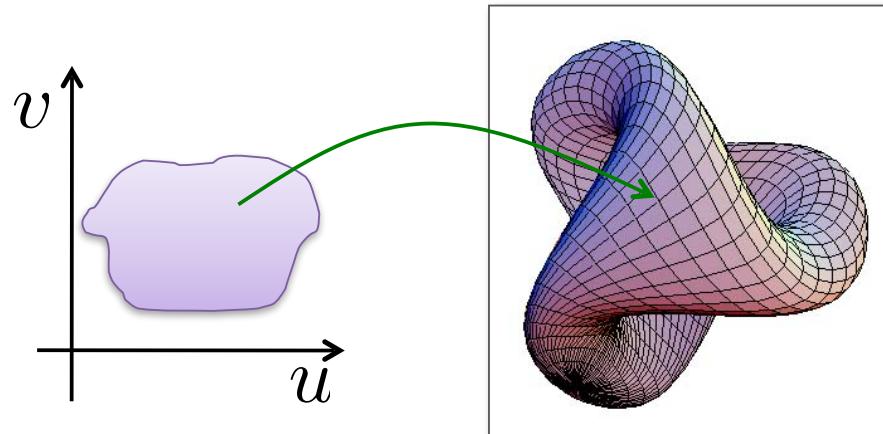


Meshes

# Parametric Representation

Range of a function  $f : X \rightarrow Y, X \subseteq \mathbb{R}^m, Y \subseteq \mathbb{R}^n$

Surface in 3D:  $m = 2, n = 3$



$$s(u, v) = (x(u, v), y(u, v), z(u, v))$$

# Parametric Curves

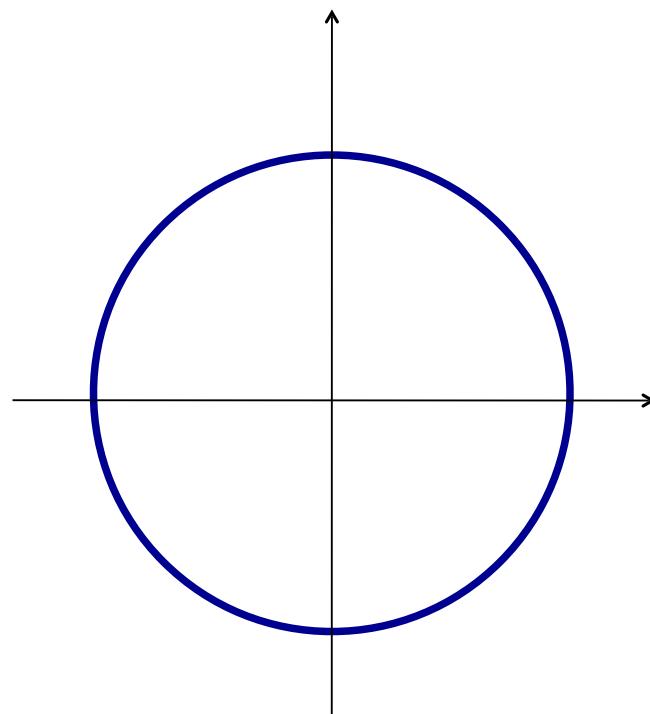
Explicit curve/circle in 2D

$$\mathbf{p} : \mathbb{R} \rightarrow \mathbb{R}^2$$

$$t \mapsto \mathbf{p}(t) = (x(t), y(t))$$

$$\mathbf{p}(t) = r (\cos(t), \sin(t))$$

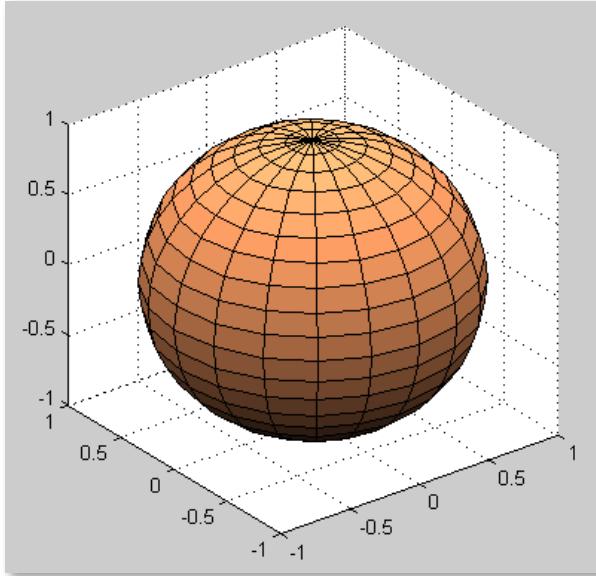
$$t \in [0, 2\pi)$$



# Parametric Surfaces

Sphere in 3D

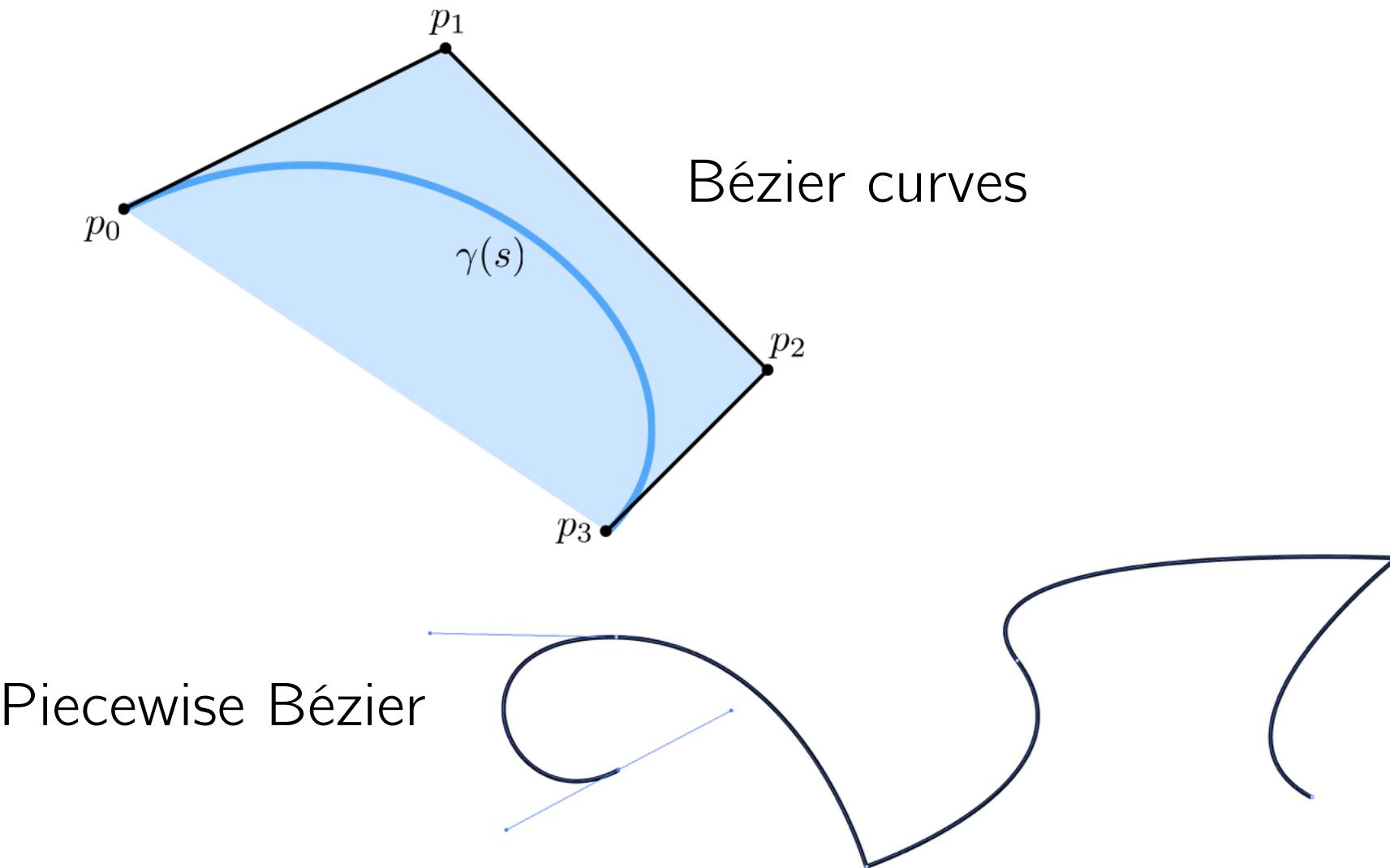
$$s : \mathbb{R}^2 \rightarrow \mathbb{R}^3$$



$$s(u, v) = r (\cos(u) \cos(v), \sin(u) \cos(v), \sin(v))$$

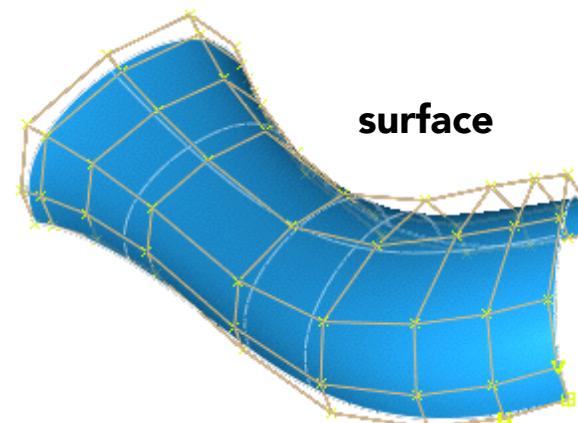
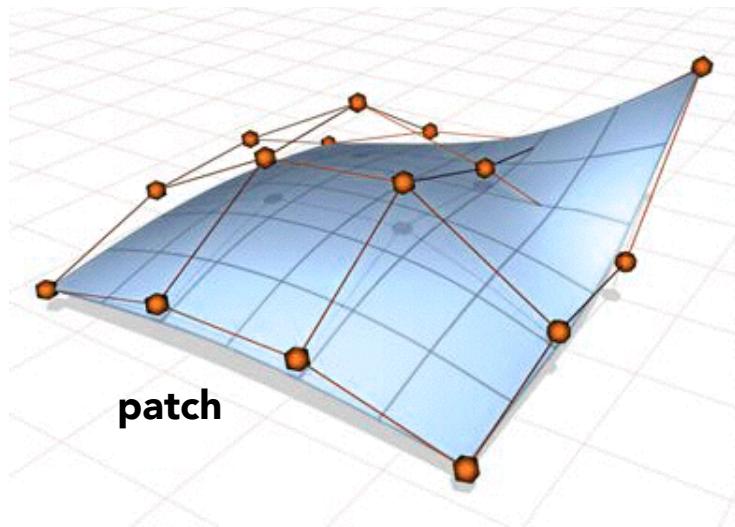
$$(u, v) \in [0, 2\pi) \times [-\pi/2, \pi/2]$$

# Bézier Curves



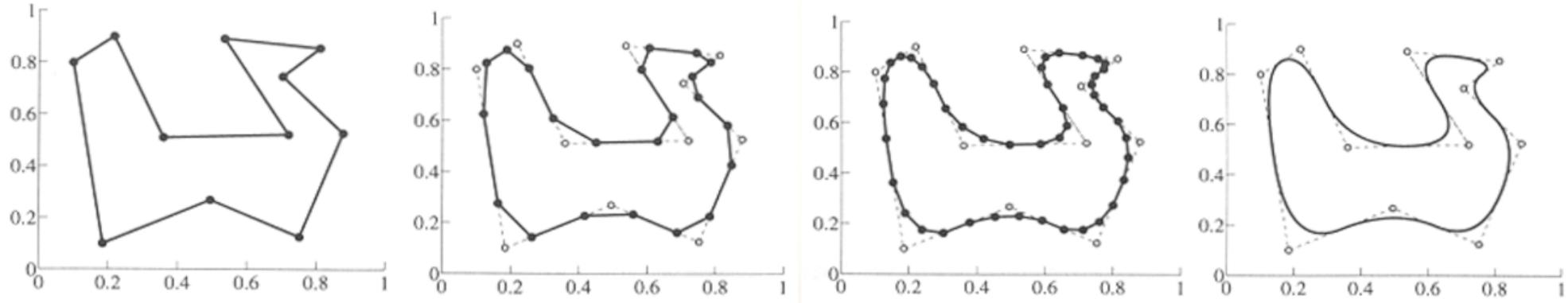
# Bézier Surfaces

Use tensor product of Bézier curves to get a patch:

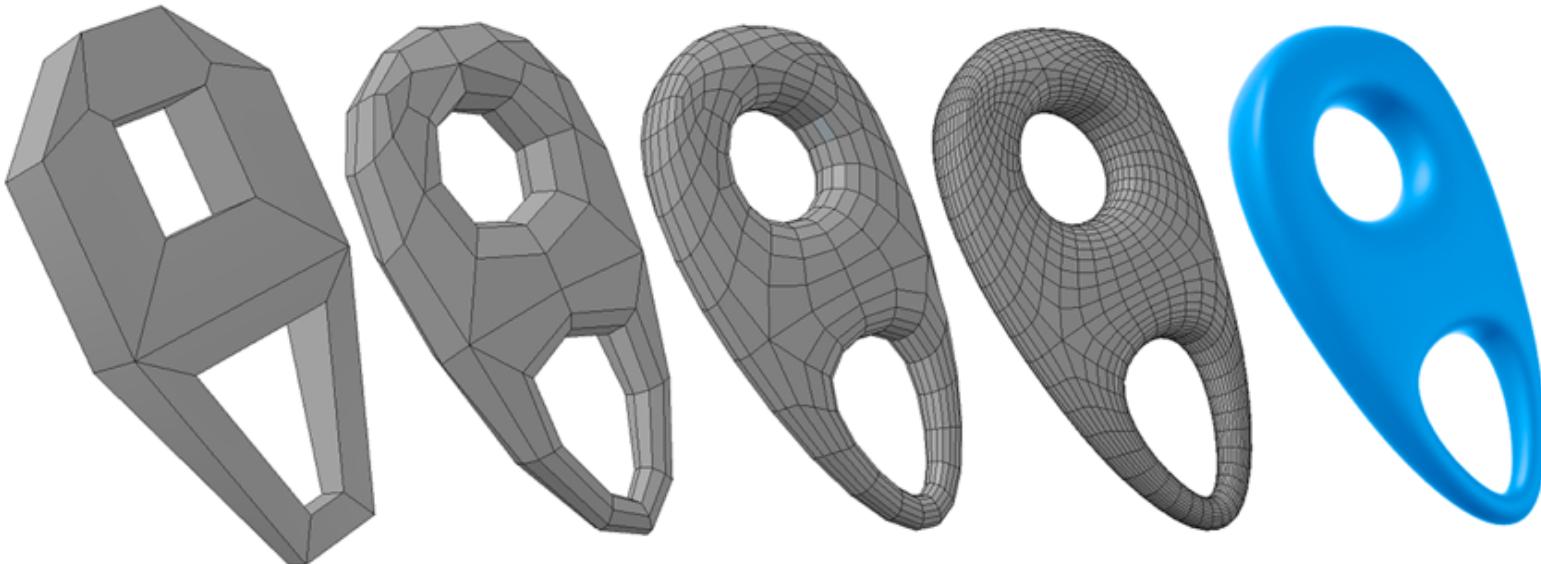


Multiple Bézier patches form a surface.

# Subdivision Curves/Surfaces



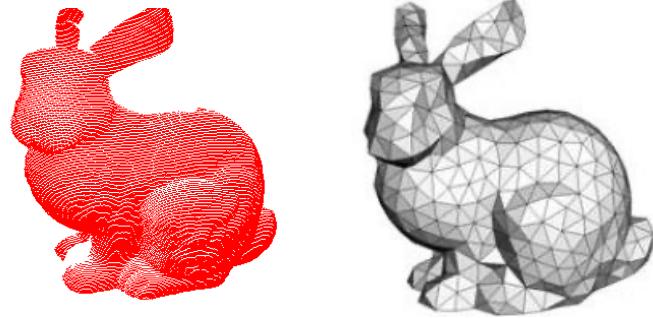
Slide cribbed from Keenan Crane, cribbed from Don Fussell.



# Shape Representations

Non-parametric

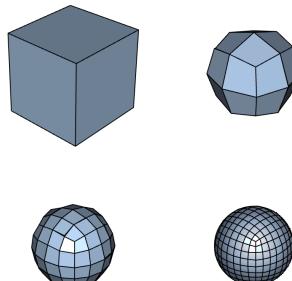
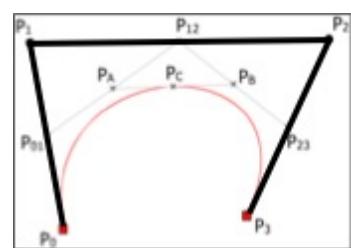
Explicit



Points

Meshes

Parametric



Splines

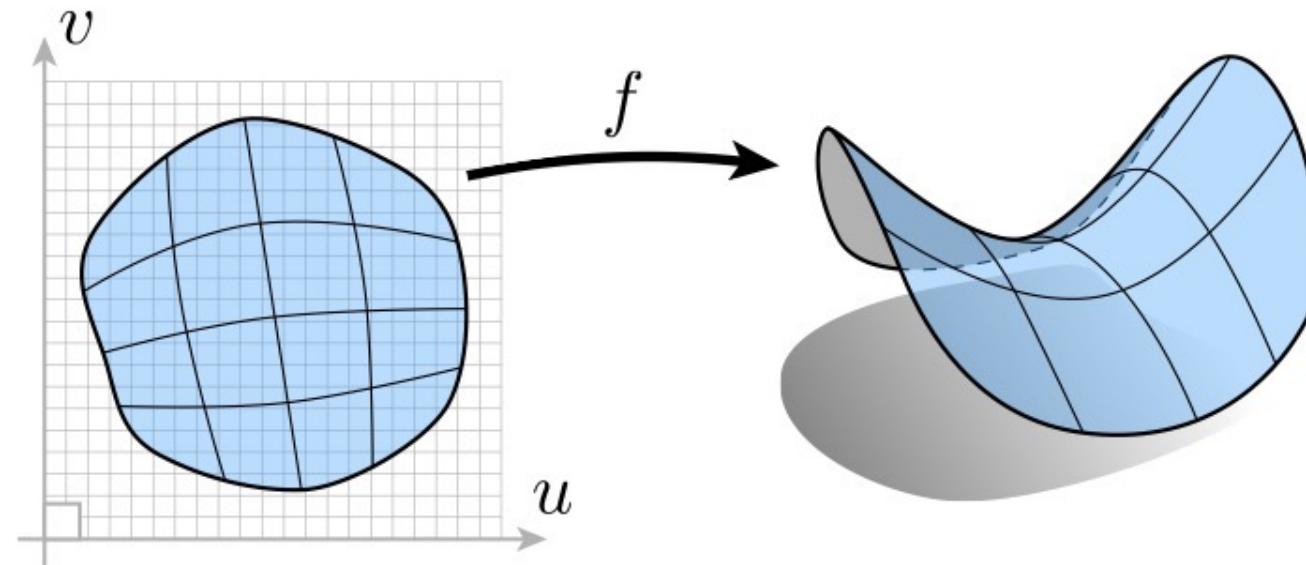
Subdivision  
Surfaces

# “Explicit” Representations of Geometry

All points are given directly.

Generally:

$$f : \mathbb{R}^2 \rightarrow \mathbb{R}^3; (u, v) \mapsto (x, y, z)$$

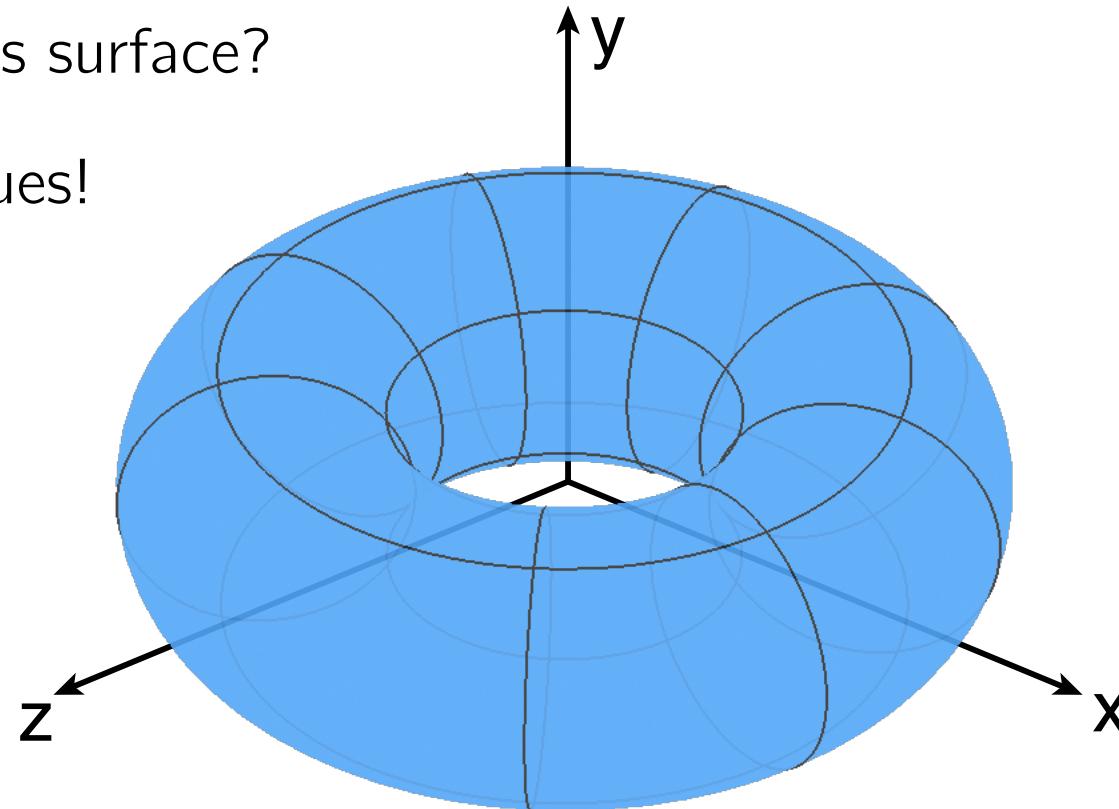


# Explicit Surface – Sampling Is Easy

$$f(u, v) = ((2 + \cos u) \cos v, (2 + \cos u) \sin v, \sin u)$$

What points lie on this surface?

Just plug in  $(u, v)$  values!



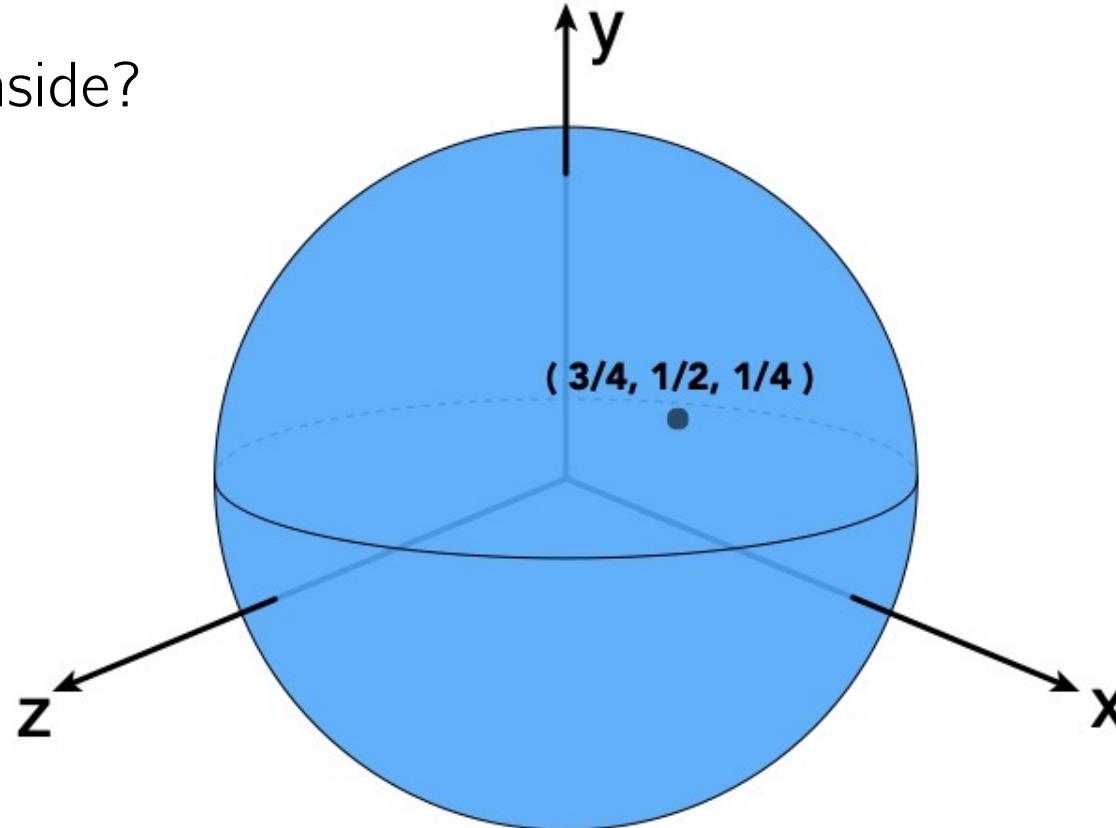
Explicit representations make some tasks easy.

Slide credit: Ren Ng

# Explicit Surface – Inside/Outside Test Hard

$$f(u, v) = (\cos u \sin v, \sin u \sin v, \cos v)$$

Is  $(3/4, 1/2, 1/4)$  inside?



Some tasks are hard with explicit representations.

