1	Regime	Detection	Measures	for th	ne Practical	Ecologist

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04 Placeholder

Identifying abrupt changes in the structure and functioning of systems, or system 105 regime shifts, in ecological and social-ecological systems leads to an understanding of relative and absolute system resilience. Resilience is an emergent phenomenon of 107 complex social-ecological systems, and is the ability of a system to absorb disturbance 108 without reorganizing into a new state, or regime. Resilience science provides a 109 framework and methodology for quantitatively assessing the capacity of a system to 110 maintain its current trajectory (or to stay within a certain, and often desirable regime). 111 If and when a system's resilience is exceeded, it crosses a threshold and enters into an 112 alternate regime (or undergoes a regime shift). 113 I will use Fisher Information to detect regime shifts in time and space using avian 114 community data obtained from the North American Breeding Bird Survey within the 115 area east of the Rockies and west of the Mississippi River. Fisher Information is a 116 technique that captures the dynamic of a system, and this metric will be calculated 117 about a suite of bird species abundances aggregated to the route level for all possible

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time periods. Transmutation (aggregation error) about inclusion or exclusion of certain bird species, functional groups, and guilds will be analyzed. Efforts have been 120 made to develop early warning indicators of regime shifts in ecosystems, however, for 121 most ecosystems there is great uncertainty in predicting the risk of a regime shift, 122 regarding both when and how long it will take to happen and if it can be recognized 123 early enough to be avoided when desired. We will complement the use of Fisher 124 Information with multiple discontinuity analyses about body mass distributions at 125 the route-level to achieve the aim of identifying individual species that best serve 126 as early-warning indicators of regime shifts. For those species found on the edges 127 of body mass aggregations, we test the hypothesis that the background variance in 128 their abundances (on Breeding Bird Survey routes) will increase more than those not 129 observed at the edge of discontinuity aggregations. Identification of early-warning 130 indicators of regime shifts in ecological systems allows management efforts to focus on 131 a single or a small number of species that inform us about ecosystem resilience and 132 trajectory. 133 These methods transcend the primary objective of the Breeding Bird Survey (to monitor population trends) and use this expansive dataset in such a way that information about ecosystem order, trajectory, and resilience emerge. Here, we utilize an expansive dataset (the Breeding Bird Survey) to make broad-scale estimations and predictions 137 about ecosystem resilience, regime status and trajectory, and ecosystem sustainability. 138 Identification of regime shifts and early-warning indicator species may afford us the 139 ability to predict system regime shifts in time.

Table of Definitions

Research surrounding regime shifts, threshold identification, change-point detection, bifurcation theory, etc. is muddled with jargon. Here, I provide a table of definitions (Table 1.1) for terms and concepts that may either be unfamiliar to the practical ecologist, or may have multiple meanings among and within ecological researchers and practitioners. With this table, I aim to both improve the clarity of this dissertation and highlight one potential issue associated with regime detection methods in ecology: semantics.

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature.

Term	Definition	Synonyms
Abrupt	A relative value of the speed and/or intensity of the	big, fast,
	change; the time period over which the regime shift	quick, large
	occurs relative to the time observed (or expected to have	
	been) in a particular state.	
Alternative	Controversially can be distilled as one of either:	
Stable State	the number of unique stable configurations that a	
	system can adopt (see Lewontin 1969), or the	
	impacts that processes or pressures can have on a	
	system's state (see May 1977).	
Attractor	The set of values towards which a system tends regardless	
	of its initial (starting) vaules.	

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature. *(continued)*

Term	Definition	Synonyms
Basin-	The parameter values for a system that causes	non-local
Boundary	the system to shift between alternate attractors.	bifurcation
Collision		
Catastrophe	The study of abrupt changes within a dynamical system.	
Theory		
Catastrophic	A relatively abrupt jump to an alternate	
Bifurcation	attractor due to initial attractor.	
Change-Point	See also 'Regime Shift'. A term often used in computer	
	science, climatology, data science; represents the point at	
	which a state changes its configuration.	
Change-Point	A change point method which does not require	
Detection	supervision; identifies potential change points	
	without a priori potential change points.	
Change-Point	A change point method which DOES require supervision;	
Estimation	identifies potential change points when given a set of	
	potential change points; well-developed in computer	
	science, statistics, data mining, etc.; although	
	well-developed, still lacks with giving statistical	
	significance of change-points.	
Chaos	A system with extreme sensitivity to initial	
	conditions.	
Critical Slowing	When the recovery rate (time to return) of a system	
Down (CSD)	decreases (approaches zero) as a system approaches a	
	critical point (possibly a threshold or tipping point). A	
	characteristic observed in some empirical systems data	
	(e.g. nutrient loading in shallow lakes).	
Degrees of	The number of system parameters or components	
Freedom	which vary independently.	

