Developer Manual for TreeScaper

Zhifeng Deng

August 4, 2020

1 Installation

CLVTreeScaper requires a CLAPACK properly installed and linked on your machine. CLAPACK-3.2.1 has been attached to this repository. You may also download in here.

See detailed instruction on using BLAS library optimized for your machine in CLA-PACK/README.install at step (4).

For a fast default installation, you will need to

- Clone TreeScaper repository from GitHub	(see step 1 below)
- Relocate CLAPACK-3.2.1 and modify CLAPACK make.inc file	(see step 2 below)
- Modify TreeScaper makeCLVTreeScaper.inc file	(see step 2 below)
- Make CLAPACK library	(see step 3 below)
- Make CLVTreeScaper binary	(see step 3 below)

Procedure for installing CLAPACK.

(1) git clone -b zdver https://github.com/TreeScaper/TreeScaper.git to build the following directory structure:

this file TreeScaper/README.install

TreeScaper/makeCLVTreeScaper.inc compiler, compile flags and library

definitions for TreeScaper.

CLAPACK attached in TreeScaper. TreeScaper/CLAPACK-3.2.1/

TreeScaper/CLAPACK-3.2.1/make.inc compiler, compile flags and library

definitions, for TreeScaper.

(2) Move /CLAPACK-3.2.1 outside TreeScaper and modify /CLAPACK-3.2.1/make.inc. For default installation, you need to only modify the OS postfix name PLAT in /CLAPACK-3.2.1/make.inc. For advanced installation, please refer to /CLAPACK-3.2.1/README.install

Update the path of CLAPACK: CLAPPATH in makeCLVTreeScaper.inc and make sure the OS postfix name is consistent with CLAPACK setting, i.e. PLAT in /CLAPACK-3.2.1/make.inc and in makeCLVTreeScaper.inc must be the same.

(2)' If there is a CLAPACK already built in your machine. Make sure it has the following

directory structure:

CLAPACK/BLAS/ C source for BLAS

CLAPACK/F2CLIBS/ f2c I/O functions (libI77) and math functions (libF77)

CLAPACK/INSTALL/ Testing functions and pre-tested make.inc files

for various platforms.

CLAPACK/INCLUDE/ header files - clapack.h is including C prototypes

of all the CLAPACK routines.

CLAPACK/SRC/ C source of LAPACK routines

Update the path of CLAPACK: CLAPPATH in makeCLVTreeScaper.inc and check the OS postfix name of lapack_XXX.a and blas_XXX.a and modify PLAT in makeCLVTreeScaper.inc

For example, if the naming is lapack_MAC.a and lapack_MAC.a then, modify

PLAT = _LINUX

in makeCLVTreeScaper.inc. If the naming is lapack.a and blas.a, modify

PLAT =

in makeCLVTreeScaper.inc.

(3) Go to TreeScaper directory. To install the CLAPACK, run make CLAPACK

To compile the TreeScaper, run make or make CLVTreeScaper.

You may move the binary CLVTreeScaper to other location for your, convenience. Make sure you also move the default parameters files nldr_parameters.csv and dimest_parameters.csv to maintain the structure:

/CLVTreeScaper the CLVTreeScaper binary parameters for nldr routines

/dimest_parameters.csv parameters for dimension estimation routines

To update the 'zdver' GitHub branch,

- 1) Keep your customized makeCLVTreeScaper.inc file.
- 2) Run git pull
- 3) If the makeCLVTreeScaper.inc got overwritten, restore your customized version.
- 4) If there is no change on CLAPACK side, which is usually the case, run make CLVTreeScaper to get the new binary.

Warning: you are not suggested to comment any local modification on this branch.

2 Command structure

The command line version binary file accept a long list of arguments for particular tasks, especially for complicated tasks on trees. Figure 1 shows the structure of keywords <code>-dimest</code>, <code>-nldr</code> and <code>-trees</code> with their outputs and possible dependency between these output. In this figure, solid arrowed line represents output file of routine and dashed arrowed line represents possible dependency between files and routines.

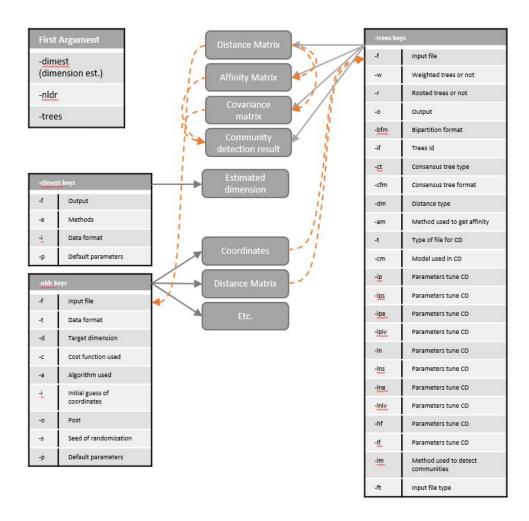


Figure 1: Argument List and routine structure of the current version.

TreeScaper binary takes a long command to execute a complicated task like performing community detection on a set of trees. The typical procedures TreeScaper is going to perform are

- 1. compute bipartition matrix of trees;
- 2. compute trees distance matrix and affinity matrix or compute bipartition covariance matrix;
- 3. perform community detection methods.

These procedures are specified with one command like

./CLVTreeScaper -trees -f test.tre -ft trees -r 1 -w 1 -o Community -t Affinity -dm RF -cm CNM -lm auto

and produce bipartition matrix, affinity/covariance matrix and CD results, which is what the dashed line between output files from keyword -trees. Since these dependency happen internally in one command, we have no control over the intermediate results, i.e., modifications like manually setting threshold for affinity before CD is not possible.

Such commands are inconvenient and also difficult to cooperate with the GUI system we are building on CloudForest. Therefore, keyword and command structure shown in Fig.2 is proposed, while the old structure will remain in the TreeScaper binary until the new system become reliable.

