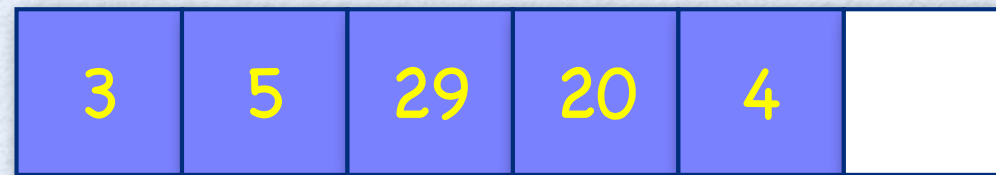


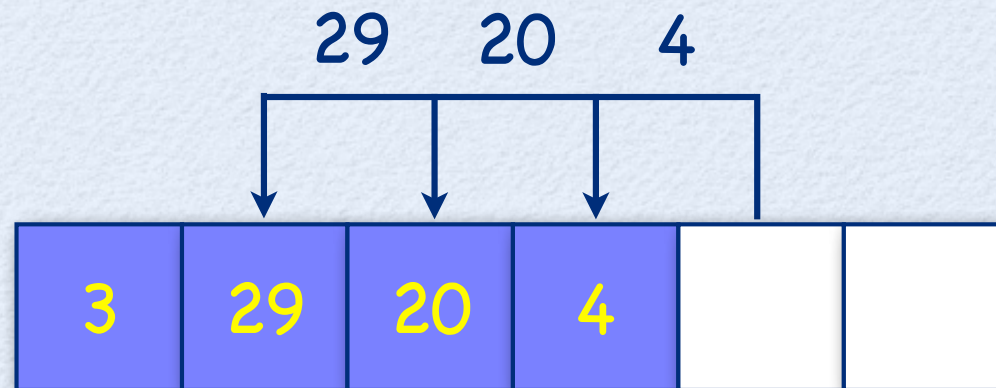
Problems with Arrays

- An array is a contiguous storage that provides insufficient abstractions for handling addition and deletion of elements.
- Addition and deletion require $n/2$ shifts on average.
- The computation time is $O(n)$.
- Resizing affects performance.

Deletion Requires Relocation



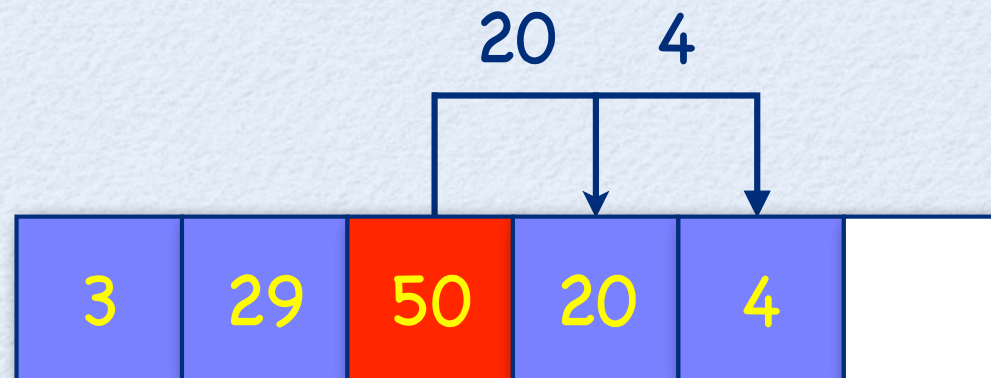
↑
Delete 5



Insertion Requires Relocation



Insert 50 after 29



Singly-Linked Lists

- A **singly-linked list** is a sequence of data items, each connected to the next by a pointer called **next**.

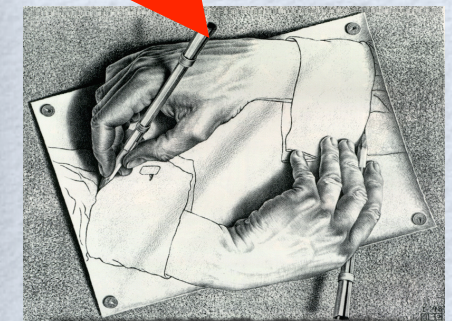


- A data item may be a primitive value, a composite value, or even another pointer.
- A singly-linked list is a recursive data structure whose nodes refers to nodes of the same type.

Impossible Singly-Linked List Structure in C++:

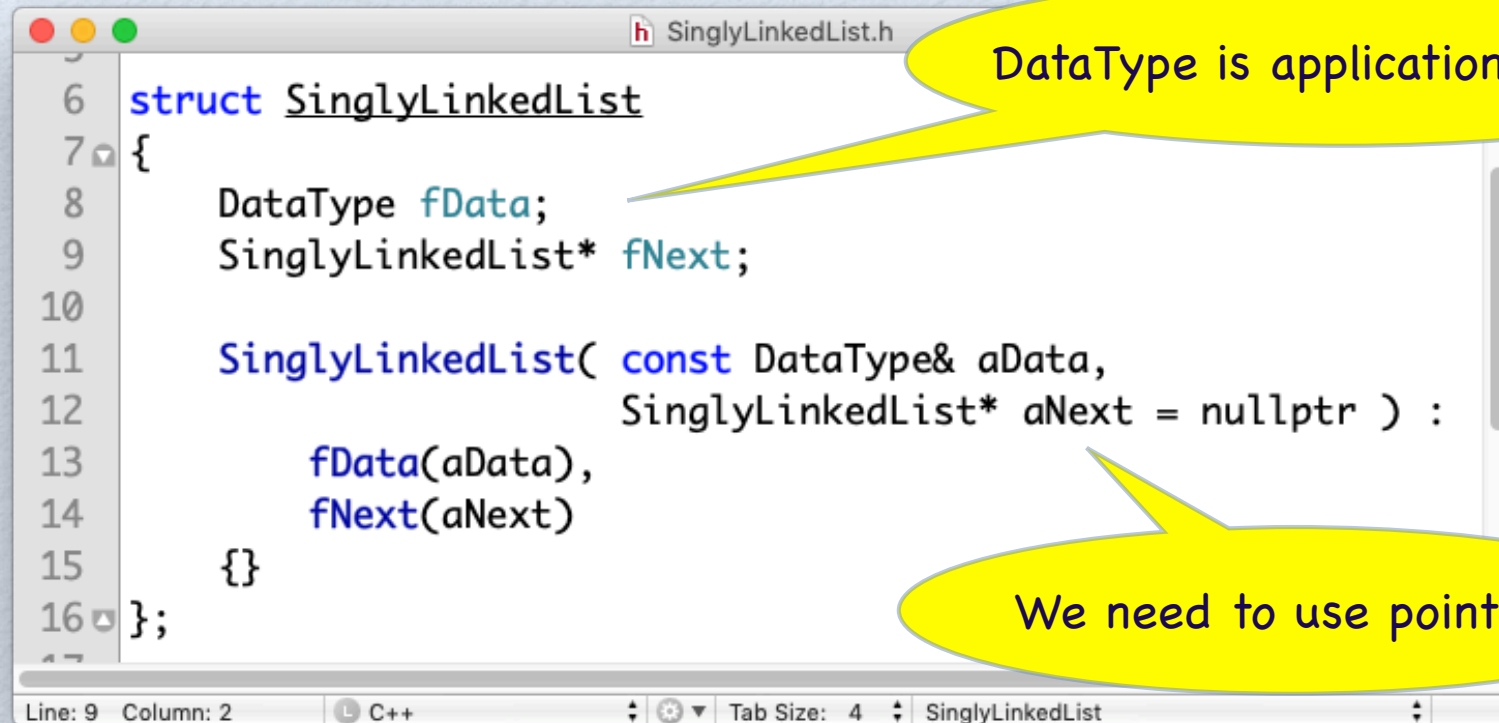
```
SinglyLinkedList.h
1 // impossible singly-linked list
2
3
4
5
6 // impossible singly-linked list
7
8 struct SinglyLinkedList
9 {
10     DataType fData;
11     SinglyLinkedList fNext;
12
13     SinglyLinkedList( const DataType& aData,
14                     const SinglyLinkedList& aNext ) :
15         fData(aData),
16         fNext(aNext)
17     {}
18 };
19
```

X = X → X → X → X → ...



Field fNext has incomplete type.

Singly-Linked List Using Pointers



```
6 struct SinglyLinkedList
7 {
8     DataType fData;
9     SinglyLinkedList* fNext;
10
11     SinglyLinkedList( const DataType& aData,
12                      SinglyLinkedList* aNext = nullptr ) :
13         fData(aData),
14         fNext(aNext)
15     {}
16 };
```