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature. (continued)

Term	Definition	Synonyms
Domain of	The range of values around which a system fluctuates.	zone of
Attraction		fluctuation,
		basin of
		attraction,
		stable point,
		attractor
Driver	A widespread anthropogenic source of change	
	which leads to one or more pressures (e.g.,	
	land-use change).	
Driver-Threshold	When a rapid change in external driver induces a rapid	
Regime Shift	change in ecosystem state.	
Dynamical	A time-dependent system which can be described	
System	in state-space.	
Dynamical	The study of complex systems theory; the study of	
Systems Theory	time-dependent systems.	
${\bf Equilibrium}$	The set of values around which a system revolves	
	and does not change.	
Exogeneous	An external process influencing the state of the dynamical	
Process (Forcing,	system.	
Driver)		
First-Order	When the mean is constantant over the	
Stationarity	observations.	
Fold Bifurcation	This occurs when a stable point collides with an unstable	
	point; when crossing a tipping point induces hysteresis.	
Fractal	A measurement of geometrical self-similarity;	ergodic
Properties	when a system has similar structure regardless of	
	the scale of observation.	

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature. *(continued)*

Term	Definition	Synonyms
Hysteresis	A system which is state-dependent (e.g. magnets); when	
	a tipping point or threshold is crossed such that the	
	previous state cannot be achieved by reversing the	
	conditions.	
Leading	When the statistical properties of the fluctuations	
Indicators	(of the data) approach a critical transition.	
Lyapunov	A value that conveys the average rate of trajectory	
Exponent (and	divergence that is caused by an endogenous force; how	
Stability	quickly (if at all) a system will tend away from a stable	
	point if it starts near the stable point.	
Measure	The study of measures and measurement (e.g.	
Theory	volume, mass, time).	
Moving (Sliding)	When a subsample of the data \X_t is used in lieu of	
Window Analysis	a single observation, \$\$x_t\$\$.	
Noise	Processes manifested in data which are	
	unaccounted for; sometimes referred to as	
	meaningless; random variability.	
Non-Stationarity	Infers that a trend or a periodicity is present in the time	
of the Mean Value	series.	
Online	Real-time updating of model parameters,	
	predictions, etc. (c.f. offline).	
Persistent	A relative value of the longevity of the observed change in	long-lasting
	values.	
Phase Space	A graphical representation of two or more	
	trajectories where one axis is not time. In this	
	representation an equilibrium is defined as a	
	single point in the state space.	

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature. (continued)

Term	Definition	Synonyms
Prediction	A temporal forecast. Is intrinsic when a model and	
	paramters are used to make forecast, is realized when the	
	prediction becomes the actual state of the system.	
Pressure	A perturbation which negatively influences a	
	system, and can be defined as pulse, press, or	
	monotonic.	
Red Noise	Noise having zero mean, constant variance, and serial	
	autocorrelation; autocorrelated random variability.	
Regime	A set of system values that define a particular	
	system state. Not necessarily stable, but some	
	state variables or outputs of the system remain	
	relatively constant over a defined period of time.	
Regime Shift	"abrupt" and "persistent" change in a system's structure	
	or functioning.	
Second-Order	The nean is constant and the covariance is a	
Stationarity	function of a time lag, but not of time.	
Self-Similarity	A system satisfied by power-law scaling.	
Stable	An equilibrium is stable when small	
Equilibrium	perturbations do not induce change.	
State Space	The set of all possible configurations of a system.	
State-	When a graduaal change in external driver	
Threshold	induces a rapid change in ecosystem state (e.g,.	
Regime Shift	System crosses a threshold).	
Stationarity	When the probability density function of a system does	
	not change with time.	

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature. *(continued)*

Term	Definition	Synonyms
Statistical	A system with statistical properties unchanging	
Stationarity	over time. This concept extends to periodic	
	stationarity for systems exhibiting periodic	
	behavior.	
Strange Attractor	An attractor which has fractal structure (an observable	
	fractal dimension).	
Supervised	When classifiers are used to train the data a	
Machine	priori.	
Learning		
System State	The observed (current) instance of the system within a	
	state space.	
Threshold	A point where the system reacts to changing	
	conditions.	
Tipping Point	A point in a system's trajectory where a small change in	
	an endogenous force induces a large change in sytem state	
	or values; the point where a system can flip into an	
	alternative state.	
Trajectory	The path of an object or system through	orbit, path
	space-time.	
Transient	A behavior or phenomenon which is responsive to intial	
	(starting) conditions, or its effect declines over time.	
Trend	Local averaging of values such that the	
Smoothing	non-systematic components of the system are	
	washed out.	
Unstable	An equilibrium is unstable when small perturbations	
Equilibrium	induce change.	