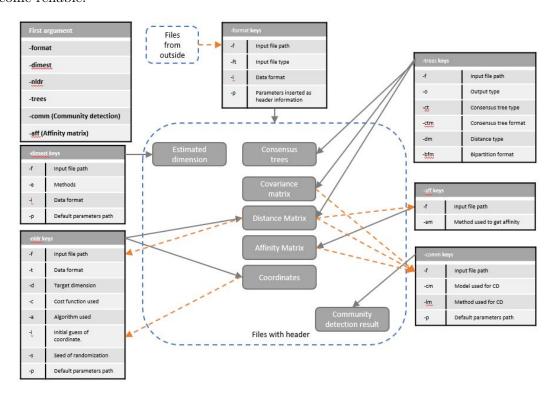


Figure 2: Argument List and routine structure of the new version.

New key arguments <code>-format</code>, <code>-comm</code> and <code>-aff</code> are added to TreeScaper. The new structure is centered at files with header information (in order to simplify file names and shorten argument list). <code>-format</code> takes care of converting files from other source with different format to files consistent with TreeScaper.

-aff and -comm which stand for affinity and community detection are separated from -tree, which now only takes care of computing bipartition matrix, distance matrix and covariance matrix from tree file. Users are now able to perform any modification on output files from -tree, for example, send them to -nldr. Then -comm will take these (modified) files and other necessary information to perform CD methods.

The specific argument list of these keys are given in following sections. Note that the current beta version of TreeScaper still accepts old commands, yet those keys are not suggested to use anymore and will also be erossed in the argument table. The default option, if there is any, will be colored in red.

2.1 -dimest arguments

Currently, the key -dimest for dimensional estimation is a self-contained subroutine. It takes in a distance matrix D or coordinates matrix X of n points $\{p_i\}, i = 1, \dots, n$ and return the estimated rank of the matrix along with the analysis result. This could be used as an instruction on nonlinear dimension reduction task.

Arguments	Description	options
-f	Source file	
-е	Algorithm	CORR_DIM, NN_DIM, EIG_DIM, MLE_DIM
-i	Data type	DIS, COR
-p	Parameter file	

Table 1: Argument list of -dimest

2.2 -nldr arguments

The key -nldr takes in a distance matrix of n points p_i , $i=1,\dots,n$ on certain metric space and return coordinates of p_i , lies on Euclidean space \mathbb{R}^k along with other useful information. In particular, the coordinates matrix \tilde{C} of \tilde{p}_i stores in Coordinate.out and the Euclidean distance matrix \tilde{D} stores in Distance.out.

Arguments	Description	options
-f	Source file	
-t	Data type	COR, DIS
-d	Target dimension, k	2
-с	Cost function	CCA, SAMMON, CLASSIC_MDS ¹
		KRUSKAL1, NORMALIZED
-a	Algorithm	STOCHASTIC, METROPOLIS, GAUSS_SEIDEL
		LINEAR_ITERATION, MAJORIZATION
-i	Initial guess	RAND, CLASSIC_MDS ²
-0	Output postfix	
-post	Output postfix	none, time, NLDR, AnyString
	Parameter file	

Table 2: Argument list of -nldr

Note that classical scaling, the algorithm used to optimized the cost function CLASSIC_MDS only works for Euclidean case, i.e., when D is a Euclidean distance matrix on \mathbb{R}^n , which makes this method less desirable for our tree space. However, it can be used as a way to obtain a good enough initial guess for other methods.

Also notice that -o for output postfix label is dropped and you are recommend to use -post for creating standard filename like Distance_XXX.out. The default -post is time, which will create file like Distance_m_d_hrs_min.out.

2.3 -trees arguments

The key -trees is able to accomplish multiple tasks:

- 1. Distance: it takes in n trees and return a distance matrix $D \in \mathbb{R}^{n \times n}$
- 2. Affinity: it takes in n trees or a distance matrix D and return an affinity matrix A computed from D or certain distance matrix from the input trees set.
- 3. Consensus tree: it takes in n trees and return the consensus tree from input trees set.
- 4. Covariance: it takes in n trees and return the covariance matrix $\mathcal{R} \in \mathbb{R}^{m \times m}$ of m bipartition appeared in the trees set.
- 5. Community: it takes in affinity matrix or covariance matrix and perform the community detection method.

Note that all tasks are coupled with each other if there is mathematical dependence. For example, when -o Affinity appears, -trees computes and outputs bipartition matrix, distance matrix and affinity matrix; when -o Community -t Covariance appears, -trees computes and outputs bipartition matrix, covariance matrix and community detection results.

Arguments	Description	options
-f	Source file	
-ft 3	Data type	Trees, Cova
_M	Weighted tree flag	
-r	Rooted tree flag	
-0	Output type	Dist, Cova, Consensus
		Affinity, Community
-bfm	Bipartition output format	list, matrix
-if	Tree id file	
-ct	Consensus Tree type	Majority, Strict
-ctm	Consensus Tree format	Nexus, Newick
-dm	Distance type	RF, URF, Mat, SPR
-am	Affinity type	Rec, Exp
-cm	Community detection method	CNM, CPN, ERNM, NNM
-lm	Community detection	auto, manu
	parameter setting	
-t	Type of label used in	Affinity, Covariance
	community detection	
-post	Output postfix	none, time, AnyString

Table 3: Argument list of -trees

2.4 -aff arguments

The key -aff takes in any distance matrix D and return affinity matrix A computed from D.

Arguments	Description	options
-f	Source file	
-am	Affinity type	Rec, Exp
-post	Output postfix	none, time, AnyString

Table 4: Argument list of -aff

2.5 -comm arguments

The key -comm takes in any adjacency matrix A from a graph and performs community detection algorithm on it. This matrix is usually assumed to be a covariance matrix of bipartitions from a set of trees or an affinity matrix from distance matrix of a set of trees. The former constructs a graph with bipartition as nodes and the latter constructs one with trees as nodes. However, generally A can be an adjacency matrix of any kind of weighted non-directed graph. Therefore, the key accepts argument to set the node type as well.

Arguments	Description	options
	Source file	· r · · · ·
-cm	Community Detection method	CNN, CPM, ERNM, NNM
-lm	Parameter tuning ⁴	auto, manu
-node	Node type	
-post	Output postfix	none, time, AnyString
-hf 5	Tunning parameter	1
$-lf^6$	Tunning parameter	0
-1p	Manual Tunning parameter	
-ln	Manual Tunning parameter	
-lps	Manual Tunning parameter	
-lpe	Manual Tunning parameter	
-lpiv	Manual Tunning parameter	
-lns	Manual Tunning parameter	
-lne	Manual Tunning parameter	
-lniv	Manual Tunning parameter	

Table 5: Argument list of -comm

Note that the arguments for manually tuning CD will later be combine into a parameter_comm.csv.