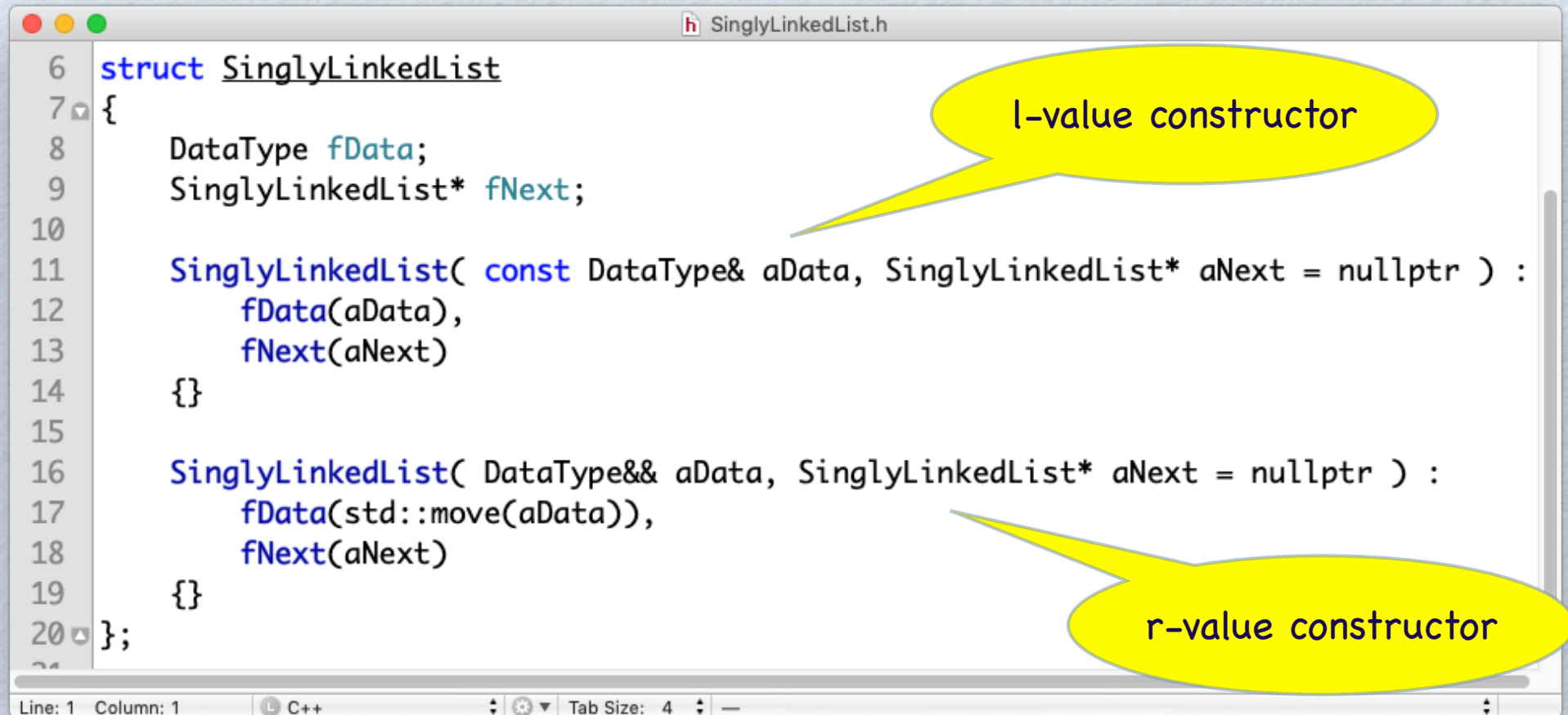
DataType is application-specific

We need to use pointers

Line: 9 Column: 2 C++ Tab Size: 4 SinglyLinkedList

- A list manages a collection of elements.
- The class `SinglyLinkedList` defines a value-based sequence container for values of type `DataType`.
- To break infinite recursion, we have to use pointers to the next elements. This way, the compiler can deduce the size of a singly-linked list element and compile the definition.

Singly-Linked List with R-Values



```
6 struct SinglyLinkedList
7 {
8     DataType fData;
9     SinglyLinkedList* fNext;
10
11     SinglyLinkedList( const DataType& aData, SinglyLinkedList* aNext = nullptr ) :
12         fData(aData),
13         fNext(aNext)
14     {}
15
16     SinglyLinkedList( DataType&& aData, SinglyLinkedList* aNext = nullptr ) :
17         fData(std::move(aData)),
18         fNext(aNext)
19     {}
20 };
```

l-value constructor

r-value constructor

- The r-value constructor can “steal” the memory of the argument `aData` to initialize the payload `fData`. To use this constructor, the parameter `aData` must be a temporary of literal value.

R-Value References (C++-11)

L-Values and L-Value References &

- The references that we have seen so far are l-value references, that is, references to l-values.
- The term **l-value** refers to a thing that can occur on the left side of an assignment, named objects that have a defined storage location (i.e., an address). **L-value references can only be bound to l-values** (exception: we can bind an r-value to a const l-value reference):

```
int var = 42;           // l-value: initialized variable declaration
```

```
int& ref = var;         // l-value reference to an l-value
```

```
int& ref2 = 42;         // error: non-const l-value reference cannot bind to temporary
```

```
const int& ref3 = 42;    // const l-value reference to an r-value
```


R-Values and R-Value References &&

- The term **r-value** refers to things that can occur on the right side of an assignment, literals and temporaries that **do not** have a defined storage locations.
- **R-value references only bind to r-values:**

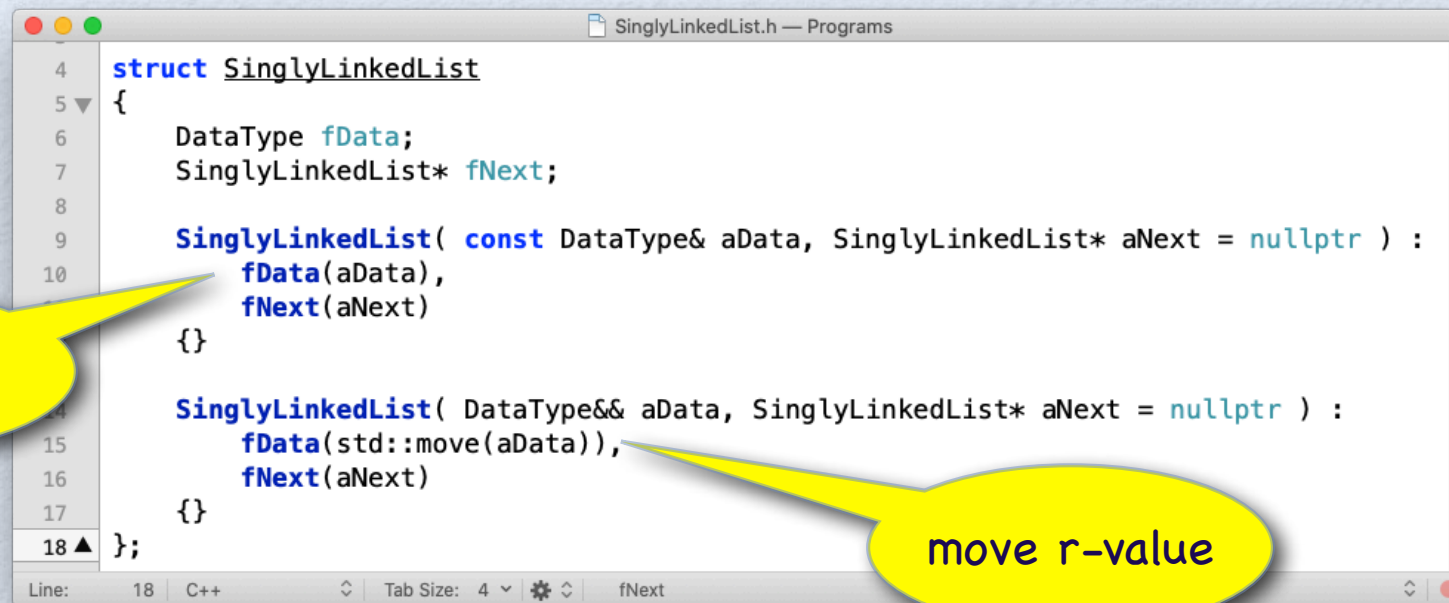
```
int&& ref = 42;      // r-value reference to an r-value
```

```
int val = 42;       // l-value: initialized variable declaration
```

```
int&& ref2 = val;    // error: r-value reference cannot bind to l-value
```


Move Semantics (std::move)

- R-values are typically temporary and so can be freely modified: if you know that your function parameter is an r-value, you can use it as temporary storage, or “steal” its contents without affecting program correctness.
- This means that rather than copying the contents (expensive) of an r-value, you can move the contents (cheap).



```
SinglyLinkedList.h — Programs
4  struct SinglyLinkedList
5  {
6      DataType fData;
7      SinglyLinkedList* fNext;
8
9      SinglyLinkedList( const DataType& aData, SinglyLinkedList* aNext = nullptr ) :
10         fData(aData),
11         fNext(aNext)
12     {}
13
14     SinglyLinkedList( DataType&& aData, SinglyLinkedList* aNext = nullptr ) :
15         fData(std::move(aData)),
16         fNext(aNext)
17     {}
18 };
```

copy l-value

move r-value

std::move is a function that performs a type cast of its argument to an r-value.

Using L-Values and R-Values

```
SinglyLinkedList.h — Programs
4 struct SinglyLinkedList
5 {
6     DataType fData;
7     SinglyLinkedList* fNext;
8
9     SinglyLinkedList( const DataType& aData, SinglyLinkedList* aNext = nullptr ) :
10         fData(aData),
11         fNext(aNext)
12     {}
13
14     SinglyLinkedList( DataType&& aData, SinglyLinkedList* aNext = nullptr ) :
15         fData(std::move(aData)),
16         fNext(aNext)
17     {}
18 };
```

- Using the different constructors, we can write:

```
string lValue = "COS30008";
SinglyLinkedList lNodeWithCopy( lValue );
SinglyLinkedList lNodeWithMove( "COS30008" );
```

copy
l-value

move
r-value

Using L-Values and R-Values: No Move

```
SinglyLinkedList.h — Programs
4 struct SinglyLinkedListCopyOnly
5 {
6     DataType fData;
7     SinglyLinkedListCopyOnly* fNext;
8
9     SinglyLinkedListCopyOnly( const DataType& aData, SinglyLinkedList* aNext = nullptr ) :
10         fData(aData),
11         fNext(aNext)
12     {}
13 };
Line: 15:19 C++ Tab Size: 4 SinglyLinkedList
```

- If a class does not support move semantics, then the compiler will use copy semantics. That is, an r-value decays to an l-value.

```
string lValue = "COS30008";
```

```
SinglyLinkedListCopyOnly lNodeWithLValue( lValue );
```

```
SinglyLinkedListCopyOnly lNodeWithRValue( "COS30008" );
```

copy l-value

copy
r-value

**We discuss more details
later when we study
memory management.**

A Simple List of Integers

```
2  #include <iostream>
3  #include <string>
4
5  using namespace std;
6
7  using DataType = string;
8
9  #include "SinglyLinkedList.h"
10
11 int main()
12 {
13     string lA = "AAAA";
14     string lC = "CCCC";
15
16     SinglyLinkedList One( lA );
17     SinglyLinkedList Two( "BBBB", &One );
18     SinglyLinkedList Three( lC, &Two );
19
20     SinglyLinkedList* lTop = &Three;
21
22     for ( ; lTop != nullptr; lTop = lTop->fNext )
23     {
24         cout << "Value: " << lTop->fData << endl;
25     }
26
27     return 0;
28 }
29
```

define DataType a synonym for string

```
Microsoft Visual Studio Deb...
Value: CCCC
Value: BBBB
Value: AAAA
```


Using Declaration — C++11 Type Aliases

- A type alias is a name that refers to a previously defined type.

```
using identifier = type;
```

- Type aliases are commonly used for three purposes:
 - To hide the implementation of a given type.
 - To streamline complex type definitions making them easier to understand, and
 - To allow a single type to be used in different contexts under different names.
- Type aliases establish a **nominal equivalence between types**.
- Type aliases are similar to **typedef**. However, type aliases are better suited when creating alias templates.