Table 1.1: A table of definitions for terms, theories, and phrases often appearing in ecological regime shift literature. (continued)

Term	Definition	Synonyms
Unsupervised	When no prior training of the data is required	
Maain Learning	(i.e. no classifications necessary a priori) to	
	classify it.	
White Noise	Noise having zero mean, constant variance, and is not	
	autocorrelated; uncorrelated random variability.	

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Chapter 7

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239 Data Quality and Quantity

7.1 Introduction

Ecological systems have many unpredictable and variably interacting components (Jørgensen et al. 2011). Methods for analyzing these complex systems, e.g. Dynamic Bayesian Networks, network models, and food webs are designed to handle these complexities, yet require data- and knowledge-intensive models. Although ecological data collection and data management techniques are improving (La Sorte et al. 2018), the aforementioned approaches to modeling and understanding complex system are often infeasible in ecosystem research and management (Clements et al. 2015).

A growing concern with anthropogenic impacts on the environment has increased
the demand for mathematical and statistical techniques that capture these dynamics.
These often undesirable changes in the structure or functioning of ecological systems
are often referred to as "regime shifts", "regime changes", "state change", "abrupt

change", etc. (Andersen et al. 2009). A yet-unattained goal of ecological research and
management is to reach a point where these methods can predict impending regime
shifts in real-time and with high confidence. Ideally, ecological regime shift detection
methods (hereafter, regime detection measures) would require little knowledge of the
intrinsic drivers of the system, and the users of the method would not be required to
know if and where a regime shift occurred in the data.

Despite the suite of regime detection measures in the environmental and ecological 258 research literatures, they are not used in ecological management. We can describe 259 the current state of regime detection measures as being either system—specific (i.e., 260 the method is not widely applicable or generalizable across systems) or not. Methods 261 of the latter type are convenient in that they can be applied across various system 262 and data types, but the results of these analyses require some degree of subjective 263 interpretation (Clements and Ozgul 2018; c.f. Batt et al. 2013). Efforts to develop 264 and/or improve regime detection measures that can handle these biases will aid the 265 advance of regime detection measures research and application.

Current efforts to improve regime detection measures may be stunted by the lack of 267 application beyond simple and/or theoretical (toy) systems data. Like most statistical 268 and mathematical approaches, the evolution of many regime detection measures begins with application to theoretical data, followed by application to empirical data. Current applications of regime detection measures to empirical, ecological data are largely 271 limited to data describing populations (e.g., Anderson and Piatt 1999, Alheit et al. 272 2005, deYoung et al. 2008), climatic, marine (e.g., Lipizer et al. n.d., Nicholls 2011), 273 and Paleolithic regime shifts (Spanbauer et al. 2014, Yang et al. 2017, Kong et al. 274 2017), with few applications to terrestrial data (c.f. Bahlai et al. 2015; Sundstrom et 275 al., 2017). Although testing the performance and inference boundaries of theoretical 276 and simple systems is important, they are of little use to ecosystem managers if they 277 are not proven to be easily and reliably applicable to their system. Additionally, 278

7.1. Introduction 21

regime detection measures should be capable of handling empirical ecological data are
often sparse and noisy.

Ecological systems data is not only expensive to capture, but are often difficult 281 to perfectly capture due to the large process and observation errors. The variability 282 resulting from imperfect observation influences data quality and quantity, sometimes 283 limiting the potential numerical tools used to identify trends and changes in the 284 system in question (Thrush et al. 2009). Some methods, new and old, are proposed 285 in the literature as regime detection measures which are capable of handling data 286 limitation and quality issues inherent in ecological data and require few subjective 287 decisions for choosing state variables and interpreting results. For example, variable 288 reduction techniques, e.g. principal components analysis (Rodionov 2005, Andersen 289 et al. 2009, Reid et al. 2016) and clustering algorithms (Weijerman et al. 2005, 290 Weissmann and Shnerb 2016), an index of variance (Brock and Carpenter 2006) and 291 Fisher Information (Cabezas and Fath 2002, Fath and Cabezas 2004, Karunanithi et 292 al. 2008) were introduced as methods which collapse the system into a single indicator 293 of ecological regime shifts. Although these methods have been tested on empirical 294 ecological systems data, their robustness to empirical data quality and quantity have 295 yet to be examined.