Slide credit: Ren Ng

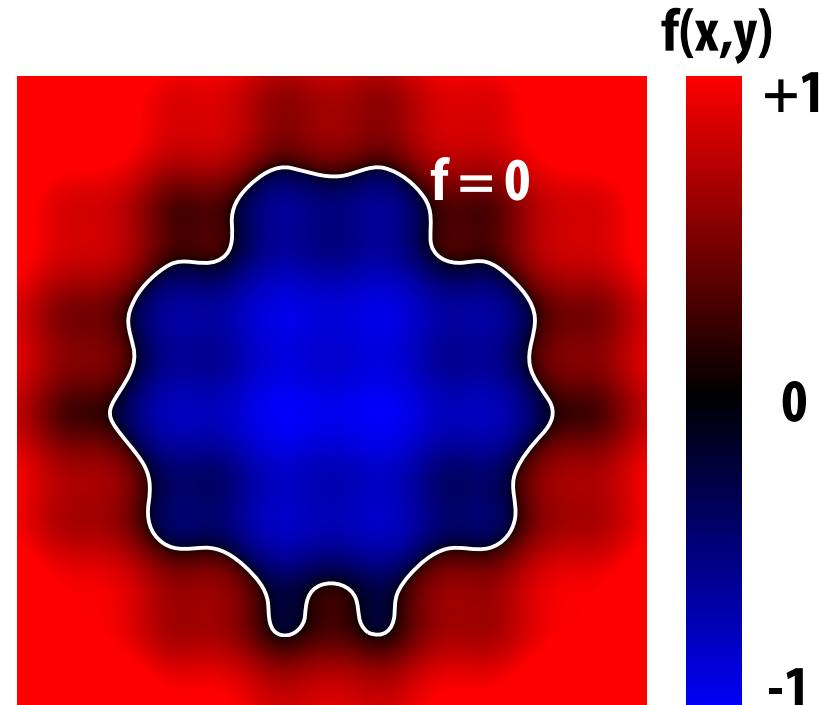
# “Implicit” Representations of Geometry

Based on classifying points

- Points satisfy some specified relationship.

E.g., sphere: all points in 3D, where  $x^2 + y^2 + z^2 = 1$

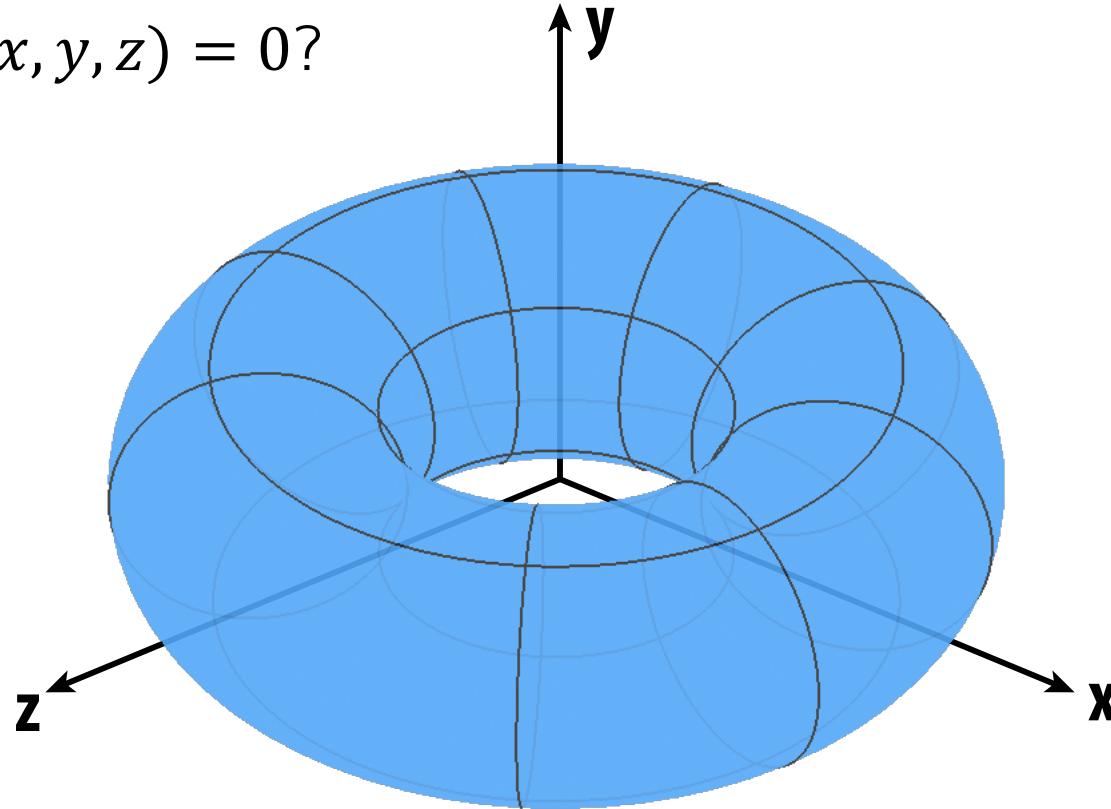
More generally,  $f(x, y, z) = 0$



# Implicit Surface – Sampling Can Be Hard

$$f(x, y, z) = (2 - \sqrt{x^2 + y^2})^2 + z^2 - 1$$

What points lie on  $f(x, y, z) = 0$ ?



Some tasks are hard with implicit representations.

Slide credit: Ren Ng

# Implicit Surface – Inside/Outside Tests Easy

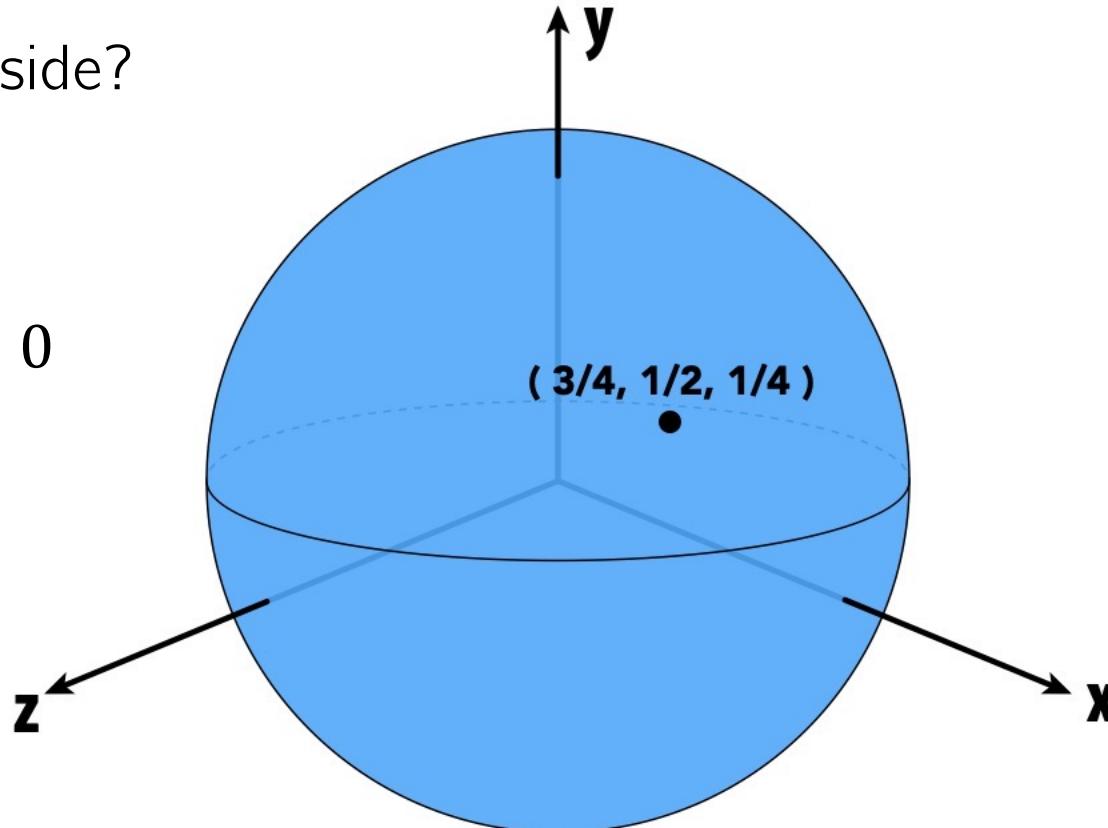
$$f(x, y, z) = x^2 + y^2 + z^2 - 1$$

Is  $(3/4, 1/2, 1/4)$  inside?

Just plug it in:

$$f(x, y, z) = -1/8 < 0$$

Yes, inside.



Implicit representations make some tasks easy.

# Algebraic Surfaces (Implicit)

Surface is zero set of a polynomial in  $x, y, z$ .



$$x^2 + y^2 + z^2 = 1$$



$$(R - \sqrt{x^2 + y^2})^2 + z^2 = r^2$$



$$(x^2 + \frac{9y^2}{4} + z^2 - 1)^3 =$$

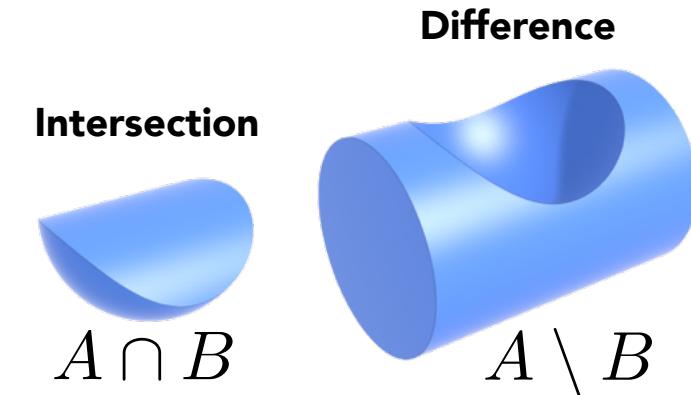
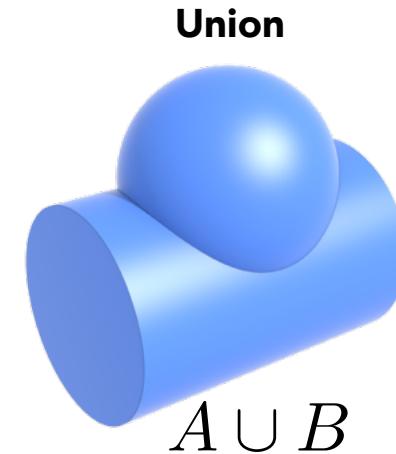
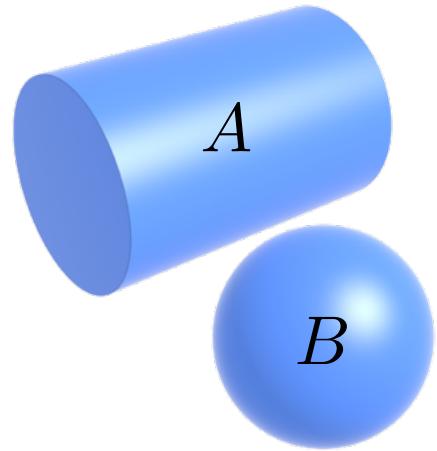
$$x^2 z^3 + \frac{9y^2 z^3}{80}$$



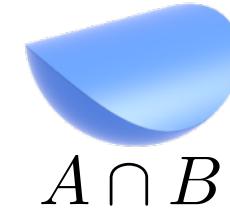
More complex shapes?

# Constructive Solid Geometry (Implicit)

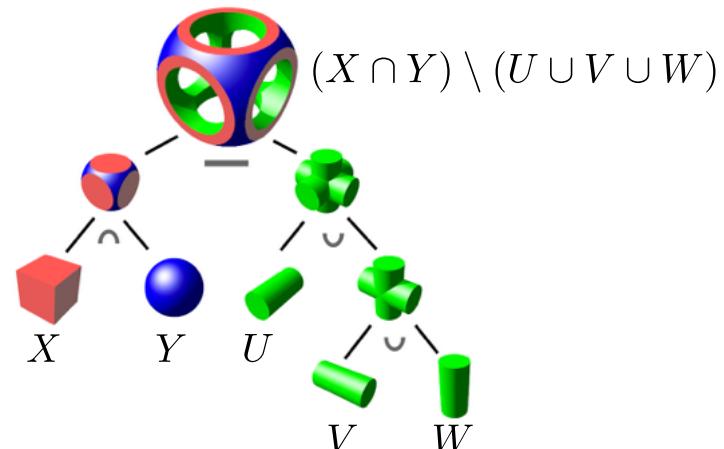
Combine implicit geometry via Boolean operations



**Intersection**



Boolean expressions:



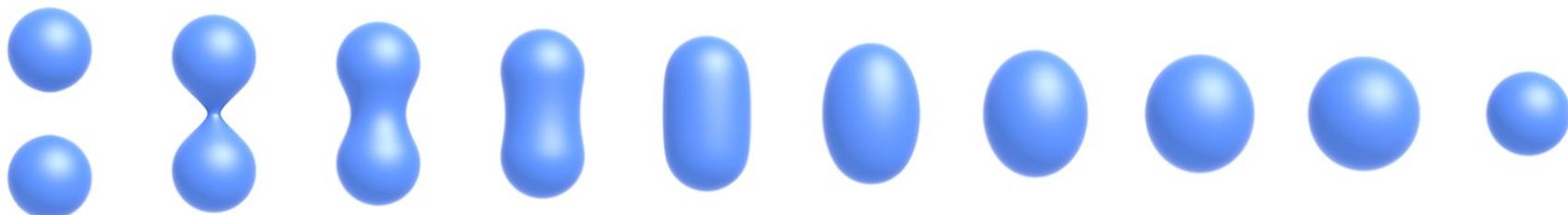
Slide credit: Ren Ng

# Distance Functions (Implicit)

Instead of Boolean, gradually blend surfaces together using

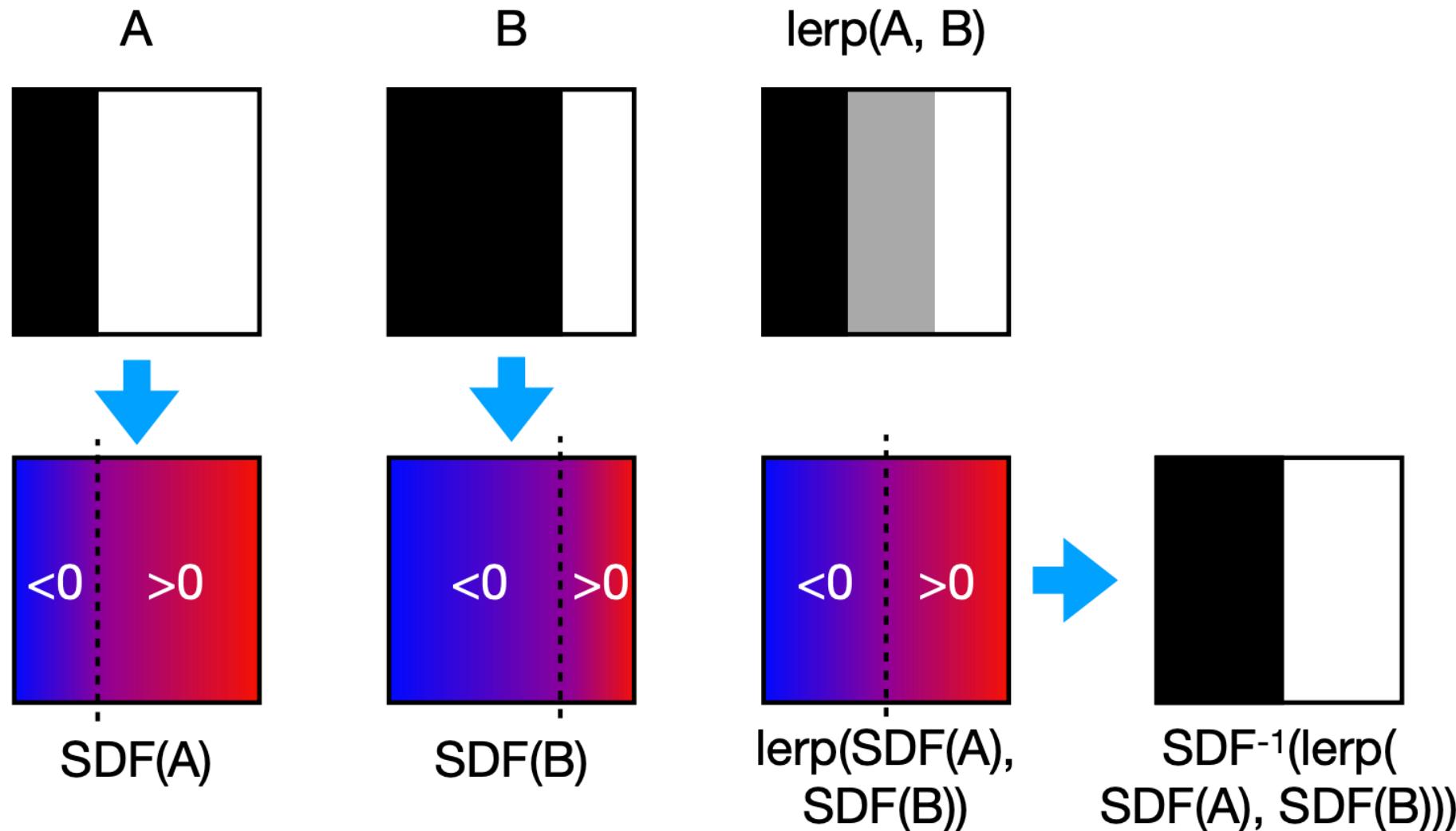
Distance functions:

Giving minimum distance (could be **signed** distance) from anywhere to object



# Distance Functions (Implicit)

Example: Blending (linear interp.) a moving boundary

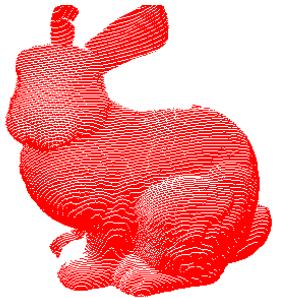
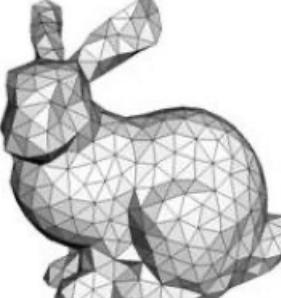
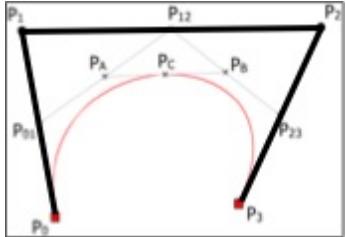
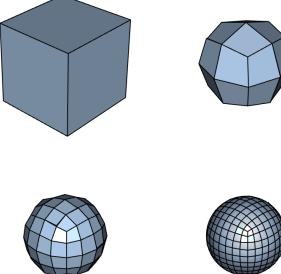
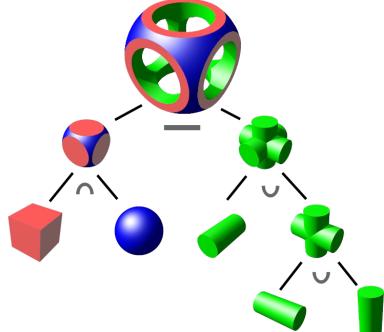


# Scene of Pure Distance Functions (Not Easy!)



See <http://iquilezles.org/www/material/nvscene2008/nvscene2008.htm>

# Shape Representations

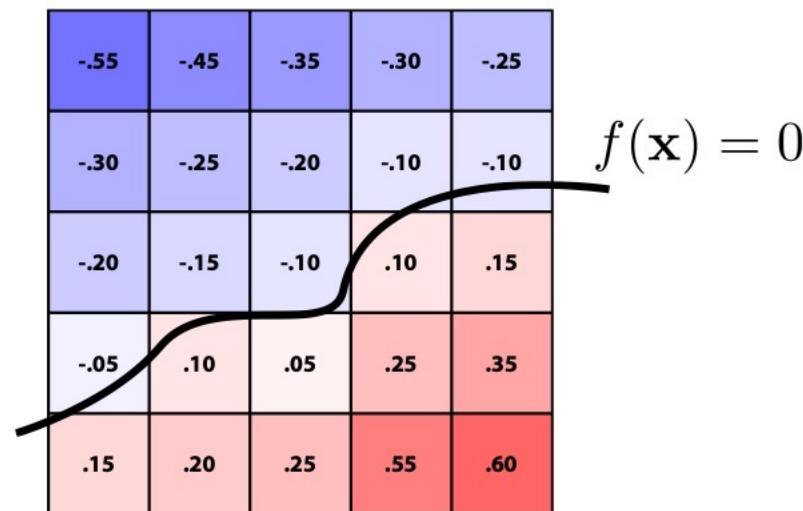
	Explicit	Implicit
Non-parametric	 Points	 Meshes
Parametric	 Splines	 $x^2 + y^2 + z^2 = 1$
	 Subdivision Surfaces	 Constructive Solid Geometry

# Level Set Methods (Implicit)

Implicit surfaces have some nice features (e.g., merging/splitting).

But hard to describe complex shapes in closed form

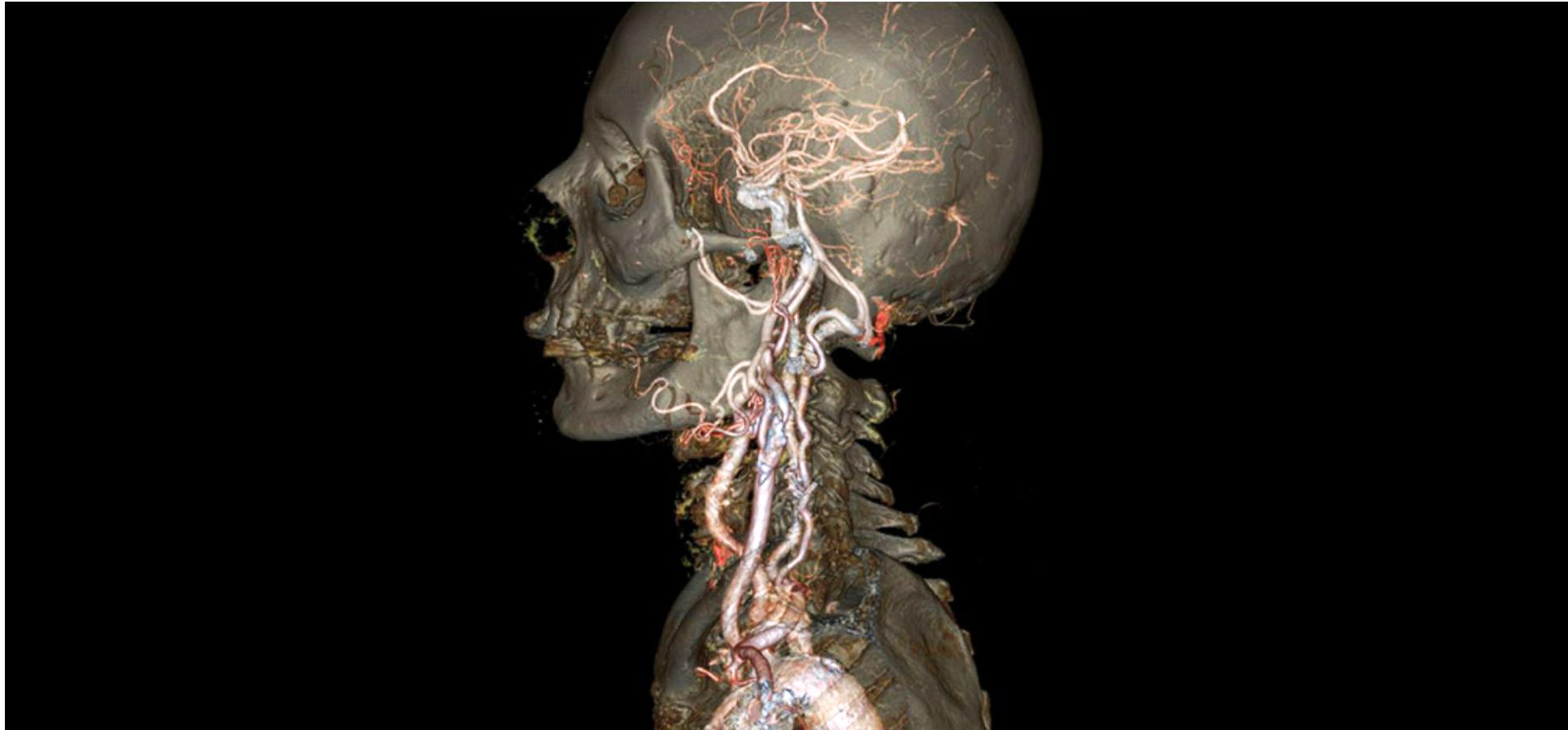
Alternative: store a grid of values approximating function



Surface is found where interpolated values equal zero.

