MATH3332 Quiz 1

1.
$$(30pts)$$
Let $\mathbf{A} = \begin{bmatrix} 7 & 8 & 9 \\ 3 & 2 & 1 \end{bmatrix}$, $\mathbf{B} = \begin{bmatrix} -1 & 0 & -1 \\ 2 & 1 & 0 \end{bmatrix}$, $\mathbf{x} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$, $y = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$
Find $\mathbf{A}\mathbf{x}$, $\mathbf{A}^T\mathbf{y}$, $\mathbf{A}\mathbf{B}^T$

2. (a) (40pts) Solve the following system using Gaussian elimination:

$$x - y - 4z = -6$$

$$-2x + y + 6z = 7$$

$$3x - 2y - 5z = -3$$

(b) (30pts) Calculate the LU decomposition of the above linear system (please write explicitly the matrices L and U).