In this Chapter I examine the influence of observation and process errors on the inference obtained from select multivariable regime detection measures. There are two major objectives:

- 1. Identify the effects of data quality on regime detection measure inference.
- 2. Identify the effects of data quantity on regime detection measure inference.
- 302 3. Explore the relative performance of velocity (described in Chapter 6) to the abovementioned methods under multiple scenarios.

This Chapter provides baseline relative performance estimates of select, multivariable

regime detection measures under various scenarios of data quality and quantity. The results from this Chapter inform the practical ecologist of the potential limitations to consider when applying these regime detection measures to their data, and has potential to inform the data collection process. Additionally, the software accompanying this Chapter allows the end user to implement these methods on this diatom system, a toy system, or their own data.

$^{_{\scriptscriptstyle{11}}}$ 7.2 Data and Methodology

7.2.1 Study system and data

I used paleodiatom time series from a freshwater system in North America (Foy Lake, 313 present day Montana) that apparently underwent a rapid shift in algal community 314 dynamics at multiple periods in time. This datum comprises a single soil core sample, 315 from which the relative abundances of 109 diatom species were identified at 768 316 observations (time points) over $\approx 7,000$ years [7.1]. Althouh the soil core was sampled 317 at regular distances, the soil accumulation process is not necessarily linear over time, 318 resulting in irregularly-sampled observations (i.e., time elapsed between sampling 319 points differs varies; see 7.2). This datum was published in T. L. Spanbauer et al. (2014) and can be downloaded at the publisher's website.

7.2.2 Regime detection measures

Fewer model-free regime detection metrics exist than do model-based metrics [Chapter 3] and of these, only a few are suggested for handling multivariable data. Here, I examine the regime detection metrics that are model-free and can handle multivariable data: velocity [Chapter 6], the Variance Index (Brock & Carpenter, 2006) and Fisher Information. These methods and the primary sources are described below.

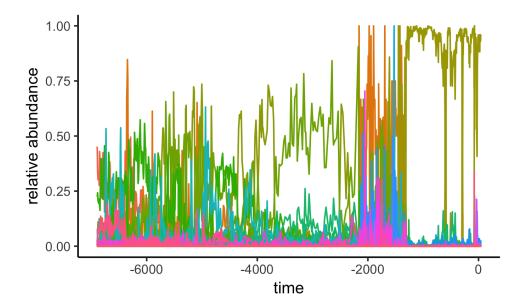


Figure 7.1: Relative abundances of the diatom species in Foy Lake over the time period.

$\mathbf{Velocity}(v)$

In Chapter 6, I describe a new method, **velocity**, v, as a potential dimension reduction and regime detection method. First introduced in by Fath, Cabezas, & Pawlowski (2003) as one of multiple steps in calculating their variant of Fisher Information, velocity calculates the cumulative sum of the square root of the sum of the squared change in all state variables over a period of time [Eq. (7.1)]. Steps for calculating this metric are described in detail in Chapters 4 and 6.

$$\Delta s_i = \sqrt{\sum_{j=1}^n (x_{i,j} - x_{i-1,j})^2} s_k = \sum_{i=2}^k \Delta s_i 2 \le k \le nv = \frac{\Delta s}{\Delta t}$$
 (7.1)

Variance Index

The Variance Index was introduced by Brock & Carpenter (2006), and is simply defined as the maximum eigenvalue of the covariance matrix of the system over some period (window) of time. The Variance Index (also called Variance Indicator) was originally applied to a modelled system (Brock & Carpenter, 2006), and has since

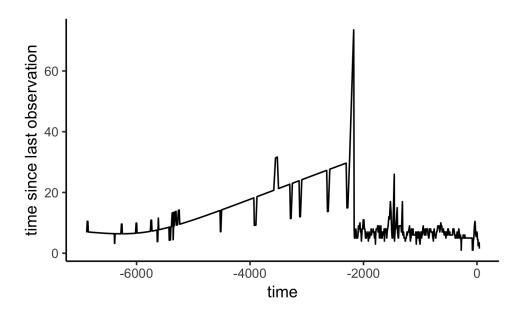


Figure 7.2: The amount of time elapsed between observations.

been applied to empirical data (T. L. Spanbauer et al., 2014; Sundstrom et al., 2017).