Provides much more explicit control over shape (like a texture)

# Level Sets from Medical Data (CT, MRI, etc.)

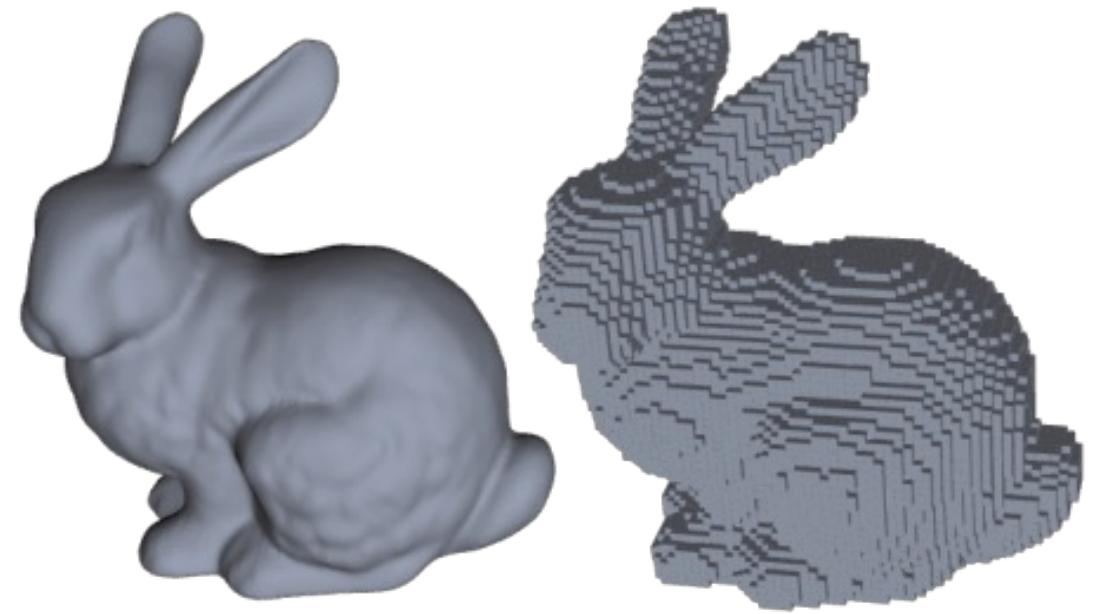
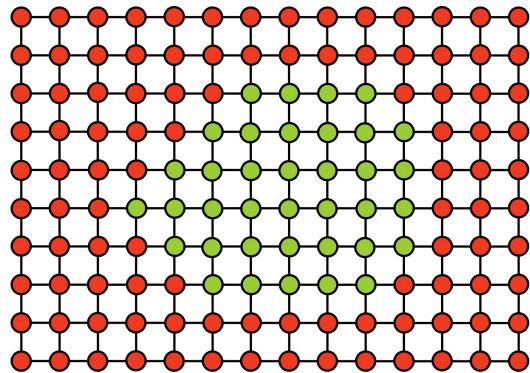
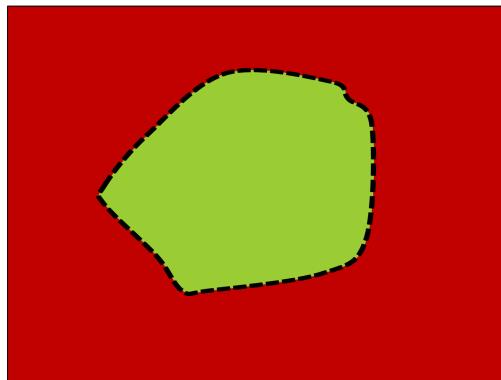


Level sets encode, e.g., constant tissue density

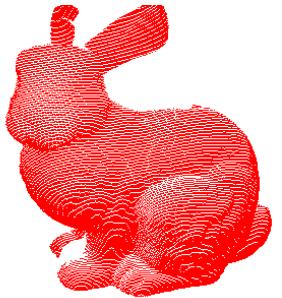
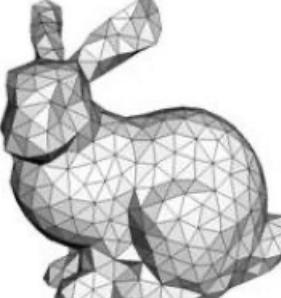
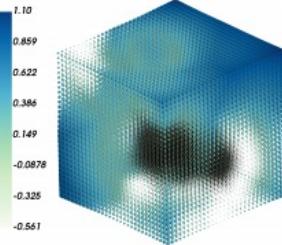
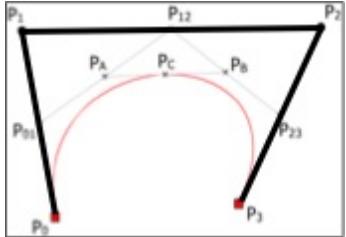
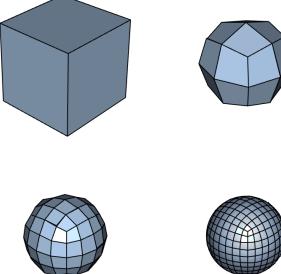
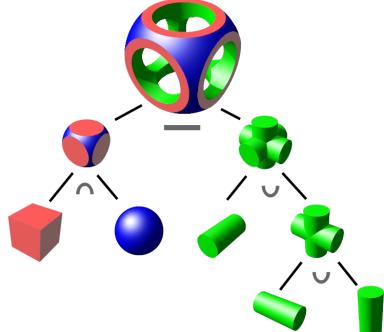
Slide credit: Ren Ng

# Related Representation: Voxels

- Binary thresholding the volumetric grid



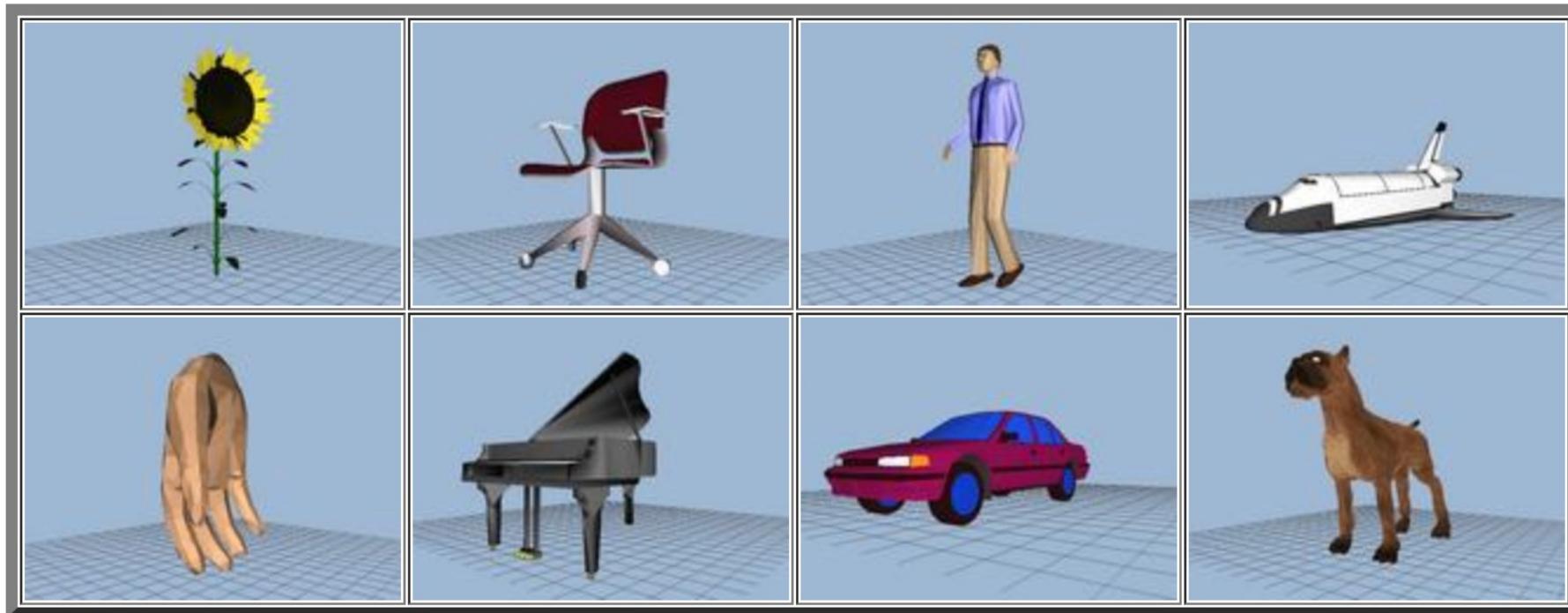
# Shape Representations

	Explicit		Implicit	
Non-parametric				
Parametric			 $x^2 + y^2 + z^2 = 1$	
	Points	Meshes	Voxels	Level Sets
	Splines	Subdivision Surfaces	Algebraic Surfaces	Constructive Solid Geometry

# AI + Geometry: Datasets

# Princeton Shape Benchmark

- 1814 Models
- 182 Categories



# Datasets Prior to 2014

Benchmarks	Types	# models	# classes	Avg # models per class
SHREC14LSGTB	Generic	8,987	171	53
PSB	Generic	907+907 (train+test)	90+92 (train+test)	10+10 (train+test)
SHREC12GTB	Generic	1200	60	20
TSB	Generic	10,000	352	28
CCCC	Generic	473	55	9
WMB	Watertight (articulated)	400	20	20
MSB	Articulated	457	19	24
BAB	Architecture	2257	183+180 (function+form)	12+13 (function+form)
ESB	CAD	867	45	19

Table 1. Source datasets from SHREC 2014: *Princeton Shape Benchmark (PSB)* [27], *SHREC 2012 generic Shape Benchmark (SHREC12GTB)* [16], *Toyohashi Shape Benchmark (TSB)* [29], *Konstanz 3D Model Benchmark (CCCC)* [32], *Watertight Model Benchmark (WMB)* [31], *McGill 3D Shape Benchmark (MSB)* [37], *Bonn Architecture Benchmark (BAB)* [33], *Purdue Engineering Shape Benchmark (ESB)* [9].

# Datasets for 3D Objects

- Large-scale Synthetic Objects: ShapeNet, 3M models
- ModelNet: absorbed by ShapeNet
- ShapeNetCore: 51.3K models in 55 categories



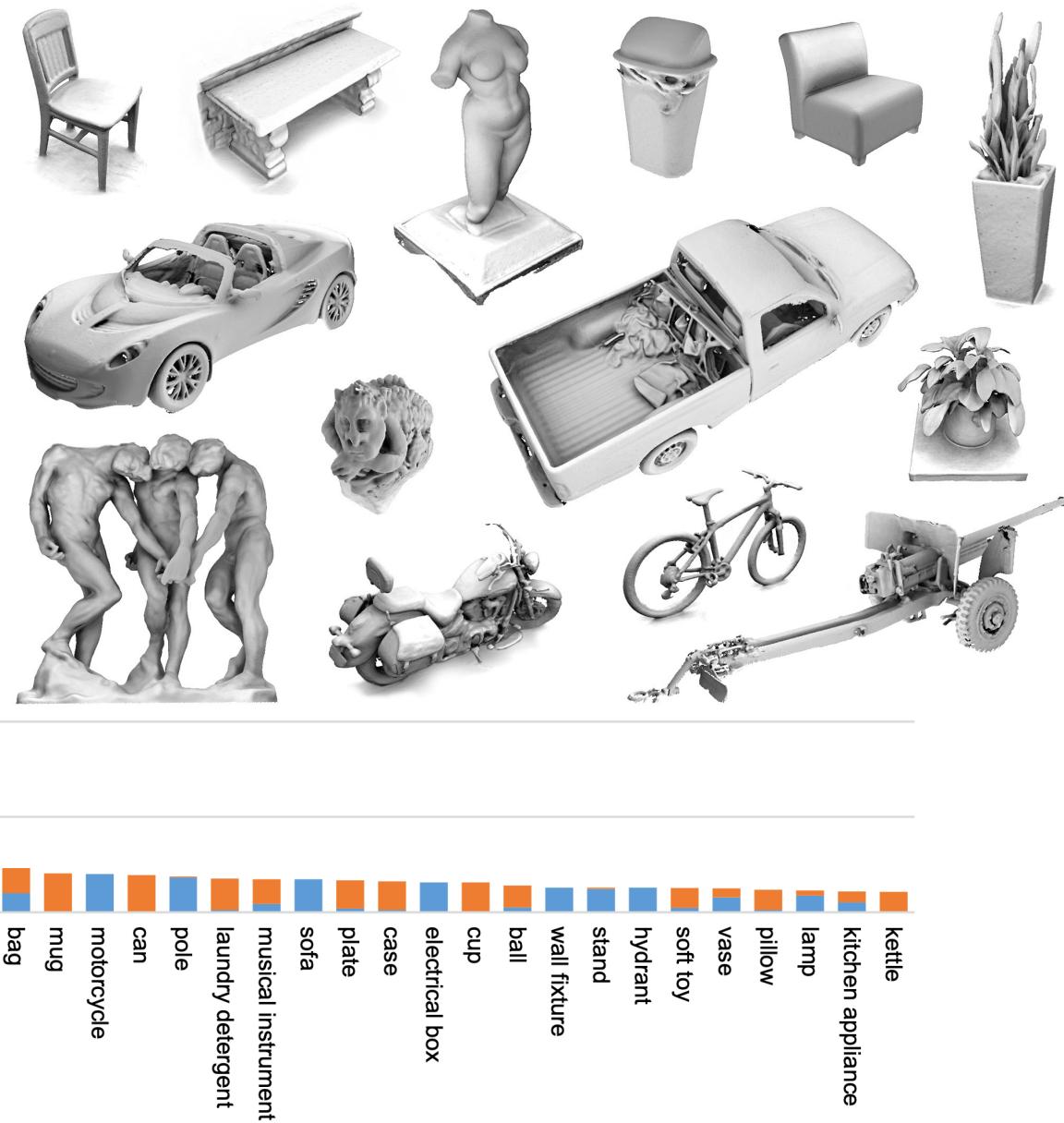
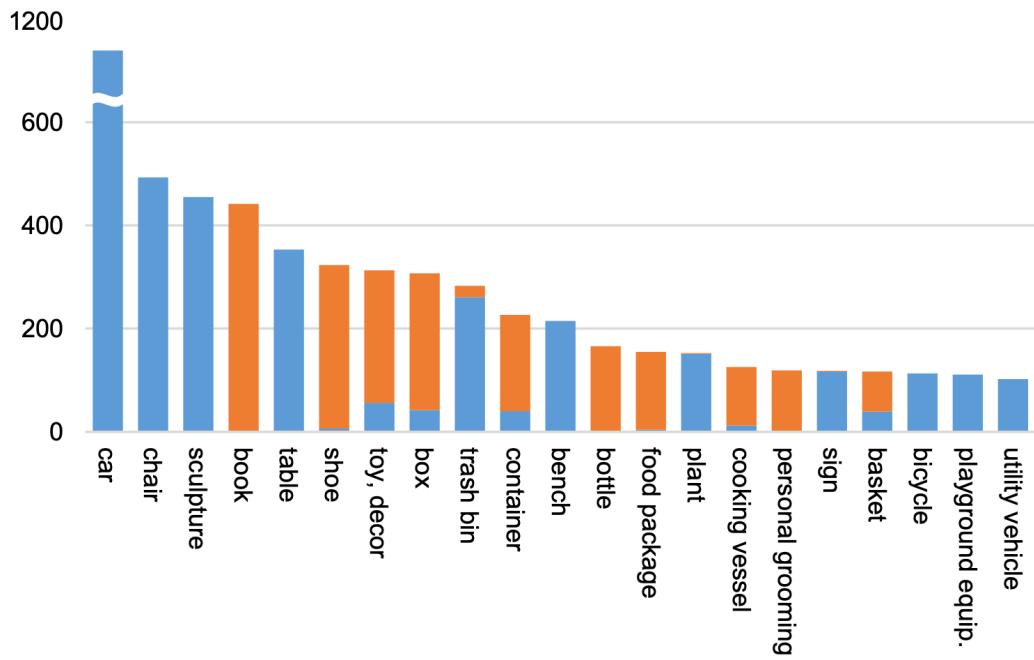
Chang et al. ShapeNet. arXiv 2015  
Wu et al. 3D ShapeNets. CVPR 2015

# Objverse (800K) and Objverse-XL (10M)



# Object Scan

- 10,933 RGBD scans
- 441 models



# CO3D

- 19,000 videos
- 50 categories



# From Objects to Parts

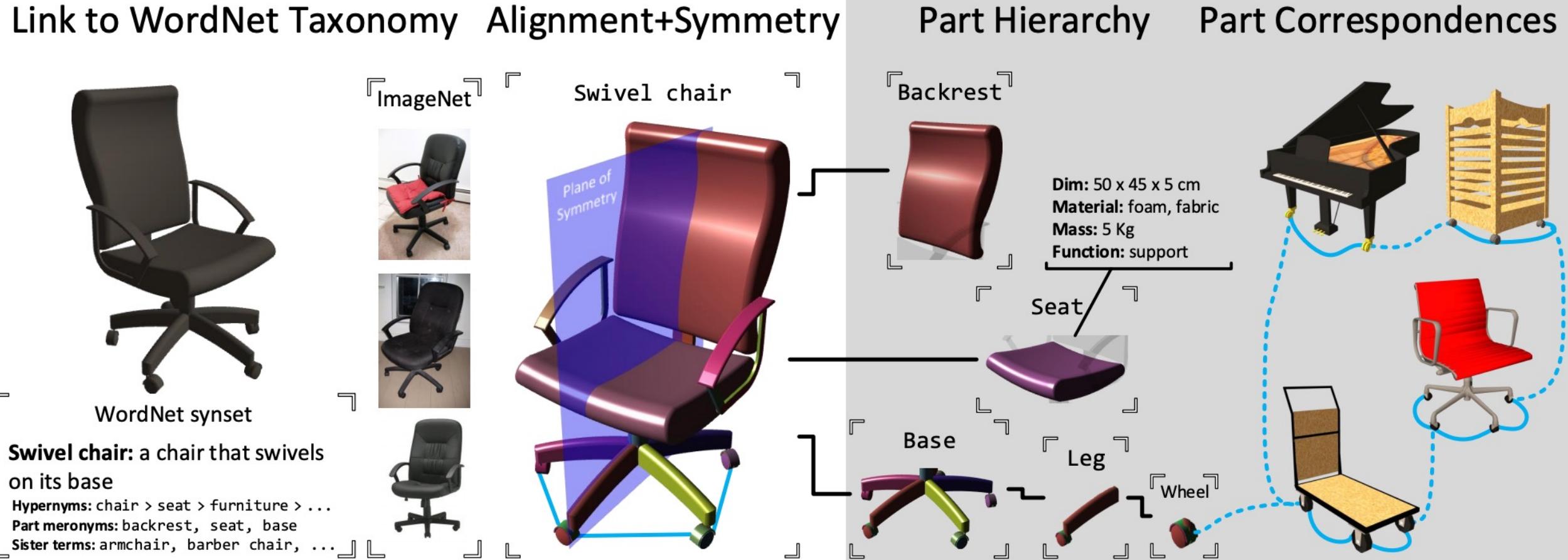
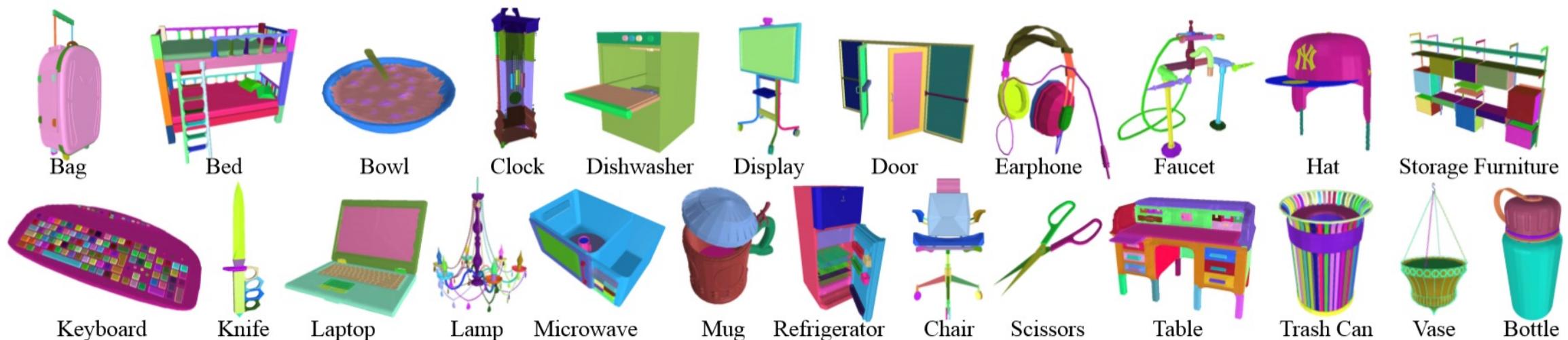


Figure from the ShapeNet paper, Chang et al. arXiv 2015

# Datasets for 3D Object Parts

## Fine-grained Parts: PartNet

- Fine-grained (+mobility)
- Instance-level
- Hierarchical



# Datasets for Indoor 3D Scenes

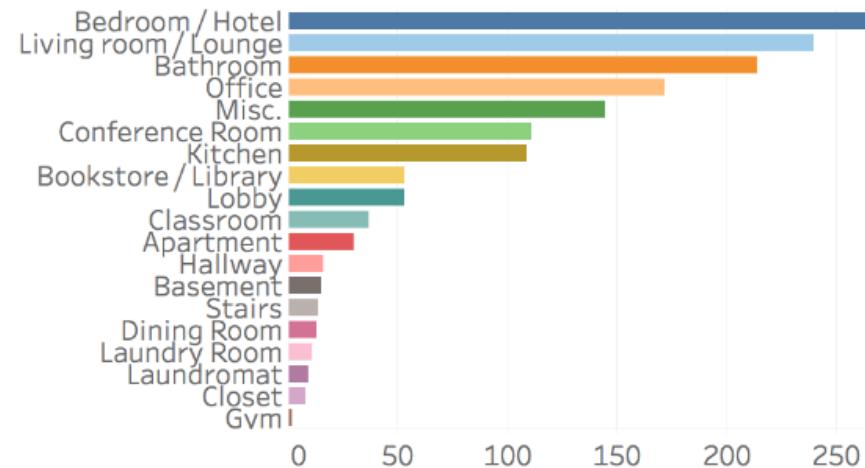
## Scanned Real Scenes: ScanNet

- 2.5M Views in 1,500 RGBD scans
- 3D camera poses
- Surface reconstructions
- Instance-level semantic segmentations



## Most recently:

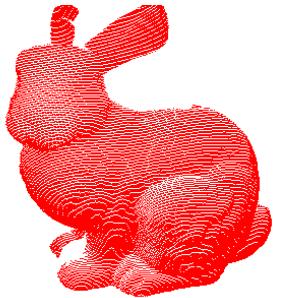
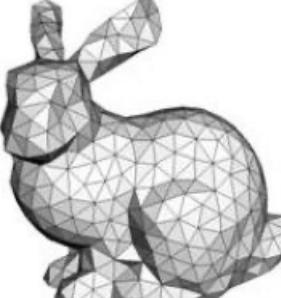
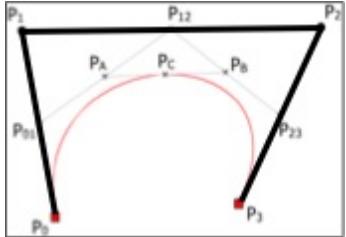
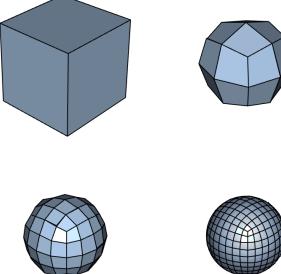
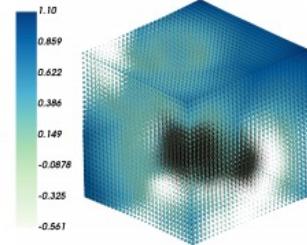
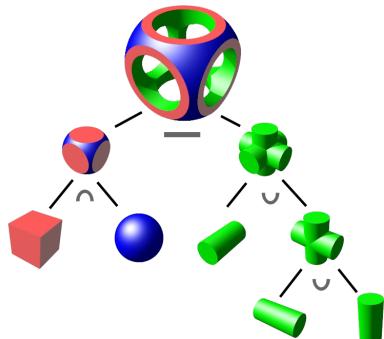
- ARKitScenes,
- ScanNet++ (with DSLR images)



# AI + Geometry: Tasks

- $P(S)$  or  $P(S|c)$  --- Generative models
  - Learning (conditional) shape priors
  - Shape generation, completion, & geometry data processing
- $P(c|S)$  --- Discriminative models
  - Learning shape descriptors
  - Shape classification, segmentation, view estimation, etc.
- Joint modeling of 3D and 2D data
  - Large-scale 2D datasets & very good pretrained models
  - Differentiable projection/back-projection & differentiable/neural rendering
- Joint modeling of multi-modal data beyond visual (e.g., text)

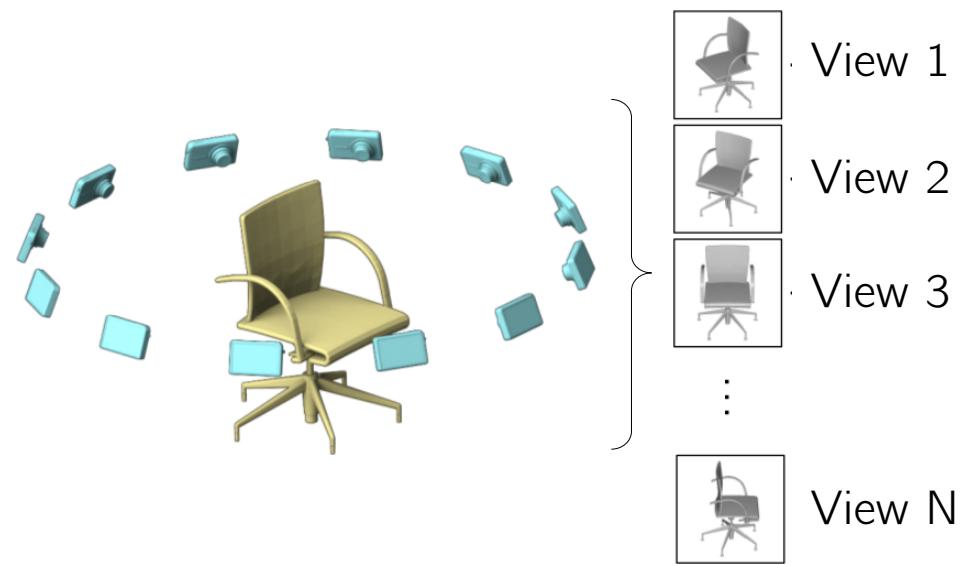
# AI + Geometry: Which Representation?