2.6 -format arguments

2.7 Command example

In this part, we give some example of calling TreeScaper for different tasks in order to help you understand the new command structure. All commands mentioned here can be found in the file command_example.txt.

Suppose there is a tree file boottrees.nhx on the root directory as well as on a sub directory.

Perform a community detection on trees based on particular distance.

The old command in one line is

./CLVTreeScaper -trees -f boottrees.nhx -ft Trees -w 1 -r 0 -o Community -dm RF -t Affinity -am Rec -cm Auto -hf 0.9 -lf 0.1

Note that the old command requires the tree file be in the same directory of the binary file. This command will sequentially generates bipartition file, distance file, affinity file and the final community detection result.

For the beta version, you are suggested to use the following set of commands to call CLVTreeScaper multiple times. Notice that the new command allows input and output in directory other than the current one.

1. ./CLVTreeScaper -trees -f sub_dir/boottrees.nhx -w 1 -r 0 -o Dist -dm RF -post test

It generates bipartition output and a distance matrix in sub_dir/Distance_test.

- 2. 'If you want to further process the distance matrix with -nldr, call
 - ./CLVTreeScaper -nldr -f sub_dir/Distance_test.out -t DIS -d 20 -c CCA -a STOCHASTIC -i RAND -post NLDR_test

It generates a coordinates matrix sub_dir/Coordinate_NLDR_test.out and a distance matrix sub_dir/Distance_NLDR_test.out. This step is not necessary.

- 3. ./CLVTreeScaper -aff -f sub_dir/Distance_NLDR_test.out -am Rec -post NLDR_test It generates an affinity matrix sub_dir/Affinity_NLDR_test.out.
- 4. ./CLVTreeScaper -comm -f example/Affinity_NLDR_test.out -lm auto -hf 0.9 -lf 0.1

It performs the final community detection method on the graph based on affinity matrix.

Note that you may perform NLDR method multiple times if necessary. Also note that you can further modify every files manually or with other software (as long as the format is maintained) before going to the next step. This is not recommended unless you are sure about the modification serves for your purpose.

Perform a community detection of bipartition based on covariance matrix.

The old one-line command for this task is

./CLVTreeScaper -trees -f boottrees.nhx -ft Trees -w 1 -r 0 -o Community -t Covariance -am Rec -cm Auto -hf 0.9 -lf 0.1

This command will sequentially generates bipartition file, covariance file and the final community detection result.

For the beta version, you are suggested to use the following set of commands to call CLVTreeScaper multiple times.

1. ./CLVTreeScaper -trees -f sub_dir/boottrees.nhx -w 1 -r 0 -o Cova -post test It generates bipartition output and a distance matrix in sub_dir/Covariance test.

2. ./CLVTreeScaper -comm -f example/Covariance_test.out -lm auto -hf 0.9 -lf 0.1

It performs the final community detection method on the graph based on covariance matrix.

2.8 Header information

The beta version of TreeScaper are now centered at the output files of each subroutine. Different subroutines communicate through the formatted header information in the file they read and the file they output. (WARNING: Header in tree file and -dimest is NOT supported.)

Here is a typical header information from a distance matrix created by $\verb"-nldr"$:

created:8_3_0_33
output_type:Distance matrix
distance_type:Robinson-Foulds
node_type:Tree
node_feature:weighted, unrooted, NLDR(20)
source:example/ATP8.tre

It is multiple lines of string inside a angle bracket. The information is stored as map<String, String> inside TreeScaper, such that each line gives a pair of key-value separated by the colon':'. These header information are formatted in human-readable fashion. The key usually have no space and the value may have more than one item, separated by ', '.

When a subroutine read a file with header, it will load in all header information, update or drop certain lines and then make use of some of them. Finally, the routine will add more information to the header and print it on the output file. Therefore, you may insert information you need in the format of KEY:VALUE and it will present in later files.

3 Basic data structures

Most of the basic data structures are constructed by Wen Huang. They includes basic array, matrix, string, mapping and file stream. They are, basically the c++ built-in structure warped up with convenient functions and operators. For example, the matrix class integrates singular value decomposition from CLAPACK. These data structures' header file and implementation files are prefixed with "w".

There are other more complicated data structures for specific algorithm and mathematical objects such as trees and community. They will be addressed in the next section.

3.1 Array

Members of array of type T are consisted of a pointer of T^* vec and a static integer length that indicates the length. The member functions and operators are given below.

1. friend std::istream &operator>

This operator does nothing and will not assign value to the array from the istream. According to particular needs of reading data, this may later be implemented with actual reading functionality.

2. friend std::ostream &operator«

This operator will output the length and its components separated by ":" and ",".

Example: an array of char[] from "a" to "e" is outputted in the format of

3. const Array& Array::operator=(const Array &right)

The assignment operator will free the pointer vec on the left and allocate a new vec. Then it assigns values from right hand side to left hand side component-wise.

The operator returns a pointer of the array on the left.

4. const Array& Array::operator+=(const Array &right)

This operator creates a new array with the right hand side attached to left hand side. It allocates Array of the correct length and then assigns values accordingly. Then call the assignment operator = to overwrite the current array.

Warning: calling = costs repeated and unnecessary copy-pasting.

5. const Array& Array::operator-=(const Array &right)

This operator creates a new array from the left hand side, with every component presented in the right removed and calls assignment operator to overwrite the current Array.

Warning: calling = costs repeated and unnecessary copy-pasting.

Warning: the new array is built incrementally and calls **resize** everytime, will brings the complexity to $O(length^2 \times right.length)$ other than $O(length \times right.length)$.

6. bool Array::operator==

Compares two array component-wise after comparing the length.

7. bool Array::operator<

The logic of the compare operator is to set the array with component-wise greater component to be the greater one. If the lengths are different, only compare the first k components where k is the smaller length. If the first k components happens to be the same (component-wise), the longer Array is greater than the shorter one.

8. Array Array::operator(const int index, const int end)

This operator extract sub-array from the current array. It takes two indices as parameters and return a new array that has the values from index to end.