Although rising variance has been useful in many real systems (van Nes and Scheffer

2003, Brock et al. 2006, Carpenter and Brock 2006), the Variance Index, which

is intended for multivariate data, appears most useful when the system exhibits a

discontinuous regime shift (Brock & Carpenter, 2006).

345 Fisher Information

Fisher Information (I) is essentially calculted as the area under the curve of the acceleration to the fourth degree (s''^4) divided by the squared velocity $[s'^2]$; also referred to as v in Chapter 6 and in the next section of the distance travelled by the system, s over some period of time (T), and is given in Eq. (7.2):

$$I = \frac{1}{T} \int_0^T dt \left[\frac{s''^2}{s'^4} \right]^2 \tag{7.2}$$

I describe this method in detail in Chapter 4.

Calculating Fisher Information and Variance Index using moving window analysis

Unlike velocity, the Variance Index and Fisher Information are calculated using moving window analysis. That is, over the entire time series, T^* , these metrics are calculated within multiple windows of time, T. In this approach, all state variables, x_i , are used to inform the calculations (of Variance Index and Fisher Information) over a time interval, T, where T is the length in [time] units of the time interval and satisfies the following conditions: $T < T^*$ and $2 \le T < (T^* - 1)$. If $T = T^* - 1$, then only a single value of the metrics will be calculated for entire time series, which does not allow for any estimate of change.

When using these metrics in the context of identifying abrupt changes in ecological systems data across T*, it is ideal the value of T meets the following conditions: $3 < T \ll T^* - 1$. The length of a time window dictates the number of calculations one can obtain over T^* , such that the number of potential metric calculations increases as $\frac{T}{T^*}$ decreases. Previous applications of moving window analyses to calculate Fisher Information found that at least eight observations (time points) should be used.

An additional parameter is required when conducting moving window analyses: the
amount of time points by which the window advances. In order to maximize the data,
I force the window to advance at a rate of one time unit. However, it is important to
note that because these data are not sampled annually and the because the window
always advances by a single time unit, the number of observations included in each
calculation will not be the same. If fewer than 5 observations are in a window, I did
not calculate metrics, advancing the window forward.

I assigned the calcuated values of Fisher Information and Variance Index within each moving window to the **end** (the last time unit) of the moving window. I temporal analyses, assigning the value to any other point in time (e.g., the beginning or the middle) muddles the interpretation of the metric over T^* . Also note that this method has the potential to result in calculating a metric for all integers between $0.20T^*$ and T^* .

7.2.3 Resampling Techniques for Simulating Data Quality and Quantity Issues

Using a bootstrap approach I calculated the regime detection measures over varying degrees of scenarios to simulate data quality and data quantity issues that are common 383 to ecological data anlaysis. The scnearios are categorized as observations and species. 384 The observations scenario simulates a loss of temporal observations (decreasing the 385 number of times the system was observed), and the species scenario simulates a loss of 386 information about the system by removing a larger proportion of the species. The loss 387 of temporal observations and the loss of species were examined at three proportions: 388 P = [0.25, 0.50, 0.75, 1.00], where P is the proportion of species and time points 389 **retained** for analysis. For example, when P = 0.25, a random selection of 25% of the 390 species are retained for analysis in the species scenario. I bootstrapped the datum 391 over 10,000 iterations for each scenario and P combination. Note that because when 392 P = 1.00, all data are retained. Therefore, no resampling was conducted at this level 393 because only a single metric (e.g. Velocity) value is possible. 394 Interpretation of the regime detection measures used in this analysis are currently 395 limited to visual inspection. Therefore, I limit inference in this study largely to the impact of data loss on the variability with a regime detection measure (i.e. how robust 397 is the measure to data loss).

7.3. Results

9 7.3 Results

7.4 Discussion

7.5 Ackowledgements

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406 Chapter 8

- Discontinuity chapter under
- 408 construction
- 8.1 Introduction
- 8.2 Data and Methods
- 8.3 Results
- 8.4 Conclusions

⁴¹³ Chapter 9

414 Conclusions

- 415 Placeholder
- 416 9.1 Method mining regime detection methods
- 9.2 Ecological data are noisy
- 9.3 Data collection and munging biases and limits findings
- 9.4 Common Limitations of Regime Detection

 Measures
- 422 9.5 Specific synthesis of chapter results

- 423 Appendix A: R package
- ${}_{\scriptscriptstyle{424}}\ \mathbf{regime Detection Measures}$
- Placeholder
- 9.6 Measures/metrics calculated
- 9.7 Example analysis

Appendix B: R package bbsRDM

Placeholder

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