	Explicit	Implicit (Eulerian)
Non-parametric		
	Points	Voxels
Parametric		
	Splines	Subdivision Surfaces
		
		Level Sets
		
		$x^2 + y^2 + z^2 = 1$
		Algebraic Surfaces
		Constructive Solid Geometry

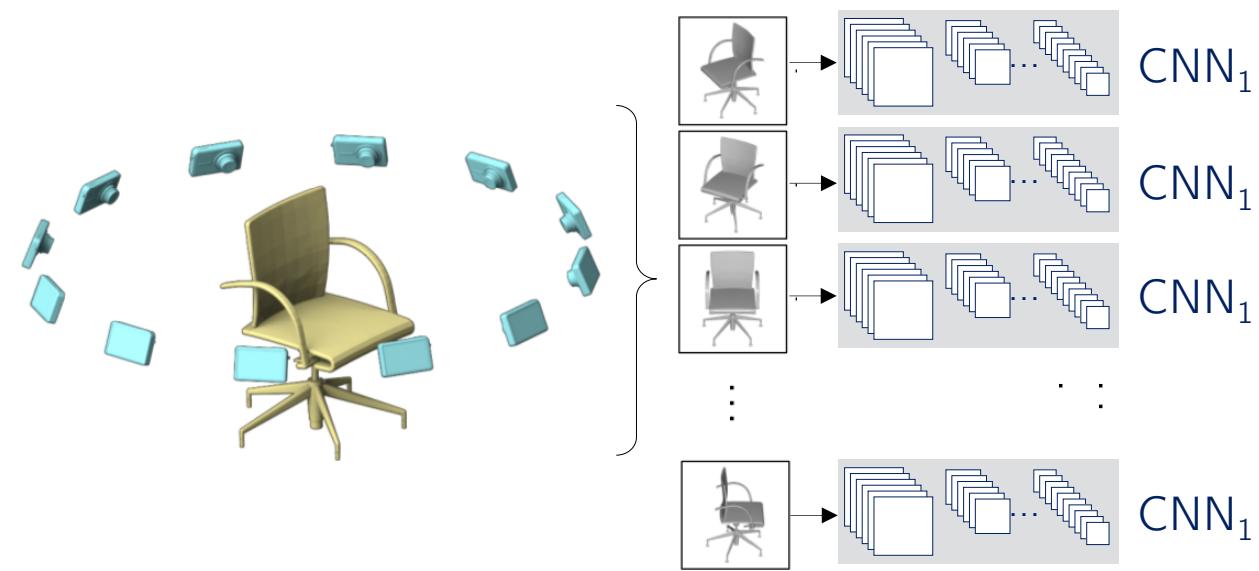
# Multi-View CNN



# Multi-View CNN

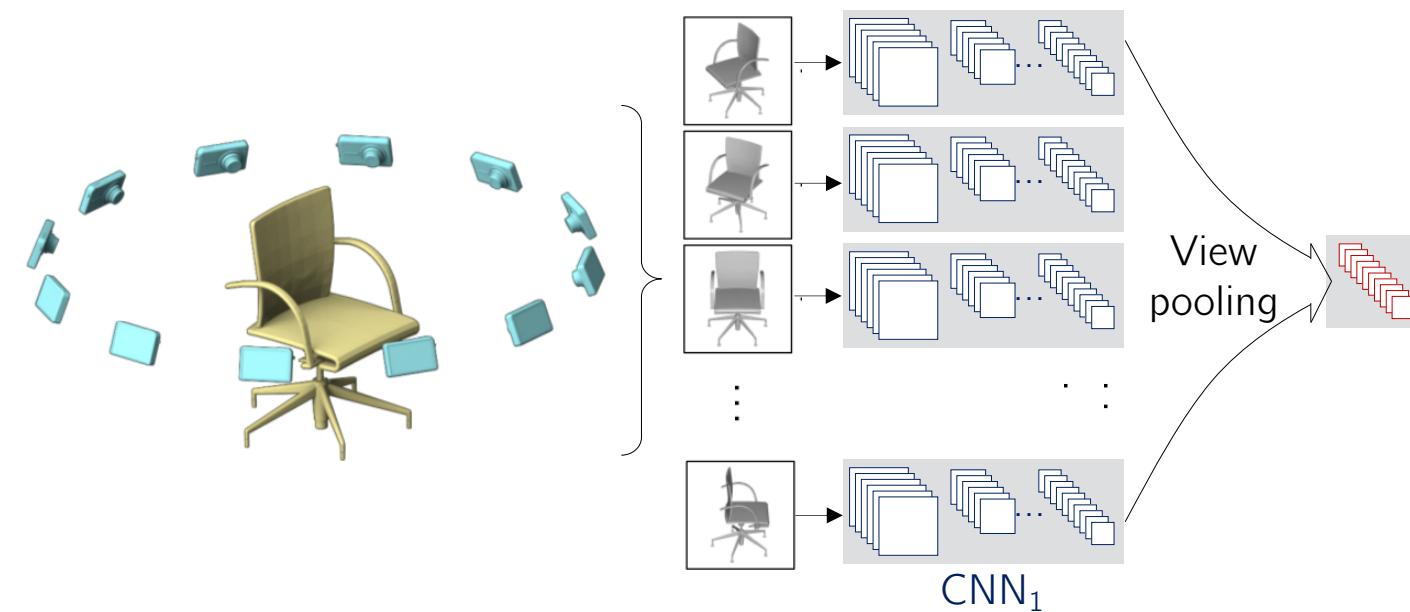


# Multi-View CNN



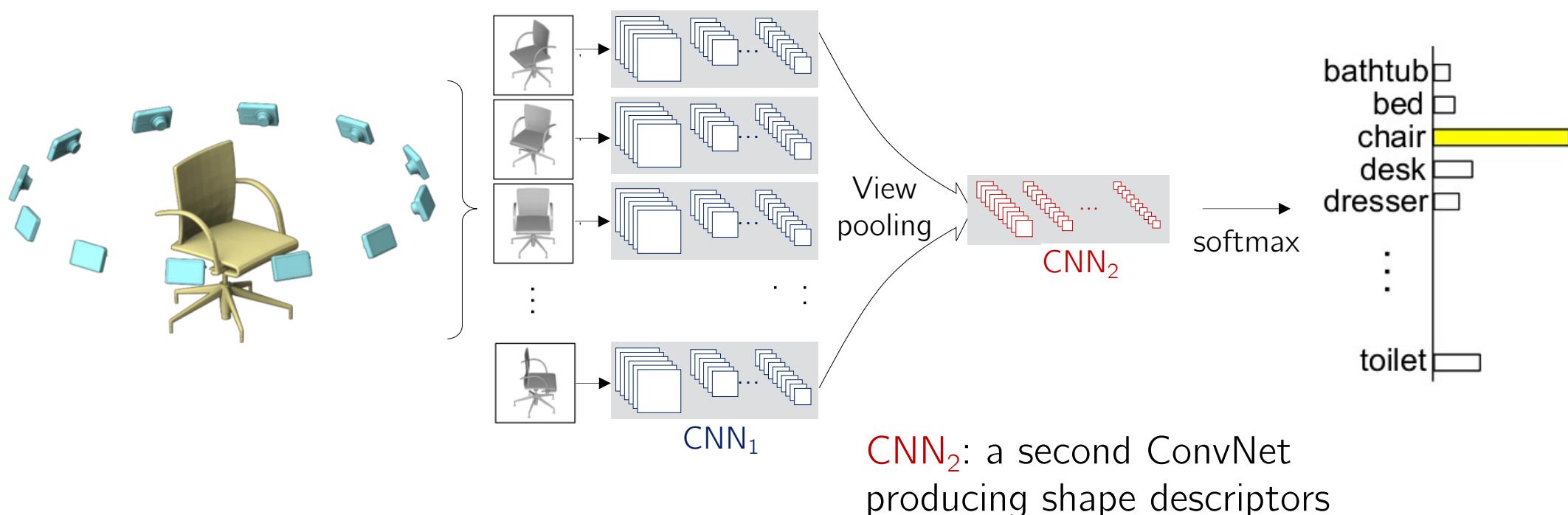
$\text{CNN}_1$ : a ConvNet extracting image features

# Multi-View CNN



View pooling: element-wise  
max-pooling across all views

# Multi-View CNN



# Experiments – Classification & Retrieval

	Method	Classification (Accuracy)	Retrieval (mAP)
Non-deep	SPH	68.2%	33.3%
	LFD	75.5%	40.9%
	3D ShapeNets	77.3%	49.2%
	FV, 12 views	84.8%	43.9%
	CNN, 12 views	88.6%	62.8%
	MVCNN, 12 views	<b>89.9%</b>	70.1%
	MVCNN+metric, 12 views	89.5%	<b>80.2%</b>
	MVCNN, 80 views	90.1%	70.4%
	MVCNN+metric, 80 views	<b>90.1%</b>	<b>79.5%</b>

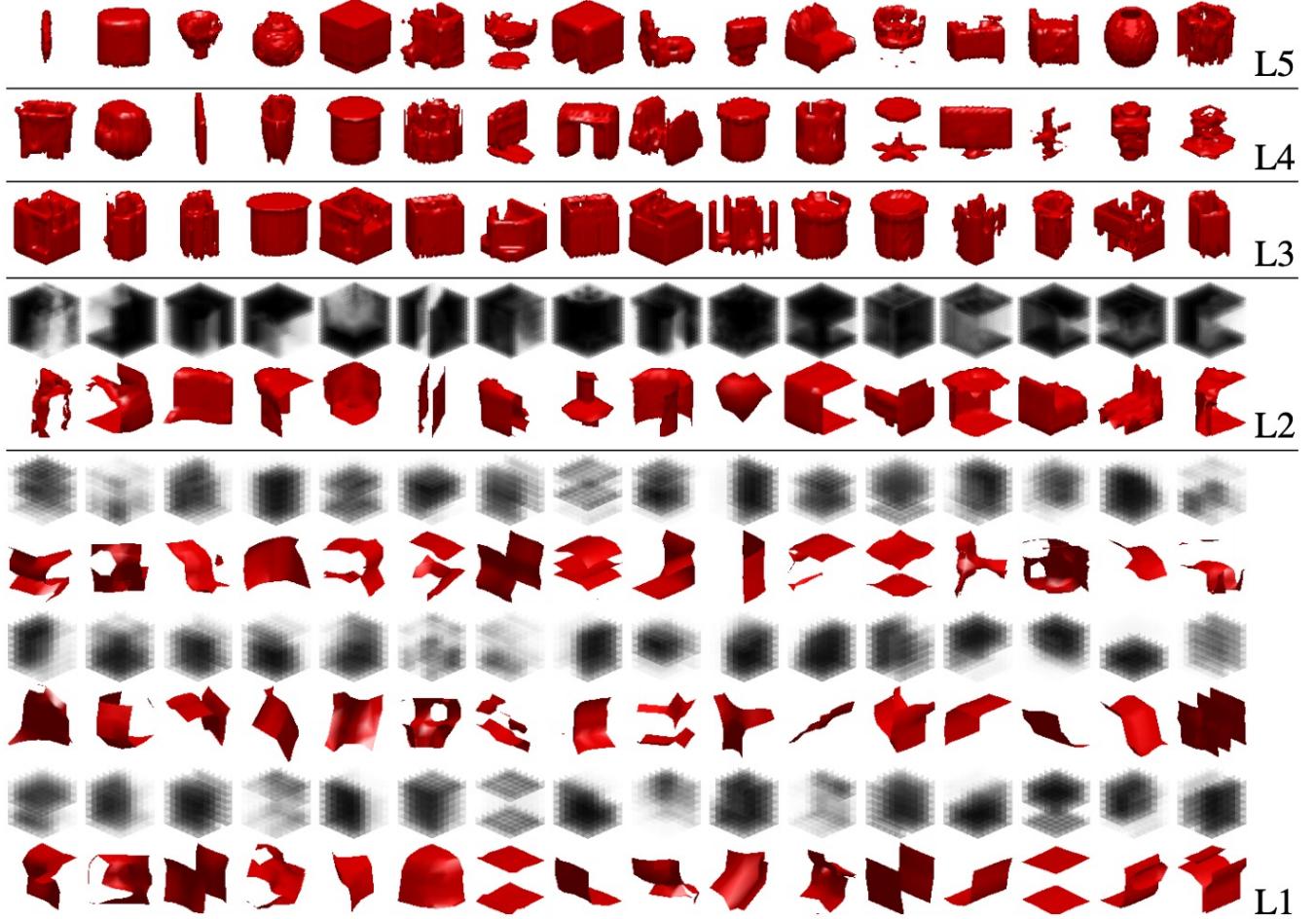
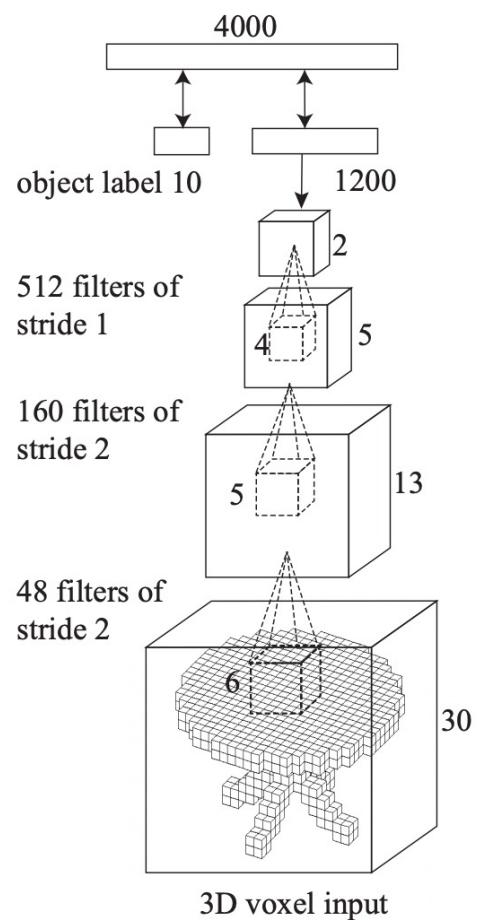
On ModelNet 40

# Multi-View Representations

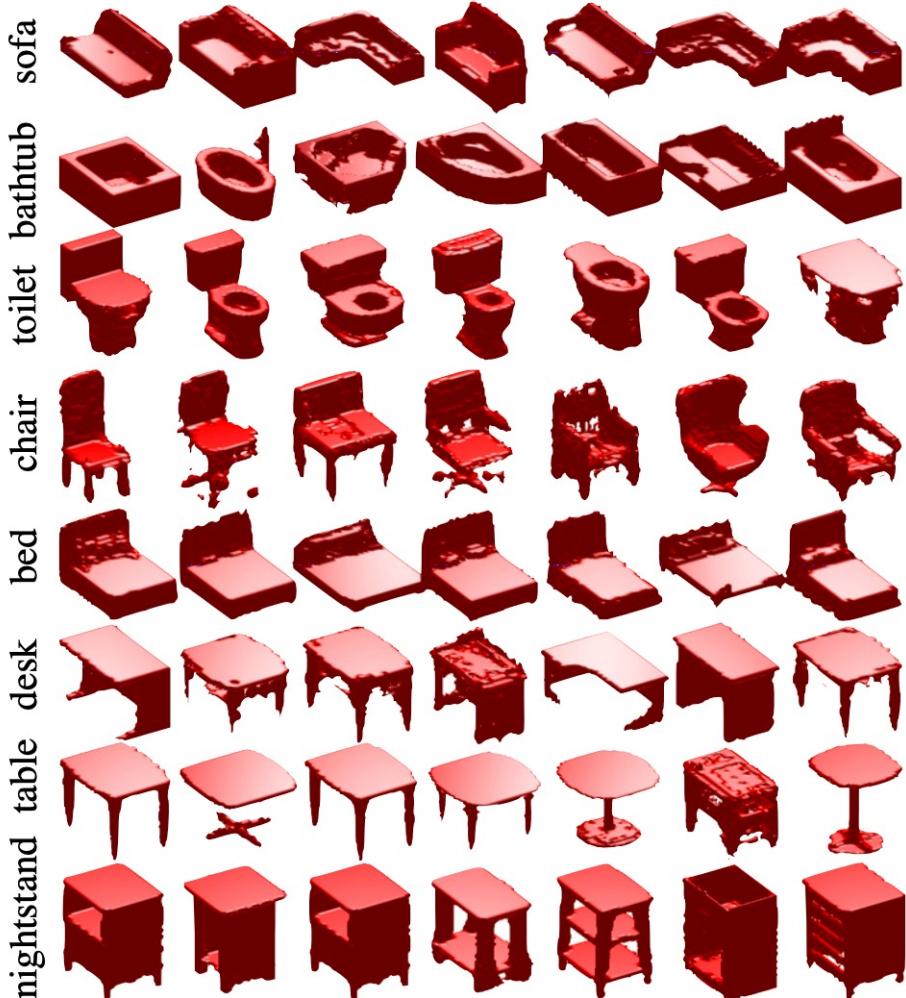
- Indeed gives good performance
- Can leverage vast literature of image classification
- Can use pretrained features
  
- Need projection
- What if the input is noisy and/or incomplete? e.g., point cloud

# Pixels -> Voxels

- 3D Conv Deep Belief Networks (CDBN)



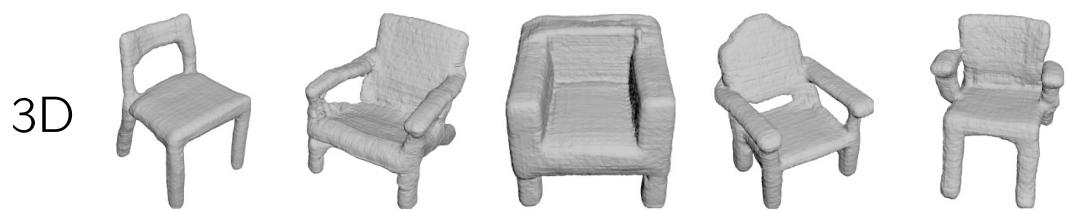
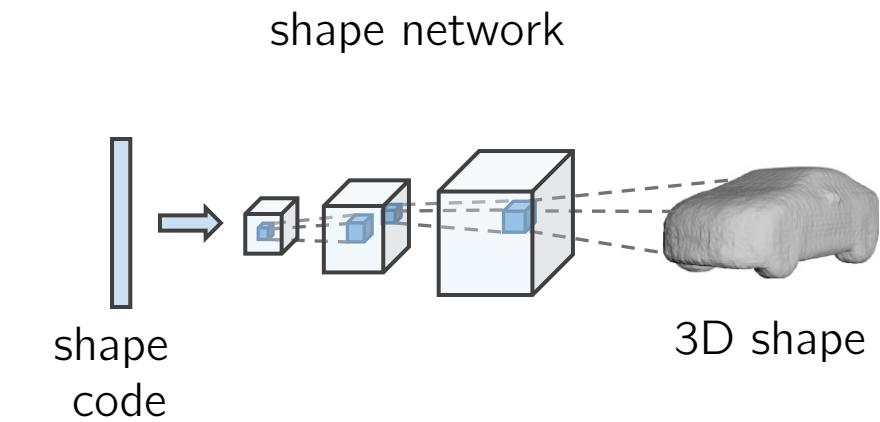
# Generative Modeling



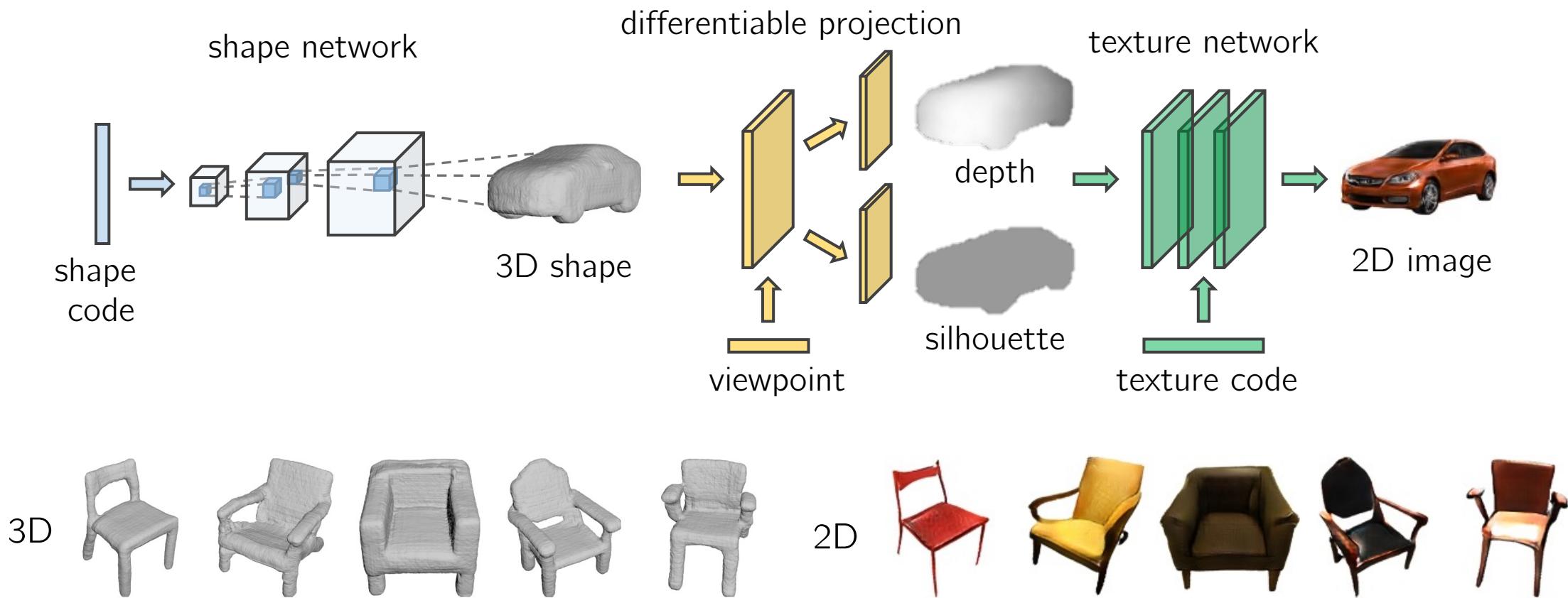
	10 classes	SPH [18]	LFD [8]	Ours
classification	79.79 %	79.87 %	83.54%	
retrieval AUC	45.97%	51.70%	69.28%	
retrieval MAP	44.05%	49.82%	68.26%	
	40 classes	SPH [18]	LFD [8]	Ours
classification	68.23%	75.47%	77.32%	
retrieval AUC	34.47%	42.04%	49.94%	
retrieval MAP	33.26%	40.91%	49.23%	

Table 1: Shape Classification and Retrieval Results.