Warning: this implementation is different than the implementation of String::operator(), which also takes two integers as parameters but the first one is the starting index and the second one is the length of the sub-string, instead of the ending index.

3.2 Matrix

Members of a matrix of type T are consisted of a pointer of pointers T** implemented inrow-major and two static integers row and col which indicate the dimensions of the matrix. This class also calls classic linear algebra algorithms from CLAPACK.

Overloaded operators are given below.

1. friend istream & operator ».

Warning: This operator does nothing, i.e., it does not assign values from the input stream.

2. friend ostream & operator «.

This operator output the matrix in the format of

```
{ (3,2) a, b, c d, e, f }
```

3. friend Matrix operator+(Matrix<T> left, Matrix<T> right).

This operator resize the left and right matrices to the lager dimension by calling member function <u>resize</u> and then create a new matrix and assign values from entry-wise addition.

Warning: the resize of left and right is silent here, which will permanently change the matrix being summed.

4. friend Matrix operator+(Matrix<T> left, S right).

This operator accepting a number right of type S on the right will add right entry-wise to each element in Matrix left, i.e., shift the matrix by right.

5. friend Matrix operator+(S left, Matrix<T> right)
Shift the matrix by left entry-wise.

6. friend Matrix operator-

See friend Matrix operator+.

- 7. Matrix operator*(const Matrix<T> &left, const Matrix<T> &right)
 Implement matrix multiplication.
- 8. friend Matrix operator*(S value, Matrix<T> mat) or (Matrix<T> mat, S value).

 This operator return a new matrix entry-wise scaled by value. Note that this operator does not change the original matrix.

Warning: the matrix getting rescaled should be passed by reference in order to avoid construction/destruction computation.

9. friend Matrix operator/(Matrix<T> mat, S value)

This operator return a new matrix entry-wise divided by value. Note that this operator does not change the original matrix. Also note that this is not the syntax used in some advanced language where A/B means $B^{-1}A$.

Warning: the matrix getting rescaled should be passed by reference in order to avoid construction/destruction computation.

10. T &operator()(const int r, const int c = 0)

This operator returns the entry at r-row and c-column.

Important member functions are given below.

1. Matrix<double> compute_scalar_product_matrix()

This function return a **double** type matrix $S \in \mathbb{R}^{n \times n}$ from the current matrix $D^{(2)} \in \mathbb{R}^{n \times n}$. S is the centering-scaled $D^{(2)}$, which is assumed to be a squared distance matrix of n points $\{p_i\}_{i=1,\dots,n}$, $D^{(2)}_{ij} = D^{(2)}_{ji} = d^2(p_i, p_j)$.

Note that the classical multidimensional scaling method, MDS assumes these n points lie on some Euclidean space \mathbb{R}^k equipped with classic 2-norm distance. And S is a squared distance matrix of transformed n points such that the arithmetic mean of new points is $0^k \in \mathbb{R}^k$. Also note that the arithmetic mean in Euclidean space is also the Karcher mean defined by

$$\arg\min_{m\in\mathbb{R}^k}\sum_{i=1}^n d^2(p_i,m).$$

The formula of computing S is given by

$$S = -\frac{1}{2}JD^{(2)}J$$

where $J = I - \frac{1}{n} \mathbf{1} \mathbf{1}^T$ and $\mathbf{1} \mathbf{1}^T$ is all-1 matrix. Also note that the transformation $D^{(2)} \to S$ preserves the solution of MDS, i.e.,

$$\arg\min_{B \in \mathbb{R}^{n \times k}} \left\| BB^T - D^{(2)} \right\|_F^2 = \arg\min_{B \in \mathbb{R}^{n \times k}} \left\| -\frac{1}{2} JBB^T J + \frac{1}{2} JD^{(2)} J \right\|_F^2$$

where B is the Euclidean coordinate matrix of n points in \mathbb{R}^k which generates (approximately) the squared distance matrix $D^{(2)}$.

Error: The invariance of transformation seems to be only true for Euclidean space. For more abstract $D^{(2)}$ generated from more general metric on Riemannian manifold, the scaling $-\frac{1}{2}JD^{(2)}J$ does not preserves positive definiteness of the squared distance matrix, which further causes negative eigenvalues in the following PCA, the eigendecomposition, process.

Warning: The squared distance matrix $D^{(2)}$ used in here is inconsistent with the distance matrix D computed in compute_Distance_Matrix in difference of entry-wise squared or not.

2. Matrix<double> compute_Distance_Matrix()

This function return a **double** type matrix $D \in \mathbb{R}^{n \times n}$ computed from the current matrix $M \in \mathbb{R}^{n \times k}$. M is consider as coordinate matrix of n points in k-dimensional Euclidean space, i-th row represents the k-tuple Euclidean coordinates of a point p_i . And D is the distance matrix where $D_{ij} = D_{ji} = d(p_i, p_j) = ||p_i - p_2 j||_2$ is the 2-norm distance between points p_i, p_j .

Warning: the resulting distance matrix D is dense, the symmetric structure is not exploited here.

4 Algorithms

4.1 Nonlinear dimensional reduction(NLDR)

This part collects algorithms and their important subroutines implemented in TreeScaper. The main goal in these algorithms is that given a squared distance matrix $D^{(2)}$ or distance matrix D of n points $\{p_i\}_{i=1,\dots,n}$ on some metric space, find n points $\{p_i'\}_{i=1,\dots,n} \subset \mathbb{R}^k$, such that the distance matrix D' for \mathbf{p}' approximates D the best, under the cost functions defined in different algorithm. Note that these n new points \mathbf{p}' can be represents by the coordinate matrix $B \in \mathbb{R}^{n \times k}$ which is often used as the output of these NLDR algorithms.

4.1.1 Classical Multidimensional scaling(MDS)

.

Classical Multidimensional scaling assumes $D^{(2)}$ is generated from Euclidean space with typical vector 2-norm as distance. The implemented algorithm NLDR::CLASSIC_MDS contains 4 parts:

- 1. Compute centered matrix S from the given tree distance matrix D by calling ${\tt Matrix}$::compute_Scalar_Matrix.
- 2. Perform singular value decompositions(SVD) to S by calling Matrix::SVD_LIB to obtain

$$S = U\Sigma V^T$$
.

