

Mini project 2: Go Greedy Applying the Greedy Approach to real-world problems: Option 2

The number of participants: 2 students per project; the grade will be assigned at an individual level depending on the degree of contribution.

Presentation deadline: Same as the Final Exam

Deliveries

- A program in C++, MATLAB, or Python.
- The program must visualize the coverage that results from using your smart data acquisition mechanism.
- An experiment shows that your approach outperforms the area or sensor coverage of the naïve (pure greedy, and random) data acquisition policies while optimizing the budget.
- Presentation of your approach.
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Introduction

This mini-project explores the solution to a real problem using the programming tools and paradigms you have learned so far.

Rubric

This rubric only applies after the presentation; no presentation will result in a zero in this project.

- This project counts as FINAL EXAM and Mini Project 2.
- Program running: 50%
- Algorithm design: 20%
- Experiment design: 20
- Report: and presentation 10%

Learning Outcomes

Upon completing this mini-programming project, you will be able to:

1. Apply algorithm design to tackle a real problem.
2. Implement a solution, and choose the programming language that better fits the problem requirements.

3. Apply a greedy or Dynamic programming approach to solve a problem.
4. Experiment with design to demonstrate that your solution outperforms a given approach,

Problem Description

Orlando is becoming a smart city, namely, a city whose services and data support decisions. Thus, the town is interested in acquiring sensor readings of pollution at high granularity.

One of its main goals is to get a more accurate sense of the pollution levels in the city. Thus, the town subcontracts a data collection campaign to a new startup company in Lakeland. The company's name is (Data Structures & Algorithms -FALL2022). They specialize in profitable high-tech projects with a focus on algorithm design.

Sketching a data collection campaign

The first decision is to collect data with high granularity and accuracy. Thus, the company decides to crowdsource the data collection to all the citizens of Lakeland who own a smartphone. The recruitment campaign follows the next steps.

1. The company released an app that interested participants can download and install on their smartphones.
2. The app enables the necessary phone sensors to collect pollution data (assumption: all the phones have a sensor for that purpose)
3. The app allows participants to send to the company the following information: the sensing measurements, its location, and the bid price (asking price for the collected sample)
4. The company checks the data quality, selects the winners based on their competitive bid price, and notifies the selected winners.
5. The selected winners receive their bid price (payment for the samples).

The following graph shows an example of the locations of participants in a given city. Every participant submits the sensing sample location (GPS) and the collected sample's bid price.



Figure1. Case 1 Sketch of participants whose locations follow a uniform distribution.

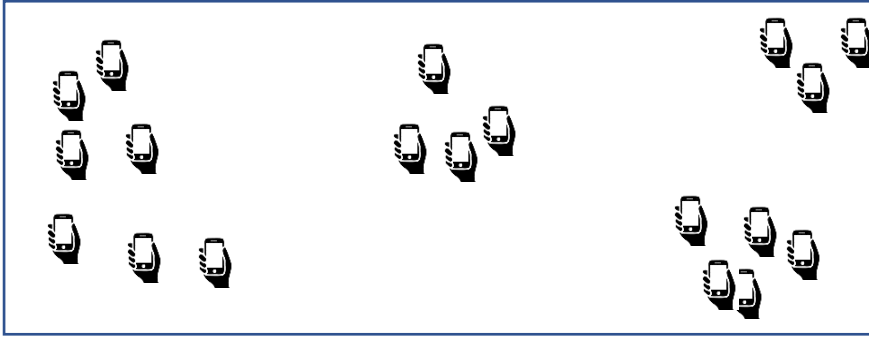


Figure 2. Case 2. More realistic distribution, people usually are in neighborhoods more clustered

Sensor model

We assume each phone sensor has a radius R at which is the sensing confidence

$$f(d(u_i, u_j)) = \begin{cases} 1 & \text{If } d(u_i, u_j) \leq R \\ 0 & \text{Otherwise} \end{cases}$$

Where $d(u_i, u_j)$ is the Euclidean distance between a sensor u_i and another sensor u_j , and $R > 0$ is a constant that defines each sensor's coverage area. Indeed, this function establishes a disk centered at sensor u_i with radius R . All sensors within such a disk have a coverage measure of 1 and are said to be covered by sensor u_i . On the other hand, all sensors outside of such a disk have a coverage measure of 0 and are said to be not covered by this sensor.

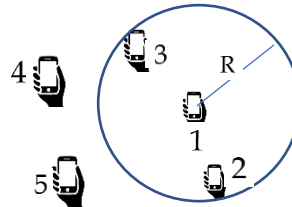


Figure 3. Sensor Model

Here, Figure 3 shows how the sensor centered at 1 covers sensors 1, 2, and 3, while sensors 4, and 5 are not covered.

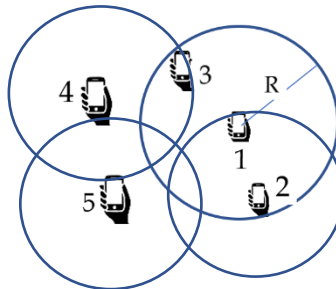


Figure 4. Sensor coverage when taking into account the disk of every sensor.

Figure 4 shows that sensor 4 covers sensor 4 and sensor 3, sensor 5 covers itself, and sensor 2 covers sensor 2 and sensor 1. Finally, sensor 1 covers sensor 1, sensor 2, and sensor 3. Thus, to cover all the sensors, we will have to buy the data of sensors 1, 2, 3, 4, and 5; however, we don't have the budget to buy all these samples. The question here is how to optimize the budget while maximizing the number of sensors covered.