# 3D-GANs



# Visual Object Networks (Geometry + Rendering)



Editing viewpoint, shape, and texture

viewpoint



shape



texture



viewpoint



shape



texture



Interpolation in the latent space

shape



texture



both



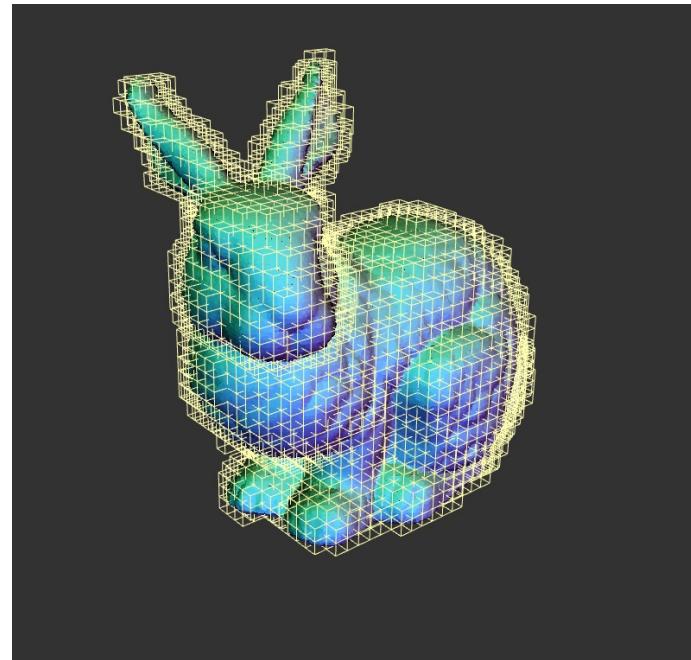
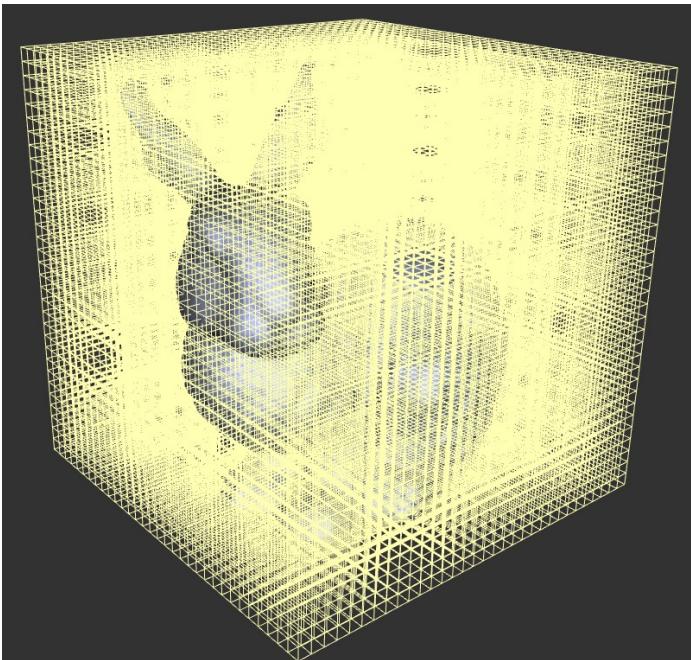
Transferring shape and texture

shape  
image

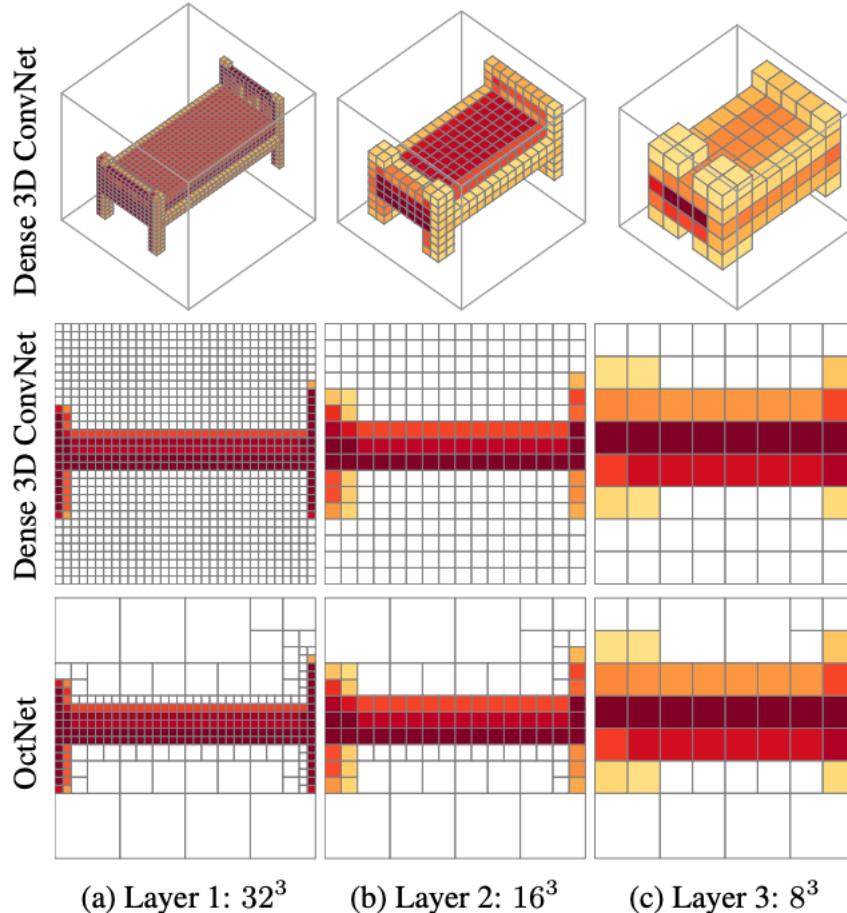


# Octave Tree Representations

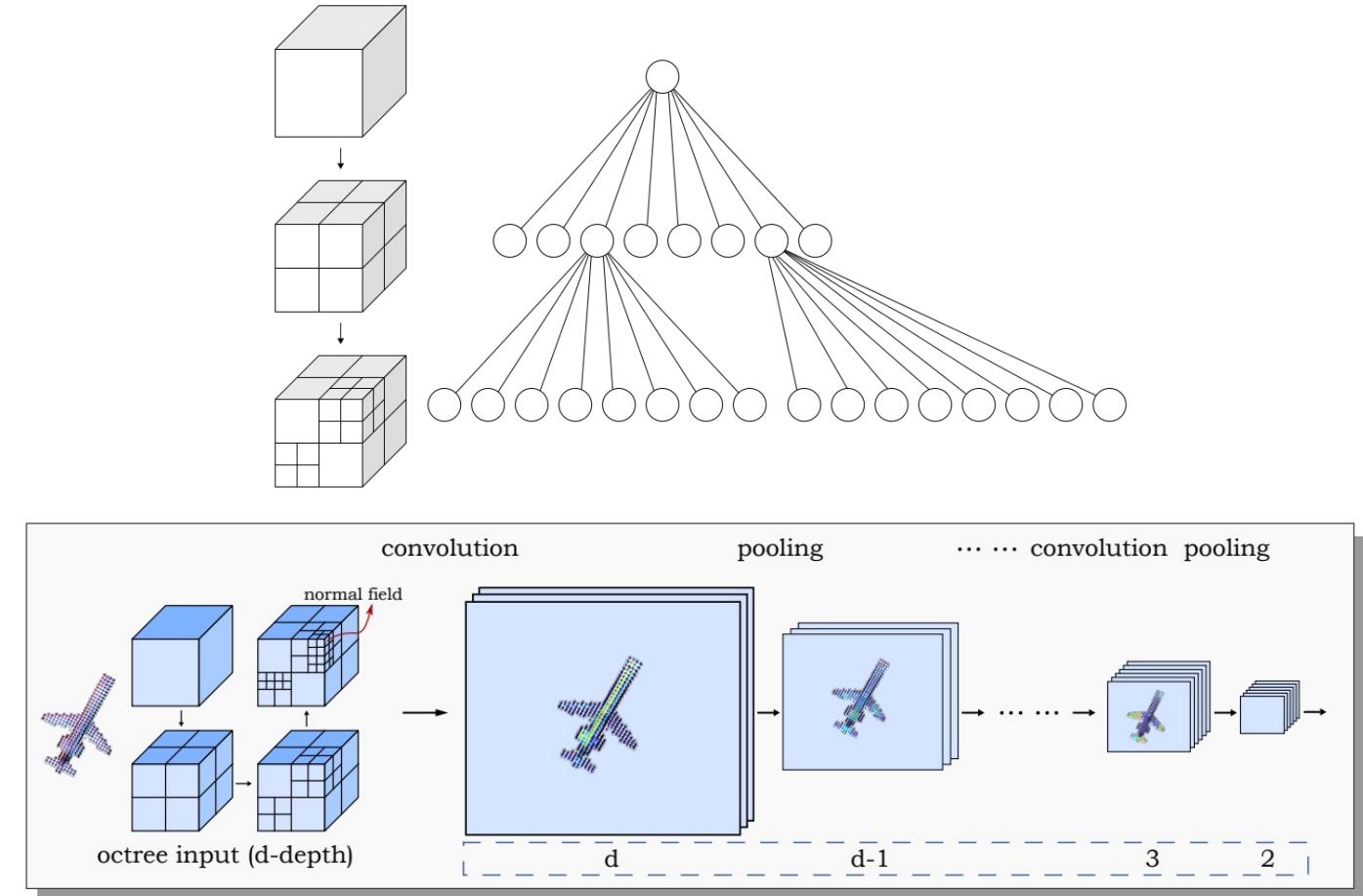
- Store the sparse surface signals
- Constrain the computation near the surface



# Octree: Recursively Partition the Space

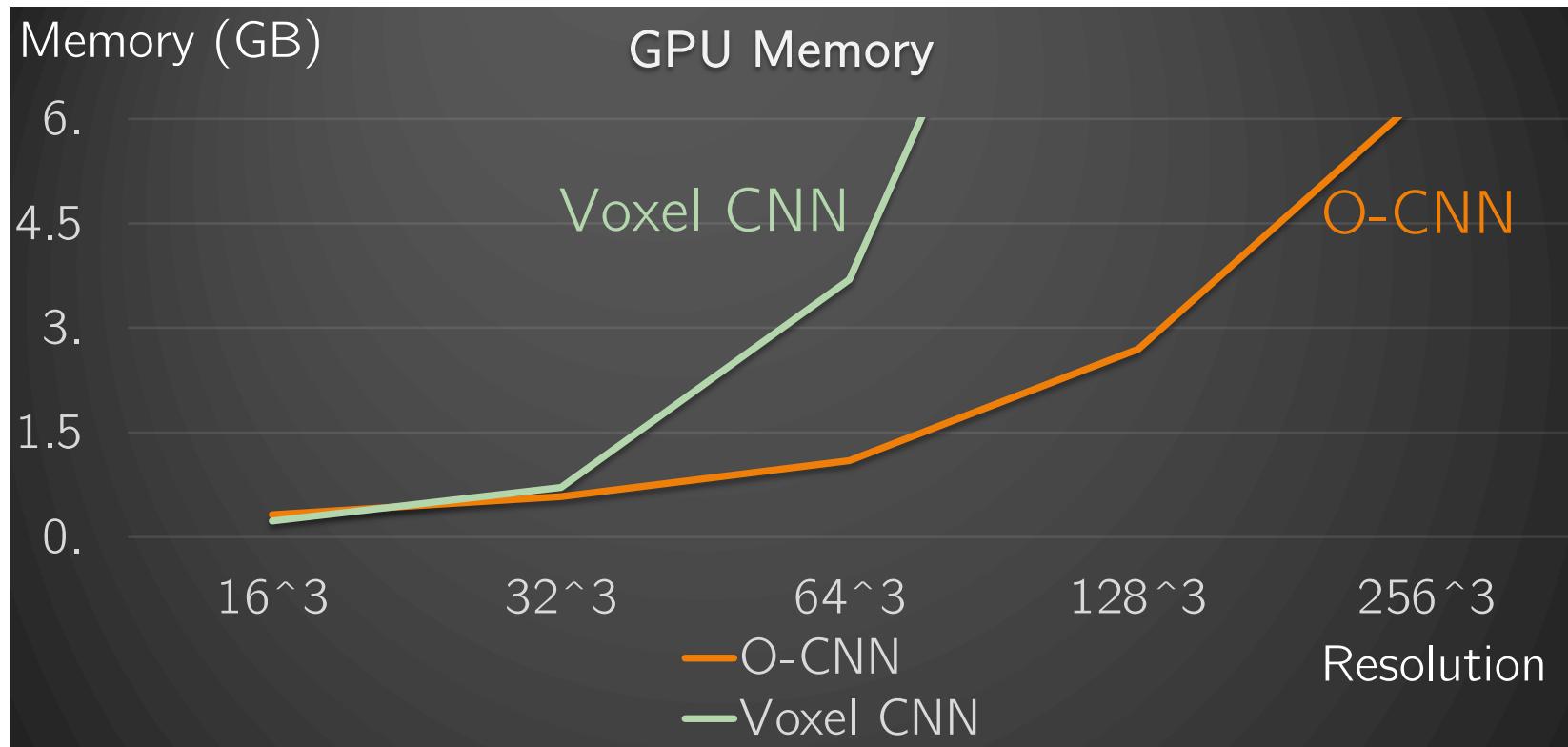


Riegler et al. OctNet. CVPR 2017



Wang et al. O-CNN. SIGGRAPH 2017

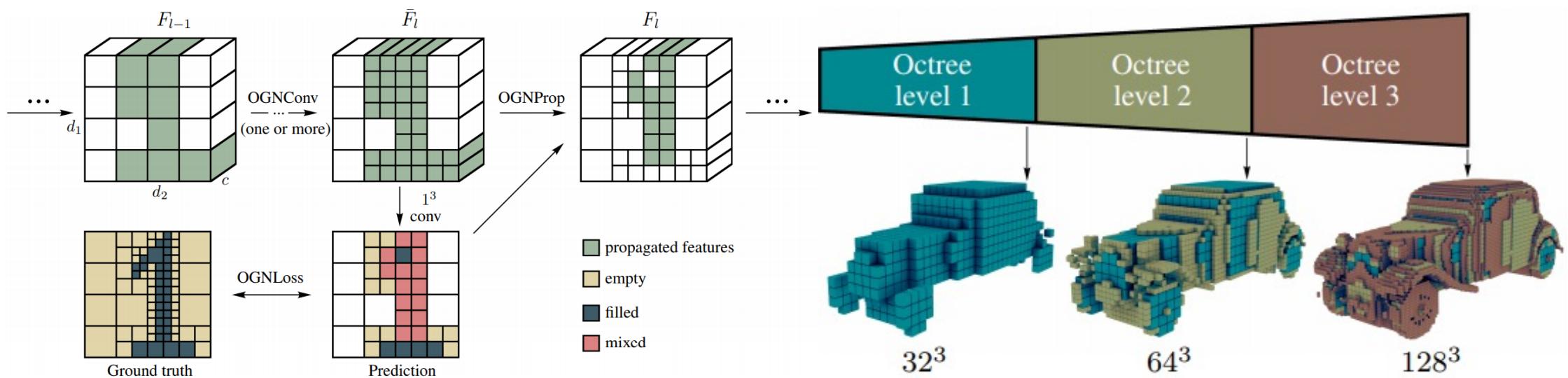
# Memory Efficiency



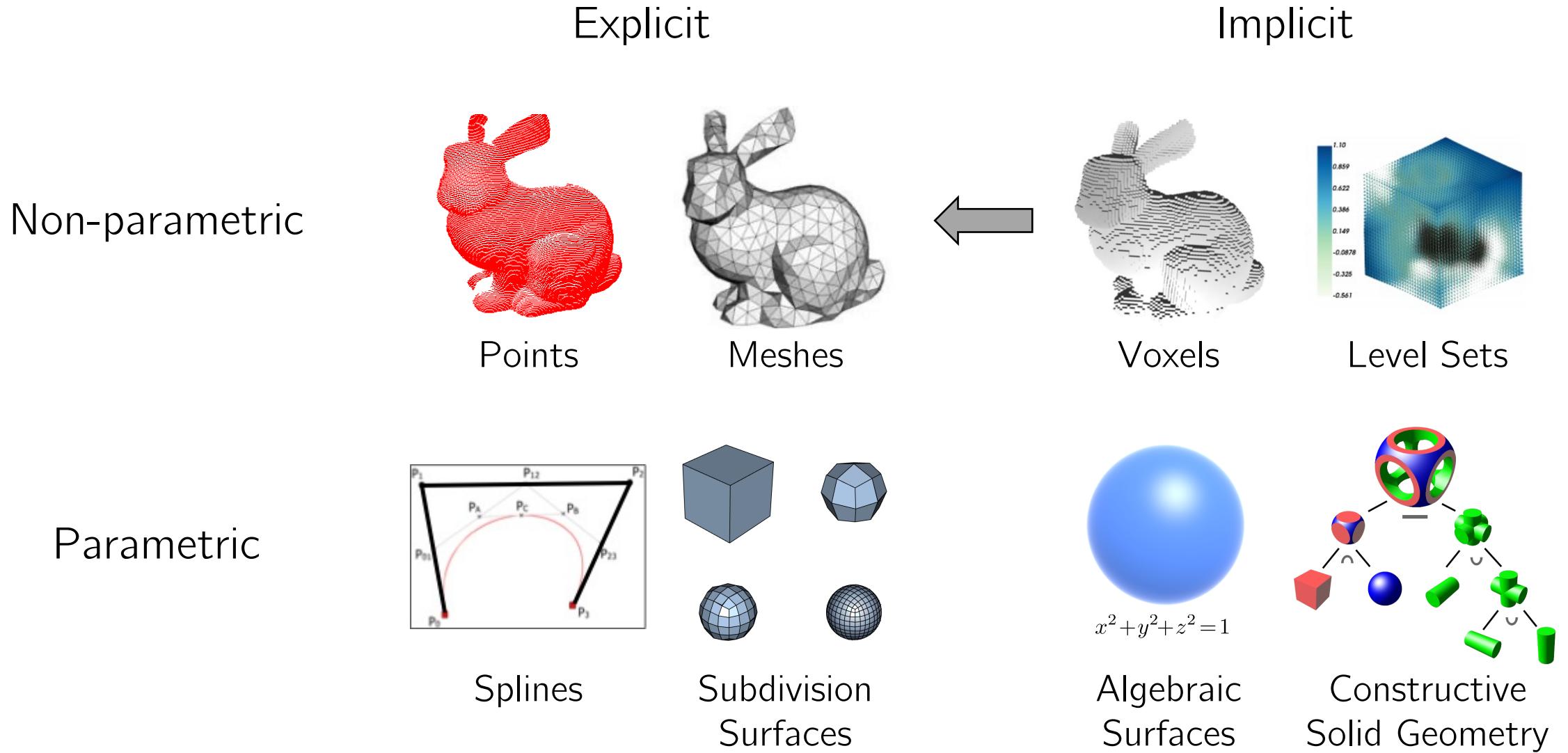
# Octree Generating Networks

Avoid  $\mathcal{O}(n^3)$  reconstruction

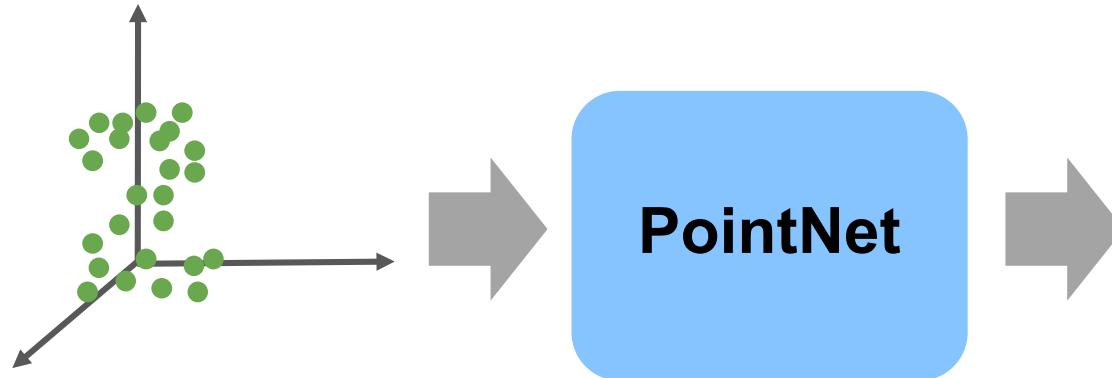
- Octree representation of shapes
- Generate the octree layer by layer



# Eulerian -> Lagrangian

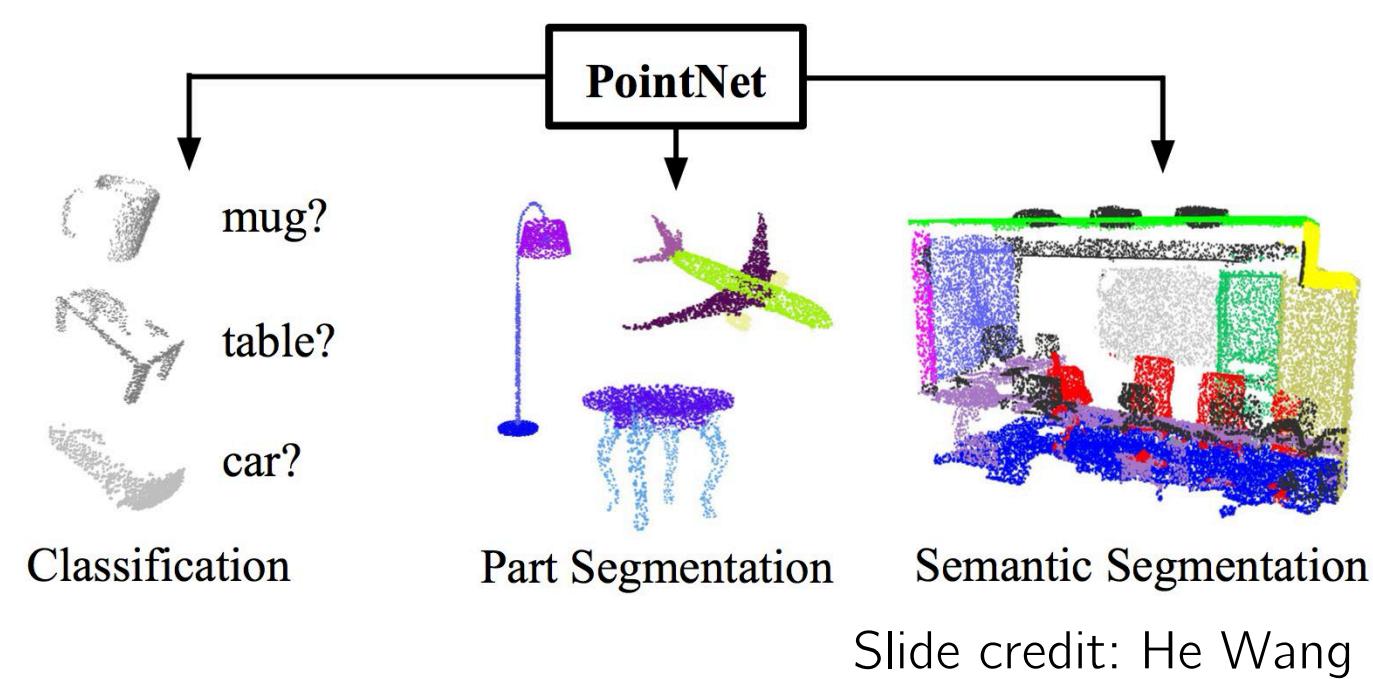


# PointNet: Learning on Point Clouds



**End-to-end learning for irregular point data**

**Unified framework for various tasks**



Charles R. Qi, Hao Su, Kaichun Mo, Leonidas J. Guibas.  
PointNet: Deep Learning on Point Sets for 3D  
Classification and Segmentation. (CVPR'17)

Slide credit: He Wang

# Invariances

*The model has to respect key desiderata for point clouds:*

## **Point Permutation Invariance**

Point cloud is a set of **unordered** points

## **Sampling Invariance**

Output a function of the underlying geometry and **not the sampling**

# Permutation Invariance: Symmetric Functions

$$f(x_1, x_2, \dots, x_n) \equiv f(x_{\pi_1}, x_{\pi_2}, \dots, x_{\pi_n}), \quad x_i \in \mathbb{R}^D$$

Examples:

$$f(x_1, x_2, \dots, x_n) = \max\{x_1, x_2, \dots, x_n\}$$

$$f(x_1, x_2, \dots, x_n) = x_1 + x_2 + \dots + x_n$$

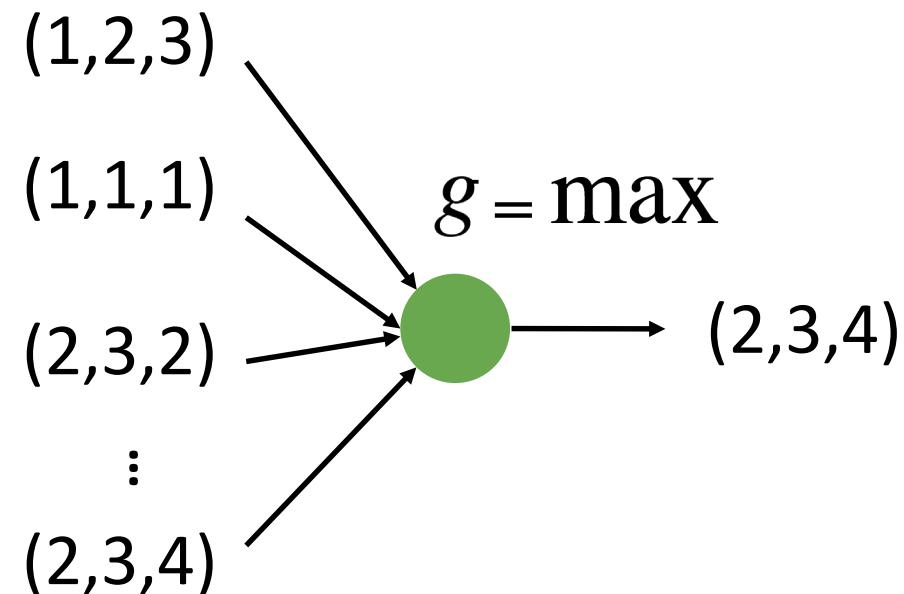
...