Can we do better?

Templates – C++'s Generic Types

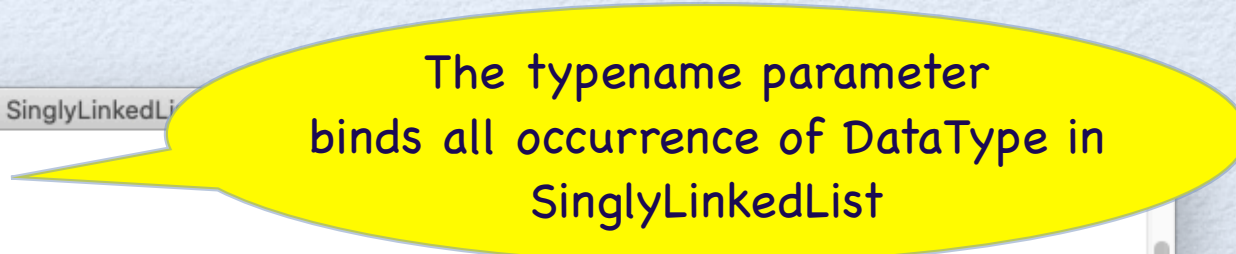
- Templates are **blueprints** from which classes and/or functions are automatically generated by the compiler based on a set of parameters.
- Note, every time a given template is being instantiated with type parameters that have not been used before, a **new version** of the class or function is generated.
- A new version of a class or function is called specialization of the template. **Specializations are not mutually compatible.**

Class Template

```
template<typename T1, ..., typename Tn>
class AClassTemplate
{
    // class specification
};
```

- A template is a parameterized abstraction over a class.
- From the language-theoretical perspective, templates are 2nd order functions from types to classes/functions.
- To instantiate a class template we supply the desired types, as actual template parameters, so that the C++ compiler can synthesize a specialized class for the template.

Singly-Linked List Class Template



```
3
4  template <typename DataType>
5  struct SinglyLinkedList
6  {
7      DataType fData;
8      SinglyLinkedList* fNext;
9
10     SinglyLinkedList( const DataType& aData, SinglyLinkedList* aNext = nullptr ) :
11         fData(aData),
12         fNext(aNext)
13     {}
14
15     SinglyLinkedList( DataType&& aData, SinglyLinkedList* aNext = nullptr ) :
16         fData(std::move(aData)),
17         fNext(aNext)
18     {}
19 };
20
```

Line: 1 C++ Tab Size: 4

The New Main

```
1  #include <iostream>
2  #include <string>
3
4  using namespace std;
5
6  #include "SinglyLinkedListTemplate.h"
7
8  int main()
9  {
10
11     using StringList = SinglyLinkedList<string>;
12
13     string lA = "AAAA";
14     string lC = "CCCC";
15
16     StringList One( lA );
17     StringList Two( "BBBB", &One );
18     StringList Three( lC, &Two );
19
20     StringList* lTop = &Three;
21
22     for ( ; lTop != nullptr; lTop = lTop->fNext )
23     {
24         cout << "Value: " << lTop->fData << endl;
25     }
26
27     return 0;
28 }
```

We instantiate the template SinglyLinkedList to SinglyLinkedList<string>.

Class Template Instantiation

```
using IntegerList = SinglyLinkedList<int>;
```

```
using ListOfIntegerLists = SinglyLinkedList<IntegerList>;
```

- Types used as arguments cannot be classes with local scope.
- Once instantiated, a class template can be used as any other class.

List Iterator Template

SinglyLinkedList Iterator Specification

```
SinglyLinkedListIterator SPEC.h — Programs
2  #pragma once
3
4  #include "SinglyLinkedListTemplate.h"
5
6  template <typename T>
7  class SinglyLinkedListIterator
8  {
9  private:
10
11     using ListNode = SinglyLinkedList<T>;
12
13     const ListNode* fList;
14     const ListNode* fIndex;
15
16 public:
17
18     using Iterator = SinglyLinkedListIterator<T>;
19
20     SinglyLinkedListIterator( const ListNode* aList );
21
22     const T& operator*() const;
23     Iterator& operator++();      // prefix
24     Iterator operator++(int);    // postfix
25     bool operator==( const Iterator& aRHS ) const;
26     bool operator!=( const Iterator& aRHS ) const;
27
28     Iterator begin();           // for-range feature
29     Iterator end();             // for-range feature
30 };
31
Line: 32 C++ Tab Size: 4 end
```

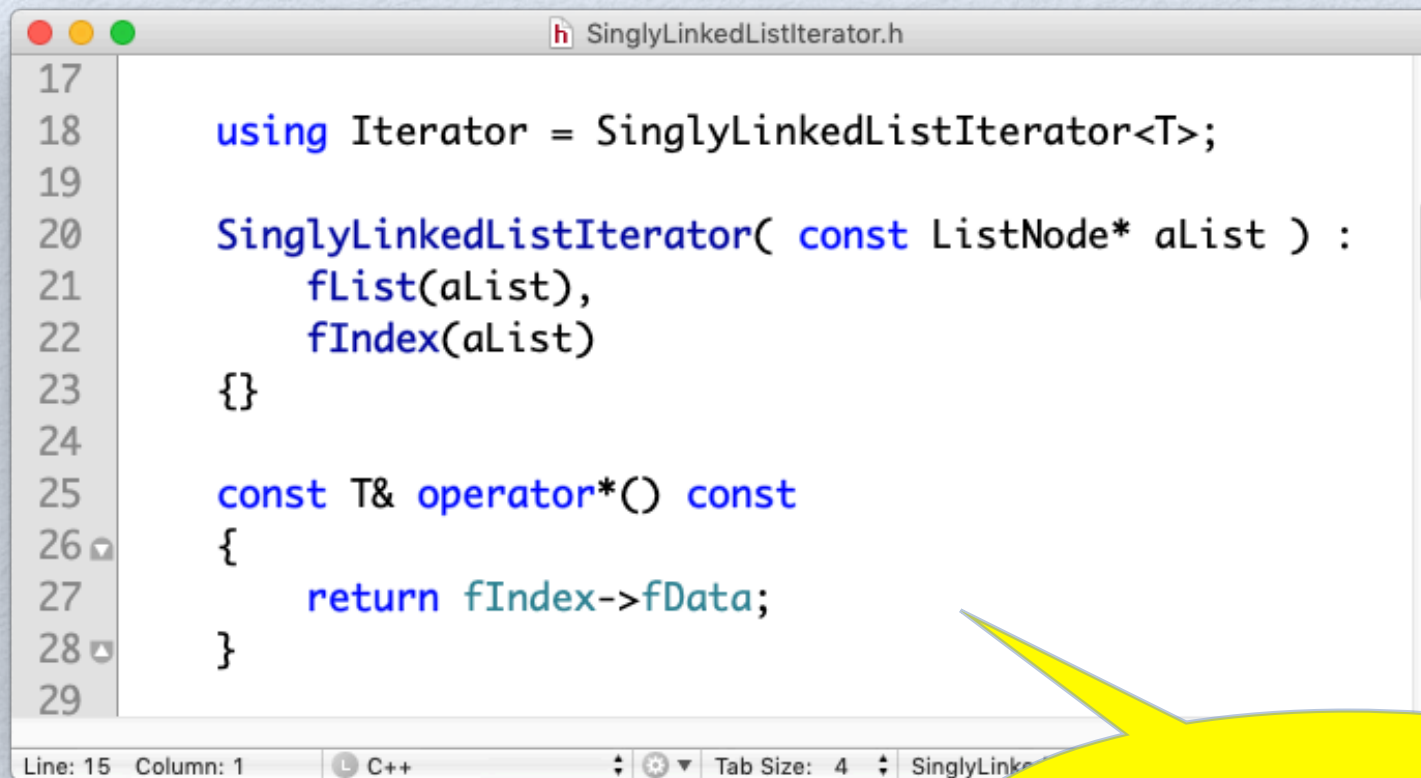
We maintain a pointer to read-only list elements

Notes on Templates

- When using templates, the C++ compiler must have access not only the specification of a template class but also to all method implementations in order to properly instantiate the template.
- Templates are not to be confused with library classes. Templates are blueprint that have to be instantiated for each separate type application.
- Think of templates as special forms of macros.
- When defining a template class, we need to implement, like in Java, all methods within the class definition, usually in a header file.

Templates have no .cpp file!

