# Thesis

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### 1 A gentle introduction to credit risk

As you might have already inferred from the title, the aim of this section is to give an overview of the topic that is at the hearth of this paper: credit risk. R ather than jumping straight into formal definitions, which might create difficulties in grasping with the content, the reader will be first provided with real-life examples characterized by the presence of such risk. Moving on, some formal definitions will be given along with a description of the agents that usually take upon this risk and how they act to assess it and quantify it with the purpose of taking proper actions to finally mitigate it. Finally, the chapter ends with an introduction to credit risk modelling, a topic that will we will refere extensively later in the analysis.

### 1.1 Introduction

To start off this section, let me provide you with a few examples of situations that occur on a daily basis, which might however serve as a great starting point to understand the topic.

Imagine yourself receving a call from one of your friends that you have not heard for quite a while. You can hear from his voice that he is really upset, and apparently, the reason for this is that he has to pay a fine by the end of the day to avoid an additional charge, but he does not have the money to pay at the moment. He tells you that the reason for this is that he had to cover fo huge expenses lately and he still has not received his monthly salary. He then ask you, whether you would be kind enough to lend him the money, promising to repay you as soon as he receives his paid. What would you do? Would you lend him the money? What if one of your colleague at work asks you the same thing? Would you do it in this case? Would it make a difference if it was someone you knew well? And if your colleague ask you to lend him money for a pizza without mentioning you when and how is going to pay you back?

Usually, the type of questions that you ask yourself before getting into these agreements, which are also a simplified version of what financial istitutions ask themselves before lending, are the following:

- 1. Who is borrowing?
- 2. How much they are borrowing?

- 3. When I will get it back?
- 4. How much is there for me?

Going back to the last example, imagine your colleague telling you that he will pay you back the week after and in addition, he is willing to take you out for lunch. In this case, he is paying you back more than what you lent him. Would you call this *interest rate*? What if instead he gives you his watch to keep until he pays you back? Now it feels a much more safer lending. Indeed, the watch in this case is usually called *collateral* (or also *security*).

The procedure that has been just introduced is usually referred to as "credit analysis", which formally can be defined as the process through which the lender elaborates if he believes the counterparty is going to honor its obligations or not. This ultimately determine whether the agent will enter in that contract, along with the relative risk associated with it, or more precisely, the credit risk.

#### 1.1.1 Credit risk

**Definition (Credit Risk):** the risk that a lender has to take into account due to the uncertainty related to the borrower either failing to repay a loan or to meet its obligations.

In simple terms, this definition suggests that the lender should consider the possibility that a borrower will not be able to pay back the principal and the interest rate according to the initial contractual agreement. He should then quantify this probability and based on the result, charge a coupon rate (i.e. interest rate) to protect against this risk. The methods to derive the aformentioned probability are part of the broad area of **Credit Risk Modelling**, which will be at the heart of the empirical analysis, and for this reason, it will be introduced later.

Ultimately, there are at least 3 additional points that is worth mentioning in the context of credit risk and that should be considered as a key takeaways from this introductory chapter:

1. Credit risk in every financial transaction: although most of the times it might come natural to associate this type of risk to transactions

that occur between a party and a financial istitution (e.g. mortgages, loans, credit cards, etc...), credit risk has a presence also at the company level, for instance, between companies and clients (e.g. paying invoices, insurance coverage, etc..)

- 2. Risk assessment: before granting new credit, as often it is the case in the business world, the bank undergo an assessment of the borrower that takes into consideration his credit history, the capabilities to repay back, the capital available, the loan's conditions and associated collateral. Such evaluation has the final goal of providing an accurate prior estimate of the credit risk, which will eventually tell whether the client should get or not the obligations, with an increasing interest rate for those who are perceived as riskier. In the case of bonds, this assessment is done by credit-rating agencies that assign a triple-A (i.e AAA) for low-risk investments, all the way down to C for high-risk investments. Although this process is tied to bonds only, our dataset provides ratings also for loans, perhaps as a result of internal procedures to assess credit risk.
- 3. Credit risk vs. other risks: so far it was assumed that the risk associated to the lending was purely driven by the borrower characteristics. However, in a typical lending transaction, usually other types of risks factor in such as market risks (e.g. economic conditions, FX rates), country-specific risks (e.g. OECD country, emerging-markets country, etc..), operational risk, issuer risk, and so on... To keep things simple, and given the nature of the data for the empirical analysis, although it might represent a far too simplistic assumption, we will stick with it and only deal with a particular type of credit risk: the CCR (Counterparty Credit Risk)

### 1.1.2 CCR - Counterparty Credit Risk

**Definition (Counterparty Credit Risk):** CCR can be defined as a measure of the **likelihood** that the counterparty to a transaction **might default** before meeting the contractual obligation.