**How can we construct a universal family of symmetric functions by neural networks?**

# Construct Symmetric Functions by NNs

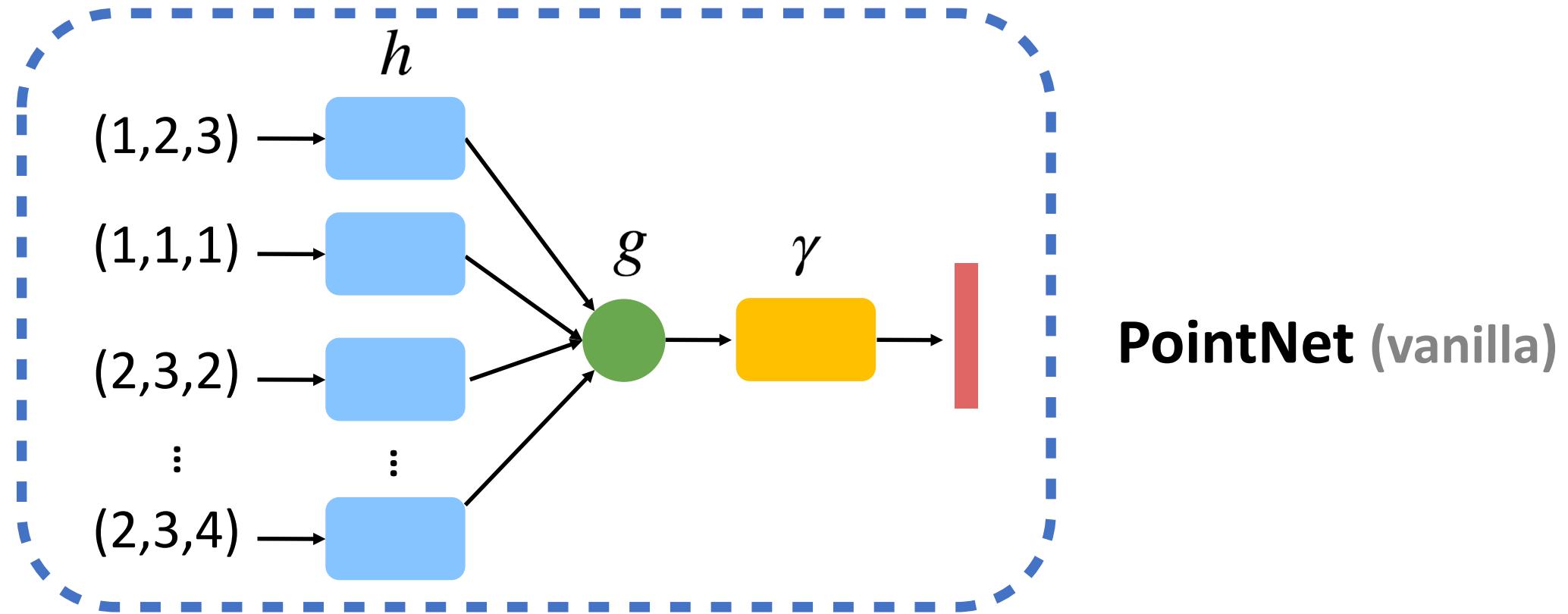
Simplest form: directly aggregate all points with a symmetric operator

**Just discovers simple extreme/aggregate properties of the geometry.**



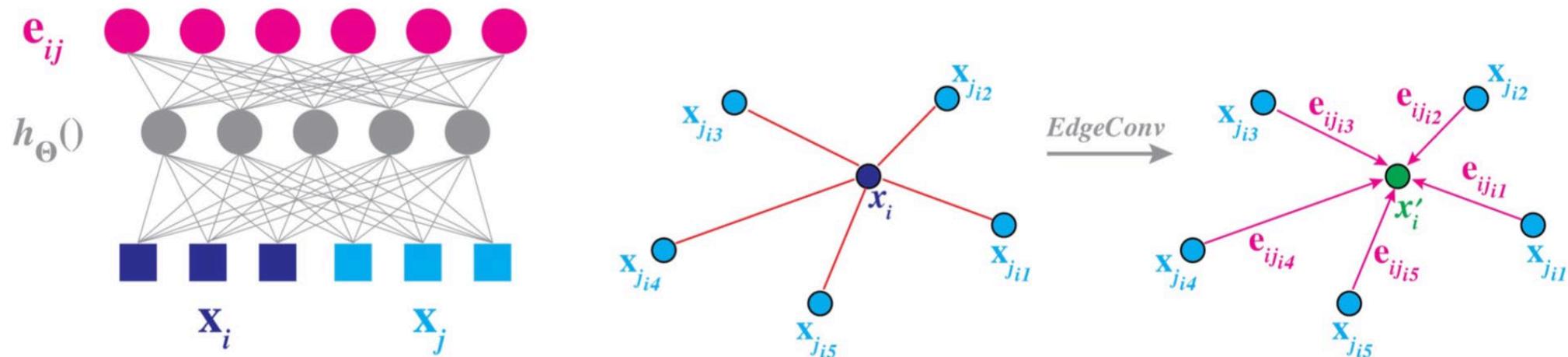
# Construct Symmetric Functions by NNs

$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric



# Graph NNs on Point Clouds

- Points -> Nodes
- Neighborhood -> Edges
- Graph NNs for point cloud processing



# Distance Metrics for Point Clouds

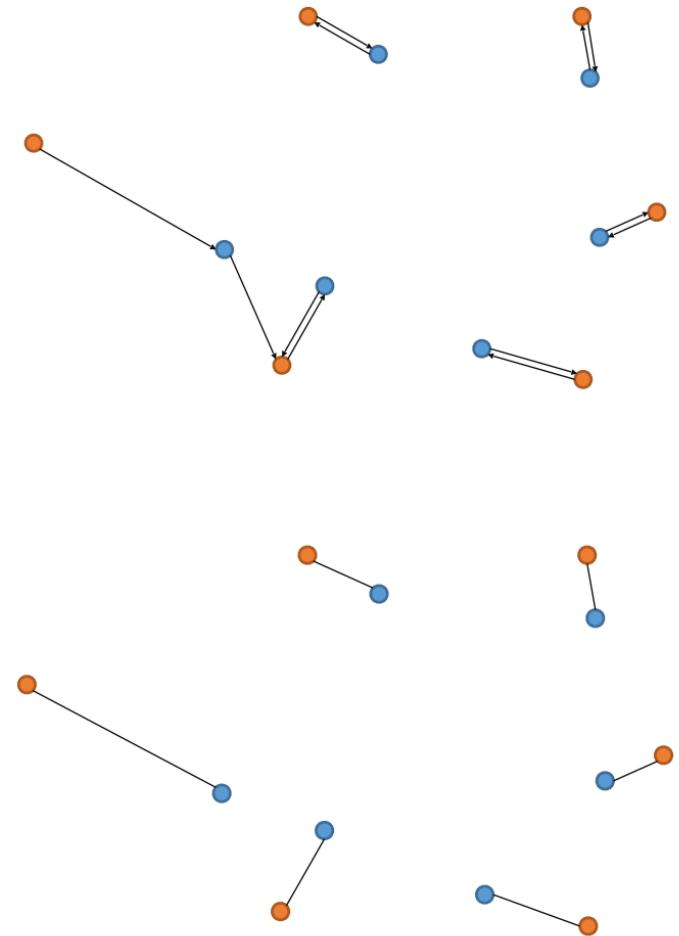
**Chamfer distance** We define the Chamfer distance between  $S_1, S_2 \subseteq \mathbb{R}^3$  as:

$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2 + \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2$$

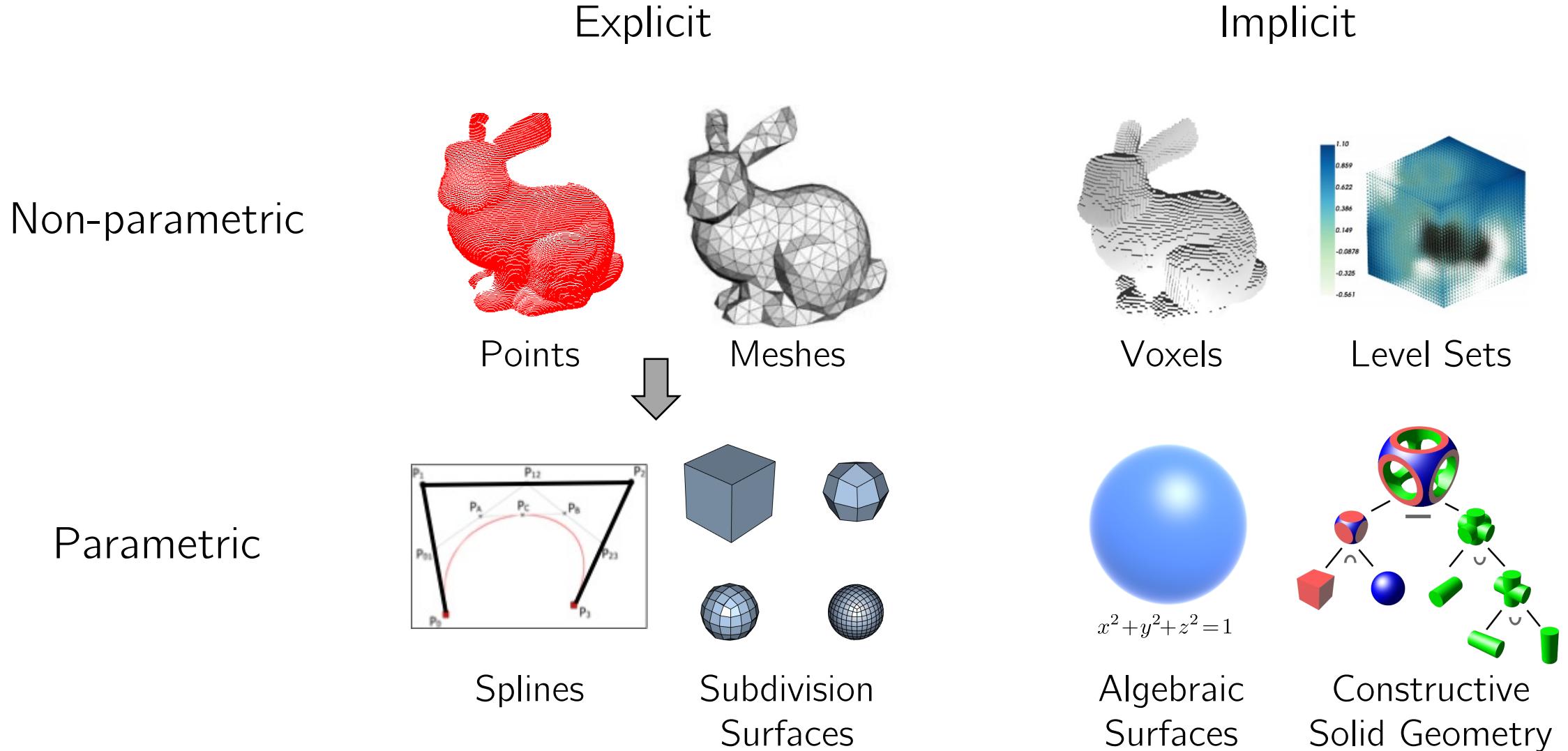
**Earth Mover's distance** Consider  $S_1, S_2 \subseteq \mathbb{R}^3$  of equal size  $s = |S_1| = |S_2|$ . The EMD between  $A$  and  $B$  is defined as:

$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \rightarrow S_2} \sum_{x \in S_1} \|x - \phi(x)\|_2$$

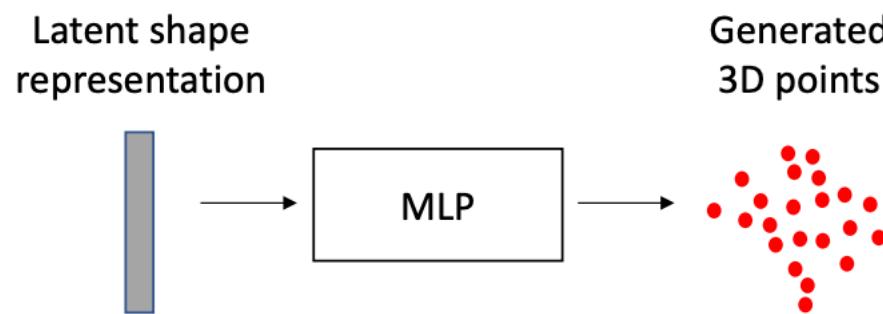
where  $\phi : S_1 \rightarrow S_2$  is a bijection.



# Non-Parametric $\rightarrow$ Parametric

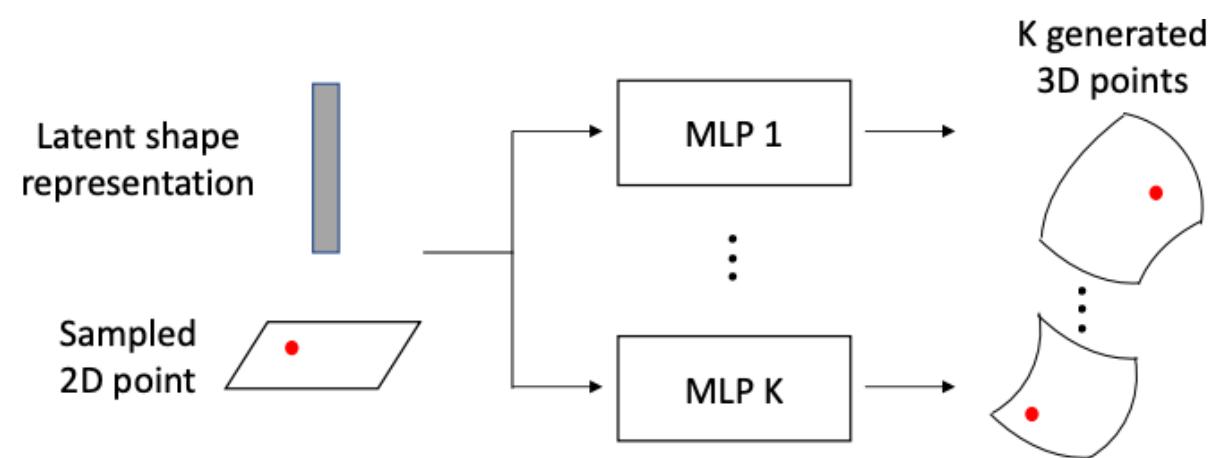
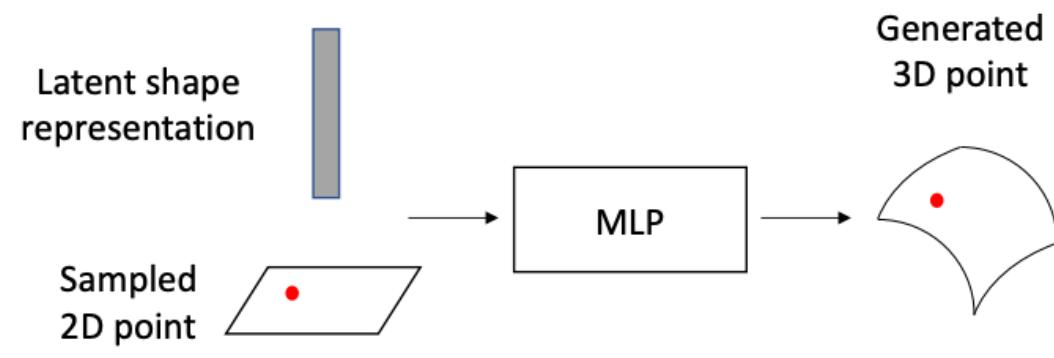


# Parametric Decoder: AtlasNet



Given the output points form a smooth surface, enforce such a parametrization as input.

$$\text{MLP}(z, u, v) \rightarrow \text{point}$$

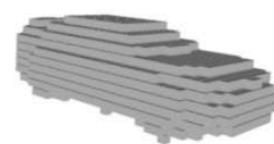
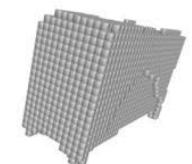
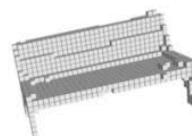


# Results

Input image



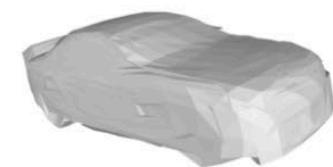
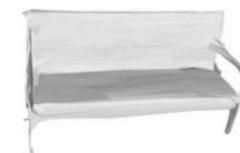
Voxel



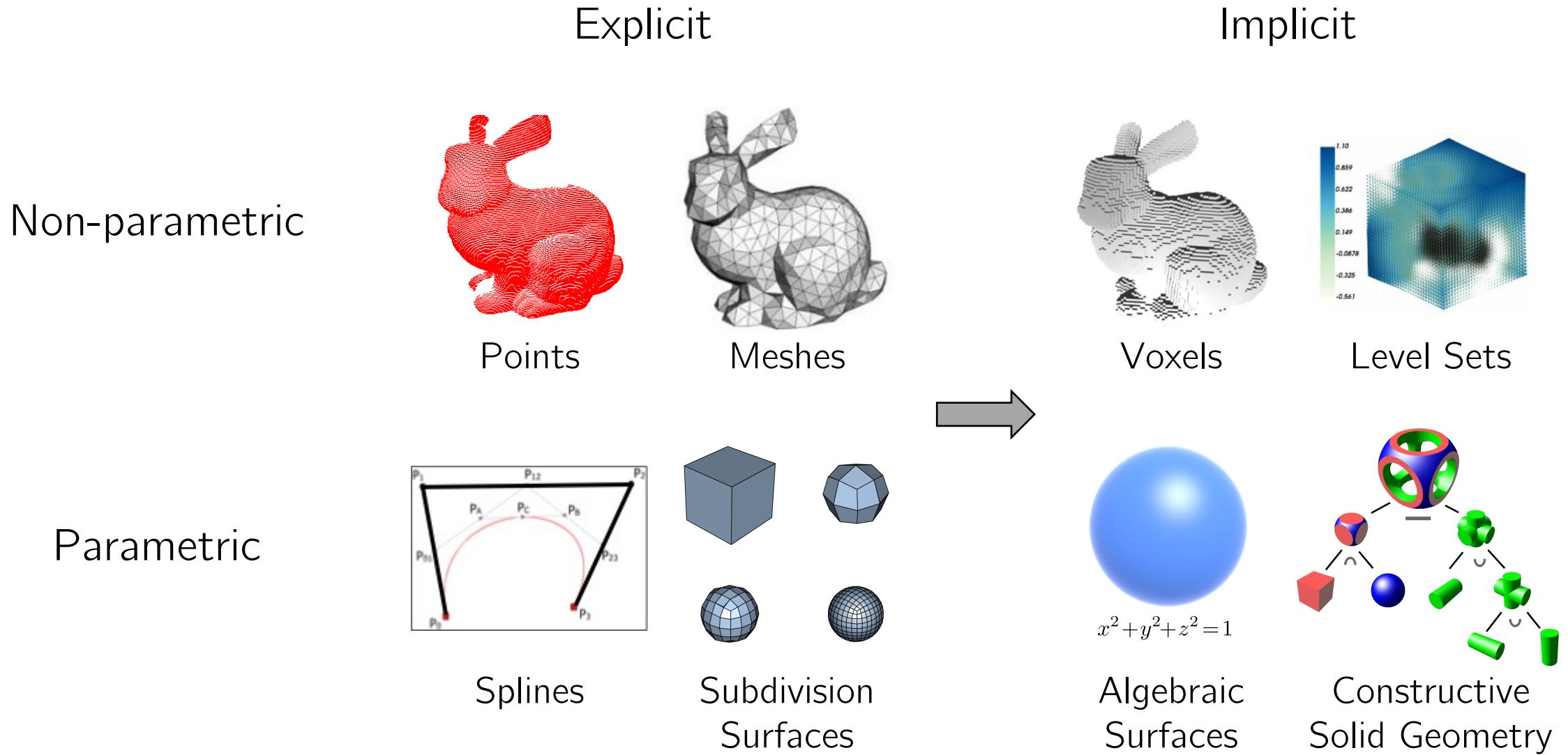
Point cloud



AtlasNet



# Explicit -> Implicit

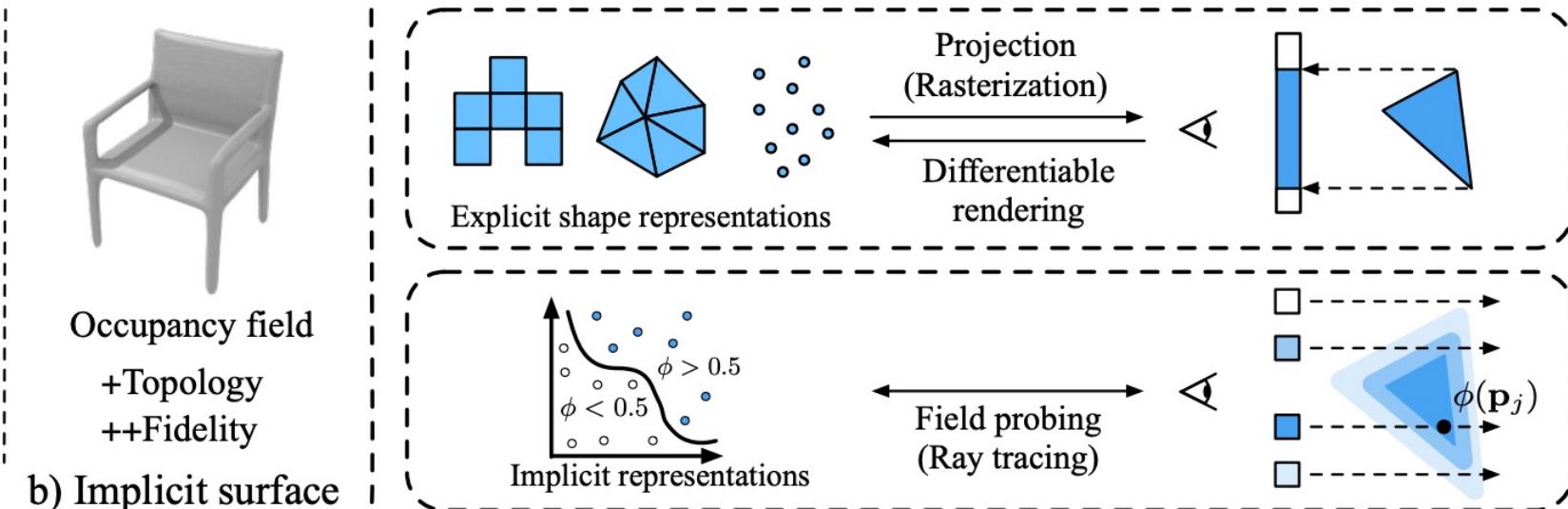


# Deep Implicit Functions



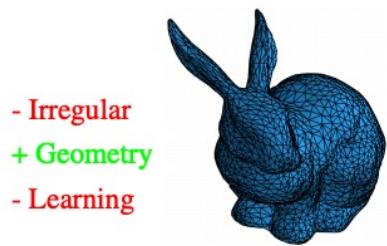
Voxel  
+Topology  
-Fidelity  
Point cloud  
+Topology  
-Fidelity  
Mesh  
-Topology  
+Fidelity

a) Explicit representation

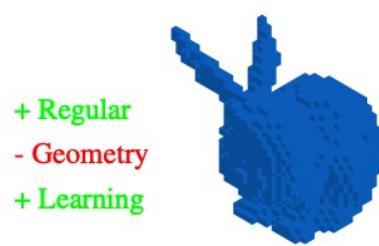


b) Implicit surface

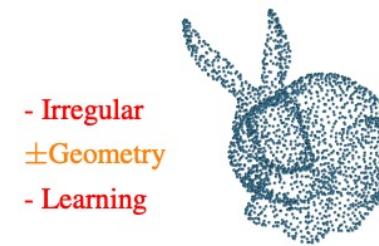
Liu et al. Learning to Infer Implicit Surfaces without 3D Supervision. NeurIPS 2019



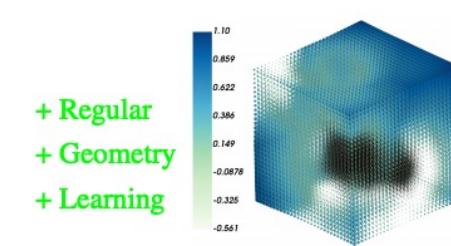
(a) Explicit representations



(b) Voxels



(c) Point cloud



(d) Level set

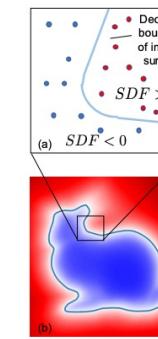
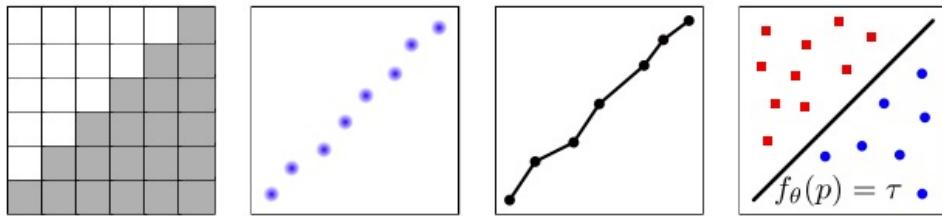


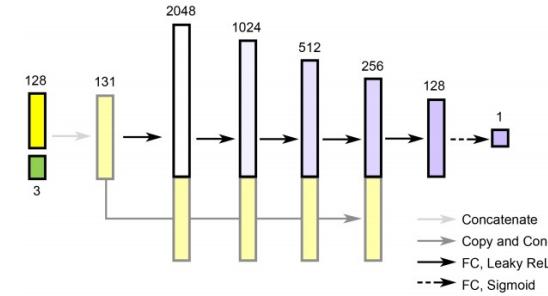
Figure 2. Four common representations of 3D shape along with their advantages and disadvantages.

Deep Level Sets: Implicit Surface Representations for 3D Shape Inference. 2019

DeepSDF. CVPR 2019



Occupancy Networks  
CVPR 2019



Chen and Zhang.  
Learning Implicit Fields  
CVPR 2019



(a) Voxel      (b) Point      (c) Mesh      (d) Ours

	Voxel
	Point cloud
	Mesh

	+Topology
	-Fidelity

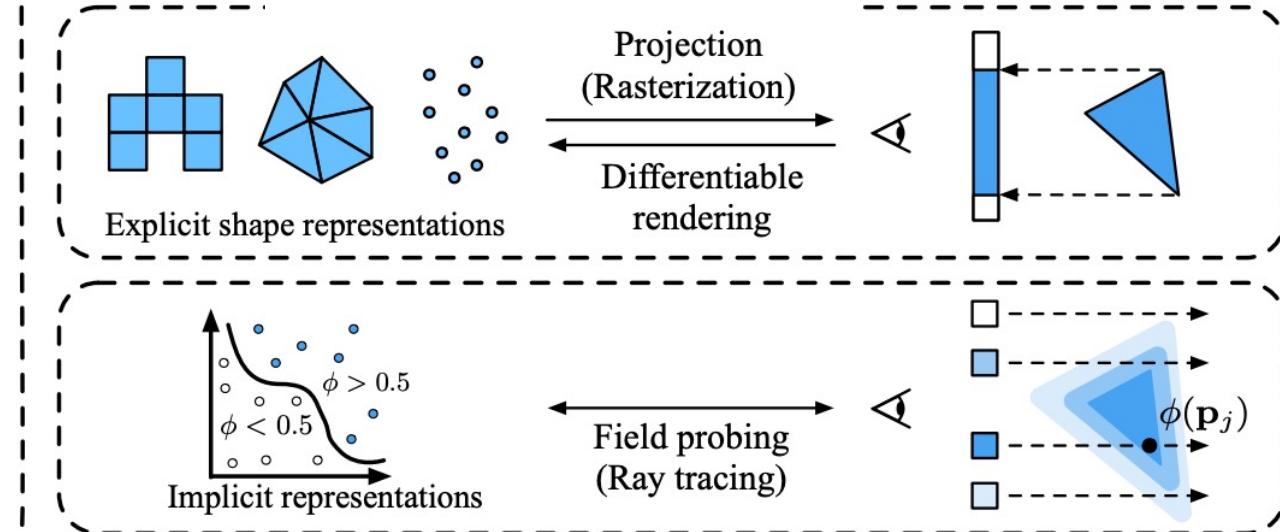
  

	+Topology
	-Fidelity

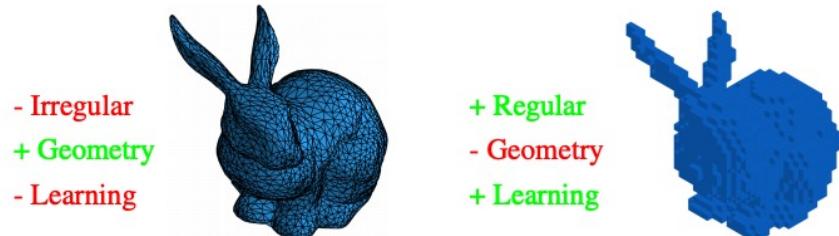
a) Explicit representation

Occupancy field  
+Topology  
++Fidelity

b) Implicit surface



Liu et al. Learning to Infer Implicit Surfaces without 3D Supervision. NeurIPS 2019



(a) Explicit representations

(b) Voxels

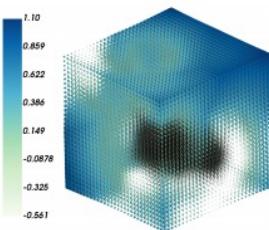
(c) Point cloud

- Irregular  
+ Geometry  
- Learning

+ Regular  
- Geometry  
+ Learning

- Irregular  
± Geometry  
- Learning

+ Regular  
+ Geometry  
+ Learning



(d) Level set

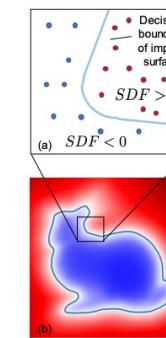


Figure 2. Four common representations of 3D shape along with their advantages and disadvantages.