Constructor & Deference

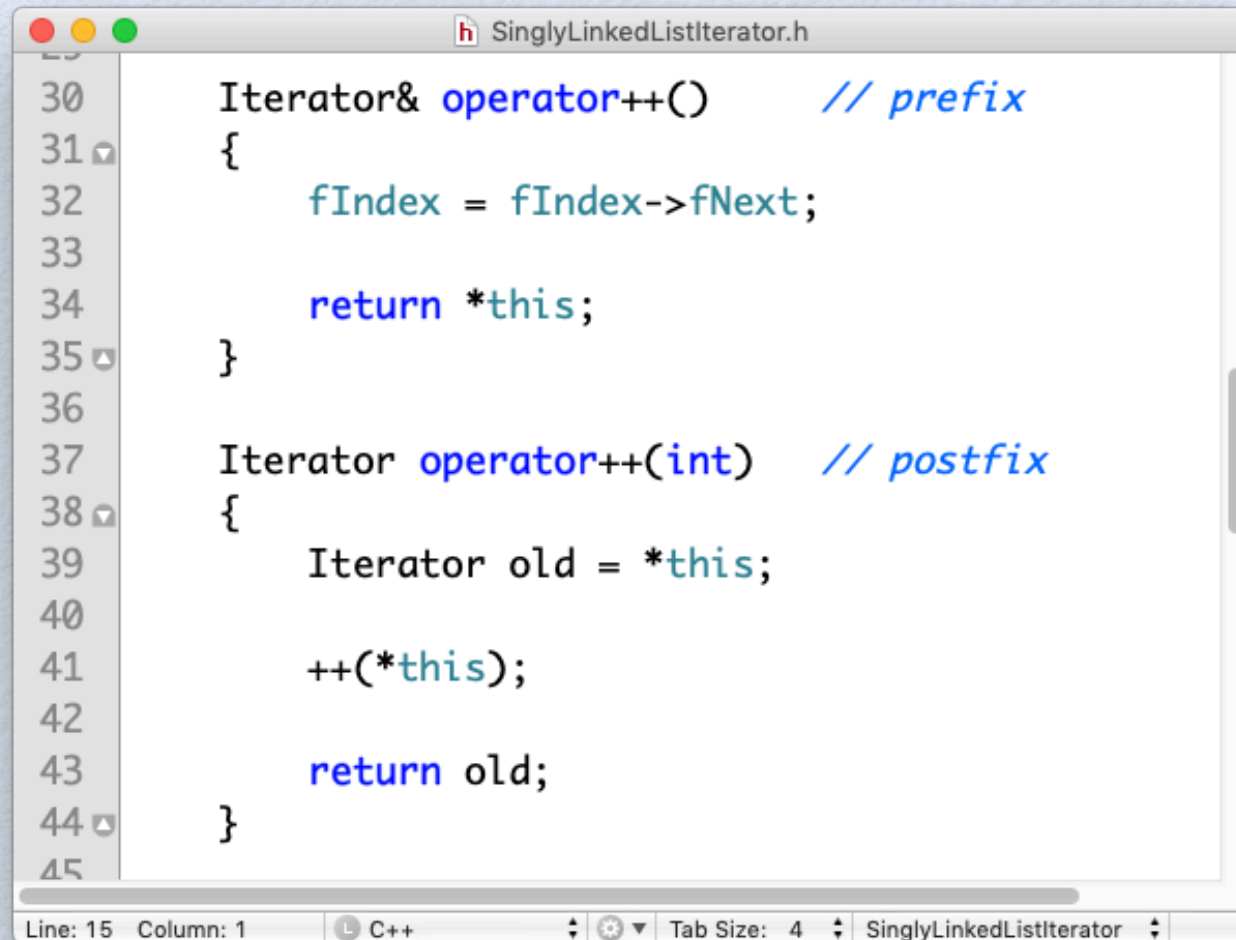


```
17
18     using Iterator = SinglyLinkedListIterator<T>;
19
20     SinglyLinkedListIterator( const ListNode* aList ) :
21         fList(aList),
22         fIndex(aList)
23     {}
24
25     const T& operator*() const
26     {
27         return fIndex->fData;
28     }
29
```

Line: 15 Column: 1 C++ Tab Size: 4 SinglyLink

For iterator implementation in header file.

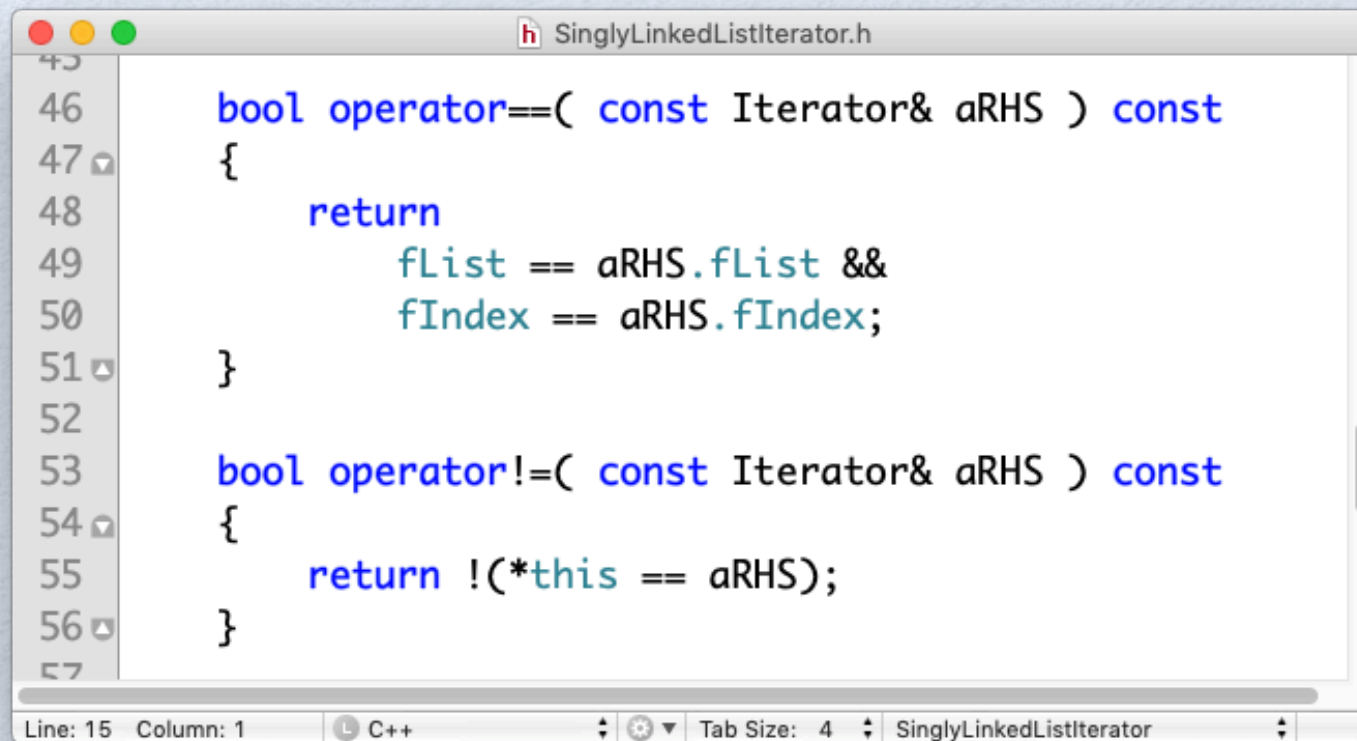
Increments



```
SinglyLinkedListIterator.h  
30  Iterator& operator++()      // prefix  
31  {  
32      fIndex = fIndex->fNext;  
33  
34      return *this;  
35  }  
36  
37  Iterator operator++(int)    // postfix  
38  {  
39      Iterator old = *this;  
40  
41      ++(*this);  
42  
43      return old;  
44  }  
45
```

Line: 15 Column: 1 C++ Tab Size: 4 SinglyLinkedListIterator

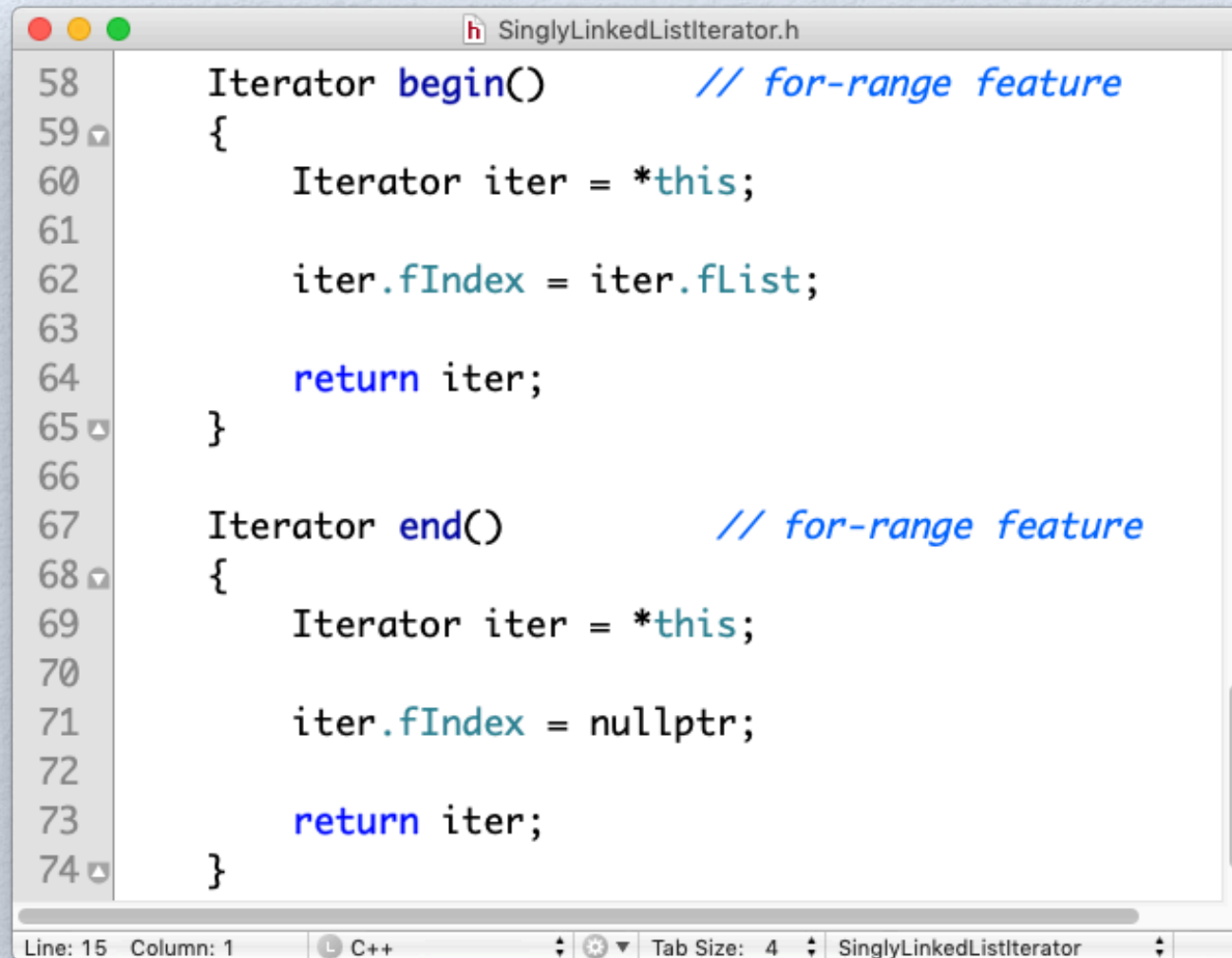
Equivalence



```
SinglyLinkedListIterator.h
45
46     bool operator==( const Iterator& aRHS ) const
47     {
48         return
49             fList == aRHS.fList &&
50             fIndex == aRHS.fIndex;
51     }
52
53     bool operator!=( const Iterator& aRHS ) const
54     {
55         return !(*this == aRHS);
56     }
57
```