According to the definition of *credit risk* provided above, there is a subtle but fundamental difference between the two type of risk, and in order to make it clear also to the reader, and example on loans is going to be provided. Imagine that a counterparty was able to obtain an incredibly high amount

through a loan that was extended for whatever reason from a bank. The latter assessed whether the borrower would be able to pay back the amount also within the date established by the lending contract. This process is also called "credit risk assessment" and takes into account the possibility that the borrower might not be able to fully repay the lender according to the contractual obligations, but do not exclude that the counterparty might cover for the remaining part in the future either. Hence, the bank here is exposed (in terms of risk) only to the portion of the money lended that believes are at risk.

On the other hand, what if the banks start considering the chance that this counterparty might default on this loan such that he will never be able to pay back any of the amount received, neither in the present, nor in the future? In this case the bank not only evaluates the risk associated with the loan, but it also has to deal with the risk associated to the counterparty itself. If such event happens, and the pool of transactions with the counterparty has a positive economic value, the result would be an economic loss for the lender.

A typical transaction with the presence of CCR is usually characterized by bilateral risk of loss: either one of the party involved in the transaction might default. Bilateral exposures usually factors in the uncertainty related to market movements, as part of the value of the transaction is driven by the underlying market value. Analyzing a portfolio of loans, we will only deal with unilateral exposures: the lending bank is the only one party to be exposed to the risk of the obgligator to default.

### 2 Basel Regulatory Framework

The needs for a more comprehensive and better approach to risk management, particularly for counterparty credit risk, has emerged quite significantly after the financial crisis of 2007-2009. Since then, regulators have sharpened their existing frameworks and applied more stringent controls to the stability of financial istitutions. On this line of reasoning, this section provides an overview of how regulatory requirements in the context of counterparty credit risk have evolved over time, with a focus on the key regulatory framework in this environment: The Basel Accords. The aim is to make the reader aware of the reasons to have such framework in place, along with a brief walk-through the history to see why, as of today, the baking industry has become increasingly regulated, specially for what concern lending.

After the well-known and aformentioned 2007-2009 financial crisis event, there has been an unprecedented revision of the global framework regulating the financial sector, culminating in what is known today as the **Basel III** regulatory framework. Before reaching this result, the banking sector has experienced a relevant number of systemic crisis usually driven by various factors, including the miscalculation of risk represented by inadequate capital levels to carry out their business. Each of this crisis brought some contribution and changes to the previous framework, adding up to the first version, which consisted of 30 pages, more than 1500 pages of guidelines relating to the supervision of daily banking activities.

Why was the Basel Committee ever needed? In order to answer this question, we have to go back to 1970s, when the Herstatt Bank collapsed and was put under liquidation due to enormous trades on the foreign exchange market that did not go as planned. The license was withdrawn in the 1974, as losses have reached an amount equal to 10 times the liquidity of the bank. However, there is more to the story: US counterparties engaging in multiple transactions with Hersatt Bank released "Deutschmark" in exchange of dollars. These lenders never see their money, essentially because of time differences: US was still in morning trades when the bank was revoked its license. Although this is purely related to FX activities, and cosequently involves also FX and market risk, this event highlighted the necessity to create a central forum for banking supervision concerning matters related also to other type of risks, such as "credit risk". With the objective of enhancing the financial stability and quality of banking supervision, in 1974 multiple

central banks gave raise to a centralized committee which later on took the name of "Basel Committee on Banking Supervision". The latter expanded quite significantly and as of now, it includes 45 central banks worldwide.