Note that since S is symmetric, there exist eigen-decomposition $S = Q\Lambda Q^T$, i.e., there exists a signature matrix E, which has only 1 or -1 in diagonal and 0 elsewhere, such that $U\Sigma V^T = Q\Lambda EEQ^T = Q(\Lambda E)(QE)^T$ and U = Q, $\Sigma = \Lambda E$ and V = QE. This implies eigen-decomposition from CLAPACK is more efficient.

Also note that if $D^{(2)}$ uses vector 2-norm in Euclidean space, S is positive definite and SVD coincides with eigen-decomposition.

Warning: when there exist files named consistently that indicates SVD has been done and U, V, Σ has been stored, the routine will not do it again but simply read them from files. This is silent and could cause problem if those files are not actually inconsistent.

3. In case of performing MDS for $D^{(2)}$ from other metric space, which cause the presence of negative eigenvalues, it selects the k eigenvectors Q_{i_j} , $j=1,\dots,k$, where λ_{i_j} are the k most largest positive eigenvalues.

Error: memory leakage happens in this process whenever a negative eigenvalues encountered in the k most largest in magnitude eigenvalues. This problem is temporarily fixed but the theoretical explanation and necessity of this process is still needed. the classical MDS may not be suitable at all for Tree subjects.

4. Produce the coordinates matrix B for n points $\mathbf{p}' \subset \mathbb{R}^k$ by

$$B = \begin{bmatrix} \sqrt{\lambda_{i_1}} Q_{i_1} & \cdots & \sqrt{\lambda_{i_k}} Q_{i_k} \end{bmatrix} \in \mathbb{R}^{n \times k}.$$

5. Compute the stress that estimate how good BB^T approximate $D^{(2)}$ by calling NLDR::CLASSIC_MDS_stress. Note that classical MDS do not need to compute the stress since B already minimized the stress function. However, since Tree space is not a Euclidean space with appropriate distance, the output B does not minimize the stress function.

For more information of MDS, see here.

Implementations of some routines

Data structure

1. Matrix

Description Row-major 2-dimensional array.

Member row Number of rows.

col Number of columns.

**matrix Pointers to each row.

Member function resize Change the dimensions.

2. Ptree

Description Index base array-type unweighted tree with adjacency matrix.

Member leaf_number

*parent Array of indices of the parent.

*lchild Array of indices of the right child.

*rchild Array of indices of the left child.

**edge Adjacency matrix.

Member function none

3. NEWICKNODE

Description Linked node pointed to its children and parent.

Member Nchildren Number of children.

label weight

*child List of children.

hv1 Hash value for unknown use.

hv2 Hash value that identifies the bipar-

tition.

bitstr Bit string that represents the leaves

contained in the (sub-)tree.

parent

Member function none

4. NEWICKTREE

DescriptionA NEWICKNODE that represents the root.MemberrootA NEWICKNODE.

Member function none

5. TreeOPE

Description Operation associated to one <u>NEWICKTREE</u>. Note that

most of the method are implemented in recursive pre-

order.

Member

Member function <u>loadnewicktree</u> Read <u>NEWICKTREE</u>.

loadnewicktree2Read NEWICKTREE.floadnewicktreeRead NEWICKTREE.loadnodeRead NEWICKTREE.loadleafRead NEWICKTREE.parsetreeRead NEWICKTREE.parsenodeRead NEWICKTREE.parseleafRead NEWICKTREE.

<u>addchild</u> Link child to the parent.

dfs_compute_hash Assigned hash values to all (sub-

)tree which identifies the structure

and therefore the bipartition.

<u>bipart</u> Store hash values in one big array for

computing RF distance.

findleaf Find a leaf by the

NEWICKNODE::label.

<u>normalizedTree</u> Lift a unrooted tree to a rooted tree.

<u>newick2lcbb</u> Convert <u>NEWICKTREE</u> to <u>Ptree</u> for

computing matching distance.

 $\underline{\underline{\mathtt{newick2ptree}}} \qquad \quad \underline{\underline{\mathtt{Implementation}}} \text{ of } \underline{\underline{\mathtt{newick21cbb}}}.$

<u>sumofdegree</u>

<u>bipartcount</u> Count the occurrence of particular bi-

partition.

Addbipart Insert nodes to the current tree so

that there exist a (sub-)tree that contains only a given set of leaves.

6. Trees

Description Multiple NEWICKTREEs with member function that com-

putes different distances.

Member

Member function Read trees from file. initialTrees ReadTrees Read trees from file.

compute_numofbipart

Generate hash table for Compute Hash

computing hash values in a

tree.

Compute_Bipart_Matrix Generate a sparse matrix

> that stores the weight of bipartition, its frequency of

occurrence.

<u>Compute_Bipart_Covariance</u>Generate the covariance

matrix according to the

formula.

Generate the RF-distance Compute_RF_dist_by_hash

matrix according to the for-

mula.

Construct the adjacency pttree

matrix of a Ptree.

Generate matrix for comcompute_matrix

puting matching distance by accumulating common edges from two Ptrees.

Compute_Matching_dist Compute the matching dis-

tance between two trees by the XOR table created from

all possible bipartitions.

Compute the affinity dis-Compute_Affinity_dist

tance from the given dis-

tance matrix.

TreeOPE related routines.

1. TreeOPE::loadnewicktree.

Argument	(char *fname, int *error)	
Description	Read tree from formatted string that stores biparti-	
	tion. The implementation is given in floadnewicktree .	
	Same level of the node is paired by "()" and separated	
	by ",".	
Complexity		
Memory space		
Associated routine	<u>floadnewicktree</u> Implementation by recursive process-	
	ing the string in preorder.	
Comments	This routine is better implemented by stack structure.	
	It can only process unweighted tree. Also this routine	
	takes the file name as input while the duplication version	
	<u>loadnewicktree2</u> takes FILE type, customized fstream	
	type. This routine seems to be insecure and redundant.	
Error code	-1 Out of memory.	
	-2 Parse error, the parentheses in string	
	does not match.	

2. <u>TreeOPE</u>::loadnewicktree2.