Line: 15 Column: 1 C++ Tab Size: 4 SinglyLinkedListIterator

Auxiliaries (For-Range)



```
58     Iterator begin()           // for-range feature
59     {
60         Iterator iter = *this;
61
62         iter.fIndex = iter.fList;
63
64         return iter;
65     }
66
67     Iterator end()             // for-range feature
68     {
69         Iterator iter = *this;
70
71         iter.fIndex = nullptr;
72
73         return iter;
74     }
```

Line: 15 Column: 1 C++ Tab Size: 4 SinglyLinkedListIterator

SinglyLinkedList Iterator Test

```
2  #include <iostream>
3  #include <string>
4
5  using namespace std;
6
7  #include "SinglyLinkedListIterator.h"
8
9  int main()
10 {
11     using StringList = SinglyLinkedList<string>;
12     using StringListIterator = SinglyLinkedListIterator<string>;
13
14     string lA = "AAAA";
15     string lC = "CCCC";
16
17     StringList One( lA );
18     StringList Two( "BBBB", &One );
19     StringList Three( lC, &Two );
20
21     for ( const string& i : StringListIterator( &Three ) )
22     {
23         cout << "Value: " << i << endl;
24     }
25
26     return 0;
27 }
```

For iterator implementation
see Canvas

address of Three

SinglyLinkedList Iterator: Specification B

```
SinglyLinkedListIteratorB SPEC.h — Programs
1
2
3 #include "SinglyLinkedListTemplate.h"
4
5 template <typename T>
6 class SinglyLinkedListIterator
7 {
8 private:
9
10     using ListNode = SinglyLinkedList<T>;
11
12     const ListNode& fList;
13     const ListNode* fIndex;
14
15 public:
16
17     using Iterator = SinglyLinkedListIterator<T>;
18
19     SinglyLinkedListIterator( const ListNode& aList );
20
21     const T& operator*() const;
22     Iterator& operator++();           // prefix
23     Iterator operator++(int);         // postfix
24     bool operator==( const Iterator& aRHS ) const;
25     bool operator!=( const Iterator& aRHS ) const;
26
27     Iterator begin();                 // for-range feature
28     Iterator end();                   // for-range feature
29 };
30
31 C++ Tab Size: 4 end
```

We maintain a read-only
reference to list elements

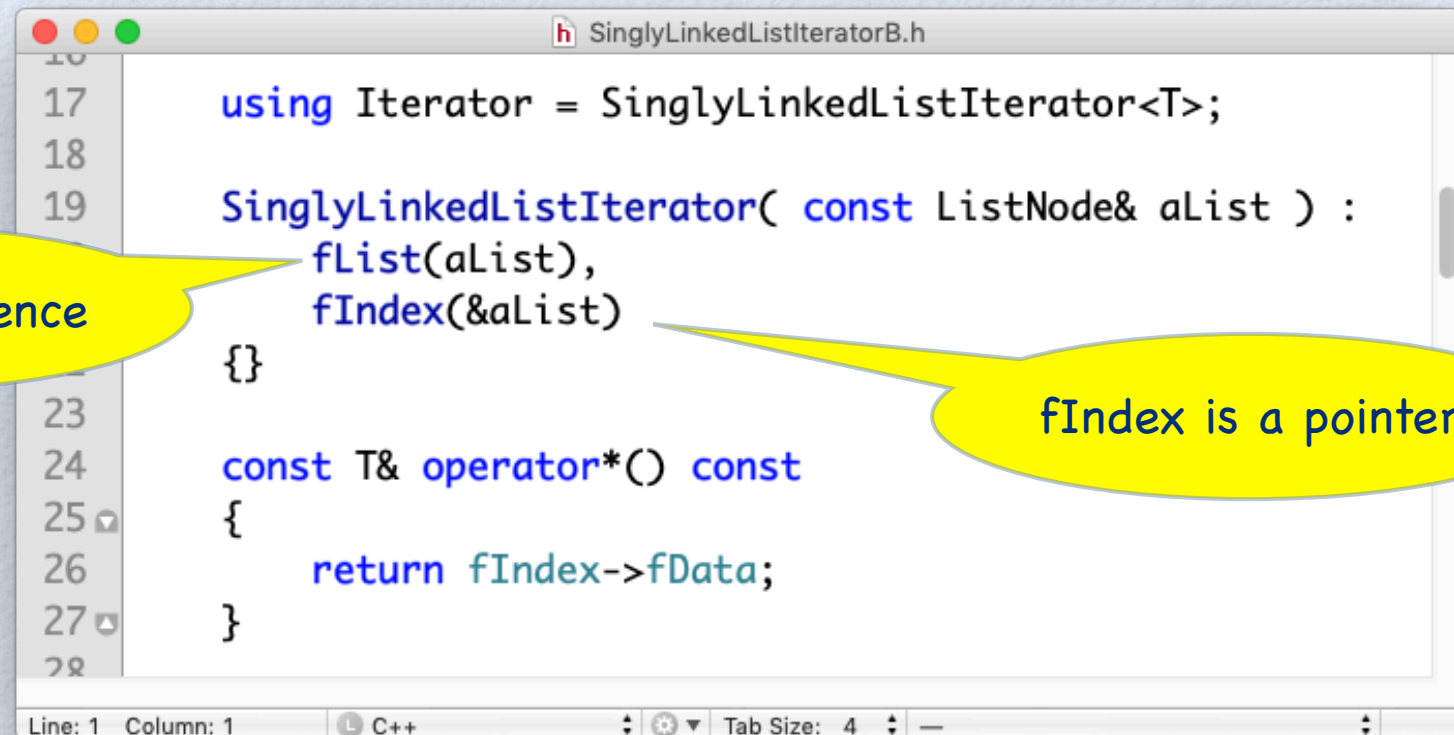
Reference Data Members

```
class ClassWithRefMember
{
private:
    SomeType& fRef;
public:
    ClassWithRefMember( SomeType& aRef ) : fRef(aRef)
    { ... }
};
```

Reference data members must be initialized before the constructor body is entered!

- Reference member variables store references to data outside an object. These references are established upon object creation via a member initializer.
- In case of iterators this might be an attractive option to avoid coping the underlying collection.
- Important: Reference data members require a constructor initializer.

Constructor & Deference B



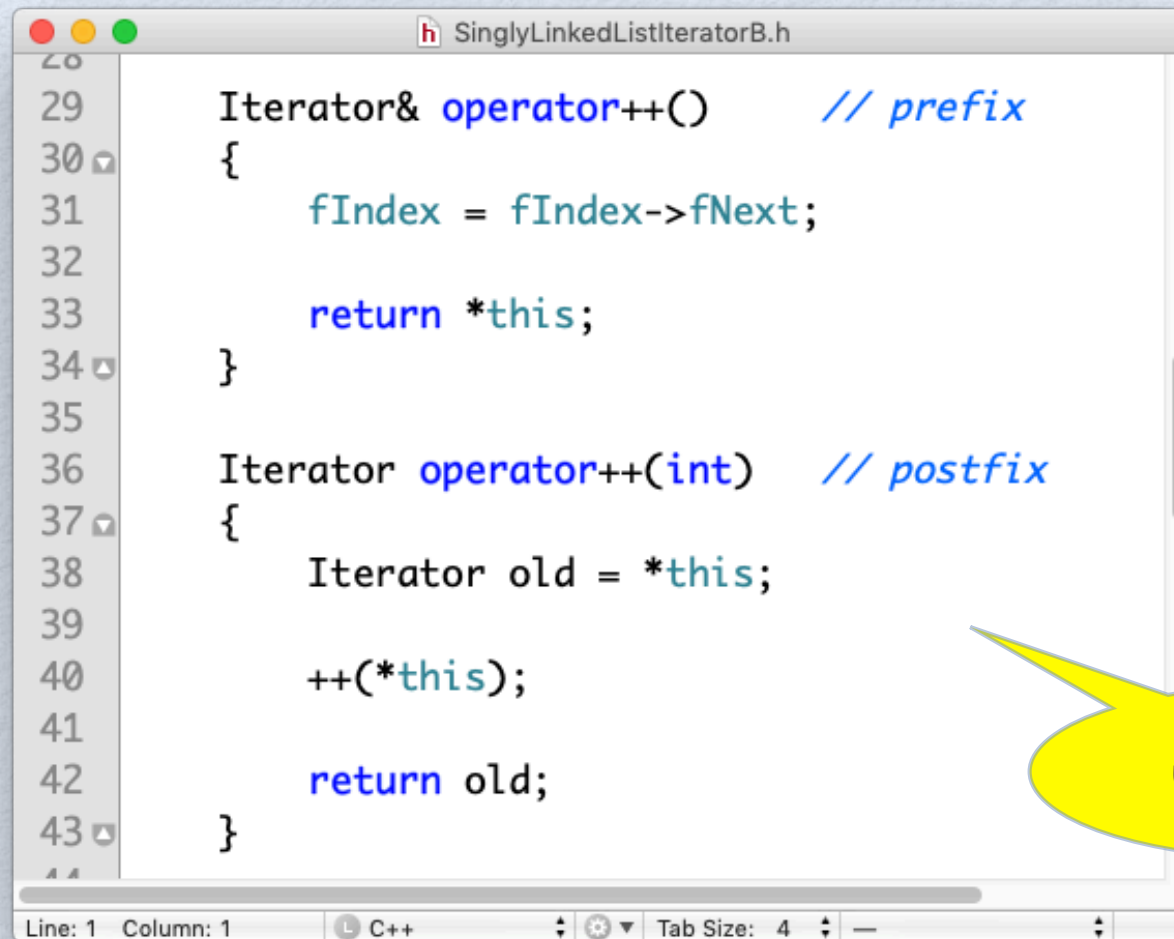
```
16
17 using Iterator = SinglyLinkedListIterator<T>;
18
19 SinglyLinkedListIterator( const ListNode& aList ) :
    fList(aList),
    fIndex(&aList)
20 {}
21
22
23
24 const T& operator*() const
25 {
26     return fIndex->fData;
27 }
28
```