The need for a regulatory framework for risk management was further strengthen during the 70s-80s period, when the surge in debt in the latin american countries combined with the raise of interest rates in US and Europe led the way to a series of critical debt restructuring efforts for many countries worldwide. Hence, the critical needs for a more clear and comprehensive framework to bring overall stability in the banking system forced the Basel committee to issue guidelines on weighted approach to risk management. Such need was satisfied with the release of the Basel 1 framework in 1988, when for the first time in history, banks were required to weigh the capital they held against the credit risk they took.

### 2.1 Basel 1

In 1988, the first regulatory framework, which later took the name of "Basel I", was released by the Basel Committee. The latter had the objective of setting up common international and shared regulations on capital adequacy supervision, something that then became the core aspect of all the activities that the Committee conduct. The relevant changes that were applied are summarized in the following points:

- Istitutions that provide any type of lending services were required to classify assets into 5 different categories based on the underlying risk of holding such assets: from 0% for most secured assets (e.g. cash) to 100% for low-quality assets (e.g. private sector debt). Since then, "RWA" (risk-weighted assets) have been the keyword to describe this weighted approach towards assets.
- Definition of the so-called **Minimum Capital Requirement**: minimum ratio of capital to risk-weighted assets (RWA). The threshold was initially set at 8%, equally spread between most absoring assets (i.e. **Tier-1 Capital**: examples are equity and retained earnings) and supplementary assets (**Tier-2 Capital**: examples are revaluated assets and subordinated debt). The latter includes assets that are more difficult to liquidate, and therefore less secure than the former. This level was introduced to ensure that financial istitutions had enough stan-

dalone capabilities to absord potential losses resulting from defaulting clients.

Despite the major alterations, the first Basel Regulation presented some shortcomings mainly related to the duration of the service, the market risk and, most importantly, the counterparty risk. Some of these issues were considered and partly assessed through amendments (such as the Market Risk Amendment). Nevertheless, the complexity introduced by some financial products (Credit default swaps, Complex derivatives, etc..) was drastically incrementing the risk taken by financial istitutions. This situation required further adjustments with the regulation and shined a light on the ever-increasing importance of accurate methodologies to assess exposures to risk.

### 2.2 Basel 2

The proposal for a replacement of the previous accord (i.e. Basel I) came in 1999, and was finally released in 2004 with the name **Basel II**. This comprised some of the aformentioned and much needed adjustments, and comprised the following 3 pillars:

- 1. **Minimum capital requirement**: developed and expanded on top of the standardized approach set out in the first approach and introduced a new capital tier that was meant to cover also for market risk (i.e. **Tier-3**)
- 2. Market discipline: effective period disclosure of risk exposures by financial istitutions to enable much more informed decisions
- 3. **Supervisory review**: provided clear guidances on period assessments of an istitution's capital adequacy and granted intervention powers in case of presence of capital pressure

Despite the efforts to bring more stability to the financial environment, the accord required substantial time and effort before being ready and released. After the publication, most financial istitutions started taking full advantage of the subprime mortgages - lending money to low credit profile - thanks to their higher expected returns. Moreover, these institutions entered in the financial crisis with way to much leverage and also took full advantage

of the favourable economic conditions afterwards despite the regulatory environment that was set in place with Basel II, These events were part of a much broader series of misfunctionality (e.g. poor governance, bad risk management, combination of excessive credit growth and credit risk mispricing) that served as key lessons for the Basel Committee to bring substantial updates to the baseline framework. Responding to these risk factors, the Committee agreed to design a reform package to outline new ways of handling credit and liquidity risk.

### 2.3 Basel 3

The agreement culminated with the publication in 2010 of what is now referred to as the **Basel III** framework. This was a very large package which aimed at improving on top of the 3 pillars of the previous accord and extend them to also other areas. The key changes can be summarized in the following points:

- 1. Capital conservation buffer: part of the common equity that, if ever breached, restricts payouts (e.g. dividends) to be used to meet the minimum common equity requirements
- 2. **New leverage ratio**: based on loss-absorbing capital and total istitution's assets and takes into consideration also off-balance sheet exposures (regardless of RWA)
- 3. Liquidity Coverage Ratio (LCR): a minimum short-term liquidity ratio to provide banks with enough liquidity to cover for at least 30-days stress period.
- 4. Net Stable Funding Ratio (NSFR): a minimum long-term liquidity ratio to address maturity mismatches over the balance sheet

Despite the introduction of all these new regulations for the financial istitutions, the Basel Committee realized that the approach of "one fits all" is hardly to meet the expectations outlined in the framwork, and therefore started with a series of reform to condition the requirements on the istitutions' size, complexity and systematic importance. This culminated once again in a series of on-going reform packages that is still happening today and should be published under the name: **Basel IV**.