Deep Level Sets: Implicit Surface Representations for 3D Shape Inference. 2019

DeepSDF. CVPR 2019

# Collection of Implicit Functions

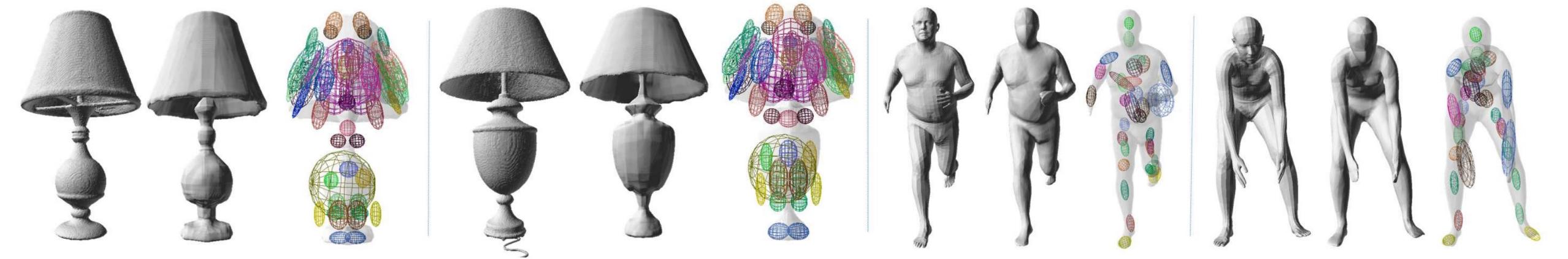
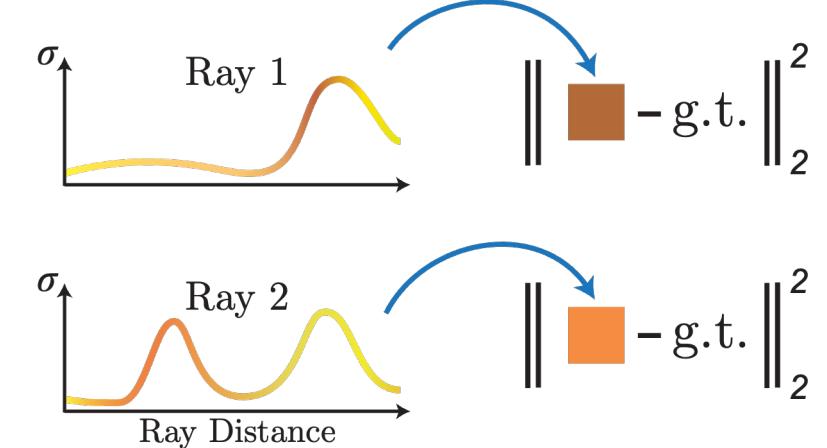
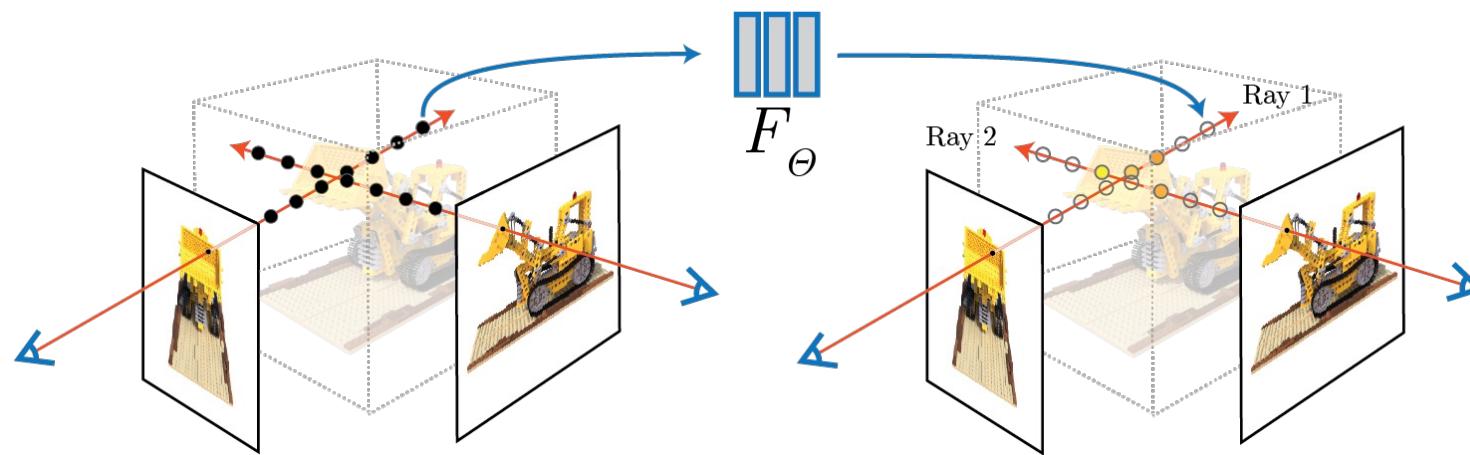
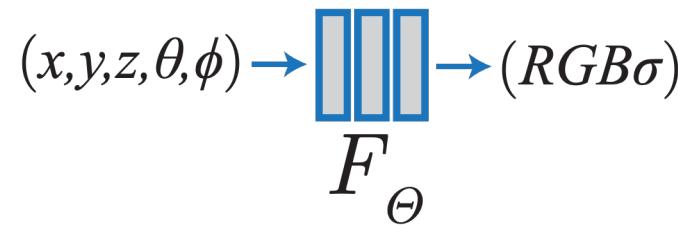


Figure 1. This paper introduces Local Deep Implicit Functions, a 3D shape representation that decomposes an input shape (mesh on left in every triplet) into a structured set of shape elements (colored ellipses on right) whose contributions to an implicit surface reconstruction (middle) are represented by latent vectors decoded by a deep network. Project video and website at [ldif.cs.princeton.edu](http://ldif.cs.princeton.edu).

# Implicit Functions for Geometry + Rendering



# Volume rendering is trivially differentiable.

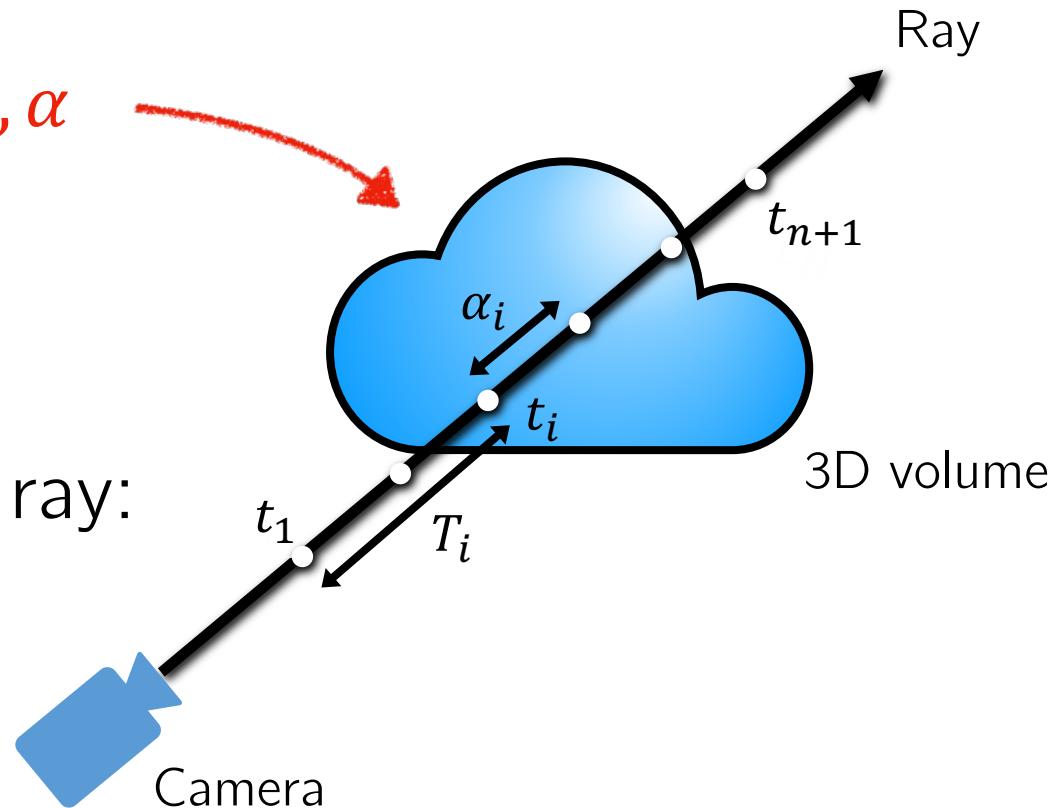
Rendering model for ray  $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$ :

$$\mathbf{c} \approx \sum_{i=1}^n T_i \alpha_i \mathbf{c}_i$$

weights

colors

differentiable w.r.t.  $\mathbf{c}, \alpha$



How much light is blocked earlier along ray:

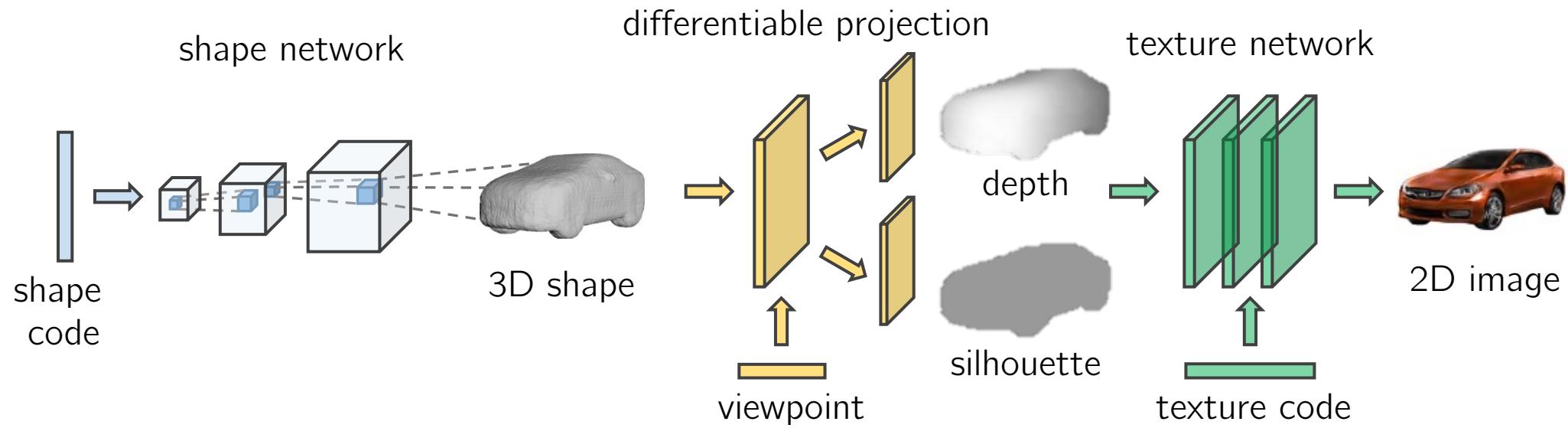
$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$

How much light is contributed by ray segment  $i$ :  $\alpha_i$

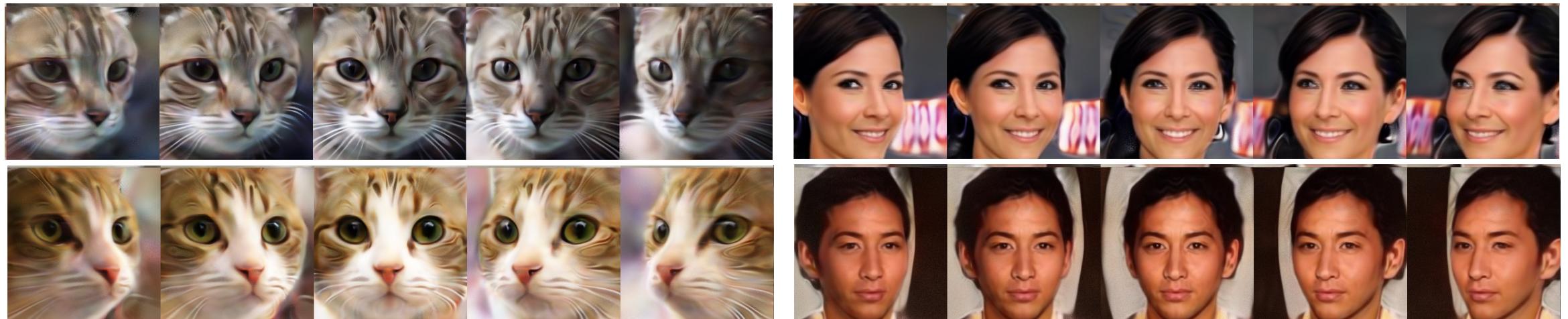
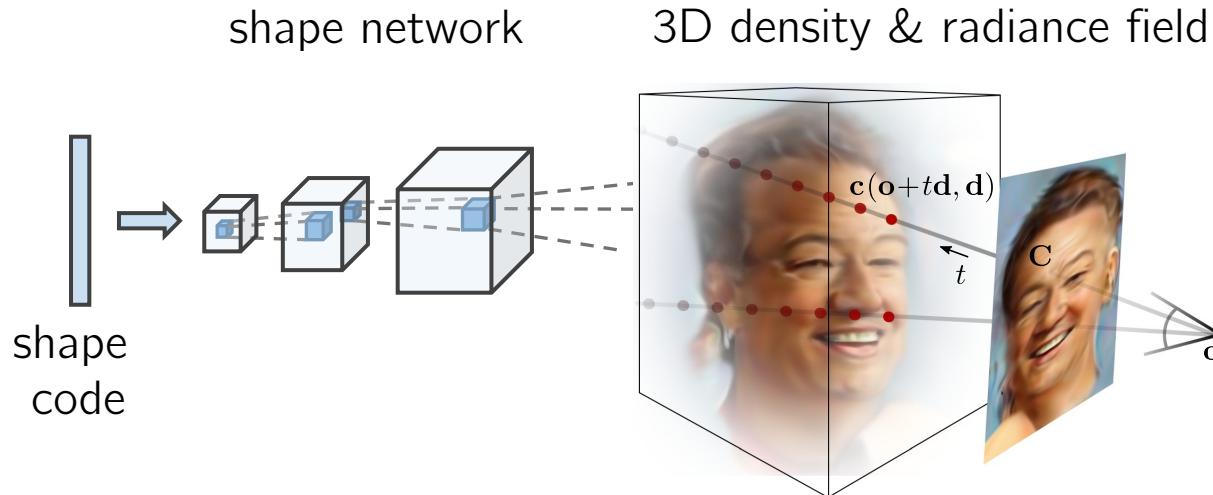
# Reconstruction & Novel View Synthesis with NeRF



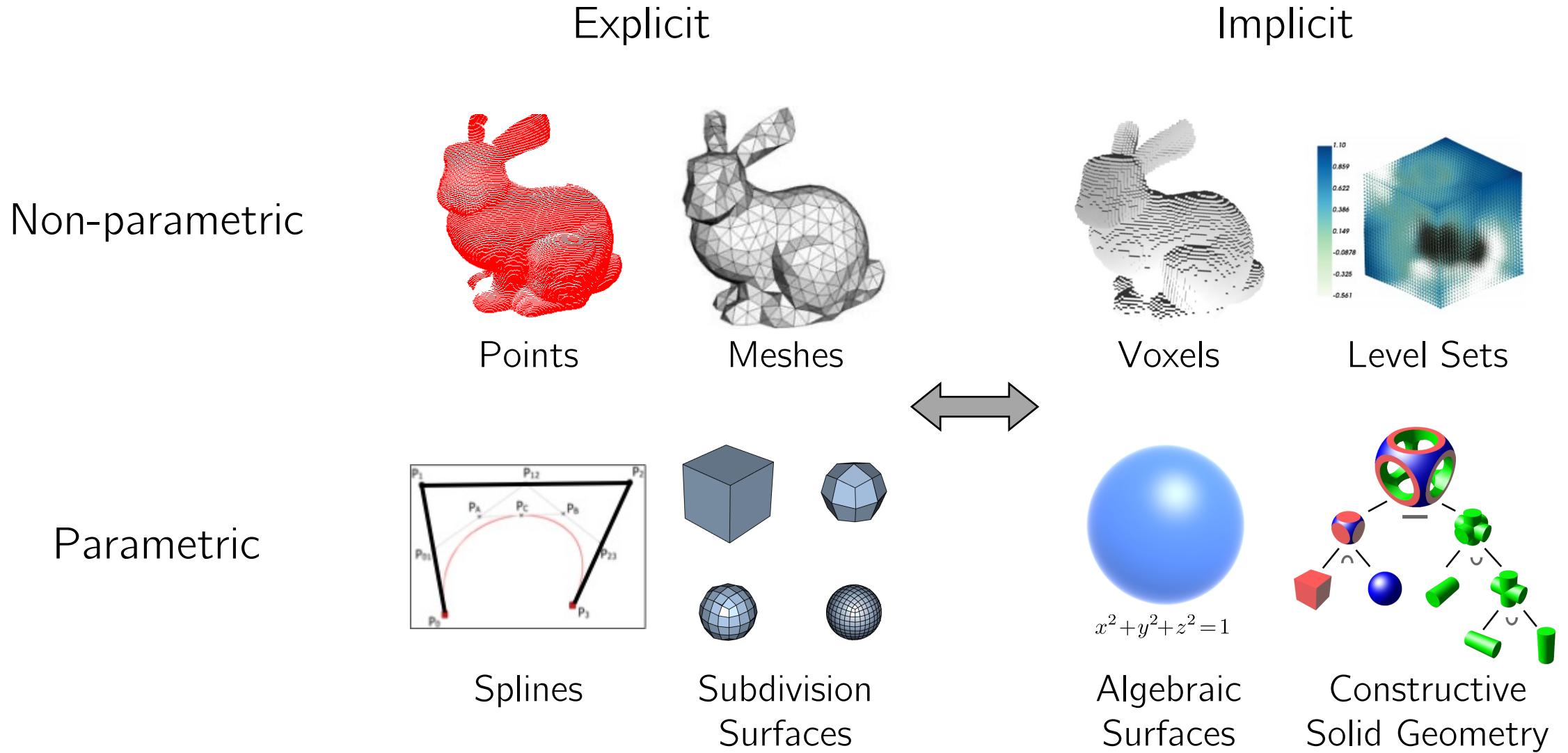
# Generative Modeling with Implicit Geometry + Rendering



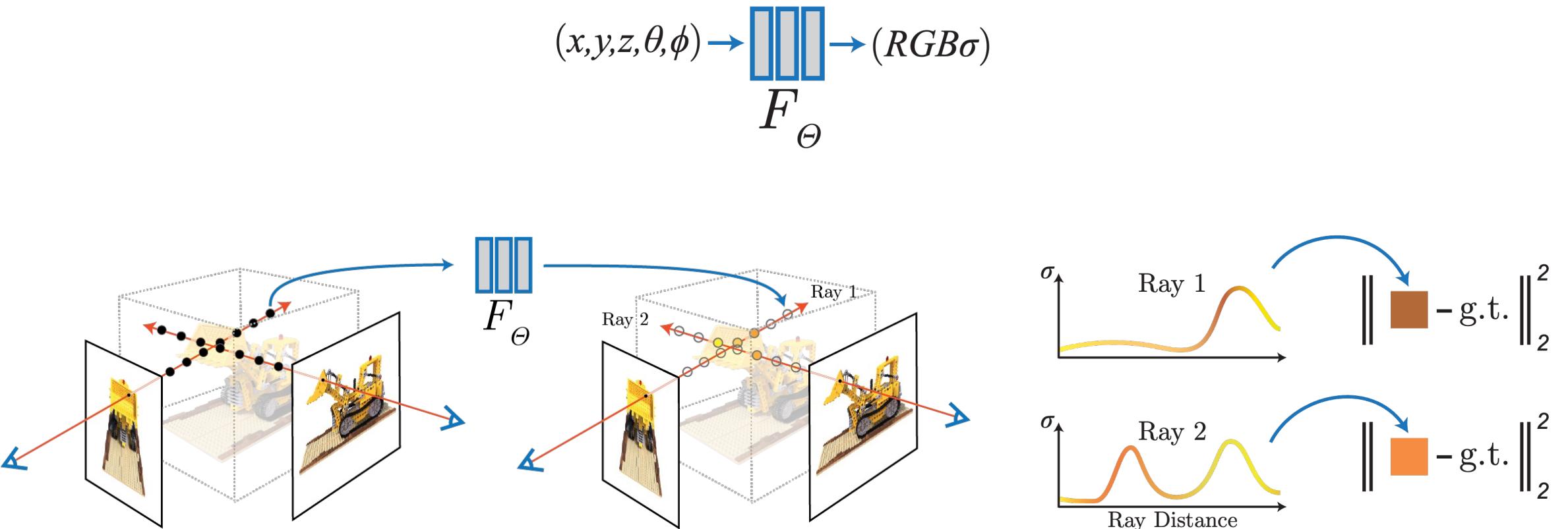
# Generative Modeling with Implicit Geometry + Rendering



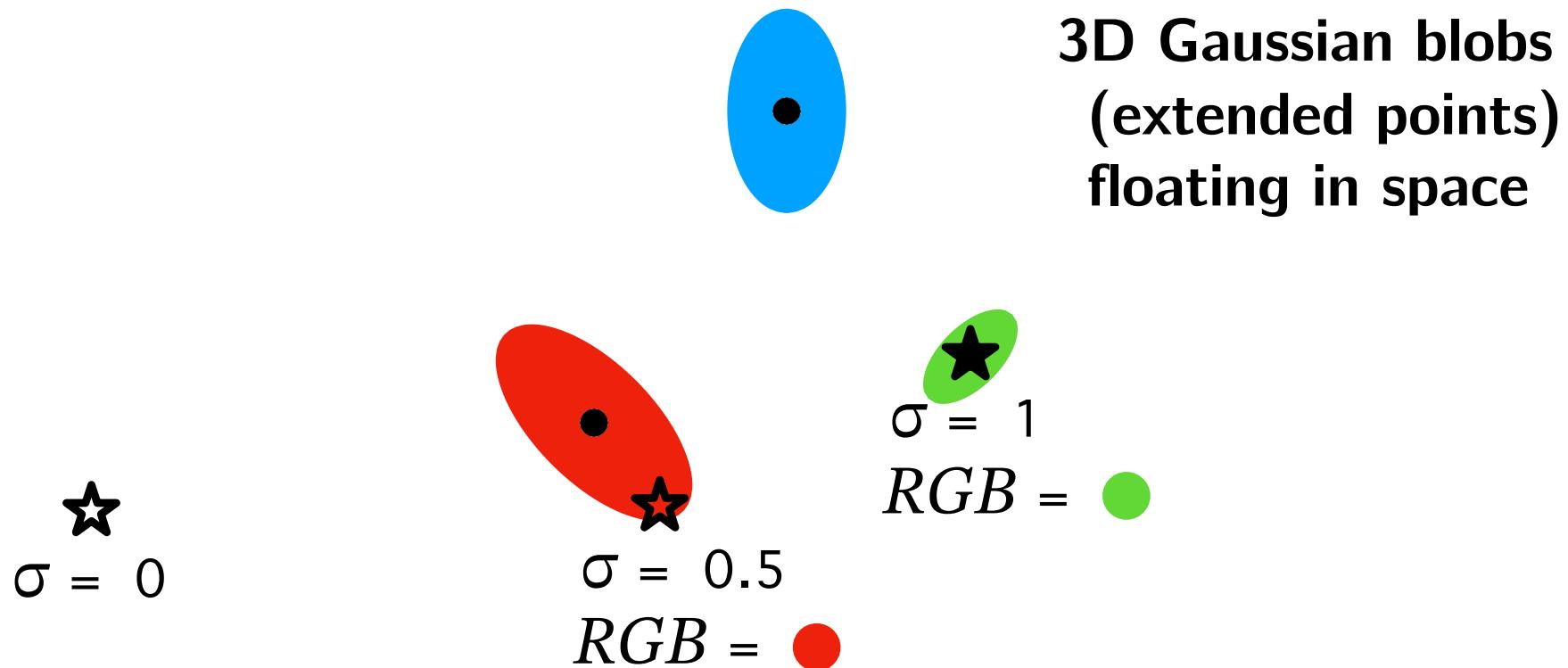
# Explicit <-> Implicit



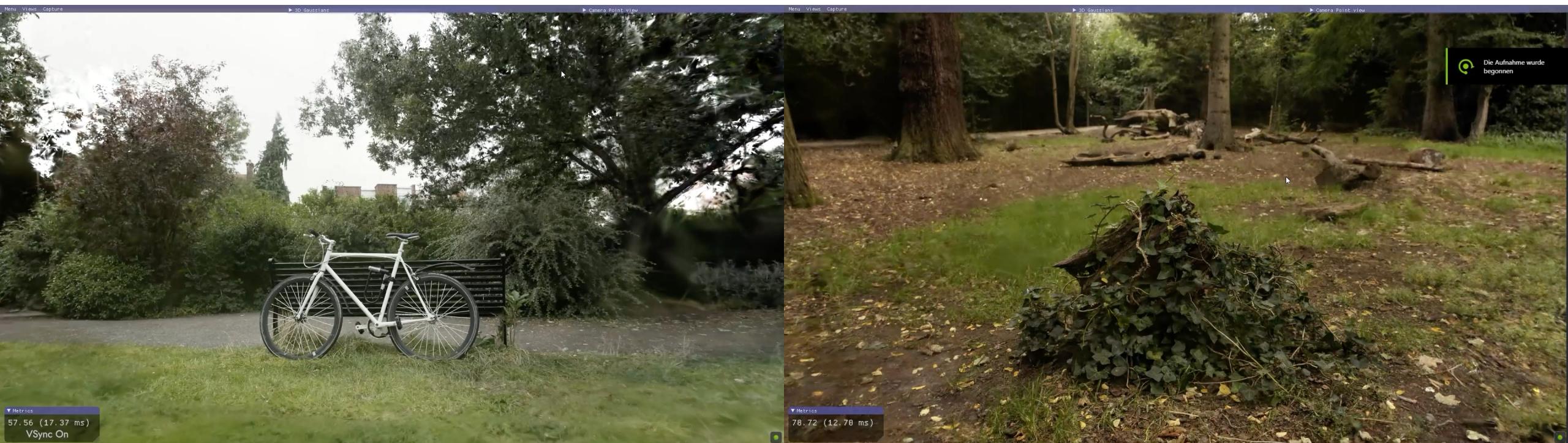
# NeRF parameterizes scenes densely, at every point in space.