Establish reference

fIndex is a pointer

Line: 1 Column: 1 C++ Tab Size: 4

Increments B

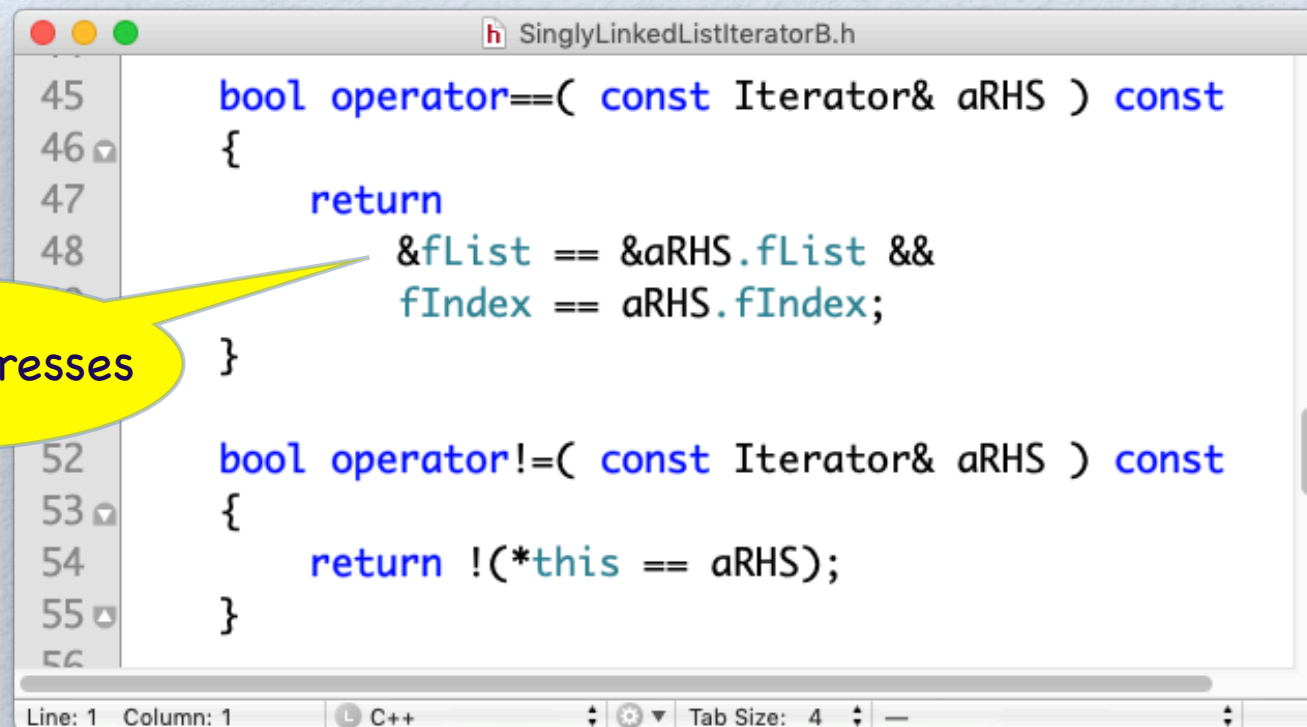


```
28
29  Iterator& operator++()    // prefix
30  {
31      fIndex = fIndex->fNext;
32
33      return *this;
34  }
35
36  Iterator operator++(int)  // postfix
37  {
38      Iterator old = *this;
39
40      ++(*this);
41
42      return old;
43  }
```

unchanged

Line: 1 Column: 1 C++ Tab Size: 4

Equivalence B

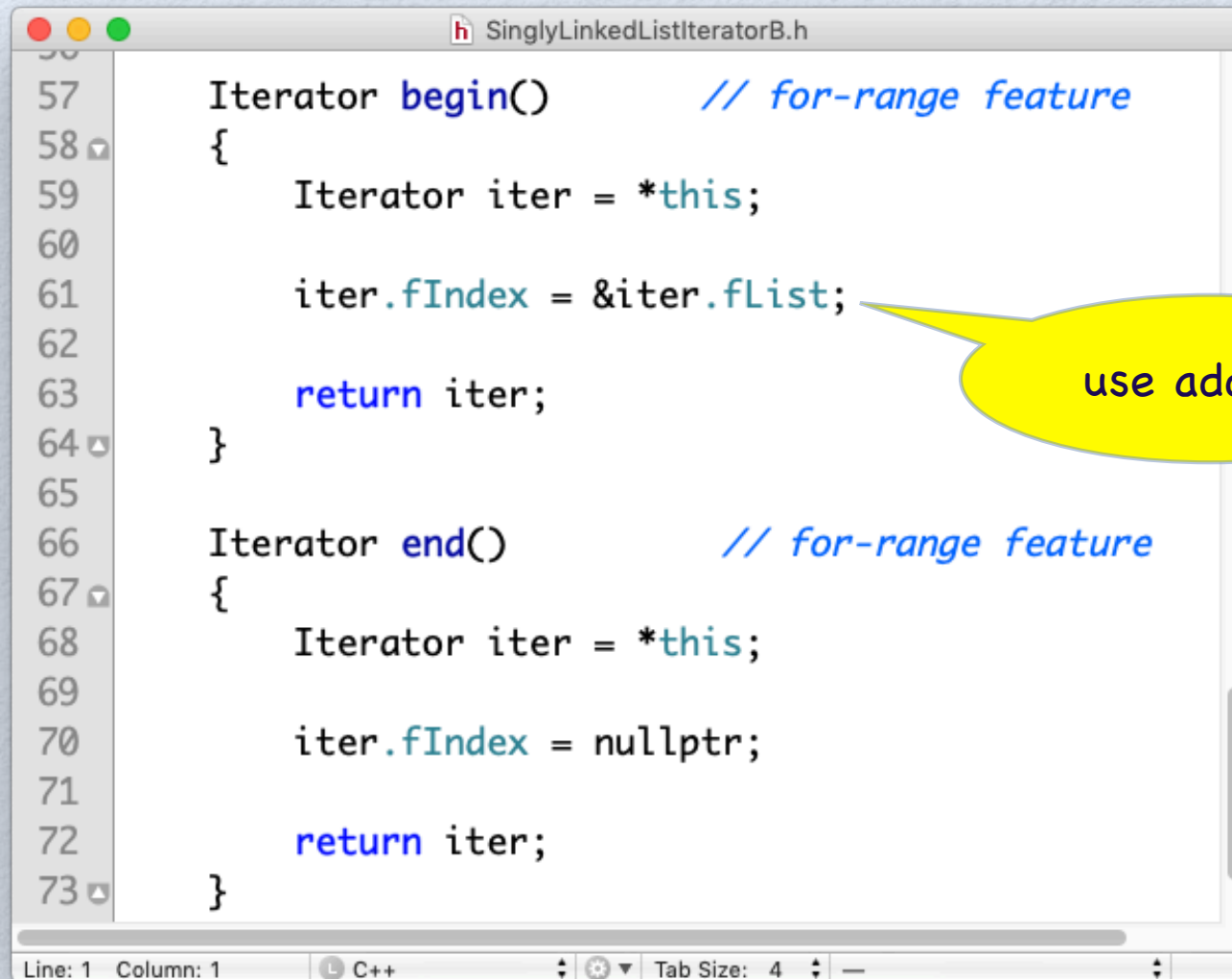


```
SinglyLinkedListIteratorB.h
45  bool operator==( const Iterator& aRHS ) const
46  {
47      return
48          &fList == &aRHS.fList &&
          fIndex == aRHS.fIndex;
49  }
50
52  bool operator!=( const Iterator& aRHS ) const
53  {
54      return !(*this == aRHS);
55  }
56
```

compare addresses

Line: 1 Column: 1 C++ Tab Size: 4

Auxiliaries (For-Range) B



```
57  Iterator begin()           // for-range feature
58  {
59      Iterator iter = *this;
60
61      iter.fIndex = &iter.fList;
62
63      return iter;
64  }
65
66  Iterator end()             // for-range feature
67  {
68      Iterator iter = *this;
69
70      iter.fIndex = nullptr;
71
72      return iter;
73  }
```

use address

Line: 1 Column: 1 C++ Tab Size: 4

SinglyLinkedList Iterator Test B

```
1  #include <iostream>
2  #include <string>
3
4  using namespace std;
5
6  #include "SinglyLinkedListIteratorB.h"
7
8  int main()
9  {
10     using StringList = SinglyLinkedList<string>;
11     using StringListIterator = SinglyLinkedListIterator<string>;
12
13     string lA = "AAAA";
14     string lC = "CCCC";
15
16     StringList One( lA );
17     StringList Two( "BBBB", &One );
18     StringList Three( lC, &Two );
19
20     for ( const string& i : StringListIterator( Three ) )
21     {
22         cout << "Value: " << i << endl;
23     }
24
25     return 0;
26 }
27
```

For iterator implementation
see Canvas

Three passed as
l-value reference

Pointers

The Need for Pointers

- A linked-list is a dynamic data structure with a varying number of nodes.
- Access to a linked-list is through a **pointer variable** in which the **base type** is the same as the node type:

```
IntegerList<int>* pListOfIntegers = &Three;
```

```
IntegerList<int>* Nil = nullptr;
```

Nil means "empty list."