### 3 Credit Risk - Empirical Analysis

After an introduction to the theoretical foundations of credit risk and a walk-through the cornerstone events that had a significant impact for the regulation of the environment, it is time to take a more empirical approach and see how can data be put into valuable use in the context of risk exposures towards counterparties' loans granted by a financial istitution. However, before jumping straight into the analysis, an high-level overview of credit risk modelling as to what it is intended within financial istitutions will be provided, along with and the key terminologies in this area

### 3.1 Credit risk modelling

### **3.1.1** Example

The motivation to develop internal credit risk models came, as we so before, from regulamentary requirements, but what was not stressed is the reason why this is such an important point for financial istitution. To better understand this, let us provide a simpliefied, but not too unrealistic example: imagine a bank is asked from a major tech company to provide a very huge loan in the size of \$5B. As already discussed, a credit analyst, who for ease the example we will call Benm will have to go through the request and see whether it is the case to grant or not this loan based on the information that he is able to gather. Let us assume that the analyst already knows that the CEO of this company has a great friendship relationship with the CFO of the bank, and, from recent studies, he discoveres that the specific sector of the company has recently experiences a steady drop in sales and moreover, the bank-internal rating system suggests this company is on its way down to a subinvestment grade (i.e. classified as risky investment). What should the analyst do at this point? The way to go usually boils down to 2 options at this point:

- 1. Reject the deal based on the information he has gather on the company and the relative market
- 2. Accept the deal BUT, protect the bank against potential losses thanks to **credit risk management instruments** (such as credit derivatives) and transfer the risk to a third-party in exchange of a fee

Hence, financial istitutions have also a way out: as individuals would do with health insurance, banks can protect themselves from the underlying exposures to risk when lending to particularly risky clients. In particular, banks had already designed ways to get loan insurance in the past and usually comprises the whole bank's credit risk portfolio, and not only some critical positions. This brings directly to the building block of credit risk modelling within a financial istitution: the **expected loss** 

### 3.1.2 Expected Loss

In order for banks to protect against this risk, they would like to know the cost that arises from a particular client (a group of clients in the case of portfolio) prior to granting the loan, so that they can charge a premium on the interest rate accordingly and add up to a reserve (also calles expected loss reserve) to cover for potential losses due to defaulting loans. What the bank is really interest here then is to know, on average, the potential loss that might occur when lending money to a client. This is also known as **Expected Loss**, and it is characterized by the following 3 main building blocks of credit risk modelling:

- 1. **Probability of Default (PD)**: the *likelihood* of a default in a defined time-horizon associated to a client. Note however that this is a general definition that may vary depending on the method used to estimate such probability. For instance, under the Basel II IRB framework, the PD per rating rate is defined as the average percentage percentage of obligators that will default over a one-year period, the time-horizon specified in the regulation for each asset class.
- 2. Exposure At Default (EAD): estimated outstanding amount given that a client defaulted
- 3. Loss Given Default (LGD): proportion of EAD that is expected not to be recovered in case of default.

The model describing the expected loss is defined on top of a probability space  $(\Omega, \Phi, \mathcal{P})$ , where  $\Omega$  consists of the sample space defining all the possible events,  $\Phi$  is the  $\sigma$ -Algebra containing all the measurable events of the sample space (such as the information on whether an obligator defaults or not) and lastly,  $\mathcal{P}$ , the probability space, which attaches a probability to each measurable event.