Description Duplication version of loadnewicktree but with customized fstream. Actual implementation is not given in here, but in floadnewicktree Complexity Memory space Associated routines Implementation by recursive processing the string in preorder. Comments This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code -1 Out of memory2 Parse error, the parentheses in string does not match.	Argument	(FILE *fp, int *error)	
Complexity Memory space Associated routines This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code Farse error, the parentheses	Description	Duplication version of <u>loadnewicktree</u> but with cus-	
Complexity Memory space Associated routines floadnewicktree Implementation by recursive processing the string in preorder. Comments This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code -1 Out of memory2 Parse error, the parentheses		tomized fstream. Actual im	plementation is not given in
Memory space Associated routines Floadnewicktree Implementation by recursive processing the string in preorder. Comments This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code 1 Out of memory2 Parse error, the parentheses		here, but in floadnewicktr	<u>ree</u>
Associated routines floadnewicktree	Complexity		
Sive processing the string in preorder. Comments This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code -1 Out of memory2 Parse error, the parentheses	Memory space		
Comments This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code 1 Out of memory2 Parse error, the parentheses	Associated routines	floadnewicktree	Implementation by recur-
Comments This routine also seems to be redundant since the main thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code -1 Out of memory2 Parse error, the parentheses			sive processing the string in
thread of TreeScaper never called it. There is another input routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code -1 Out of memory. -2 Parse error, the parentheses			preorder.
put routine parsetree, which can handle both weighted and unweighted tree, is used in TreeScaper. Error code -1 Out of memory2 Parse error, the parentheses	Comments	This routine also seems to b	be redundant since the main
Error code and unweighted tree, is used in TreeScaper. Out of memory2 Parse error, the parentheses		thread of TreeScaper never of	called it. There is another in-
Error code -1 Out of memory2 Parse error, the parentheses		put routine <u>parsetree</u> , which	ch can handle both weighted
-2 Parse error, the parentheses		and unweighted tree, is used	d in TreeScaper.
	Error code	-1	Out of memory.
in string does not match.		-2	Parse error, the parentheses
			in string does not match.

3. TreeOPE::floadnewicktree.

	Argument	(FILE *fp, int *error)		
	Description	A pair of nodes are created by <u>loadnode</u> when "(" is		
	-	encountered.	,	
	Complexity	-		
	Memory space			
	Associated routine	loadnode		
	Comments		s to be redundant since the main	
	Comments			
		thread of TreeScaper never called it. There is another input routine <u>parsetree</u> , which can handle both weighted		
		and unweighted tree, is used in TreeScaper.		
	Error code		out of memory.	
			arse error, the parentheses in string	
		d	oes not match.	
4.	TreeOPE::loadnode.			
	Argument	(FILE *fp, int *err	ror)	
	Description	Create internal nodes.	When this function is called, a	
		"(" has been read, if f	p continue to read "(", next pair	
		of nodes should be ge	nerated, i.e., <u>loadnode</u> is called	
		again, otherwise a leaf	is encountered and <u>loadleaf</u> will	
		9 ,	s encountered, it is at the end of	
			les and should exit the routine to	
		returned to previous le		
	Complexity			
	Memory space			
	Associated routine	loadleaf	Add a leaf and return to previous	
	Associated Toutiffe	Toddledi	level.	
		addchild	Add the new pair of nodes to	
		audchiid	their parent.	
		mandlahalandusimh+	Read additional information	
		readlabelandweight		
	<u> </u>	TD1::1 1	from string.	
	Comments	-	nted by stack structure. Also note	
			leaves in preorder traversal.	
	Error code	-1	Out of memory.	
		-2	Parse error, the parentheses in	
			string does not match.	
5.	TreeOPE::parsetree.			
	Argument	(char *str, int *er	ror, NEWICKTREE *testtree)	
	Description	Duplicate version of f		
	Complexity			
	Memory space			
	Associated routine	parsenode		
	Comments	This is the routine used in TreeScaper.		
	Error code		tut of memory.	
	Lifti code		arse error, the parentheses in string	
		<u> </u>	oes not match.	

6. <u>TreeOPE</u>::parsenode.

Argument	(FILE *fp, int *error)	
Description	Duplicated version load	lnode.
Complexity		
Memory space		
Associated routine	parseleaf	Add a leaf and return to previous
		level.
	addchild	Add the new pair of nodes to
		their parent.
	parselabelandweight	Read additional information
		from string.
Error code	-1	Out of memory.
	-2	Parse error, the parentheses in
		string does not match.

 $^{7. \ \}underline{\texttt{TreeOPE}}{::} \texttt{dfs_compute_hash}.$

Argument		artNode, LabelMap &lm,
	• –	ashrf, unsigned treeIdx,
	unsigned &numBit	str, unsigned long long
	m1, unsigned lon	g long m2, bool WEIGHTED,
	unsigned int NUM	I_Taxa, map <unsigned long<="" th=""></unsigned>
	long, Array <char< th=""><th>> *> &hash2bitstr, int</th></char<>	> *> &hash2bitstr, int
	numofbipartions)	
Description	It assigned hash val	lue to all leaves set, for internal node,
	the hash values are	computed by the sum of its children's
	hash values (and m	od m1 or m2). For each internal node,
	it determines a sub-	-tree rooted by itself from the current
	tree.	
	Such subtree is uni	iquely represented by the hash value
	of its root. The lea	ves contained in the subtree are also
	represented by the	bit string. For example, 01001100
	represents that the	subtree contains leaf 2, 5 and 6. The
	mapping from has	h values to the leaves it contain is
	stored in hash2bit	str.
Complexity		
Memory space		
Associated routine	Array::SetBitArra	y Set the some positions, the index of
	•	leaves, of a bit array to 1.
	<pre>Array::OrbitOPE</pre>	OR operation of bit array, it realizes
		the functionality of making the bit
		the functionality of making the bit string of the root having 1 in every
		į
	add_of	string of the root having 1 in every
Comments		string of the root having 1 in every leaf's index that the subtree has.
Comments	Note that hash va	string of the root having 1 in every leaf's index that the subtree has. Bit-wise addition for hash values. lue to subtree is bijection and sub-
Comments	Note that hash va tree to leaves it co	string of the root having 1 in every leaf's index that the subtree has. Bit-wise addition for hash values.
Comments	Note that hash va tree to leaves it co mapping hash2bit	string of the root having 1 in every leaf's index that the subtree has. Bit-wise addition for hash values. lue to subtree is bijection and sub-ontains is subjection. Therefore, the
Comments	Note that hash va tree to leaves it co mapping hash2bit	string of the root having 1 in every leaf's index that the subtree has. Bit-wise addition for hash values. lue to subtree is bijection and subortains is subjection. Therefore, the str is subjection. Also note that the on and modulus, on hash values are
Comments Error code	Note that hash va tree to leaves it co mapping hash2bit operations, additio	string of the root having 1 in every leaf's index that the subtree has. Bit-wise addition for hash values. lue to subtree is bijection and subortains is subjection. Therefore, the str is subjection. Also note that the on and modulus, on hash values are

8. <u>TreeOPE</u>::bipart.