Node Construction

```
IntegerList *p, *q;
```

```
p = new IntegerList( 5 );
```

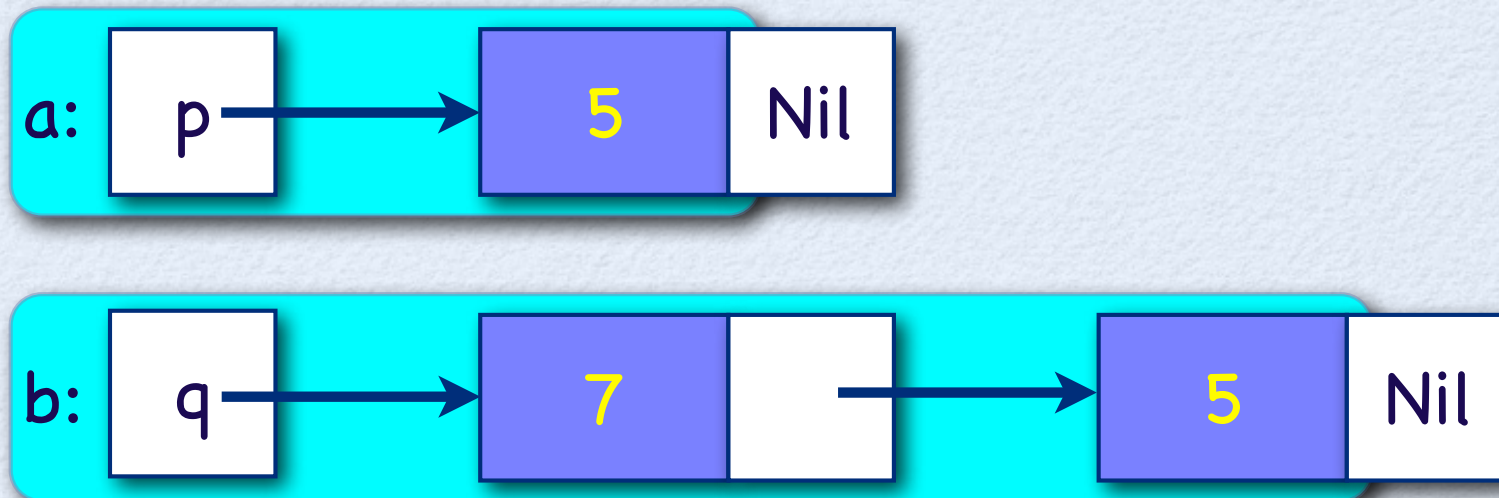
```
q = new IntegerList( 7, p );
```



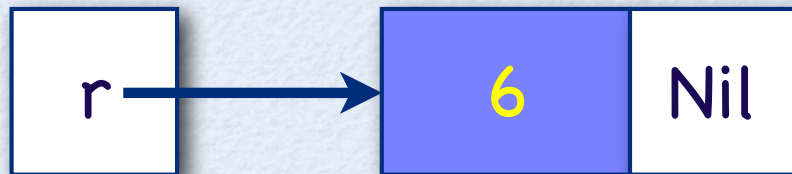
Node Access

```
int a = p->fData;
```

```
int b = q->fNext->fData;
```

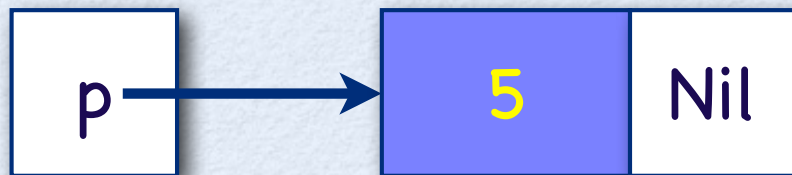


Inserting a Node



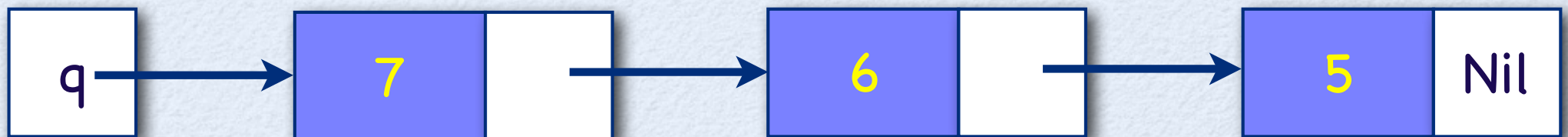
```
IntegerList *r;
```

```
r = new IntegerList( 6 );
```

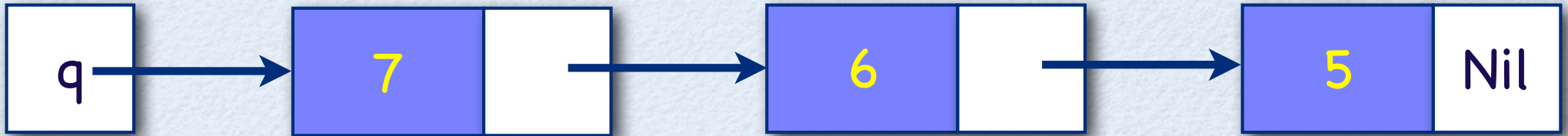


```
r->fNext = p;
```

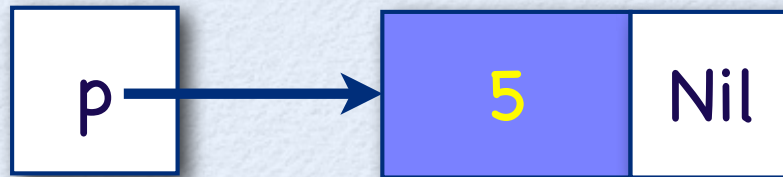
```
q->fNext = r;
```



Deleting a Node



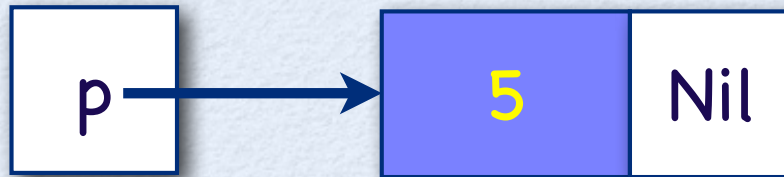
$q \rightarrow \text{fNext} = q \rightarrow \text{fNext} \rightarrow \text{fNext};$



Insert at the Top

```
IntegerList *p = nullptr;
```

```
p = new IntegerList( 5, p );
```