If we declare  $D_i$  as the event that the client 'i' defaults within a time-horizon and  $\mathcal{P}(D_i)$  as the proability associated to this event, then the loss related to the obligator can be then defined as:

$$L_i = I * EAD_i * LGD_i$$
 with  $I = \mathbf{1}_{D_i}, \quad \mathcal{P}(D_i) = PD_i$  (1)

where I is equal to the *indicator function* of the underlying event D. The variable takes value 1 when the event occur (i.e. default) and 0 when it does not occur. Note that this is a Bernoulli R.V., and as such, the expectation is equal to the probability of the event to occur. In other words, it is equal to the *Probability of Default (PD)*. Before laying down the formula of *Expected Loss*, another clarification should be provided:

- 1. To keep things simple, we will assume that the 3 constituents of the loss formula (i.e. PD, EAD, LGD) are independent among each other. Despite being a more than questionable statement and far from being true in general, this setting will allow us to state the most simple formula for the *Expected loss*.
- 2. To be able to simply define the expected loss over the whole portfolio of obligations, we also assume the joint distribution to be composed of independent and identically distributed R.V., each describing the expected loss of a specific obligator (i).

The formula of the expected loss of an obligator now comes very naturally as it is simply the expectation of the loss function defined above:

$$E[L_i] = \mathcal{P}(D_i) * EAD_i * LGD_i \tag{2}$$

where  $\mathcal{P}(D_i)$  represents the expectation of I.

At this point, it is possible to identify the expected loss of a portfolio as the proportion of obligators that might default over a time-horizon, multiplied by the expected portion of the total expected exposures that is assumed not to be recovered if the default event occurs. More formally:

$$E[L_P] = \sum_{i=1}^{N} \mathcal{P}(D_i) * EAD_i * LGD_i$$
(3)

### 3.1.3 Unexpected Loss

Note that the formula to calculate the expected losses aims at measuring the **expected** proportion of losses due to defaulting obligators based on historical default experiences, but it does not consider the **unexpected** losses that might come up as a deviation from the average experienced losses of the past. The capital held to sustain losses should then consider both, and for the sake of completeness of this chapter, the formula will be provided here:

$$UL_P = \sum_{i=1}^{N} \sigma_i * \varphi_i \tag{4}$$

where  $\sigma_i$  is the individual standard deviation of credit losses for the obligator i, while  $\varphi_i$  indicates the correlation between the credit losses of individual i and all the other obligators in the portfolio.

After this brief parenthesis, let us go back to one of the key costituents of expected loss, the probability of default.

#### 3.1.4 Probability of Default

The probability of default will be the subject of our empirical analysis where, given a pool of counterparties and associated loans, we wish to estimate how likely a loan is to default based on the information provided.

Predicting the probability of default is in itself a very challenging task as often it envolves very complicated models that need to assign a probability to each of the client in the portfolio. Banks have set up multiple department (usually under the division "risk methodology") that are in charge of estimating the 3 main constituents of the expected loss as a way to keep the situation monitored and intervene when needed. Obviously, great importance is also given to the PD.

In principle, there are many methods to estimate the probability of de-

fault, but we will list only 3 different approaches and, for the scope of our analysis we will implement the last two listed here:

- 1. Calibration from the **market data**: calibrating default probabilities on market data is not an easy task, and for this reason, there are already ad-hoc models (such as the KVM-model) that take care of this. Another option is based on credit spreads of product bearing credit risk.
- 2. Calibration from the **ratings**: default probabilities are linked with ratings (e.g. AAA,AA,..., BBB, ...) which can be provided either by internal-based methodologies or by external rating agencies (e.g. Moody's, S&P, Fitch, ...)
- 3. **Model-based** calibration: lastly, it is possible to construct a model based on the available information on the obligator and the obligation and try to predict whether the counterparty will likely default or not on that loan. Note that the dependent variable here is treated as a binary variable (i.e. taking values 0 and 1 only) and for this reason we are actually approximating a probability towards either 0 or 1 for non-default and default events respectively.

The dataset on top of which the empirical analysis will be conducted provides a sample of counterparties and relative loans, along with some information on both. In particular, as a rating is attached to each loan, we might want to calibrate the probability of default on each loan and use that estimate as a benchmark to see how the model perform on the data.

## 3.2 Empirical work

Introduction to the empirical work

4 Blockchain and asymmetric information

# 5 References