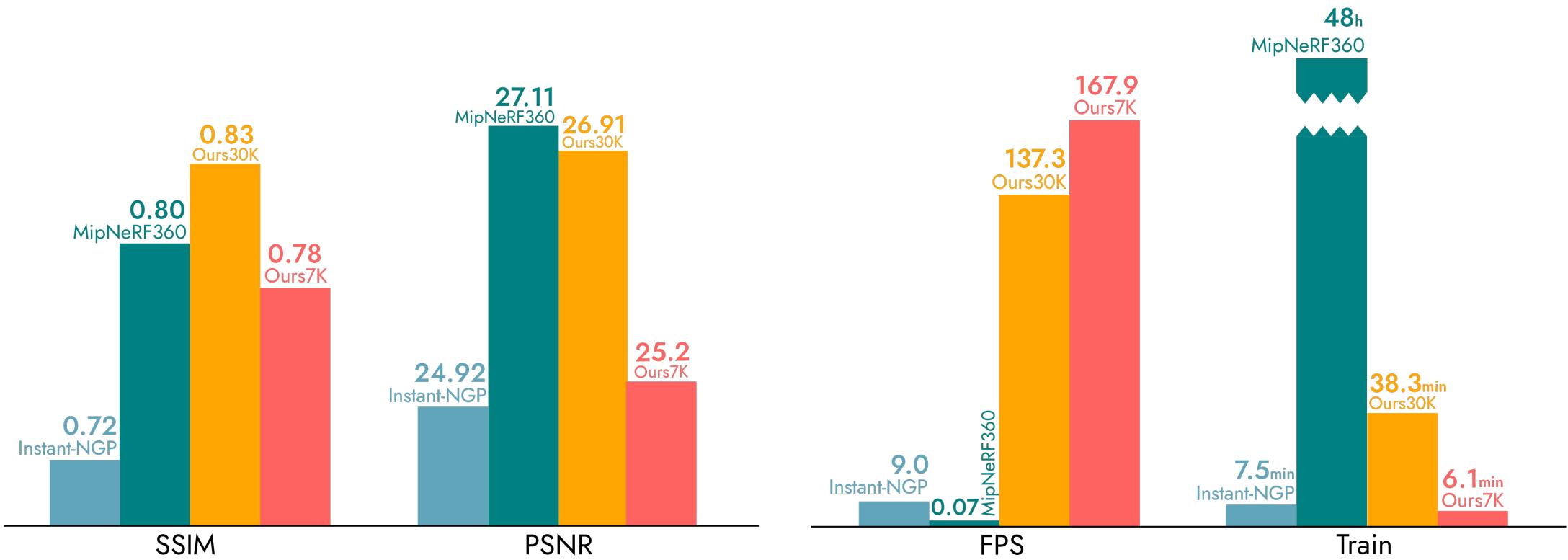
**Gaussian splatting parameterizes the scene sparsely, only where density is nonzero.**



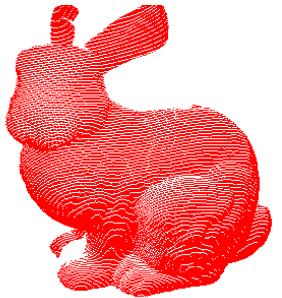
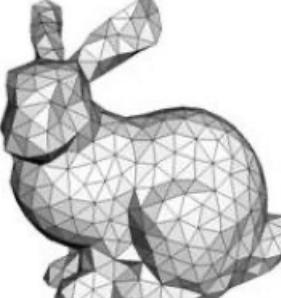
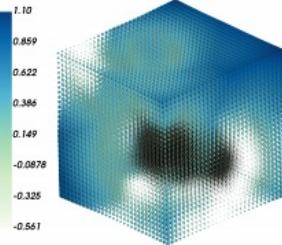
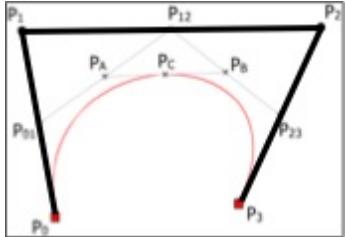
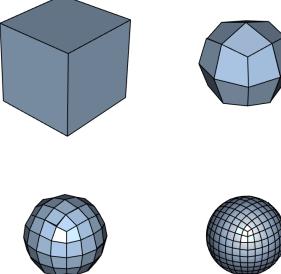
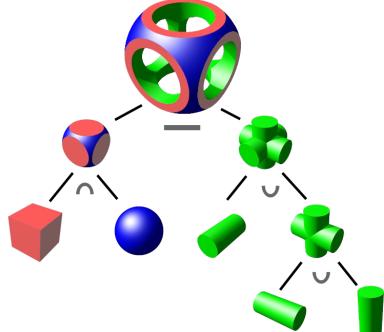
# Reconstruction Using 3DGS



# Quality & Efficiency



# Shape Representations

	Explicit		Implicit	
Non-parametric				
Parametric			 $x^2 + y^2 + z^2 = 1$	
	Points	Meshes	Voxels	Level Sets
	Splines	Subdivision Surfaces	Algebraic Surfaces	Constructive Solid Geometry

# Anatomy of a Structure-Aware Representation



=



Element Structure

+

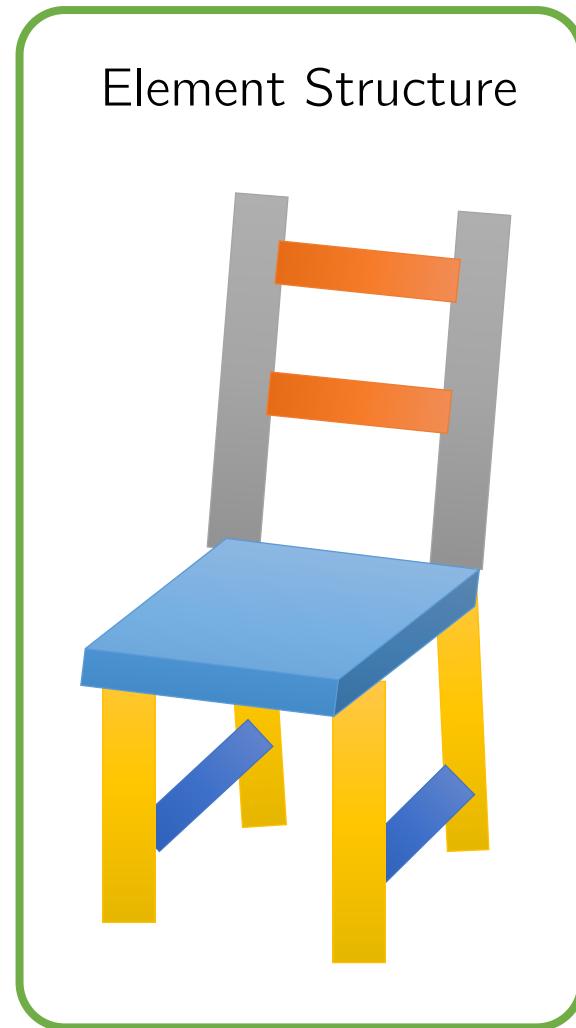


Element Geometry

# Anatomy of a Structure-Aware Representation



=



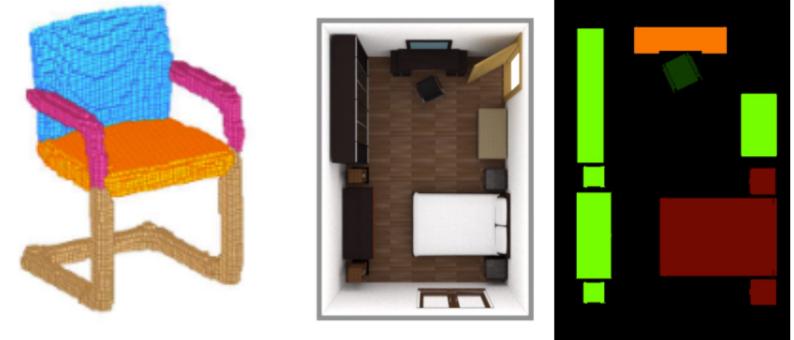
+



Element Geometry

# Representing Element Structure

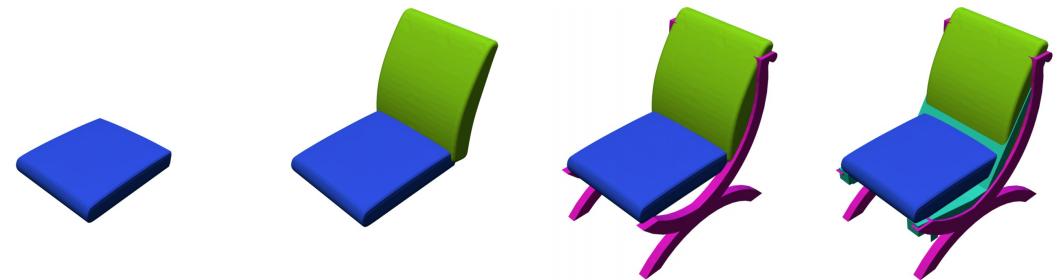
- **Segmented Geometry**



- Simple to construct
- Re-use models for unstructured geometry
- Integrity of atomic elements not guaranteed by construction (generative model must learn to output coherent segments)

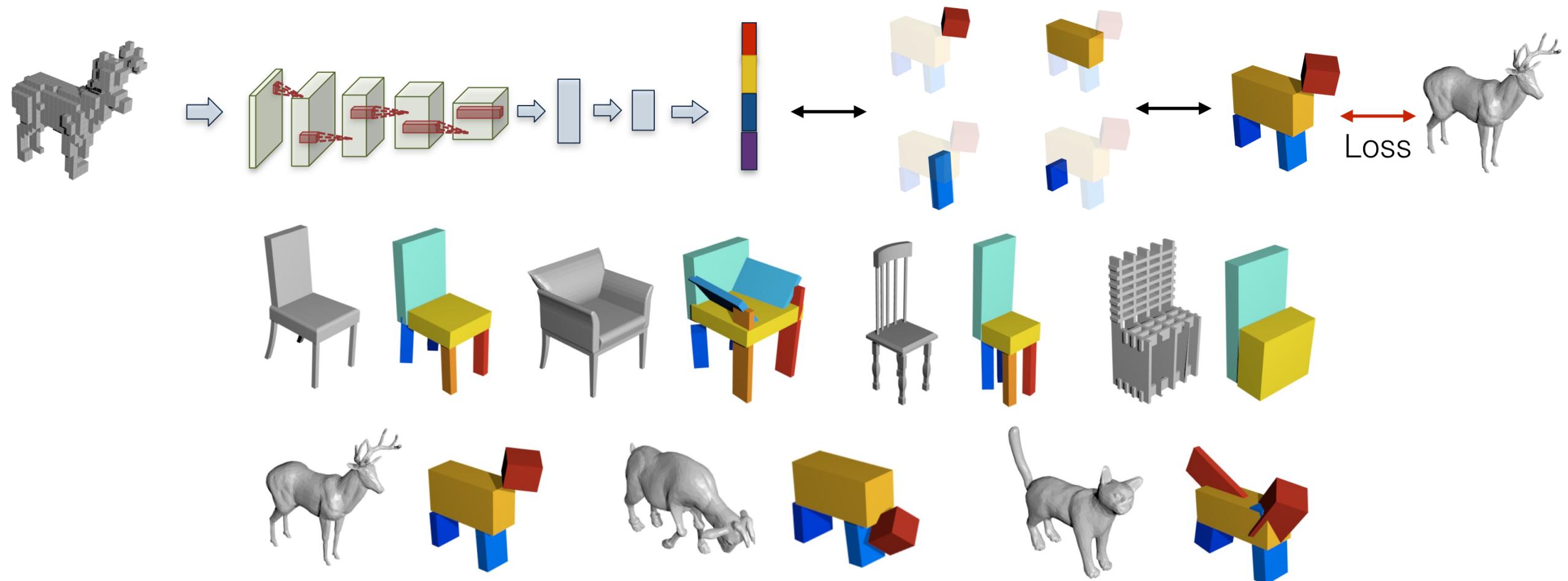
# Representing Element Structure

- Segmented Geometry
- **Part Sets**



- Part integrity guaranteed
- No relationships between parts (e.g. nothing to prevent parts from “floating”)

# Sets of Volumetric Primitives



# Sets of Implicit Functions

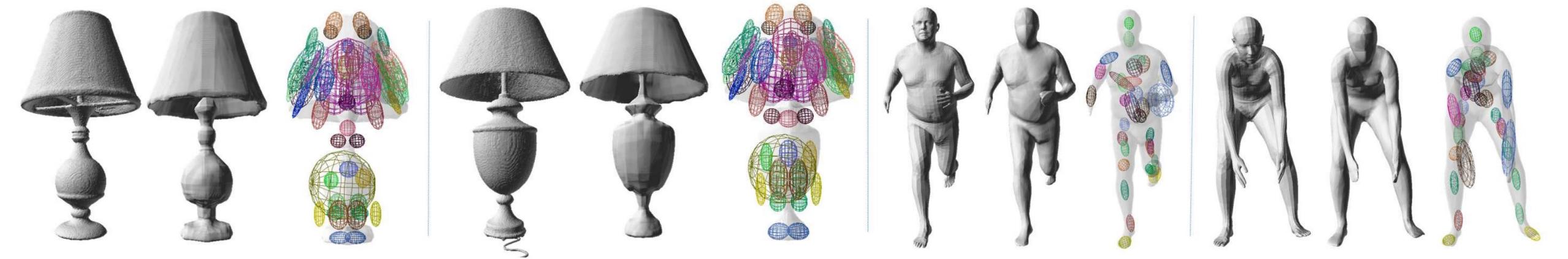
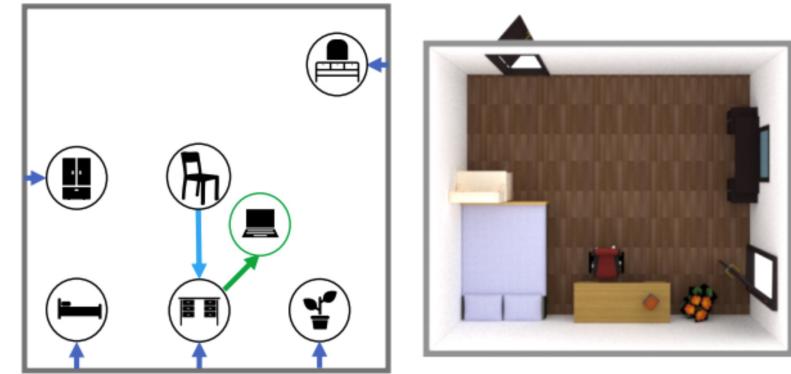


Figure 1. This paper introduces Local Deep Implicit Functions, a 3D shape representation that decomposes an input shape (mesh on left in every triplet) into a structured set of shape elements (colored ellipses on right) whose contributions to an implicit surface reconstruction (middle) are represented by latent vectors decoded by a deep network. Project video and website at [ldif.cs.princeton.edu](http://ldif.cs.princeton.edu).

# Representing Element Structure

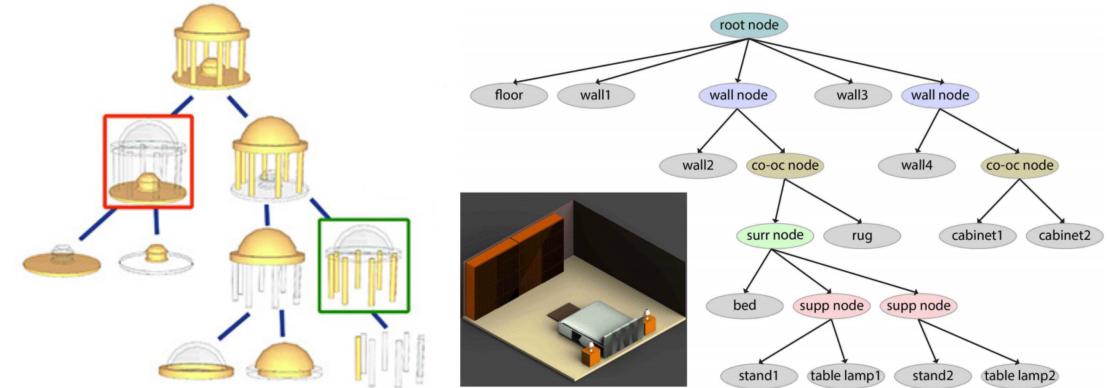
- Segmented Geometry
- Part Sets
- **Relationship Graphs**



- Can enforce important relationships (e.g. connectivity)
- In general, machine learning models for graph generation still an open problem

# Representing Element Structure

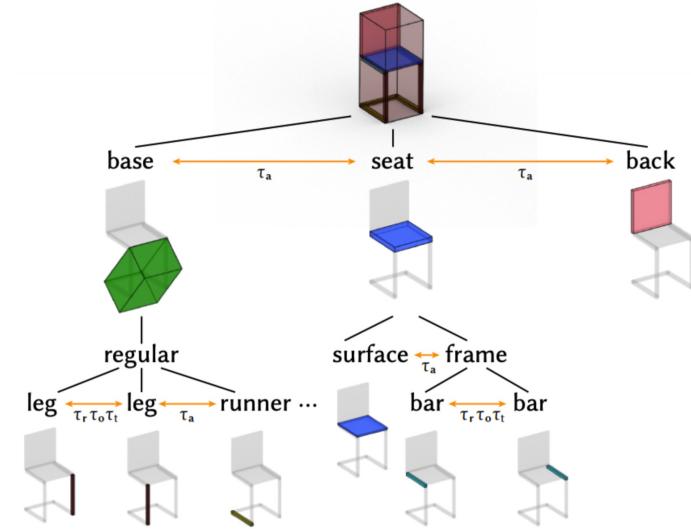
- Segmented Geometry
- Part Sets
- Relationship Graphs
- **Hierarchies**



- Tree generative models better understood than graph generative models
- Not all structures of interest can be (naturally) expressed as trees

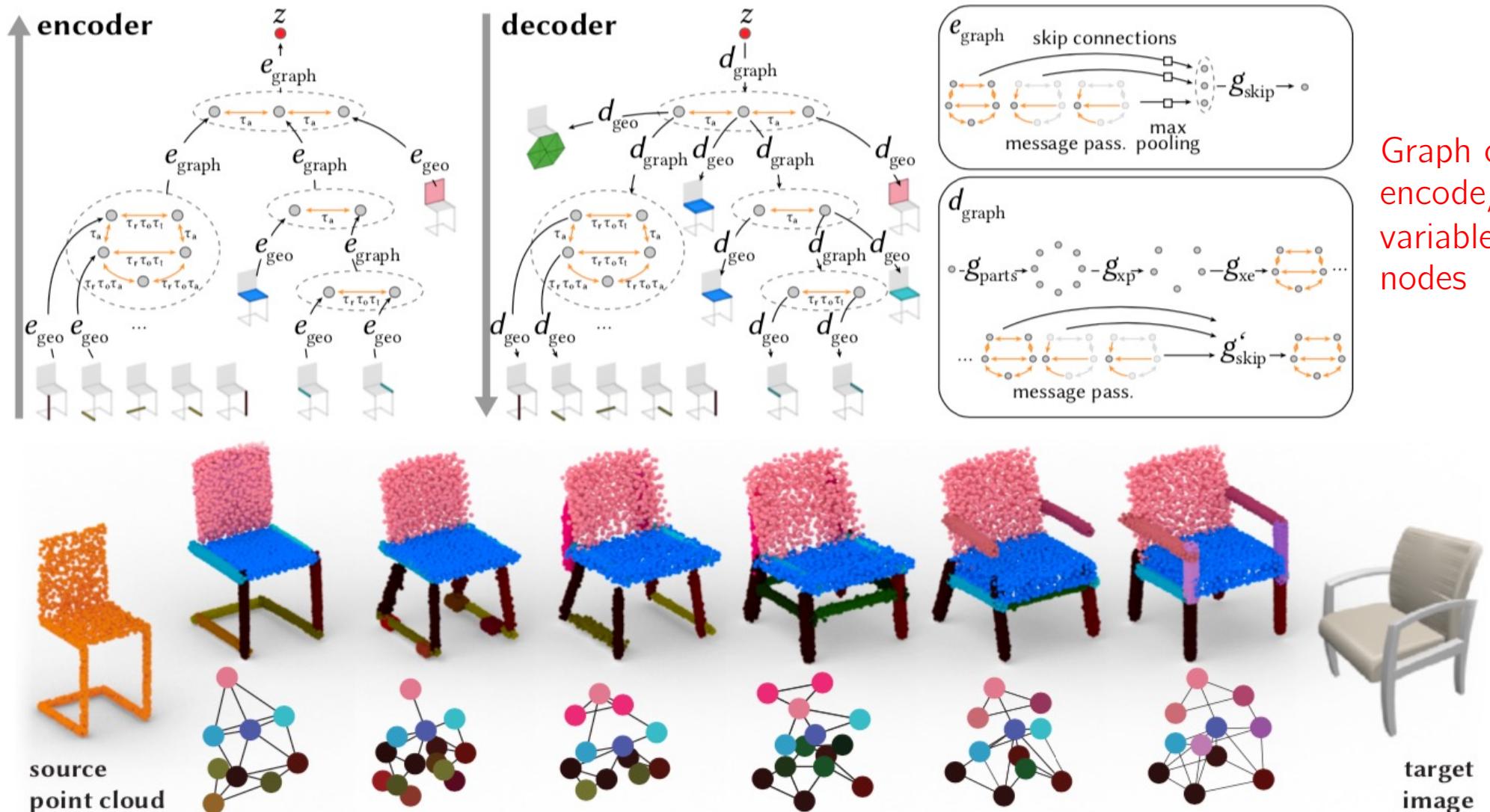
# Representing Element Structure

- Segmented Geometry
- Part Sets
- Relationship Graphs
- Hierarchies
- **Hierarchical Graphs**



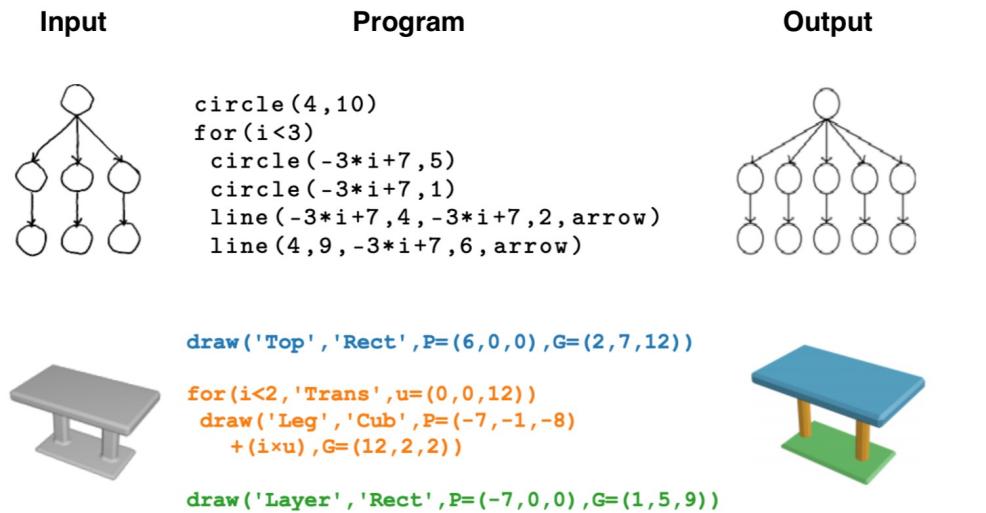
- Models both naturally hierarchical structure as well as naturally lateral relationships
- Graphs per level are simpler → easier to generate than large, general-purpose graphs
- Difficult to obtain / expensive to annotate data in this format

# Hierarchical Graph of Shape Primitives



# Representing Element Structure

- Segmented Geometry
- Part Sets
- Relationship Graphs
- Hierarchies
- Hierarchical Graphs
- **Programs**



- Subsumes all other representations (programs can generate any of them)
- Express natural degrees of freedom via free parameters
- Even more difficult to get data in this format