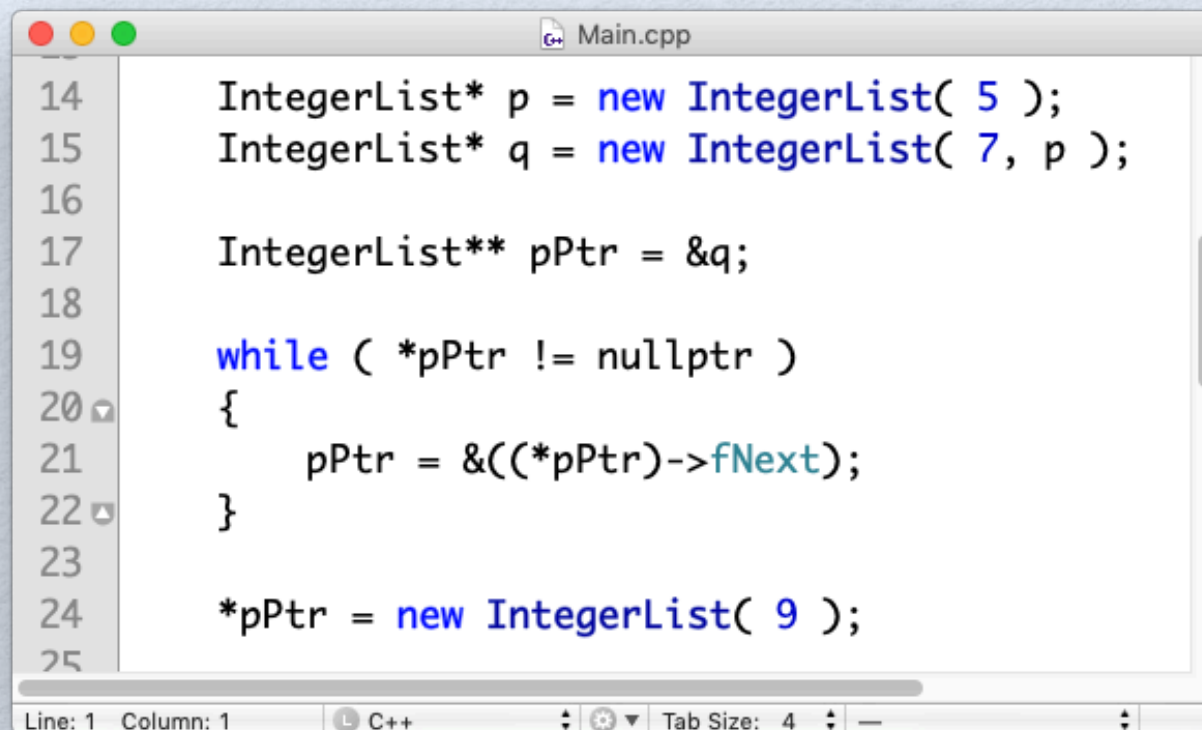


```
p = new IntegerList( 7, p );
```



Insert at the End

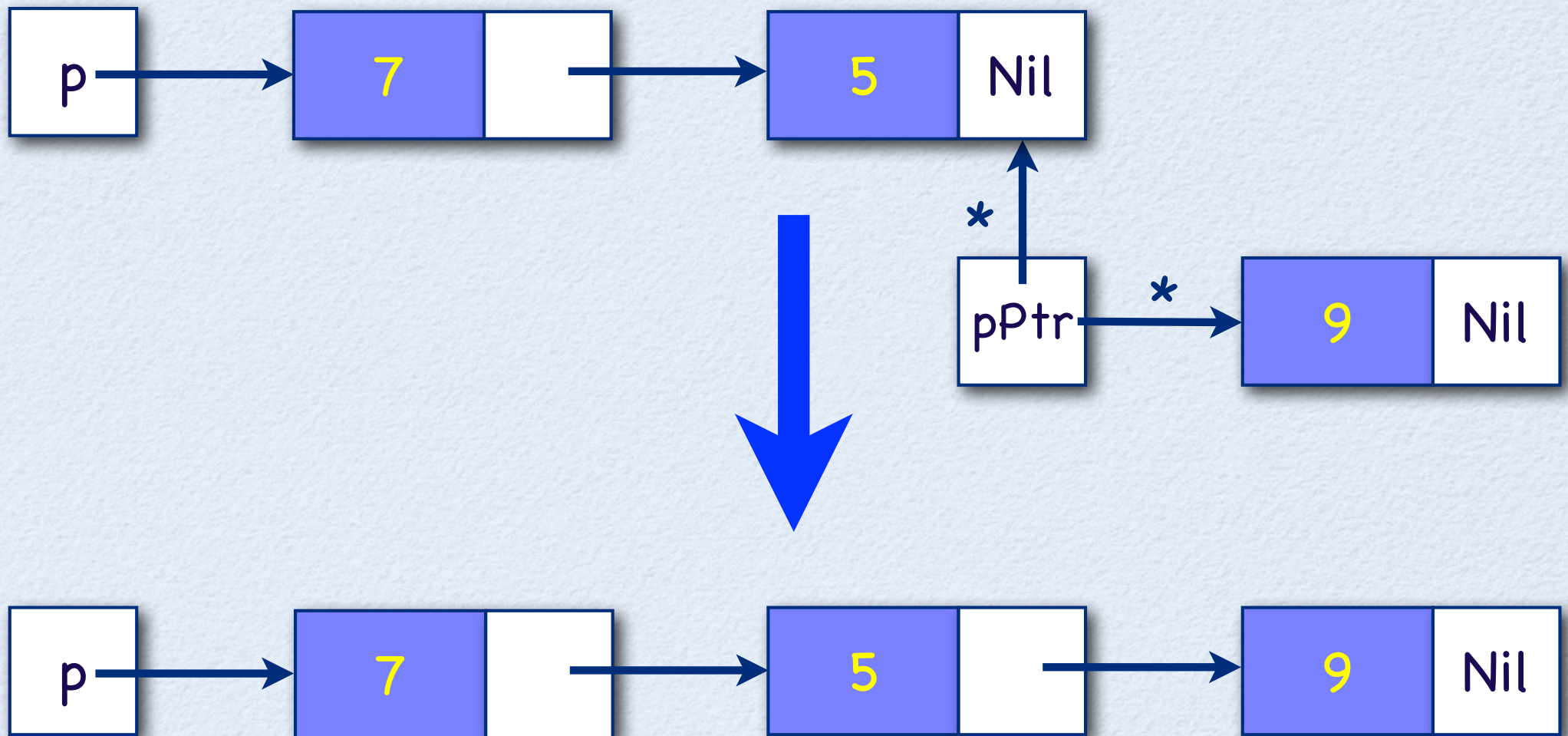
- To insert a new node at the end of a linked list we need to search for the end:



```
14 IntegerList* p = new IntegerList( 5 );
15 IntegerList* q = new IntegerList( 7, p );
16
17 IntegerList** pPtr = &q;
18
19 while ( *pPtr != nullptr )
20 {
21     pPtr = &((*pPtr)->fNext);
22 }
23
24 *pPtr = new IntegerList( 9 );
25
```

The screenshot shows a code editor window with a title bar containing a C++ icon and the filename 'Main.cpp'. The code is written in C++ and is line-numbered from 14 to 25. It demonstrates the process of inserting a new node at the end of a linked list. Line 14 creates a node 'p' with value 5. Line 15 creates a node 'q' with value 7, whose 'fNext' pointer points to 'p'. Line 17 declares a pointer 'pPtr' to 'q'. Lines 19-22 form a while loop that traverses the list by following 'fNext' pointers until 'pPtr' is 'nullptr'. Line 24 then creates a new node with value 9 and assigns it to the memory location pointed to by 'pPtr', effectively adding it to the end of the list. The editor's status bar at the bottom shows 'Line: 1 Column: 1', 'C++', and 'Tab Size: 4'.

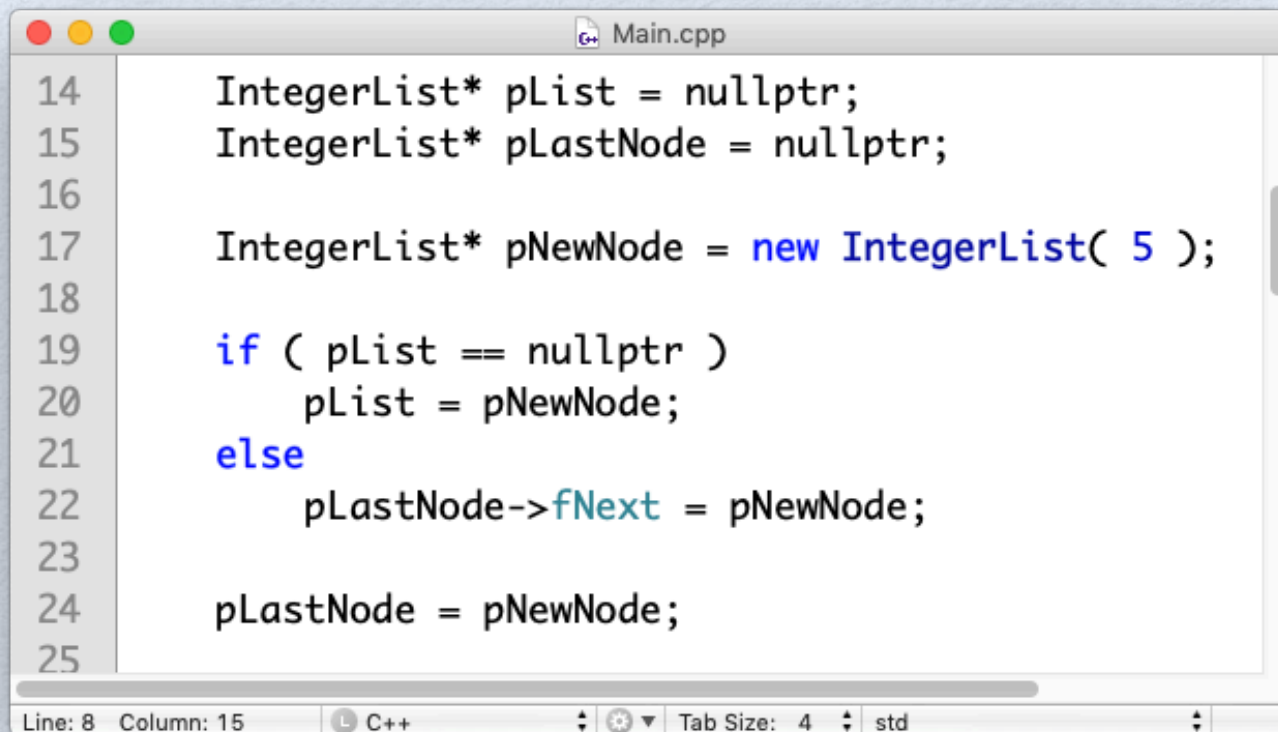
Insert at the End: The Pointers



**Insert at the end preserves
the order of list nodes.**

Insert at the End with Aliasing

- Rather than using a **Pointer-to-Pointer** we can just record the last next pointer.



```
14 IntegerList* pList = nullptr;
15 IntegerList* pLastNode = nullptr;
16
17 IntegerList* pNewNode = new IntegerList( 5 );
18
19 if ( pList == nullptr )
20     pList = pNewNode;
21 else
22     pLastNode->fNext = pNewNode;
23
24 pLastNode = pNewNode;
25
```

The screenshot shows a code editor window with a title bar containing three colored buttons (red, yellow, green) and a file icon followed by 'Main.cpp'. The code is written in C++ and is numbered from 14 to 25 on the left margin. The code initializes two pointers, `pList` and `pLastNode`, to `nullptr`. It then creates a new `IntegerList` node `pNewNode` with the value 5. An `if` statement checks if `pList` is `nullptr`; if so, it assigns `pList` to `pNewNode`. Otherwise, it assigns `pNewNode` to the `fNext` pointer of the last node (`pLastNode`). Finally, it updates `pLastNode` to point to `pNewNode`. The editor's status bar at the bottom indicates 'Line: 8 Column: 15', 'C++', 'Tab Size: 4', and 'std'.

Complications with Singly-Linked Lists

- The deletion of a node at the end of a list requires a search from the top to find the new last node.