Argument	(NEWICKNODE *const startnode, unsigned int
	<pre>&treeIdx, unsigned long long *matrix_hv,</pre>
	unsigned int *matrix_treeIdx, double
	*matrix_weight, int &idx, int depth, bool
	isrooted)
Description	Store hash values, TreeIdx and weights in the given ar-
•	rays.
Complexity	0
Memory space	
Associated routine	
Comments	Note that the "TreeIdx" is an identical array. Each tree
	will generate one set of such arrays and these arrays
	from different trees are pasted together and sorted by
	the hash values. By comparing hash values, identical
	bipartitions among different trees can be easily found.
Error code	-1 Out of memory.
21101 0040	-2 Parse error, the parentheses in string
	does not match.
	does not materi.
. <u>TreeOPE</u> ::findleaf.	
Argument	(std::string leafname, NEWICKNODE
	*currentnode, NEWICKNODE *parent, int *icpt)
Description	Find leaf leafname and return it. icpt also record which
-	subtree under root the leaf lies in.
Complexity	
Memory space	
Associated routine	none
. <u>TreeOPE</u> ::normalizedTr	ee.
Argument	(NEWICKNODE *lrpt, NEWICKTREE *newickTree, int
G	indexchild)
Description	Lift a unrooted tree to a rooted tree.
Complexity	
Memory space	
Associated routine	normalizedNode It's implementation.

11. <u>TreeOPE</u>::newick2lcbb.

	Argument	(const NEWICKTREE *nwtree, int num_leaves,	
	O	struct Ptree *tree)	
	Description	Convert NEWICKTREE to Ptree, which is used to compute	
	-	matching distance.	
	Complexity		
	Memory space		
	Associated routine	newick2ptree Implementation of <u>newick2lcbb</u> .	
	Comments	Note that Ptree does not stored hash values and	
		weights, i.e., the bipartition and weight information are	
		lost. Also note that the edges matrix of Ptree is not	
		computed here.	
12.	<u>TreeOPE</u> ::sumofdegree.		
	Argument	(NEWICKNODE *node, bool isrooted, int depth)	
	Description	Return the sum of degrees of all nodes.	
	Complexity		
	Memory space		
	Associated routine		
	Comments		
	Error code	Out of memory.	
		-2 Parse error, the parentheses in string	
		does not match.	
13.	<pre>TreeOPE::bipartcount.</pre>		
	Argument	(NEWICKNODE *node, bool isrooted, map <unsigned< th=""></unsigned<>	
		long long, unsigned long long> &bipcount, int	
		depth)	
	Description	Count the occurrence of particular subtree, bipartition,	
		by its hash value and store the result in the external	
	Complexity	mapping bipcount	
	Memory space		
	Associated routine		
	Comments		
14.	TreeOPE::Addbipart.		
	Argument	(NEWICKNODE* startNode, double freq, unsigned	
	Argument	long long hash, Array <char> &bitstr, int</char>	
		NumTaxa, bool &iscontained)	
	Description	Given bitstr that represents a set of leaves. Insert	
	•	internal nodes from leaf-set to root that collects those	
		leaves lie in bitstr so that there is a subtree containing	
		exactly the same set of leaves in the resulting new tree.	
	Complexity		
	Memory space		
	Associated routine	none	
	Comments	There is a better way to implement this functionality.	

<u>Trees</u> related routines.

1. <u>Trees</u>::initialTrees.

Argument	(string fname)		
Description	Initialize a set	of <u>NEWICKEDTREE</u> s by calling	
	<u>loadnewickedtree2</u> . For Nexus trees, it only cre-		
	ate a leaveslabel	smaps that stores the labels of leaf	
	set.		
Complexity			
Memory space			
Associated routine	<u>loadnewicktree2</u>	Create each tree.	
Comments	Complicated string operations are done here, whi		
	unnecessary.		
Error code	-1	Out of memory.	
	-2	Parse error, the parentheses in strin	
		does not match.	
	-3	Failure of opening file.	
<u>'rees</u> ::ReadTrees.	-0	Tanuic of opening me.	
		Tanure of opening me.	
Argument	none		
	none A duplicated version	on of <u>initialTrees</u> except it calls	
Argument	none A duplicated version parsetree for both	on of <u>initialTrees</u> except it calls Newicked and NEXUS type of tree.	
Argument Description	none A duplicated version	on of <u>initialTrees</u> except it calls Newicked and NEXUS type of tree.	
Argument Description Complexity	none A duplicated version parsetree for both	on of <u>initialTrees</u> except it calls Newicked and NEXUS type of tree.	
Argument Description	none A duplicated version parsetree for both	on of <u>initialTrees</u> except it calls Newicked and NEXUS type of tree.	
Argument Description Complexity Memory space	none A duplicated versic parsetree for both Also lifted the tree	on of <u>initialTrees</u> except it calls Newicked and NEXUS type of tree. if it is unrooted.	
Argument Description Complexity Memory space	none A duplicated version parsetree for both Also lifted the tree parsetree normalizedTree	on of initialTrees except it calls Newicked and NEXUS type of tree. if it is unrooted. Create each tree. Lift a unrooted tree.	
Argument Description Complexity Memory space Associated routine	none A duplicated version parsetree for both Also lifted the tree parsetree normalizedTree	on of initialTrees except it calls Newicked and NEXUS type of tree. if it is unrooted. Create each tree. Lift a unrooted tree. cring operations are done here, which	
Argument Description Complexity Memory space Associated routine	none A duplicated versic parsetree for both Also lifted the tree parsetree normalizedTree Very complicated st	on of initialTrees except it calls Newicked and NEXUS type of tree. if it is unrooted. Create each tree. Lift a unrooted tree. cring operations are done here, which	
Argument Description Complexity Memory space Associated routine Comments	none A duplicated version parsetree for both Also lifted the tree parsetree normalizedTree Very complicated strice is really unnecessary	on of initialTrees except it calls Newicked and NEXUS type of tree. if it is unrooted. Create each tree. Lift a unrooted tree. cring operations are done here, which y. Out of memory.	
Argument Description Complexity Memory space Associated routine Comments	none A duplicated version parsetree for both Also lifted the tree parsetree normalizedTree Very complicated strip is really unnecessary	on of initialTrees except it calls Newicked and NEXUS type of tree. if it is unrooted. Create each tree. Lift a unrooted tree. cring operations are done here, which y.	