Note that the sensing data provided by any phones within the area coverage (with the disk) of the center's phone is very similar.

Data acquisition Model

Here, the company allocates a budget and wants to acquire a representative set of samples within the given budget. However, if you wish to have a representative group of samples, you need to get samples from the different locations of the city, in other words, you want to maximize the area coverage.

Assumptions about the income distribution of the city

Let's assume that we have different neighborhoods with different average income distributions.

Thus, participants in low-income neighborhoods will ask for a low price for sensing samples, while those living in high-income areas will ask for a high price.

Naïve acquisition Model 1

We are acquiring all the samples offered by participants. Here, we have perfect coverage (see figure below). However, we don't have the money to buy all the samples, we have a limited budget, and we want to have some profit.

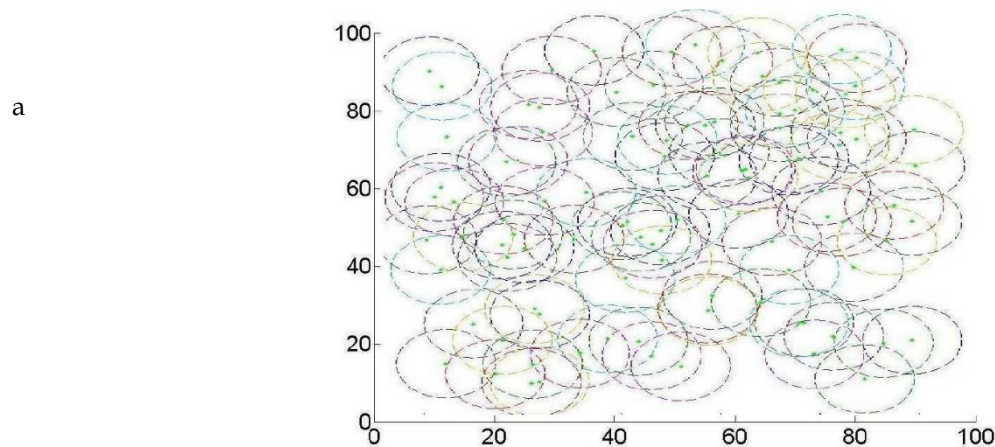


Figure 5. Acquiring all the samples, here we show a disk centered at each acquired sample.

Naïve approach Model 2: Slopy greedy

Use the budget to buy the cheapest sensing samples in ascending order until exhausting the budget. Figure 6 shows the result of this acquisition policy, given the city's income distribution.

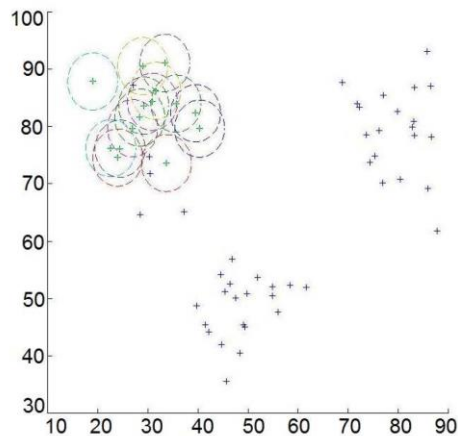


Figure 6. Data acquisition policy: Pure greedy

Here, we acquired a lot of sensing samples because participants from a populated low-income neighborhood were asking too low for their samples. Unfortunately, these readings do not constitute a representative sample of the city's pollution. We don't have samples of many places.

Your job (find a sub-set of samples that maximize coverage at minimum cost)

Design an algorithm to acquire sensing samples that maximize coverage (area or sensors) while minimizing the cost of acquisition. The running time of an exhaustive search (try all the combinations) is exponential and, therefore, not a feasible solution.

So, the company's job is to use engineering talent to design a solution (maybe greedy) to solve the problem.

Develop a solution, and show that your solution is better than

- 1) a random acquisition policy
- 2) better than a pure slopy greedy policy.

To show that your solution is better, you should generate the participants using a uniform and multi-normal distribution (generate the locations and the bits prices in clusters) to resemble the location of participants in low- and high-income neighborhoods.

Suggested strategies

This problem (find a sub-set of samples that maximize coverage at minimum cost) is a combinatorial

problem. So the exhaustive search for an optimal solution is exponential, as we learned during the first class of dynamic programming when reviewing the knapsack problem. Thus, a greedy solution getting us a sub-optimal (approximation) solution is acceptable. Therefore, you can try a greedy or a dynamic programming solution.

Check if any of these approaches could be helpful for you.

- Knapsack
- Set cover
- Budgeted Max

Tasks: Simulation

Generate the (GPS) locations (uniform, distributed, and clustered). Everything happens in a 100x100 grid

Generate the bid prices (cluster (normal distribution per cluster, and uniform distribution))

Other decisions to take

Budget=

Sensor Radius=

What are you covering: area? Or maybe other participants

What to do if you have some remaining money after buying the sensing samples.

Resources

Set Cover problem: A greedy approach to find a sub-optimal (approximation) solutions

<https://www.geeksforgeeks.org/greedy-approximate-algorithm-for-set-cover-problem/>

<https://math.mit.edu/~goemans/18434S06/setcover-tamara.pdf>

https://optimization.cbe.cornell.edu/index.php?title=Set_covering_problem

Knapsack (Greedy solutions)

Class slides (week 15)

<https://sites.radford.edu/~nokie/classes/360/greedy.html>

https://en.wikipedia.org/wiki/Knapsack_problem

<https://www.geeksforgeeks.org/fractional-knapsack-problem/>

The budgeted maximum coverage problem (Greedy paper attached with the project)

The Paper is attached to the project.