3. Trees::compute_numofbipart.

Argument	none	
Description It computes the numbers of bipartition for all trees a		
	stores them in the array <u>numberofbipartition</u> . The	
	formula is given by	
	s/2-n	
	where s is the sum of degrees and n is the number of leaf.	
Commlessites	lear.	
Complexity		
Memory space		
Associated routine	sumofdegree	

4. <u>Trees</u>::Compute_Hash.

	Argument	none		
	Description	Generate the hash table for computing the hash values		
		in a tree.		
	Complexity	ace		
	Memory space			
	Associated routine			
5.	<pre>Trees::Compute_Bipart</pre>	_Matrix.		
	Argument	none		
	Description	The arrays of indivial tree's hashvalue, tree index and weight created from <u>bipart</u> were combined and sorted. Since the hash value represents the unique subtree structure, i.e a bipartition, the number of unique bipartion can be counted via checking the hash value. As a result, a sparse bipartition matrix that stores weight of unique		
		bipartition versus t	rees is created.	
	Complexity			
	Memory space Associated routine	1.1		
	Associated routine	<u>bipart</u> Sort	Create arrays of hash values, weights with tree index of one tree. Sort the 3 arrays attached from all trees by the hash values, so that we	
		sort	can easily count the occurrence for each hash value, i.e., bipartition. Seems to be built-in sort for array that sort a temperate hash value array for certain later operation.	
	Comments	The sort which is different then Sort is confusing here. Is it the default sort in c++?		
6. Trees::Vec_multiply.				
	Argument	(const double* Vec1, const double* Vec2, int Unique_idx) It return a rank-1 matrix $M = v_1 v_2^T.$		
	Description			
	Complexity			
	Memory space			
	Associated routine	none		
	Comments It is confusing with the <u>SparseMatrix</u> :: <u>Multipl</u>			
		and should be integrated in <u>Vector</u> class.		

 $7. \ \underline{\texttt{Trees}}{::} \\ \texttt{Compute_Bipart_Covariance}.$

Argument	(bool ISWEIGHTED)			
Description	Compute the bipartition covariance matrix from the matrix, C, created by <u>Compute Bipart Matrix</u> , M. Let $M_1 = MM^T$, $v_1 = mean(M)$, $v_2 = sum(M)$, $M_2 = v2v1^T$ and $M_3 = v1v1^T$, then			
	$C = (M_1 - M_2 - M_2^T + n * M_3)/(n-1).$			
Complexity				
Memory space				
Associated routine	SparseMatrix::transpose			
120001110	SparseMatrix::Multiply	Matrix-Matrix multiplication.		
	SparseMatrix::Mean	Matrix mean.		
	SparseMatrix::Multiply_vec	$\underline{\mathbf{c}}$ Matrix-vector multiplication.		
	<pre>Trees::Vec_Multiply</pre>	Rank-1 matrix.		
Comments	Note that it is implemented multiplication.	via sparse matrix-vector		
<u> </u>	t_by_hash.			
Argument	(bool ISWEIGHTED)			
Description				
$d_{ij} = \frac{n_i + n_j - 2f_{ij}}{2}.$		$\frac{a_j - 2f_{ij}}{2}$.		
	For weighted case, it is more complicated. The result is stored in the matrix dist_URF or dist_RF.			
Complexity Memory space				
Associated routine	none			
Comments	none			
<u>Γrees</u> ::pttree.				
Argument	(struct Ptree *treeA, int			
Description	It constructs the edge matrix of treeA which should be implemented in Ptree .			
Complexity				
Memory space				
pace				

10. <u>Trees</u>::compute_matrix.

8.

9.

(int *r, int range, struct Ptree *tree1,		
struct Ptree *tree2)		
It accumulates the number common edges from two trees		
and store in a vectorized matrix, r.		
emory space sociated routine none		
none (n)		
For <i>n</i> trees, there are $\binom{n}{2} = n(n-1)$ comparisons and		
this function will be called $n(n-1)$ times.		
none		
This distance is given by the solution of Hungarian algo-		
rithm of the cost matrix, r, given by <pre>compute_matrix</pre> .		
array_to_matrix Recover r to a matrix.		
r is an $(k-3) \times (k-3)$ matrix where k is the number		
of leaves. The main complexity goes into generating		
distance matrix and running Hungarian algorithm.		
<u>rees</u> ::Compute_Matching_dist.		
none		
The matching distance is given by the solution to Hun-		
garian algorithm on the table with entries of number of		
XOR element in bitstrofatree, which are all possible		
bipartitions of one tree.		
<pre>Get_bipartitionofonetree</pre>		
Line 1415 may have a bug.		
<u>'rees</u> ::Compute_Affinity_dist.		
(String str_matrix, int type)		
This routine compute the affinity distance, d_a , from the		
given distance ,d. The formula is either		
$d_a = \frac{1}{\varepsilon_{rel} + d}$		
$\varepsilon_{rel} + d$		
or		
$d_a = e^{-d}$,		
depending on the flow time. It accents up		
depending on the flag type. It accepts un-		
weighted/weighted RF-distance, Matching-distance,		
SPR-distance or distance given in file.		
none		
none		

14. <u>Trees</u>::temp.

Argument	none	
Description		
Complexity		
Memory space		
Associated routing	ne	
Comments		
Error code	-1	Out of memory.
	-2	Parse error, the parentheses in string
		does not match.